

Technical workshop : Dynamic nuclear fuel cycle

Reactor description in CLASS

The CLASS Team

Baptiste LENIAU*

Institut d'Astrophysique de Paris

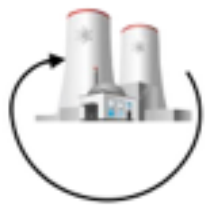
6-8 July, 2016



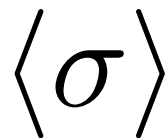
Summary



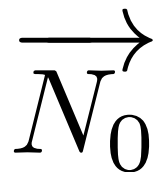
● The CLASS package : a brief overview



● Problematic of reactor description



● Mean cross section « prediction »



● Fresh fuel construction

CLASS : general informations

First code line wrote at Subatech in **2011**. Soon after the LNC-**IRSN** joins the collaboration.

CLASS is a C++ library
~15000 code lines

Involved laboratories

Subatech, Nantes
IPNO, Orsay
LPSC, Grenoble
LNC, IRSN, Fontenay aux Roses

Publications

Articles : 3 (in 2015)
Conferences : 7
Past and present PHD : 3

3 teaching workshops



Main developers

B.Mouginot (post-doc) 2011->2015
F. Courtin (PHD) 2014->2017
N.Thiollière 2011 -> -
B.Leniau (post-doc) 2013->2016

GIT/SVN repository, forum,
documentation, manual :

<https://gitlab.in2p3.fr/sens/CLASS>

<https://forge.in2p3.fr/projects/classforge>

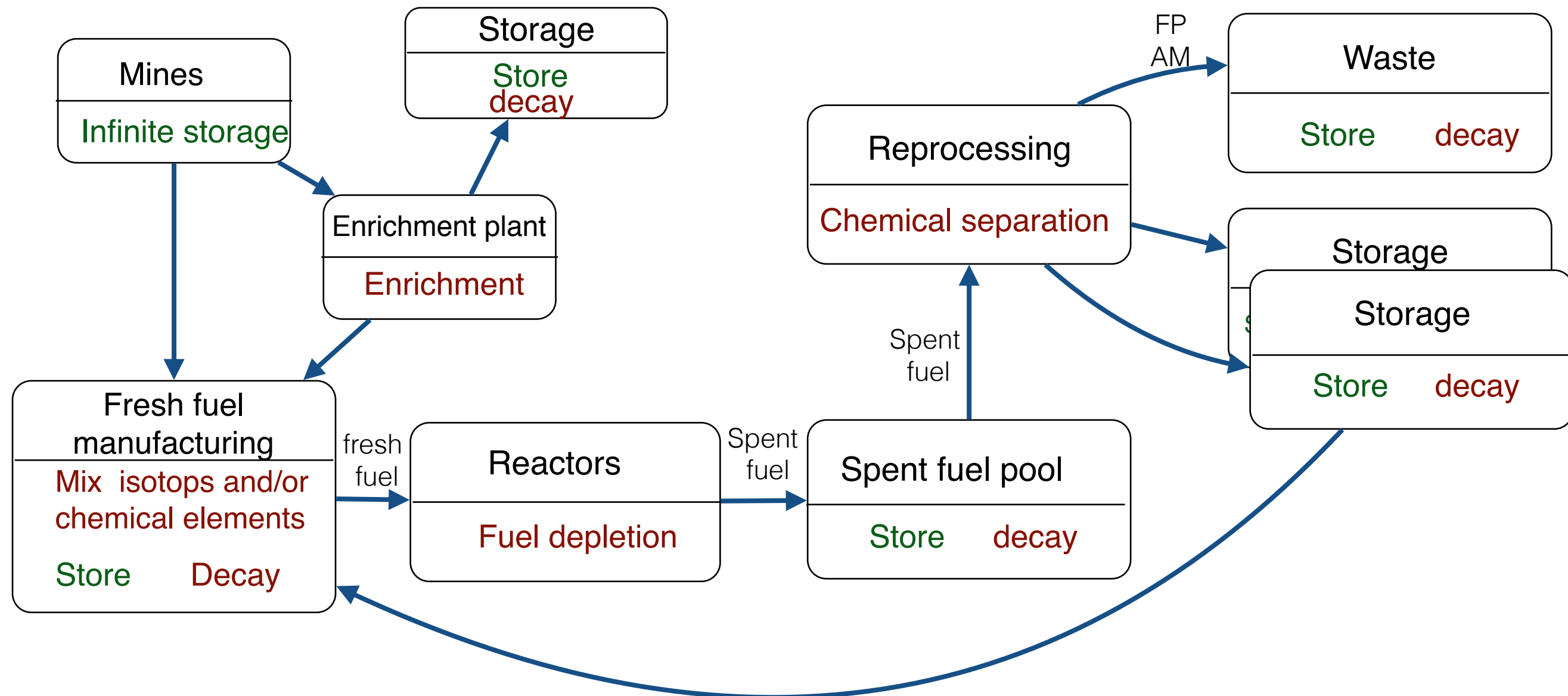
CeCILL License (in progress)

Open source code and models.

Each publication using CLASS should explicitly cite CLASS and models references

CLASS : a nuclear fuel cycle code

As any fuel cycle code, CLASS aims to describe « units » which **store** and/or **transform** and **exchange** matter. The goal being to calculate isotops inventories in units and material flux between units.



exemple of possible connexions

CLASS input : a C++ interface

Exemple of a CLASS input :

Storage :

```
/*=== Stock===*/  
//Storage for UOX  
Storage *StockUOX = new Storage(gCLASS->GetLog()); // Definition of the stock  
StockUOX->SetName("StockUOX"); // Its name  
gCLASS->Add(StockUOX); //Adding the stock to the Scenario
```

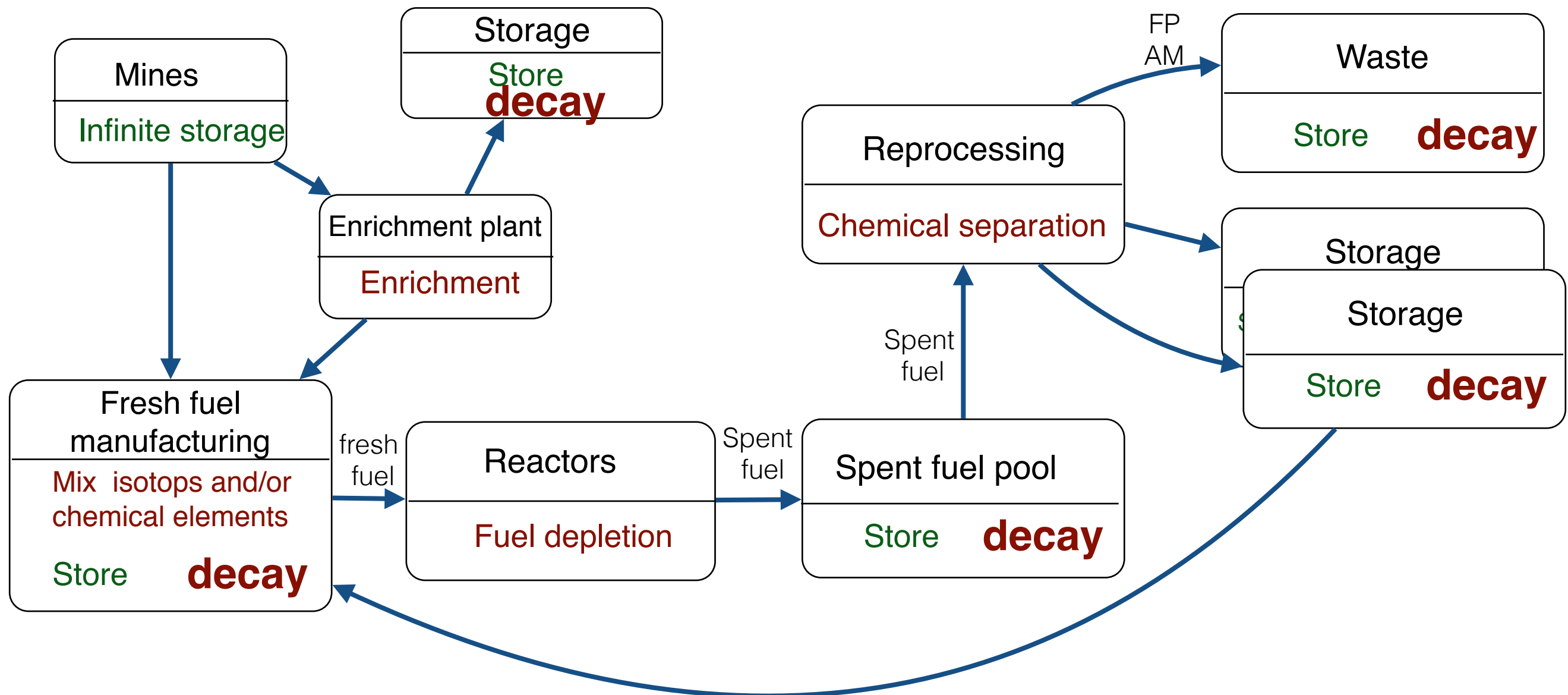
Spent fuel pool :

```
//Pool for UOX  
Pool *Cooling_UOX = new Pool(gCLASS->GetLog(),StockUOX, Temps_Cooling_UOX);  
Cooling_UOX->SetName("Pool_UOX");  
gCLASS->Add(Cooling_UOX);
```

Reactor :

```
Reactor* R_MOX = new Reactor(gCLASS->GetLog(),// Log  
PHYMOD, // The models used to build the fuel  
FP_MOX, // The FabricationPlant  
Cooling_MOX, // Connected Backend  
Temps_Debut_MOX, // Starting time  
LifeTime, // time of reactor l  
Puissance_MOX, // Power  
MasseHM_MOX, // HM mass  
BurnUp_MOX, // BurnUp  
FacteurDeCharge); // Load Factor  
  
R_MOX->SetName("The_MOX");// name of the reactor (as it will l  
gCLASS->AddReactor(R_MOX);//Add this reactor to the scenario
```


Decay handling (out core)



Decay handling (out core)

Sum of pre-calculated ascii tables

Nucleus inventory
Daughter₁ inventory
Daughter₂ inventory
...

Time

Z	A	I \ time	0	...	1,00E+08	2,00E+08	3,00E+08
94	241	0	1	...	0.858532	0.737077	0.632804
95	241	0	0	...	0.141097	0.261519	0.364194
93	237	0	0	...	0.00037098	0.00140392	0.00300153
91	233	0	0	...	1.20044e-11	4.69712e-11	1.01549e-10
92	233	0	0	...	1.17172e-10	9.40835e-10	3.10253e-09
90	229	0	0	...	3.96366e-16	6.49622e-15	3.251e-14
88	225	0	0	...	2.03528e-21	3.45768e-20	1.75189e-19
89	225	0	0	...	1.30994e-21	2.27899e-20	1.16443e-19
2	4	0	0	...	0.000371008	0.00140394	0.00300155
82	209	0	0	...	1.78109e-23	3.08871e-22	1.57801e-21
83	209	0	0	...	1.42923e-16	5.20101e-17	3.13304e-16
92	237	0	0	...	2.70291e-08	2.32053e-08	1.99225e-08

portion of a pre-calculated
decay table of ONE
NUCLEUS (²⁴¹Pu)

Example :

Considering a sample made of : N¹ nuclei of ²⁴¹Pu and N² nuclei of ²³⁸Pu
What is the composition of this sample 3 month after ?

portion of
²⁴¹Pu table

Z	A	I \ time	0	...	1,00E+08	2,00E+08	3,00E+08
94	241	0	1	...	0.858532	0.737077	0.632804
95	241	0	0	...	0.141097	0.261519	0.364194
93	237	0	0	...	0.00037098	0.00140392	0.00300153
91	233	0	0	...	1.20044e-11	4.69712e-11	1.01549e-10
92	233	0	0	...	1.17172e-10	9.40835e-10	3.10253e-09
90	229	0	0	...	3.96366e-16	6.49622e-15	3.251e-14
88	225	0	0	...	2.03528e-21	3.45768e-20	1.75189e-19

Daughter₁

$N^1 \cdot \overrightarrow{Daughter_1}$

+

$N^2 \cdot \overrightarrow{Daughter_2}$

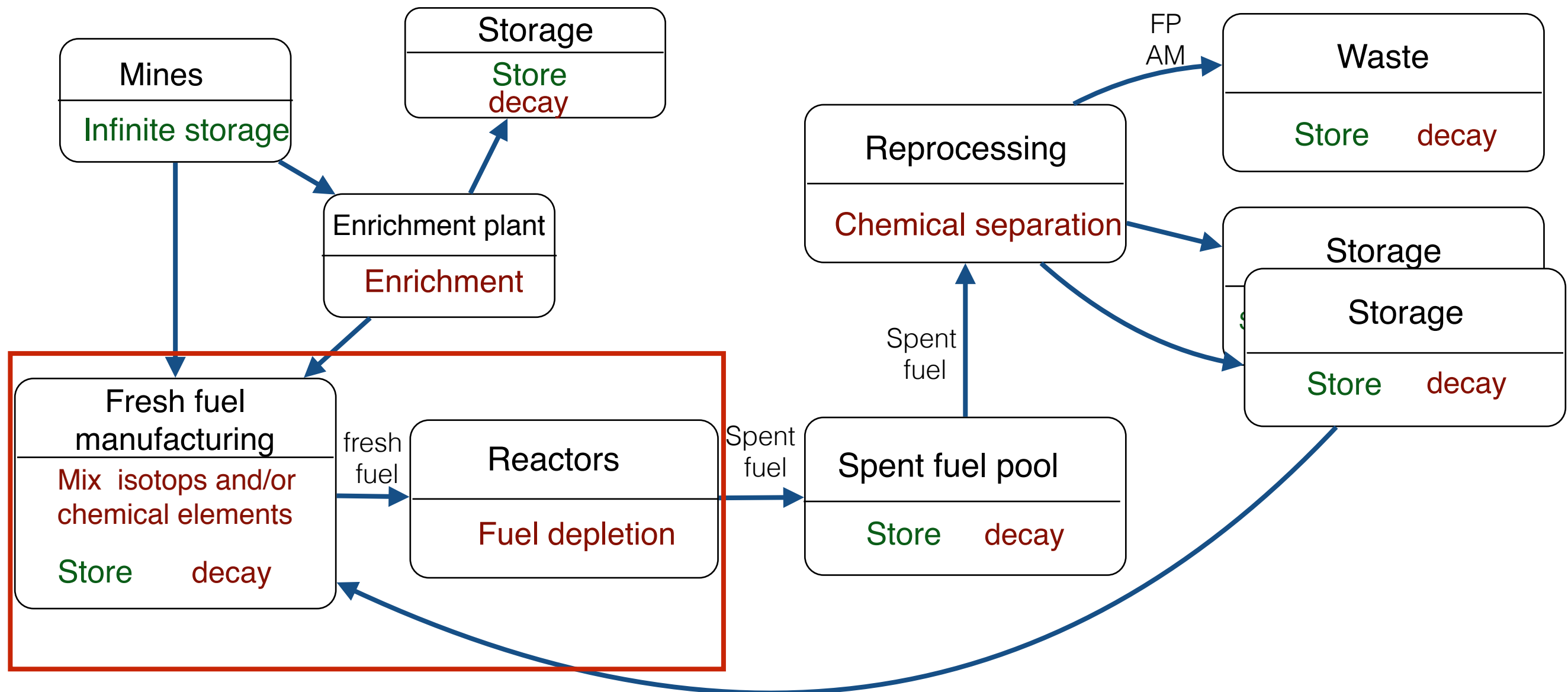
portion of
²³⁸Pu table

Z	A	I \ time	0	...	1,00E+08	2,00E+08	3,00E+08
94	238	0	1	...	0.982621	0.980163	0.977712
92	234	0	0	...	0.0173787	0.0188366	0.0222883
90	230	0	0	...	5.45339e-08	7.11686e-08	8.99978e-08
88	226	0	0	...	3.71127e-13	5.53621e-13	7.8774e-13
86	222	0	0	...	2.3802e-18	3.55962e-18	5.07497e-18
2	4	0	0	...	0.0173788	0.0198367	0.0222885
82	209	0	0	...	1.42923e-16	5.20101e-17	3.13304e-16

Daughter₂

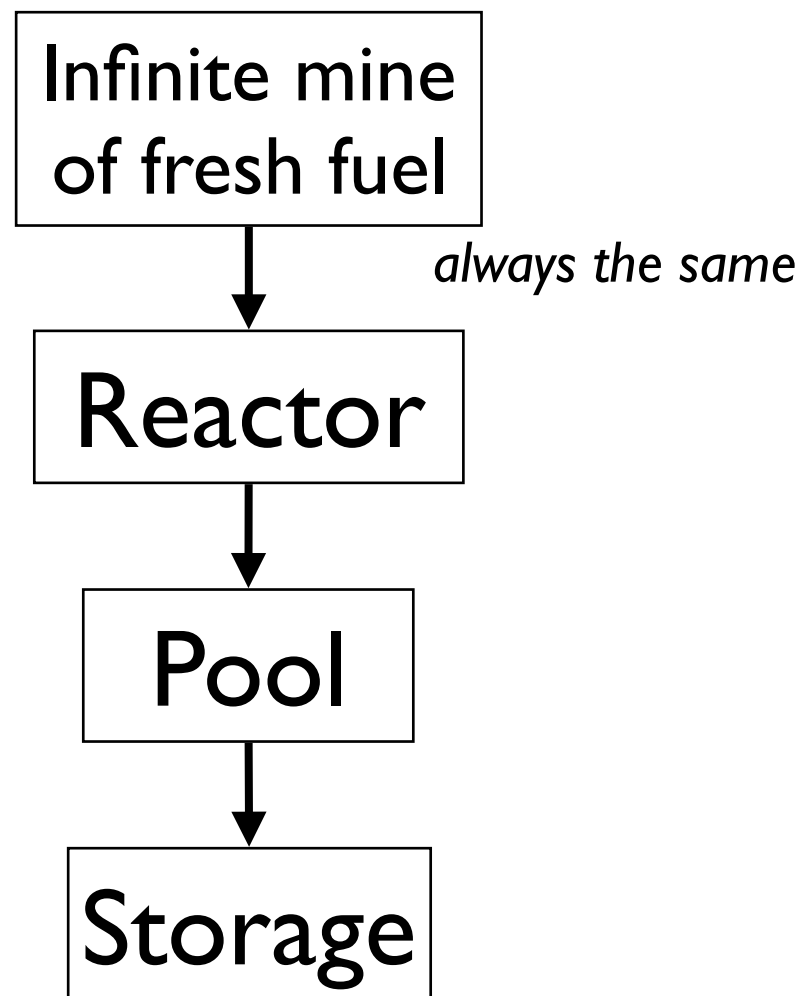
Sample with
3m of decay

Reactor handling

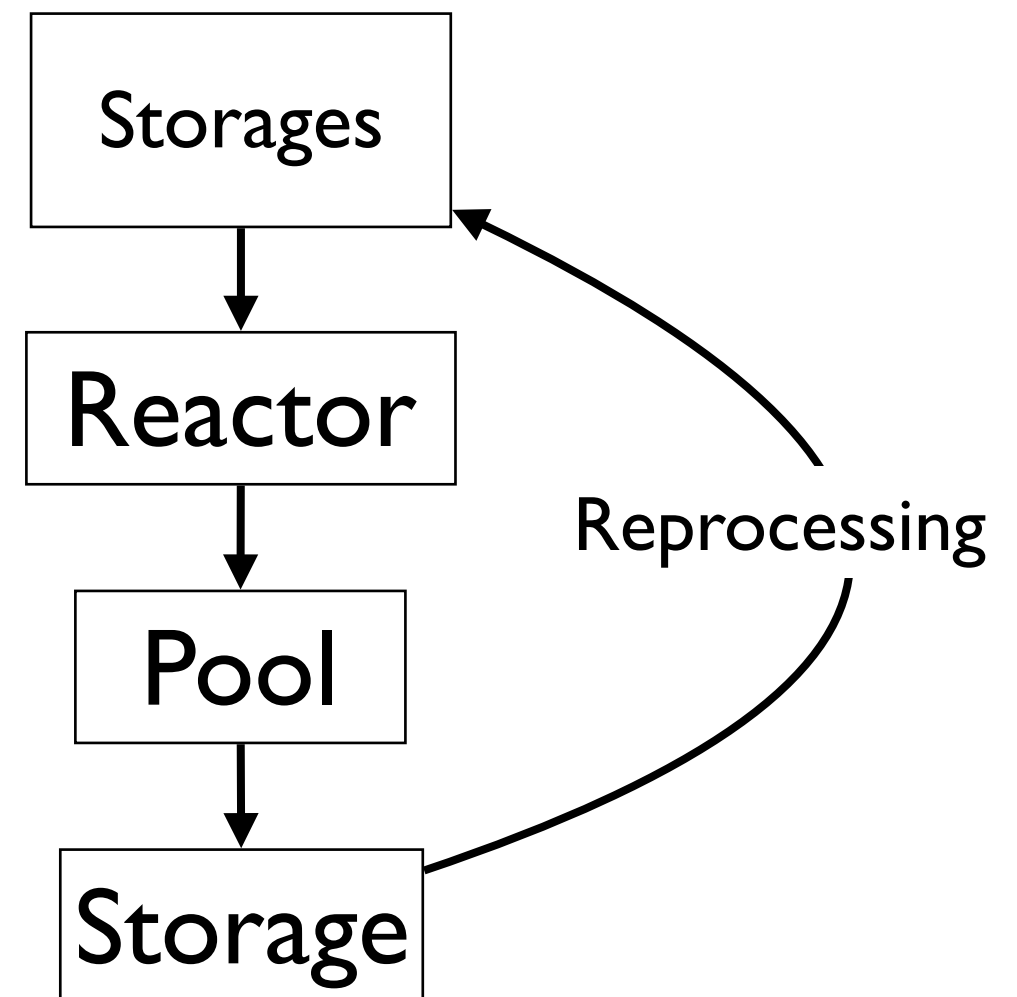


Reactor handling : two cases

Fixed fresh fuel (recipe based)

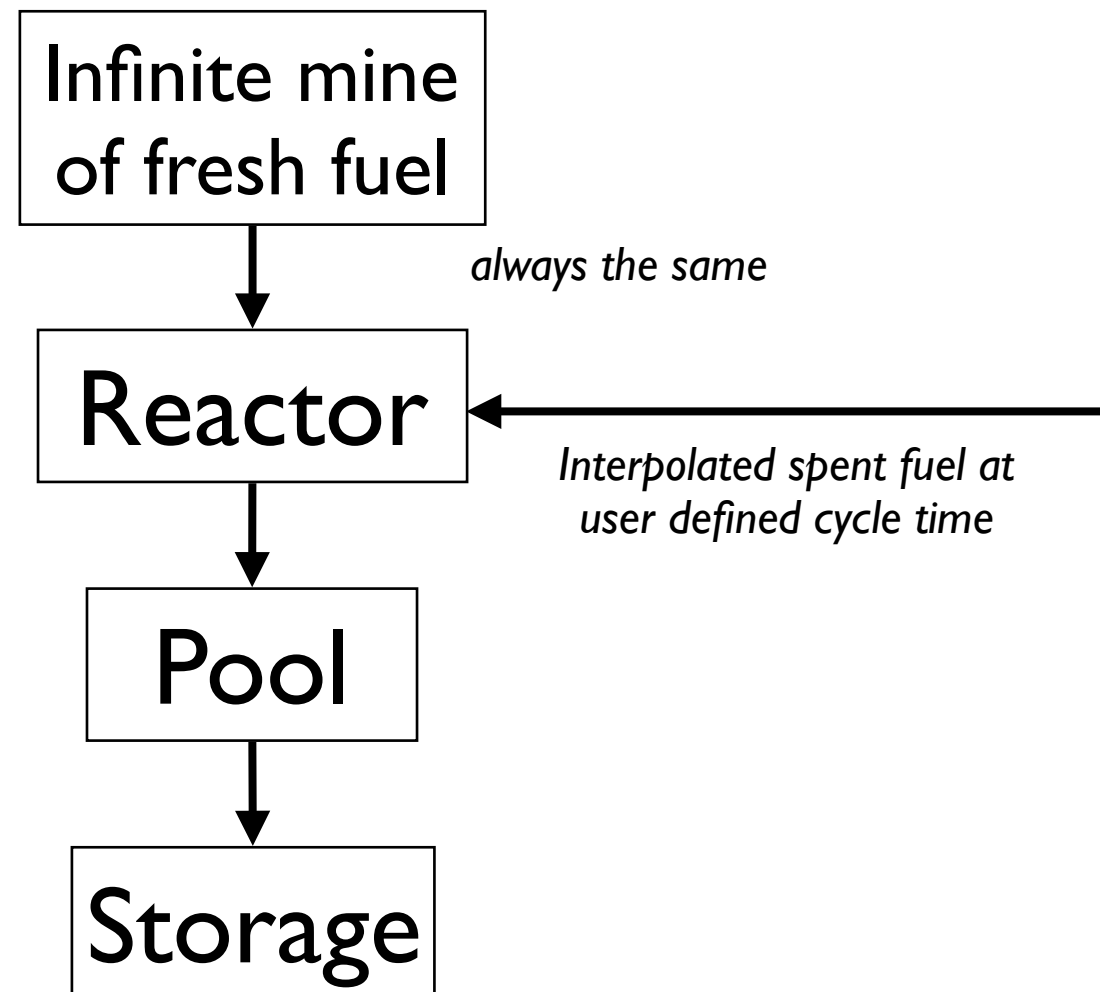


Dynamic fresh fuel



Reactor handling

Fixed fresh fuel (recipe based)

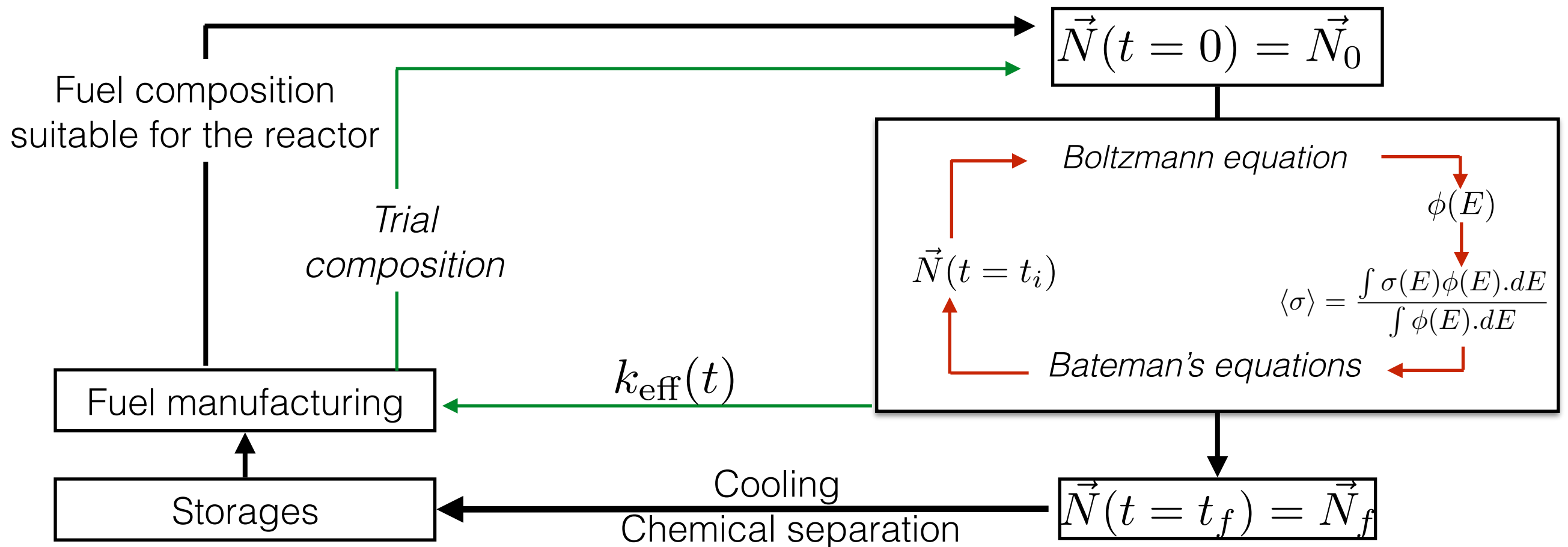


EvolutionData : pre-calculated fuel depletion

```
time 0 8640000 17280000 25920000 34560000 43200000 51840000 60480000
keff 1.368829965591431 1.291270017623901 1.254439949989319 1.222790
flux 195985884053504 207991089397760 213981310484480 22052380396748
Inv 92 238 0 1.091610706965101e+26 1.089776731669293e+26 1.08784563
Inv 92 235 0 5.209517323740204e+24 4.803020259645922e+24 4.42685367
Inv 90 234 0 1516852794621952 1599010552938496 1600768268304384
Inv 92 234 0 3.085685485060332e+19 6.149263309723297e+19 9.052727
Inv 90 230 0 11989737799680 46687456329728 102358918889472 176327
Inv 88 226 0 10160737 78770728 259498736 599404224 1138568704 191
Inv 86 222 0 56.75755310058594 475.7766418457031 1610.15893554687
Inv 2 4 0 1.738924680833227e+21 3.596563966368963e+21 5.511976970
Inv 82 210 0 85177072 620119680 1675596672 3165464576 5140426752
Inv 83 210 0 42436.4765625 347157.875 975575.125 1874426 3065808.
Inv 84 210 0 120487.234375 2015354.5 8435752 20791796 39688820 63
Inv 82 206 0 10875.70703125 408642.6875 2796857.5 9856710 2471633
Inv 82 207 0 3155653 40490964 154262512 374067744 721180544 12110
Inv 82 208 0 914631040 17555482624 97128398848 329410936832 85863
Inv 82 209 0 952.7511596679688 8829.0205078125 34459.53515625 942
Inv 83 209 0 119043.7265625 2132021.75 12169454 43239720 11855373
Inv 83 208 0 3.354406118392944 28.70504379272461 129.3545074462
Inv 83 207 0 1.294642567634583 4.502455234527588 6.3504
Inv 1 1 0 1.011051629226072e+19 2.178457770163752e+19 3.453316653
Inv 1 2 0 3.473102970080461e+18 7.05875854744984e+18 1.0800574187
Inv 1 3 0 3.964149755871966e+19 8.056561501365862e+19 1.227449393
Inv 2 3 0 2.48280291171369e+17 8.401381404536996e+17 1.6232733375
Inv 81 205 0 6.734152317047119 56.72389221191406 258.9663696289
Inv 80 204 0 3.027137279510498 5.906529426574707 14.37110
Inv 80 203 0 1.23071455955505
Inv 81 203 0 1.044107675552368 1.55852222
```

Reactor problematic : fuel from reprocessed materials

Determine the **fresh fuel composition** and **predict its irradiation** in reactor

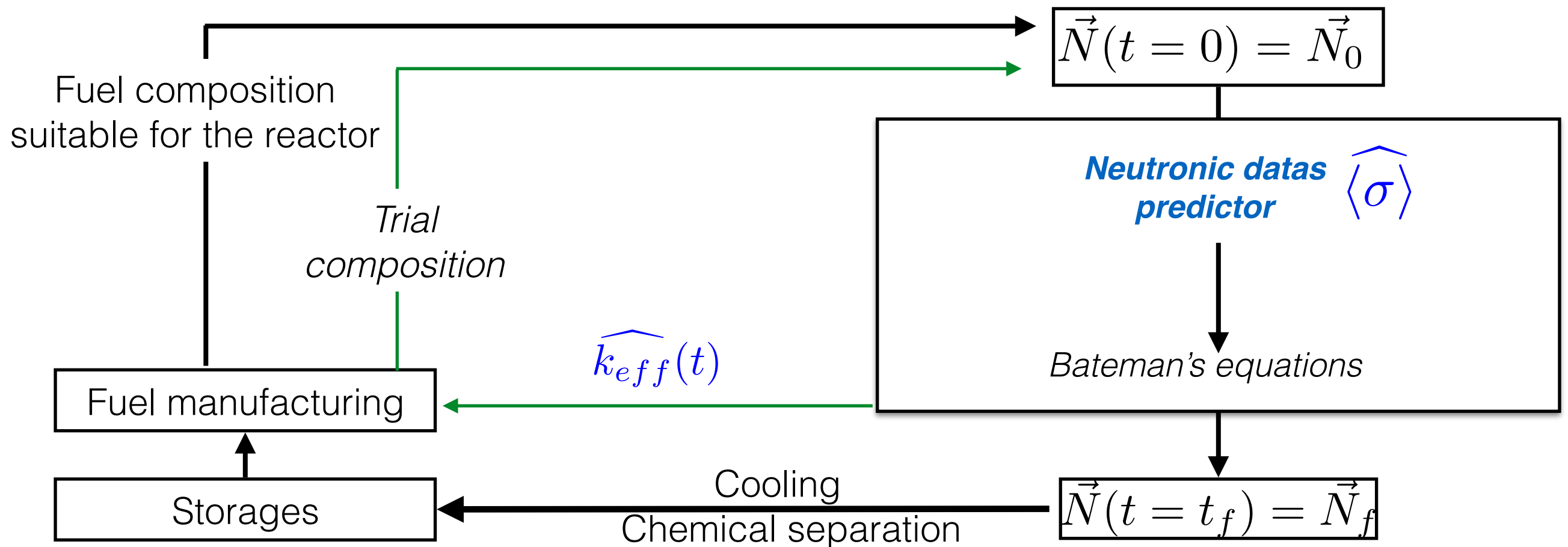


$\langle \sigma \rangle$ and $k_{\text{eff}}(t)$ strongly depends on \vec{N}_0 , which is unknown a-priori

How to avoid calls to time consuming neutron transport code ?

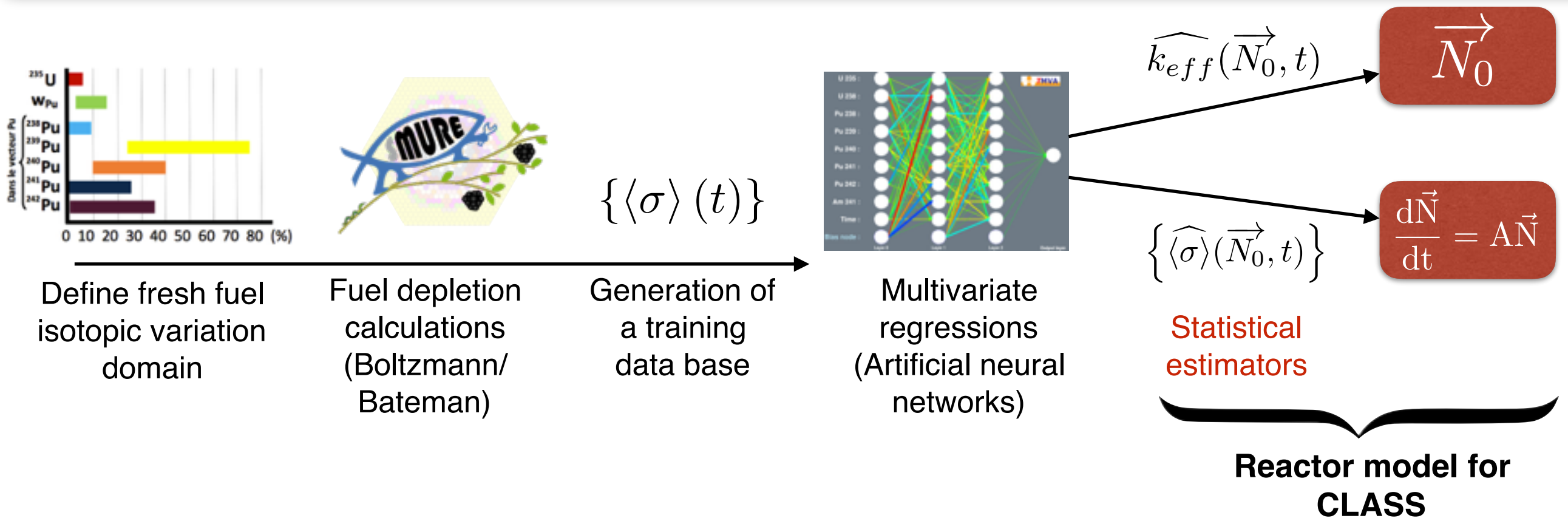
Reactor problematic : fuel from reprocessed materials

Determine the **fresh fuel composition** and **predict its irradiation** in reactor



Approach used : Replace the neutron transport code by **statistical predictors**

Methodology : Building a reactor model for CLASS



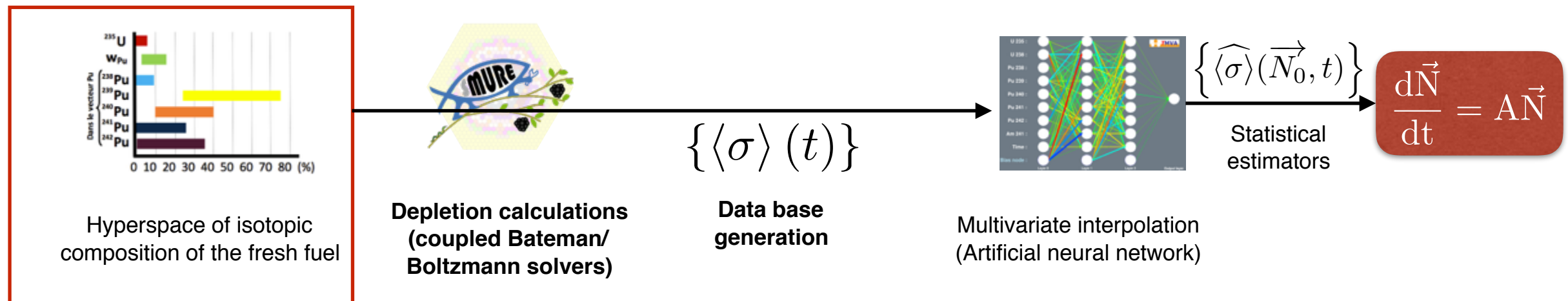
Existing models :

- PWR-UOx
- **PWR-MOX (this talk)**
- PWR-MOX on enriched uranium support.
(Fanny COURTIN's talk, this afternoon)
- SFR MOX

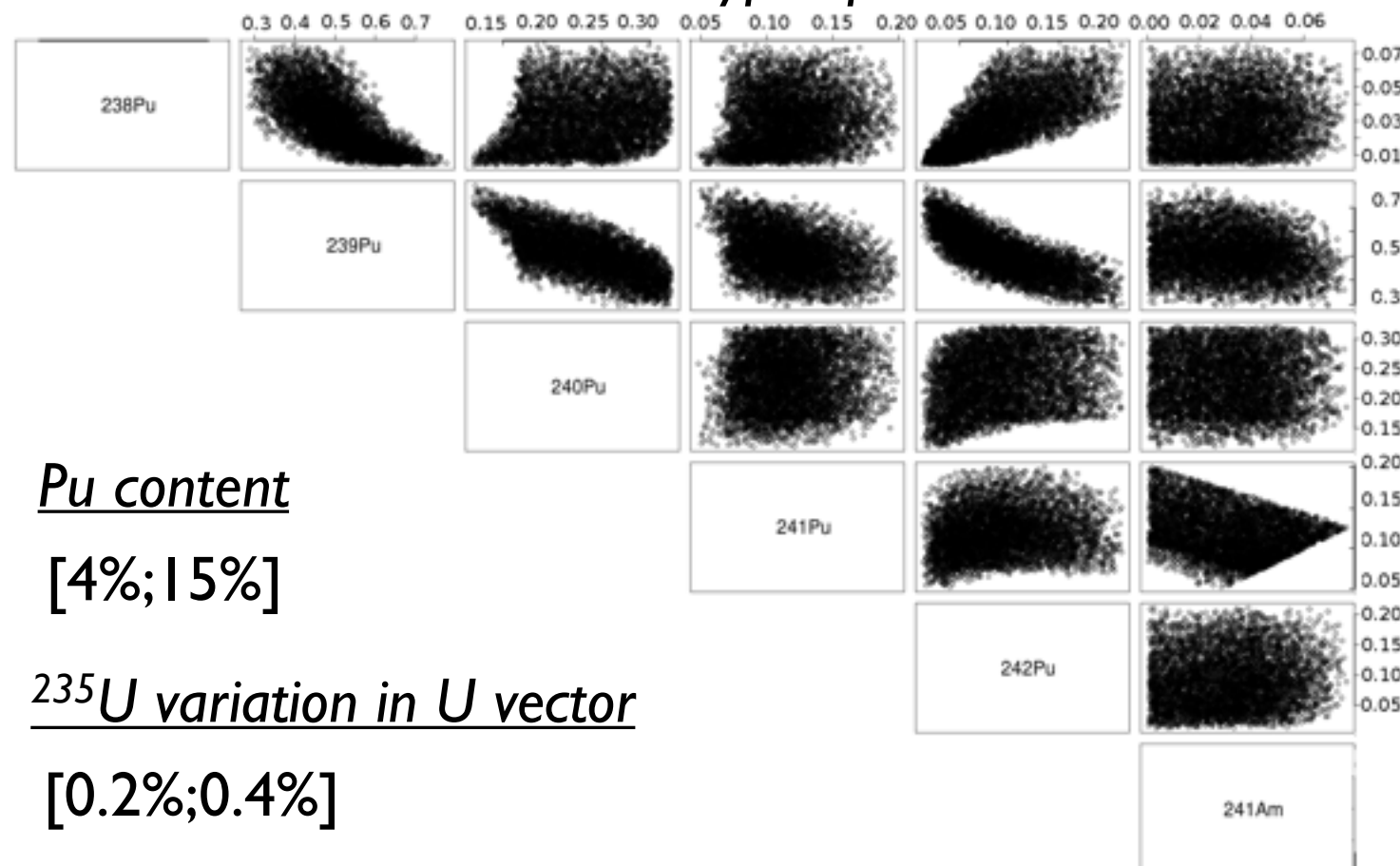
In development :

- PWR-MOX with Americium
(A. Zakari's talk Friday morning)
- ADS
- CANDU U from reprocessing

Example : PWR MOX Cross section predictors

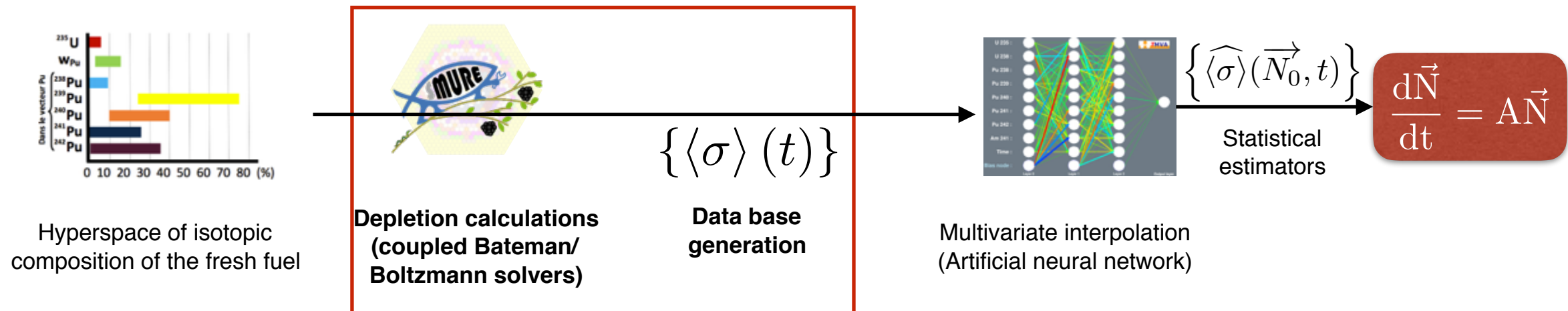


Pu hyperspace



The plutonium hyperspace is generated using 6 different PWR-UOx fuel depletion calculation (representative of the french fleet) at difference irradiation time.

Example : PWR MOX Cross section predictors



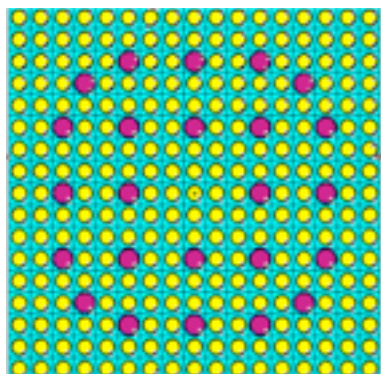
Main characteristics :

Assembly 17x17 lattice

100% MOX

Fixed power density : 30 W/g

MOX composition : Variable



Main simulation parameters :

Infinite calculation (mirror boundaries)

Impact of UOx neighbor not taken into account

Fixed boron content : 600ppm

MCNP steps : 11

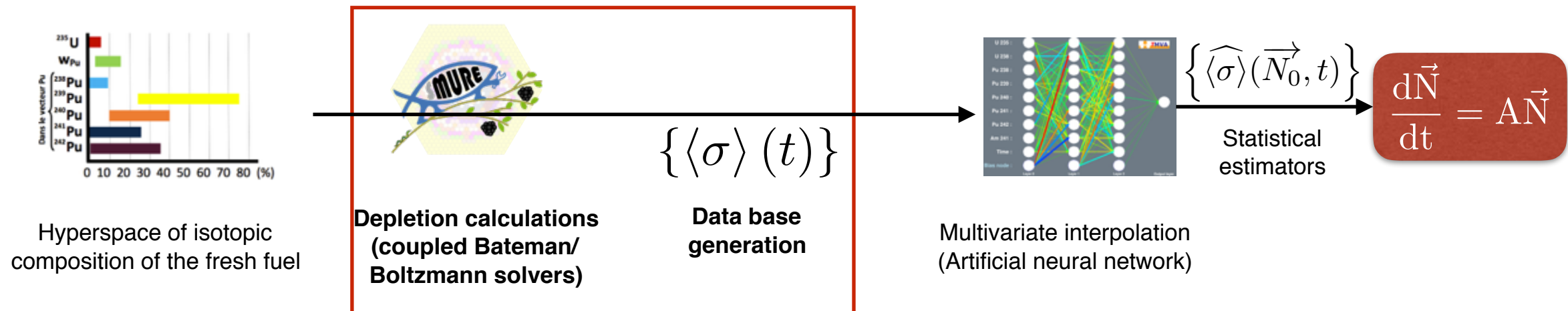
Multi-group : yes (17900 groups)

Data Bases (XS, FPYields, $S(\alpha, \beta)$) : JEFF 3.1.1

Half life threshold : 1 hour

Running time (1cpu) : ~2 hours

Example : PWR MOX Cross section predictors

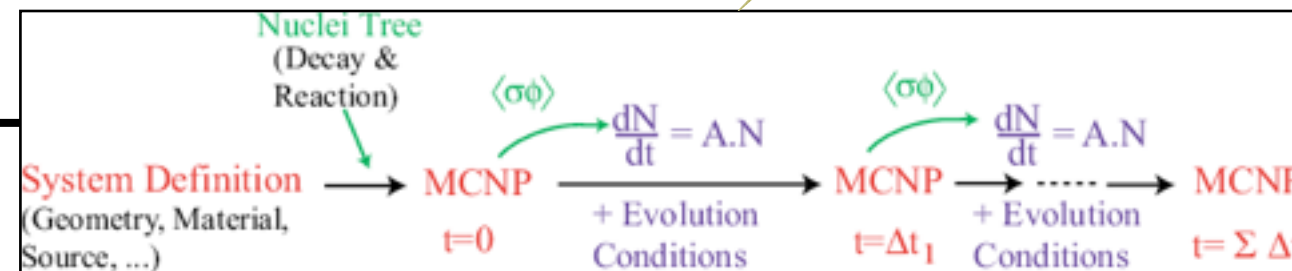


Depletion calculations

N different fresh fuel compositions

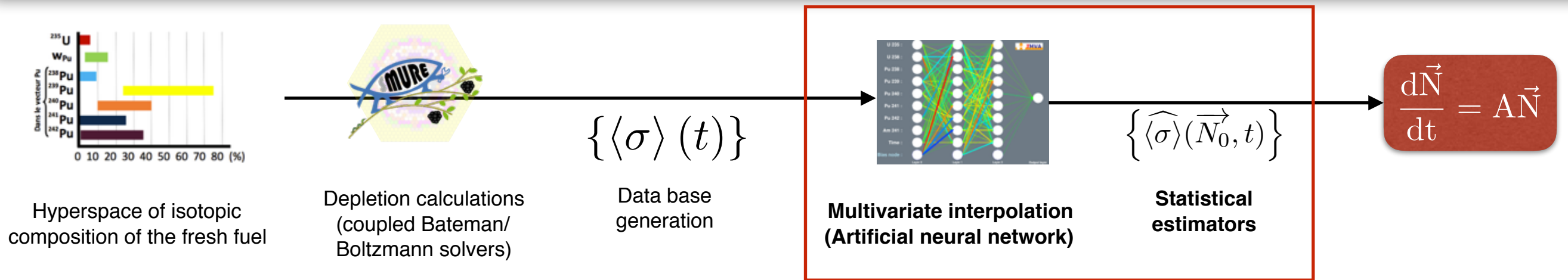
N fuel depletion calculations using the code :

N sets of results:



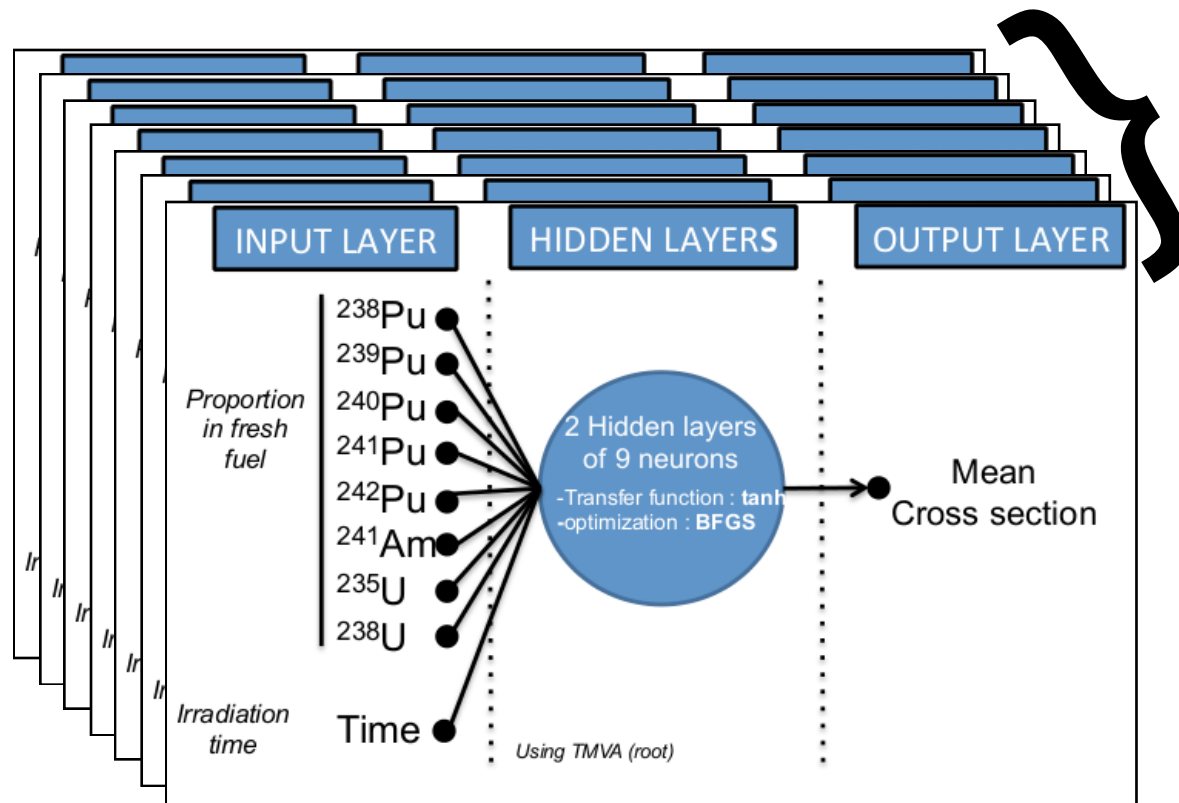
~2h per depletion calculation on 1 CPU

Example : PWR MOX Cross section predictors



Using the depletion calculations to train ANNs to predict :
 $\widehat{\langle\sigma\rangle} = f(\vec{N}_0, t)$ (Power is constant)

One neural network per reaction...



Number of reactions :

- Nuclei considered : 365
- Reaction type handle : (n,γ), (n,f) and (n,2n)
- Number of reactions : 700

PWR MOX model testing performances

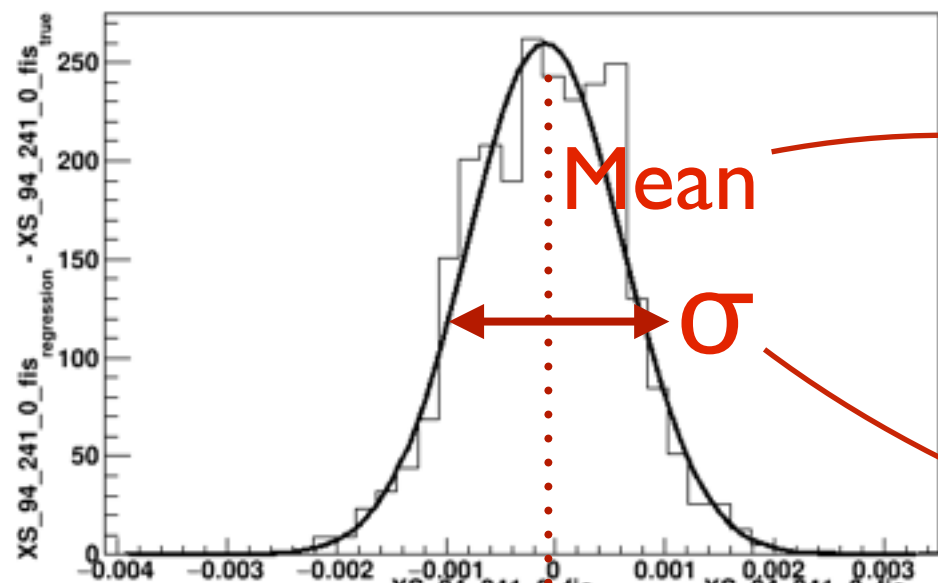
Testing procedure :

$$\text{ANN Error} = \frac{\langle \hat{\sigma} \rangle^N - \langle \sigma \rangle^{\text{test}}}{\langle \sigma \rangle^{\text{test}}}$$

$\langle \hat{\sigma} \rangle^N$ Mean cross section predict by ANN trained with **N** MURE calculations results
 $\langle \sigma \rangle^{\text{test}}$ Mean cross section calculated with MURE NOT USED FOR TRAINING

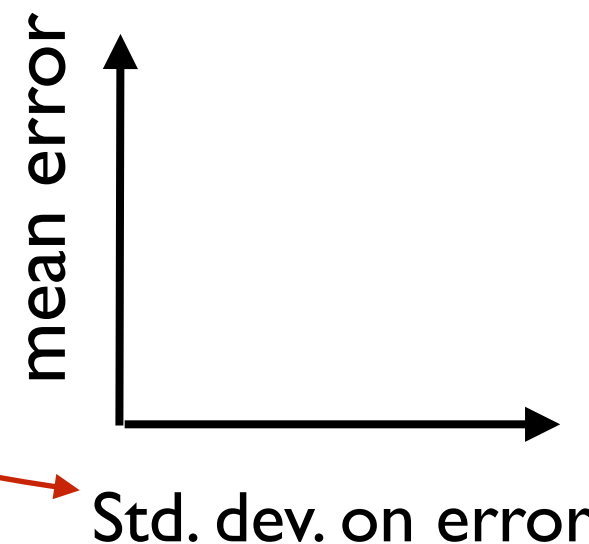
For each reaction and for each training sample size :

Plot each (mean, σ) on a graph



Example :Error distribution on $^{241}\text{Pu}(n,f)$ prediction

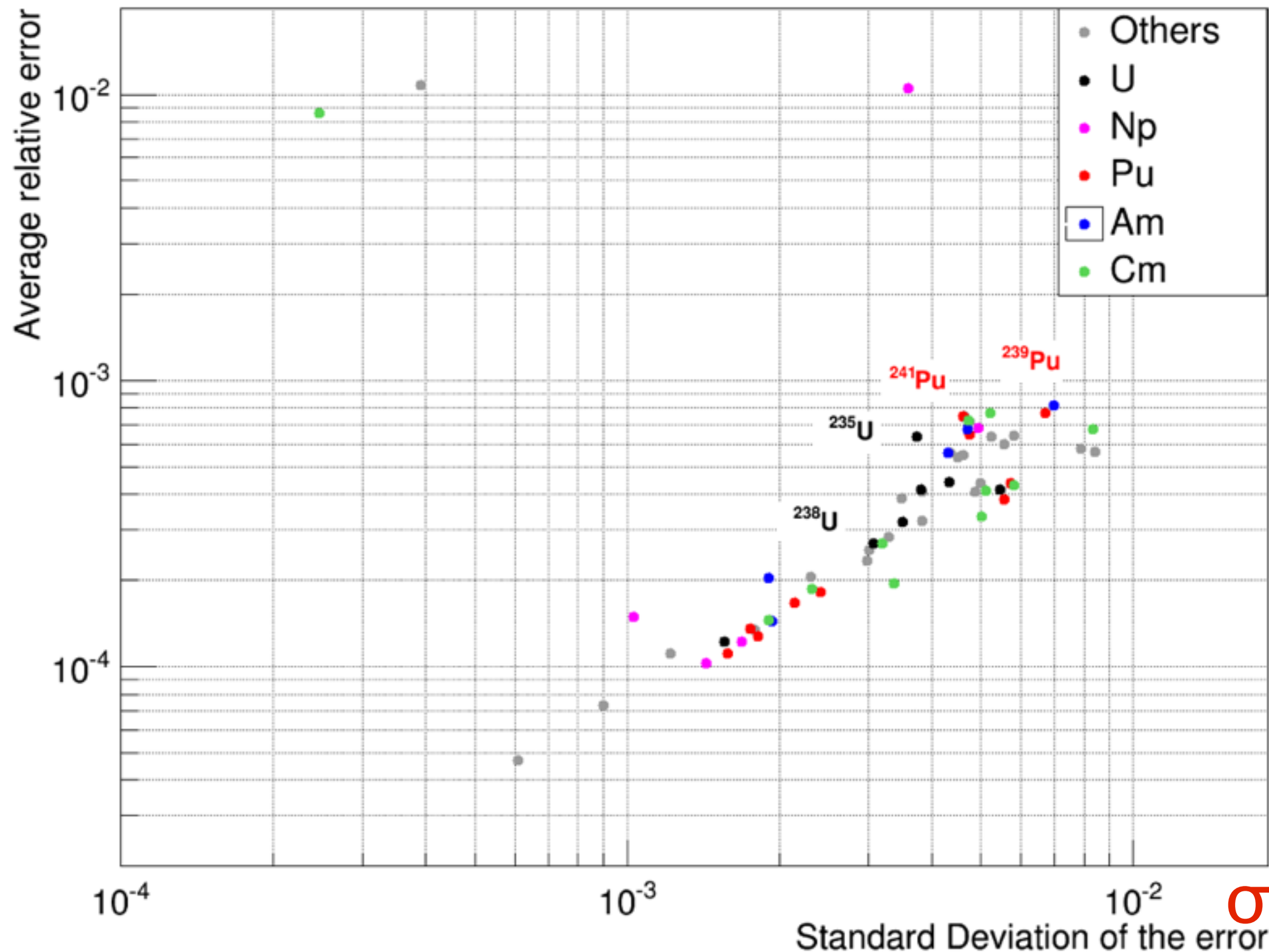
ANN Error



Std. dev. on error

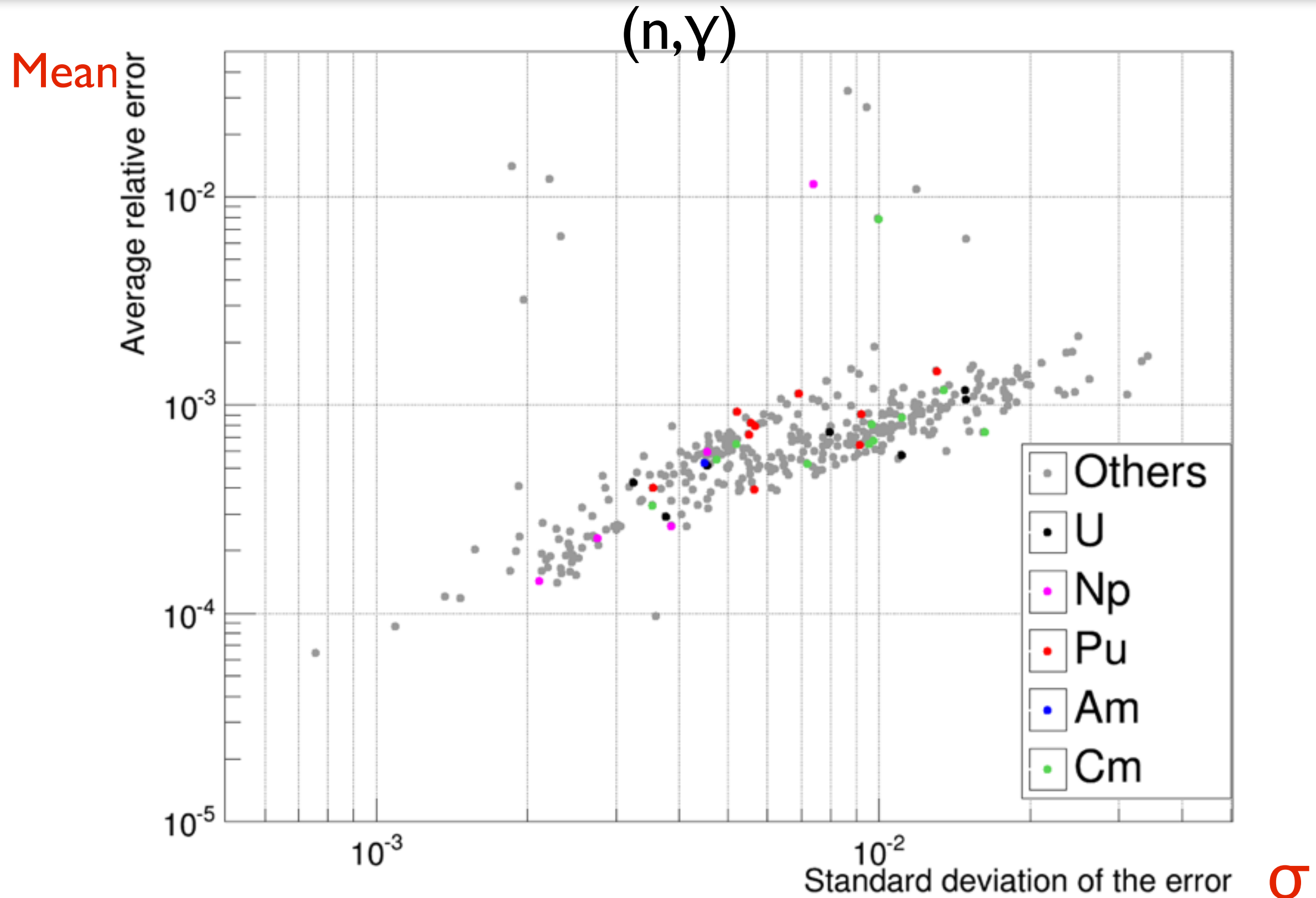
Testing performances : fission

Mean



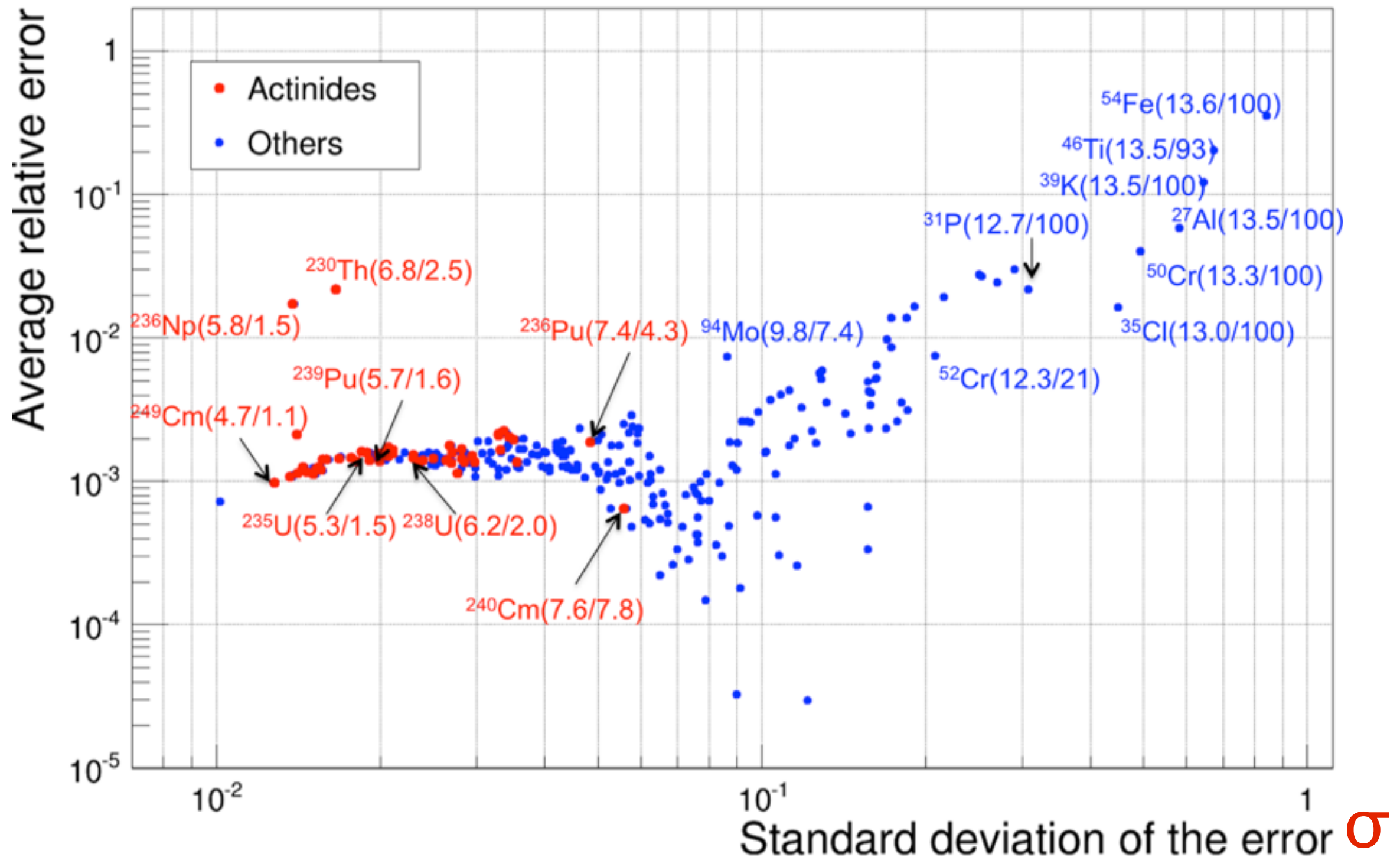
σ

Testing performances : capture



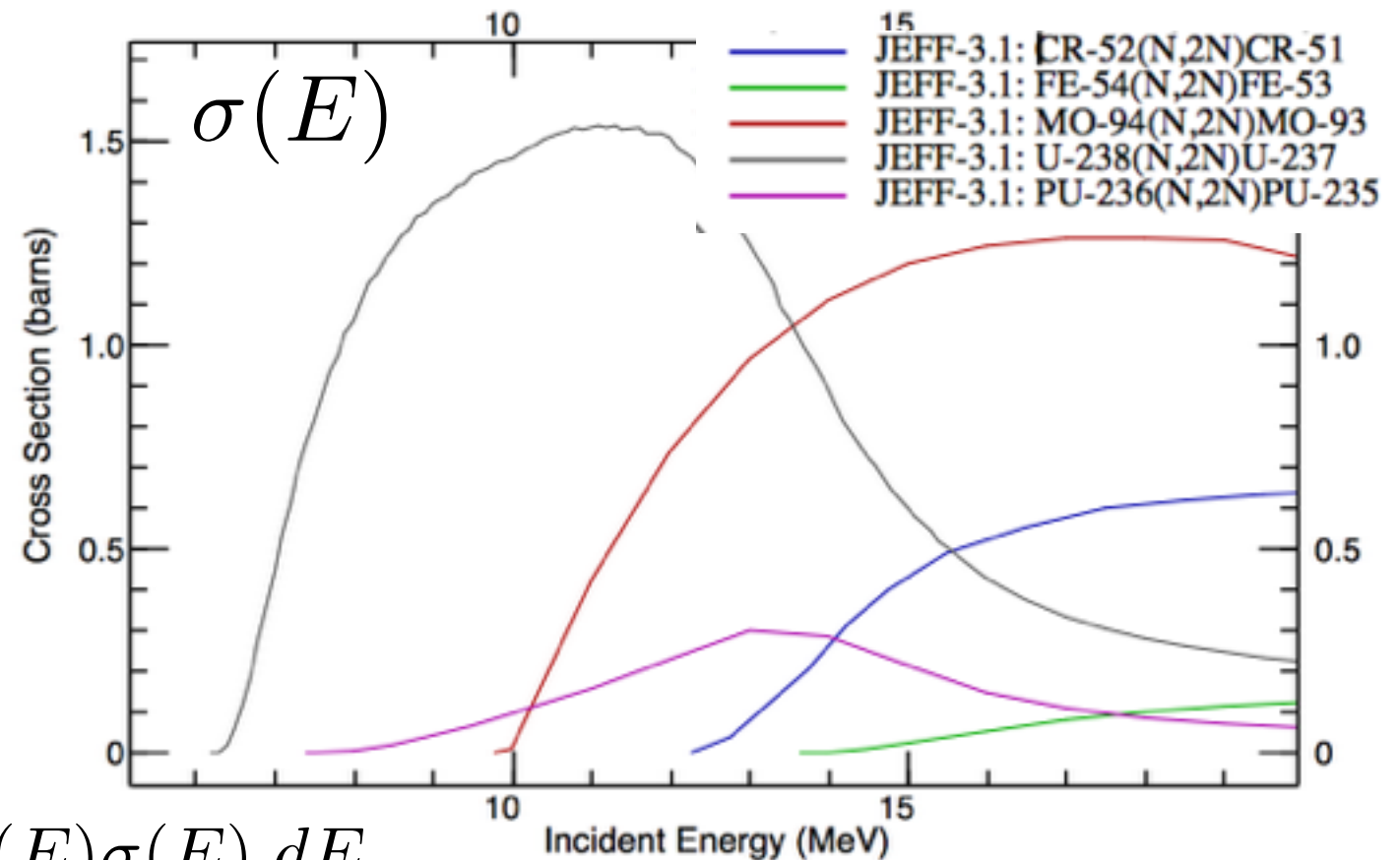
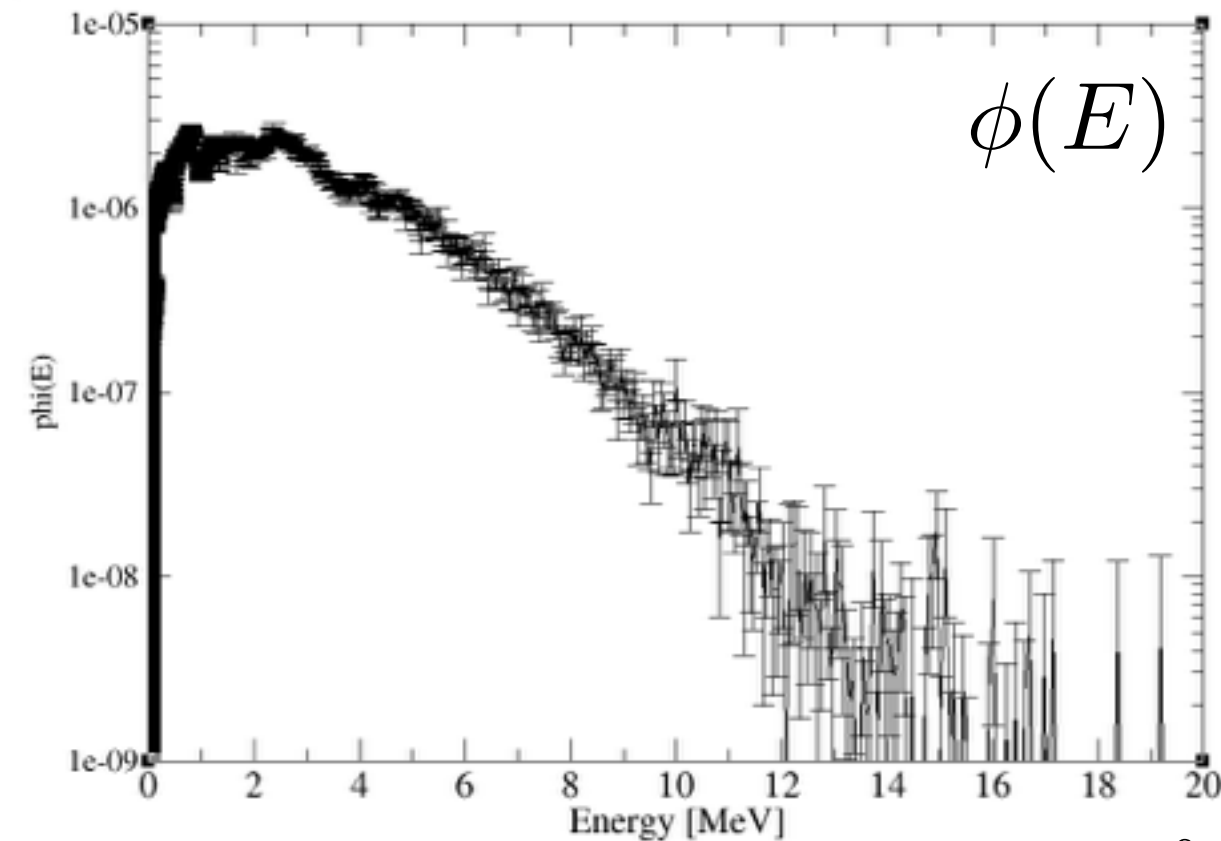
Testing performances : (n,2n)

Mean



^AX (Energy threshold, MCNP statistical error)

(n,2n) statistical error



$$\langle \sigma \rangle = \frac{\int \phi(E) \sigma(E) . dE}{\int \phi(E) . dE}$$

Error more important for (n,2n) reactions :

(n,2n) : Threshold Reaction

-> Low statistic in fast region of neutron spectrum (Monte Carlo !)

-> High statistical error on (n,2n)

-> Noisy mean cross section

-> ANN can't be better than statistical error on the training sample !

Induce errors in fuel depletion calculation

Methodology :

Reference

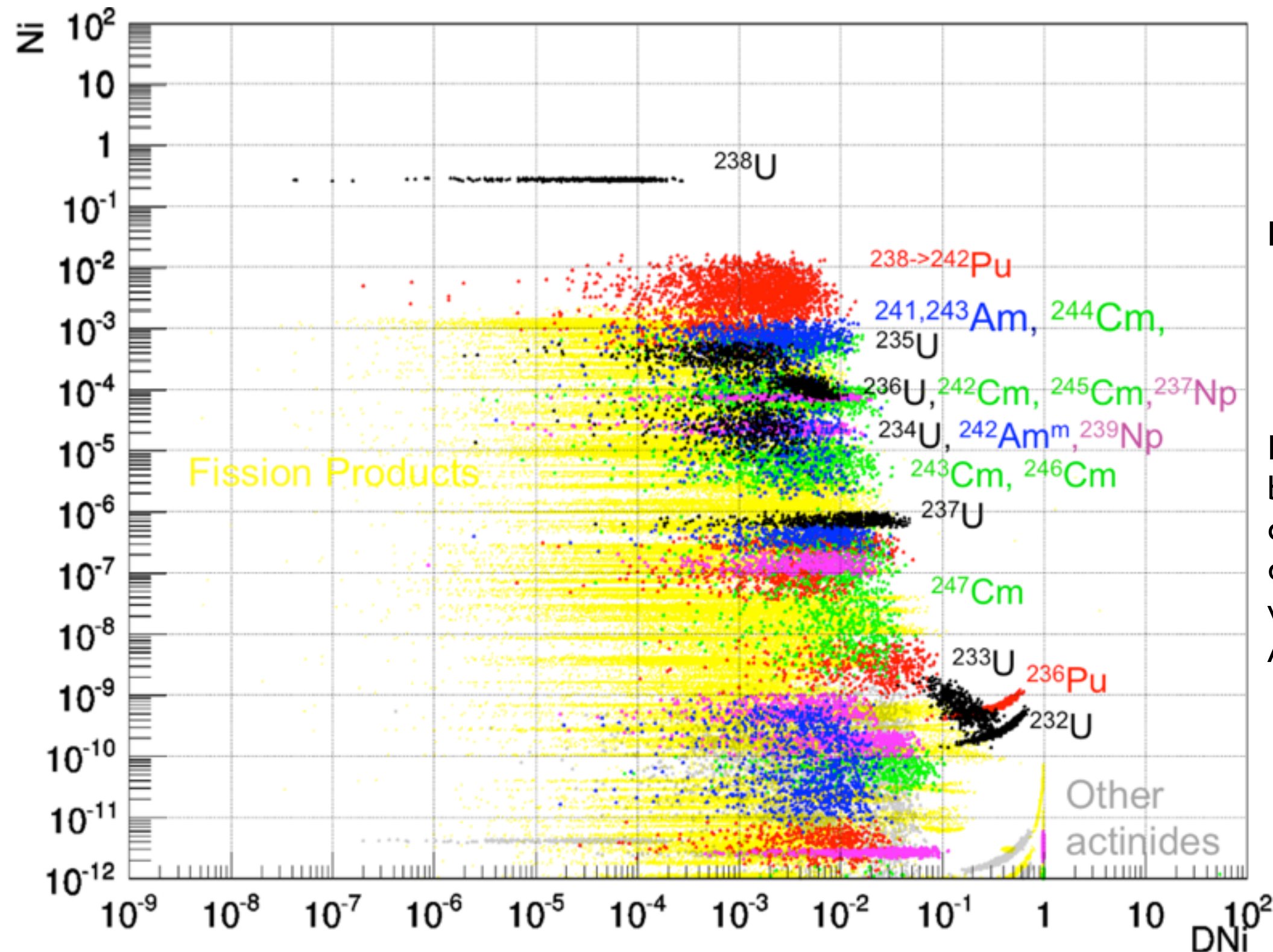
- Generation of 500 random fresh fuel compositions in the hyperspace previously defined.
- Depletion calculations (MURE) with these 500 different fresh fuels

CLASS models output

- The same 500 fresh fuel compositions are used as input for the mean cross sections predictor
- These cross sections are used by the Bateman solver of CLASS

The end of cycle inventories are compared

Induce errors in fuel depletion calculation



How to read ?

Y axis:

Proportion in spent fuel

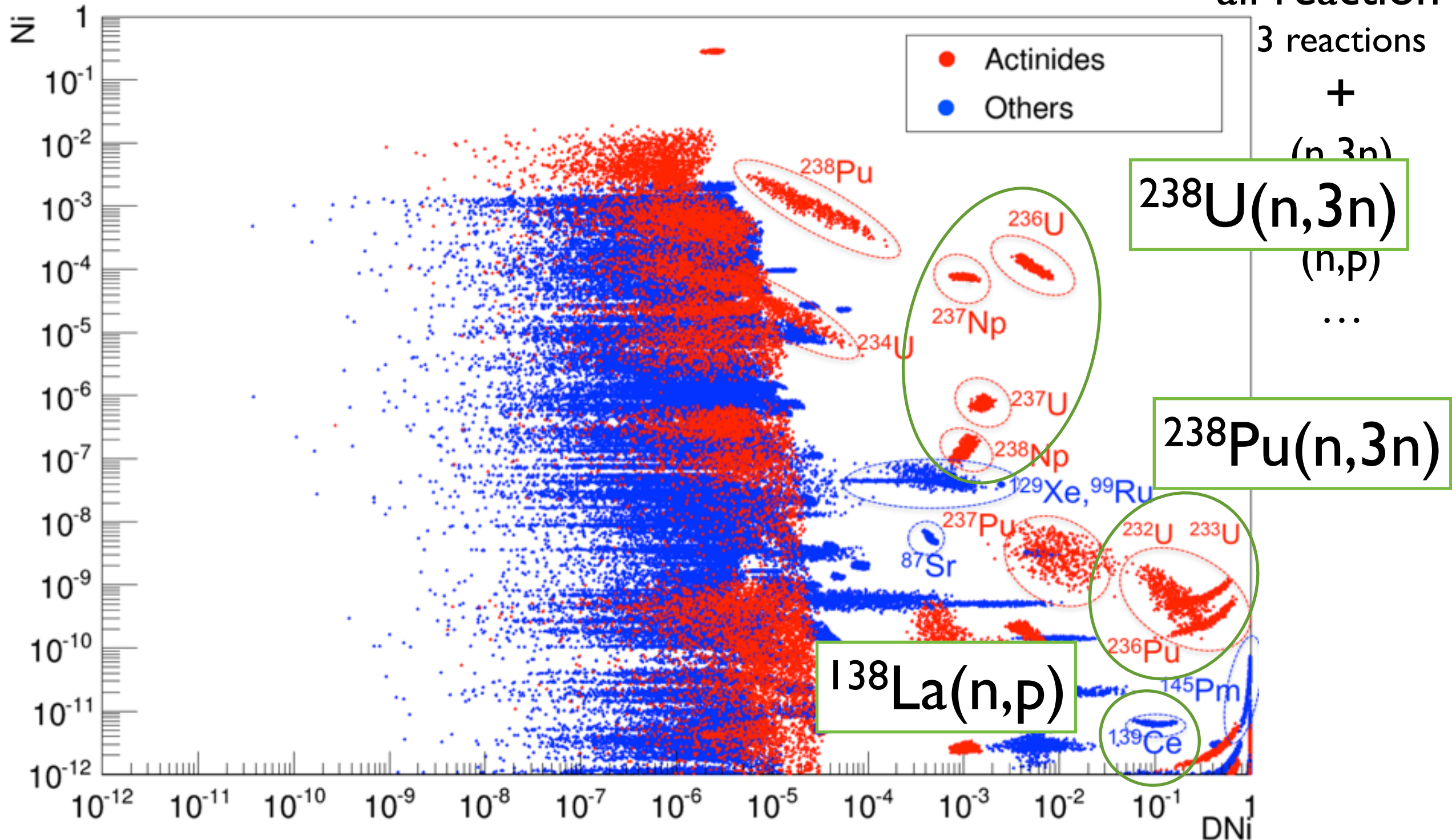
X axis:

Relative difference between a MURE calculation and a depletion calculation with predicted $\langle\sigma\rangle$ via ANN

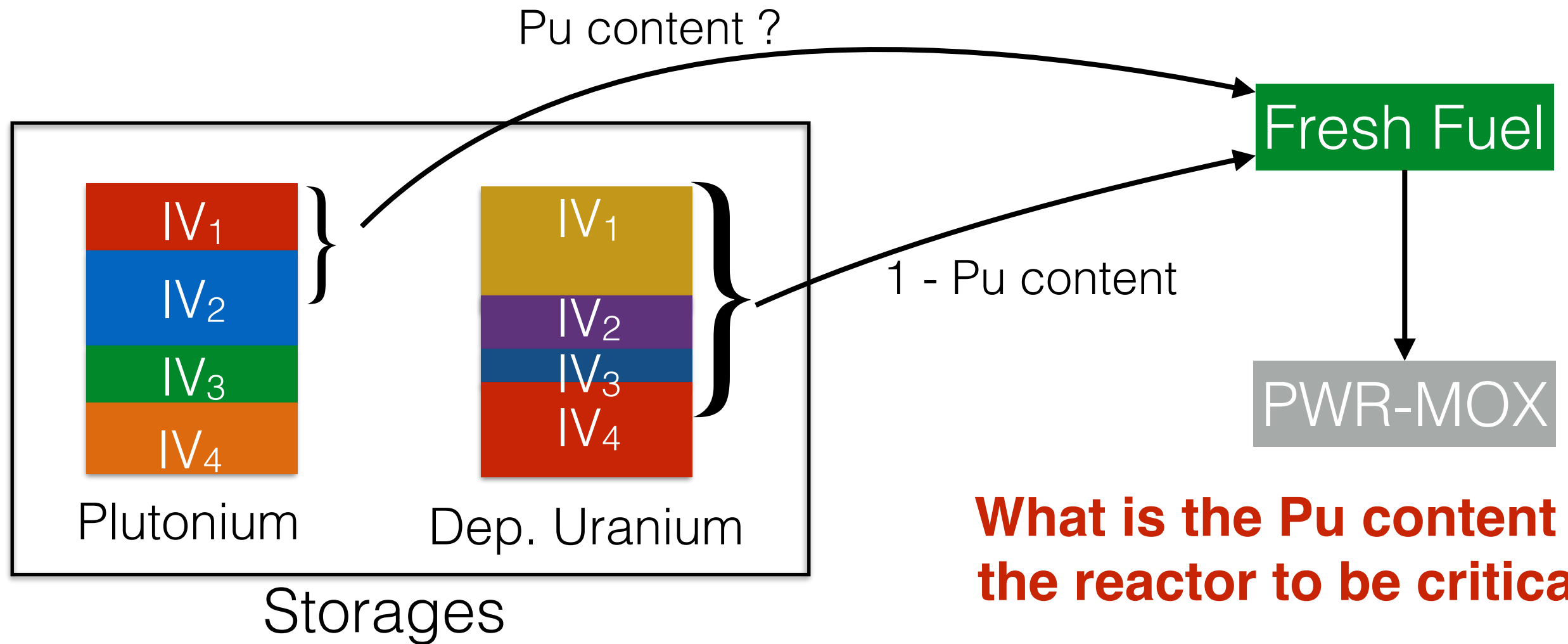
Impact of the 3 reactions assumption

CLASS 3 reactions (XS from MURE) VS MURE all reactions

all reaction :



Example of building a MOX fuel for a PWR



What is the Pu content for the reactor to be critical ?

Isotopic compositions determined during fuel cycle simulation

The averaged k_{∞} model

•The fuel management in CANDU/PWR/BWR/SFR... uses **batches** to flatter the flux profile and to **flatter the k_{eff} evolution** (fresh fuel assemblies compensate the lack of criticality of the old ones)

@ a fuel loading : 1/N assemblies are loaded, 1/N are moved in the core,...,1/N are unloaded

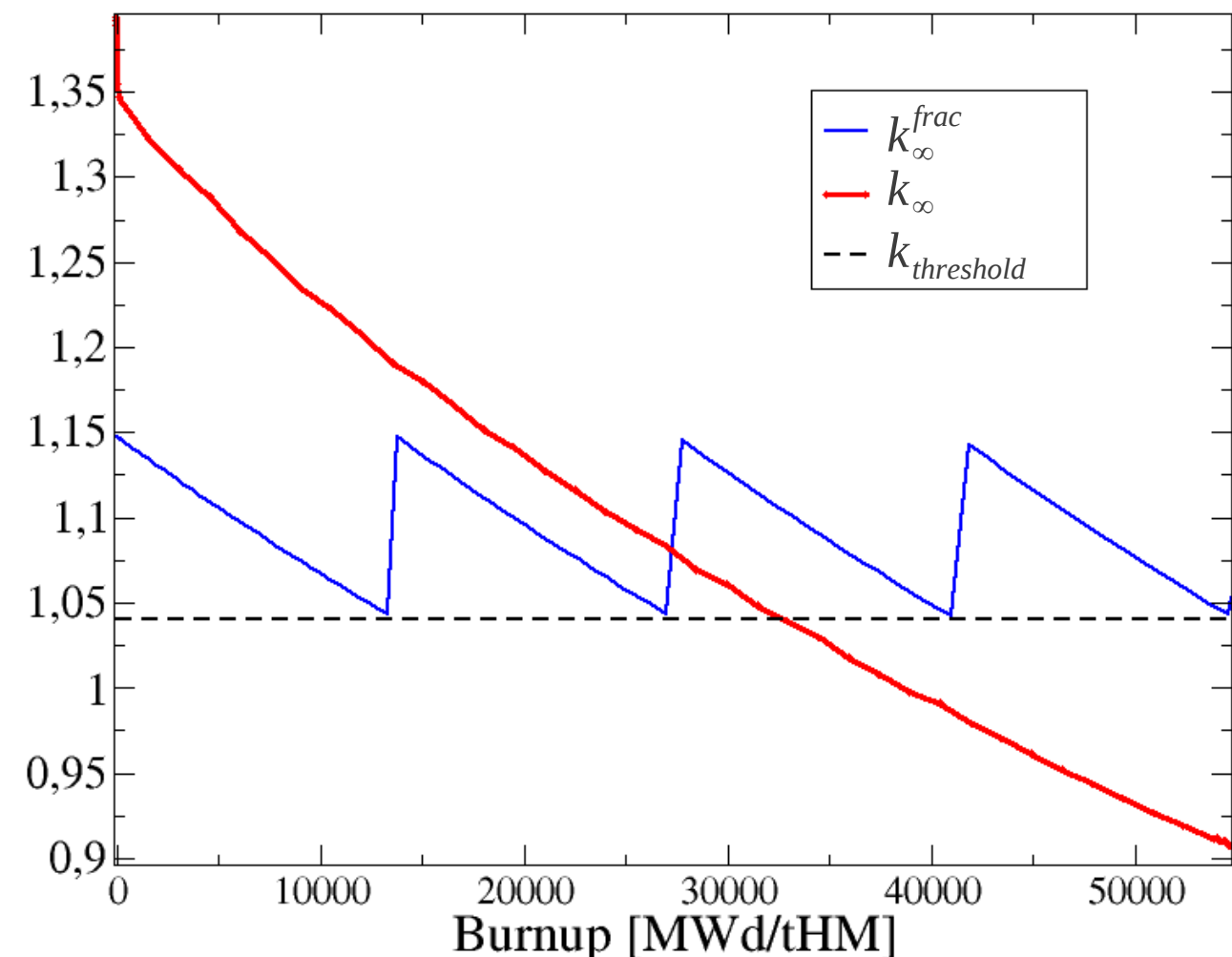
For PWR : $N = 3$ or 4 .

How to mimic batch management with infinite calculation ?

Considering that the behavior of an assembly isn't impacted by its surrounding media, we defined the average k_{∞} over the batches as :

$$\langle k_{\infty} \rangle^{batch}(t) = \frac{1}{N} \sum_{i=0}^{N-1} k_{\infty}\left(t + \frac{iT}{N}\right)$$

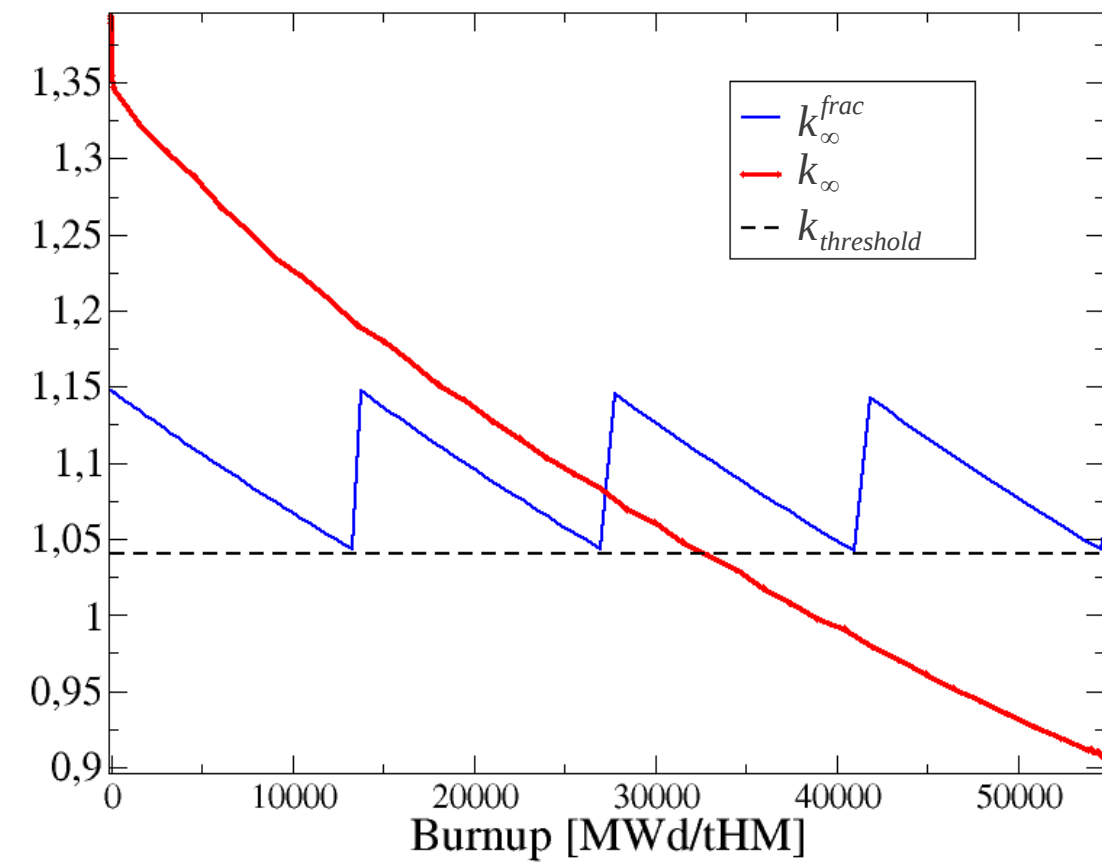
T : Irradiation time (N loading/unloading)



The averaged k_{∞} model

$$\langle k_{\infty} \rangle^{batch}(t) = \frac{1}{N} \sum_{i=0}^{N-1} k_{\infty}\left(t + \frac{iT}{N}\right)$$

T : Irradiation time (N loading/unloading)



The averaged k_{∞} model

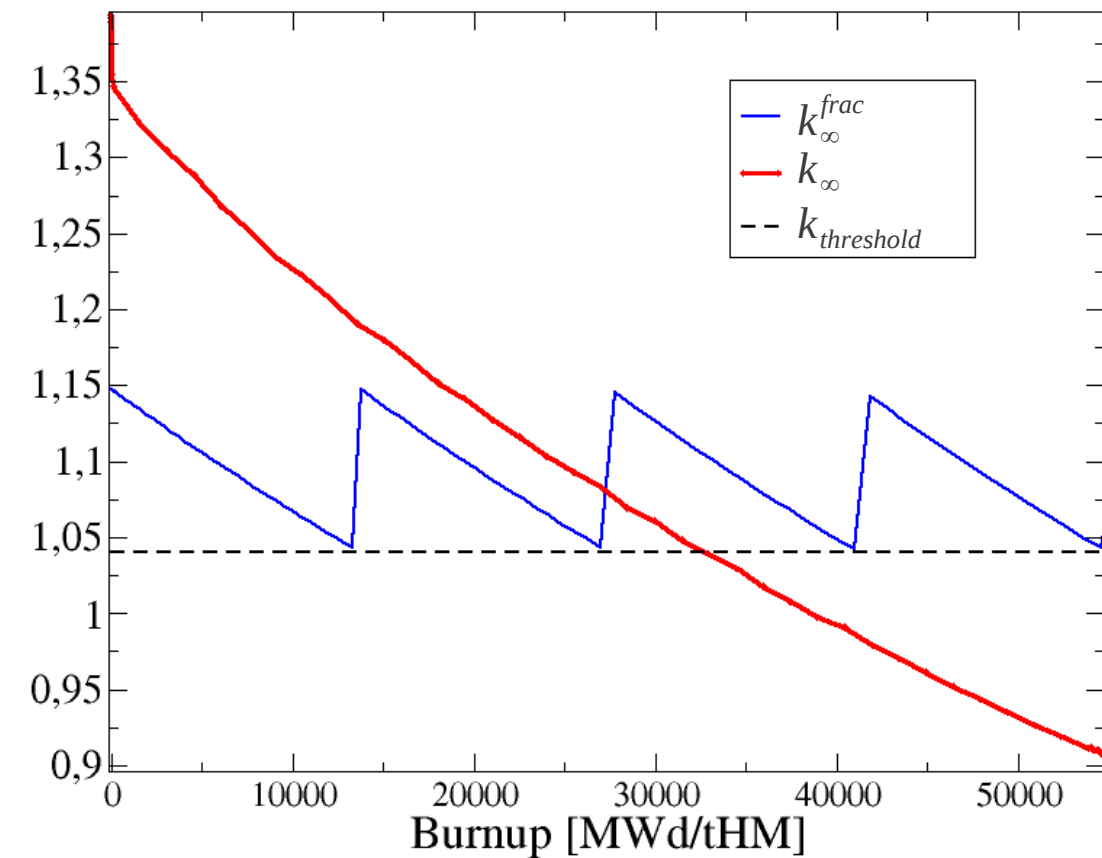
$$\langle k_{\infty} \rangle^{batch}(t) = \frac{1}{N} \sum_{i=0}^{N-1} k_{\infty}\left(t + \frac{iT}{N}\right)$$

T : Irradiation time (N loading/unloading)

The reactor has to verify :

$$k_{eff} = 1 \quad \forall t \in [0, T]$$

$$\rightarrow \langle k_{\infty} \rangle^{batch} = 1 + Leaks + CRods$$



The averaged k_{∞} model

$$\langle k_{\infty} \rangle^{batch}(t) = \frac{1}{N} \sum_{i=0}^{N-1} k_{\infty}(t + \frac{iT}{N})$$

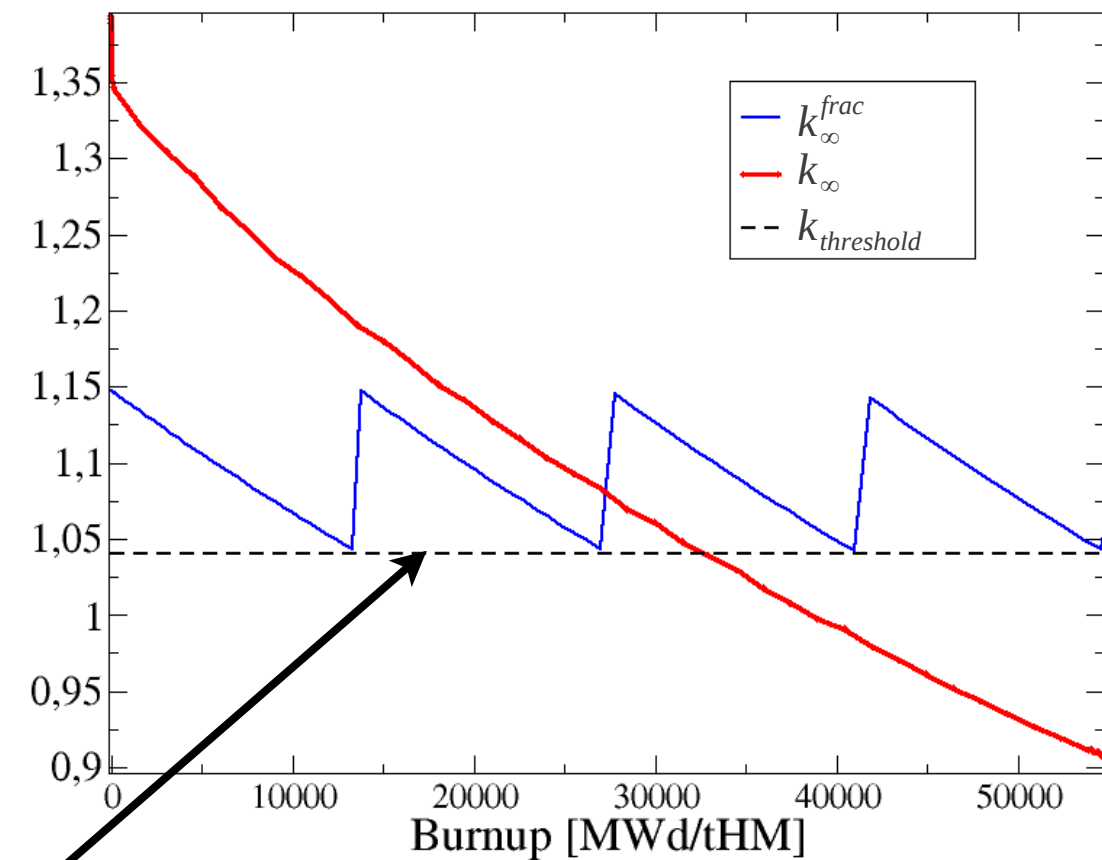
T : Irradiation time (N loading/unloading)

The reactor has to verify :

$$k_{eff} = 1 \quad \forall t \in [0, T]$$

$$\rightarrow \langle k_{\infty} \rangle^{batch} = 1 + Leaks + CRods$$

$$\langle k_{\infty} \rangle^{batch} = k_{threshold}$$



The averaged k_{∞} model

$$\langle k_{\infty} \rangle^{batch}(t) = \frac{1}{N} \sum_{i=0}^{N-1} k_{\infty}(t + \frac{iT}{N})$$

T : Irradiation time (N loading/unloading)

The reactor has to verify :

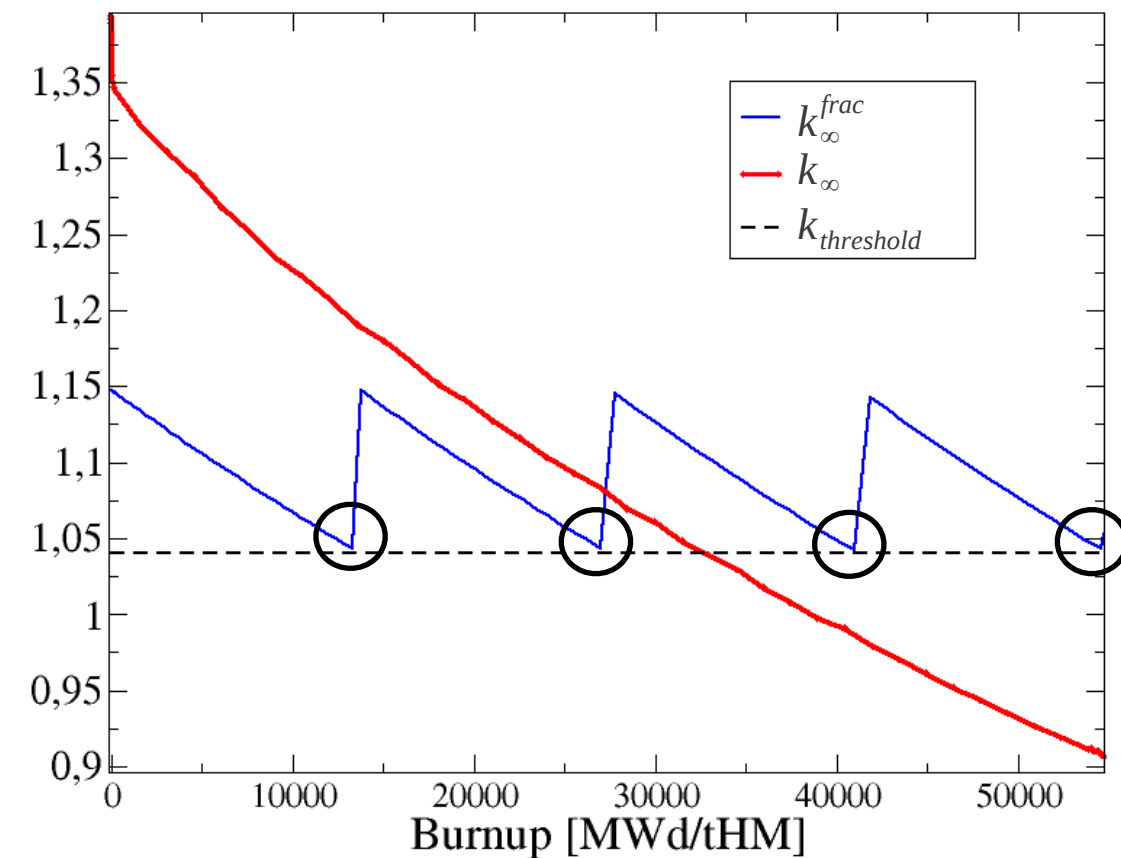
$$k_{eff} = 1 \quad \forall t \in [0, T]$$

$$\rightarrow \langle k_{\infty} \rangle^{batch} = 1 + Leaks + CRods$$

$$\langle k_{\infty} \rangle^{batch} = k_{threshold}$$

as [boron] is kept constant in simulation the criticality conditions is :

$$\langle k_{\infty} \rangle^{batch}(T/N) = \langle k_{\infty} \rangle^{batch}(2T/N) = \dots = k_{threshold}$$



The averaged k_{∞} model

The plutonium content in a fresh fuel is such as the criticality condition is verified :

Criticality condition :

$$\langle k_{\infty} \rangle^{batch} (T/N) = k_{threshold}$$

The time T is the maximum irradiation time (Burnup) a given fuel can reach : BU_{max} (Given by user)

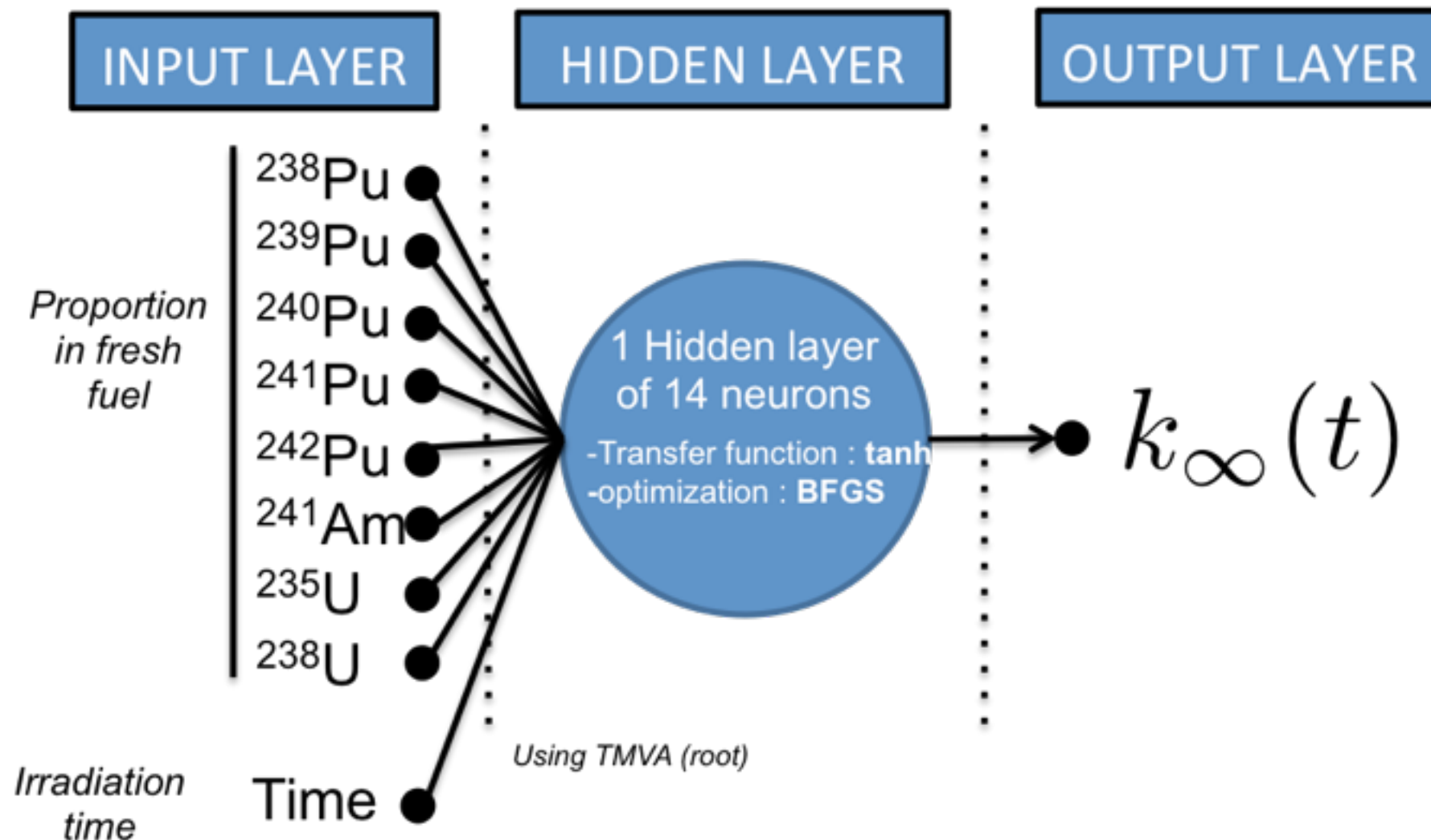
Method used to find maximum average discharged burnup in candu & pwr :

Nuttin, A., et al. "Comparative analysis of high conversion achievable in thorium-fueled slightly modified CANDU and PWR reactors." Annals of Nuclear Energy 40.1 (2012): 171-189.

This model involves to build :

- a $k_{\infty}(t)$ predictor : $\hat{k}_{\infty}(t)$
- an algorithm to find the Pu content according to the criticality condition

$\hat{k}_{\infty}(t)$: Artificial neural network (ANN) approach

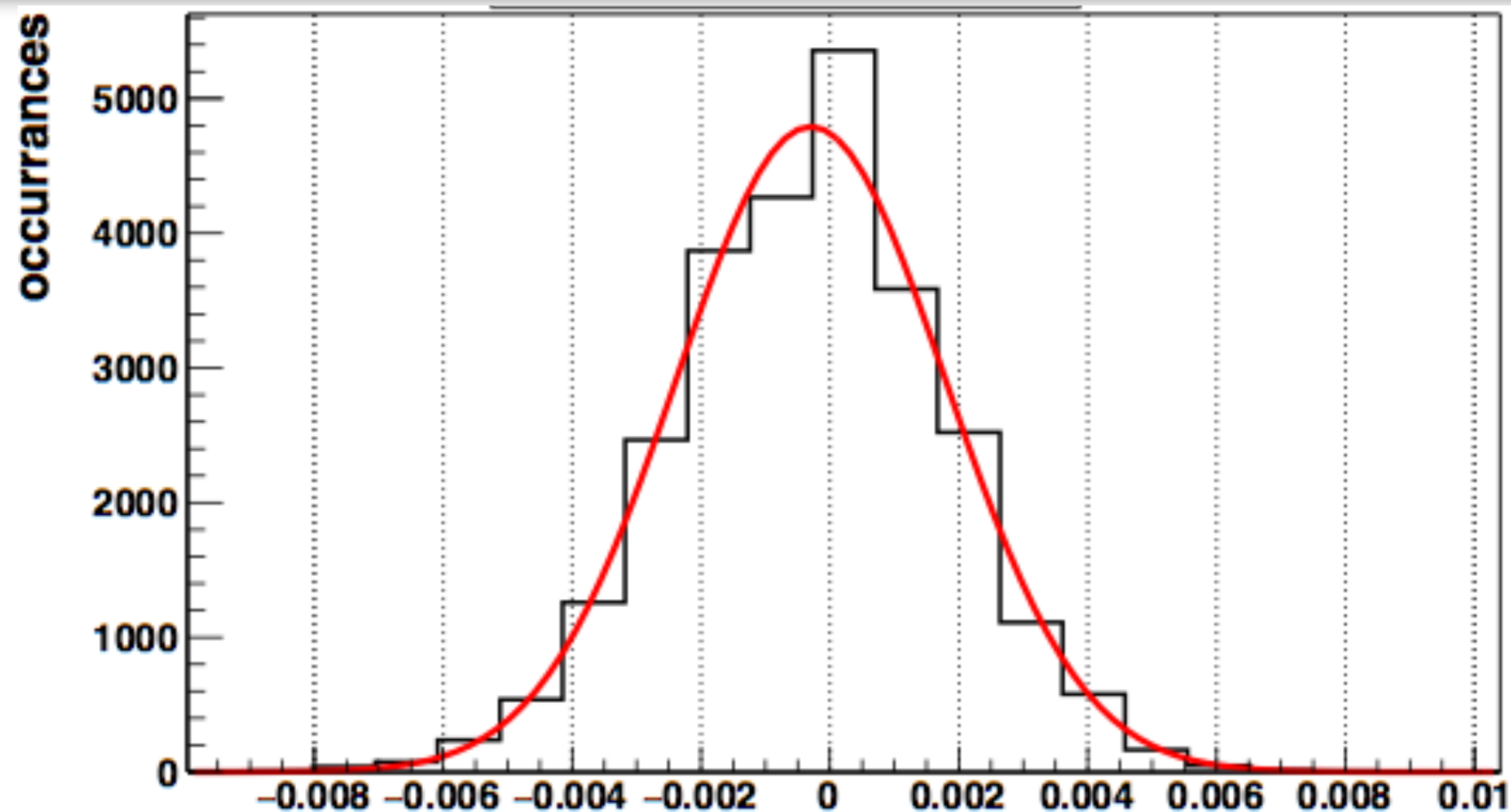


Total number of events :

5000 depletion calculation & 11 time step each : 55000 events.

Train with half (randomly picked) and tested with the other half

$\hat{k}_{\infty}(t)$ Results of the ANN testing procedure



Mean error : 30 pcm
Std. dev. on error: 200 pcm

$\frac{\hat{k}_{\infty}(t) - k_{\infty}(t)}{k_{\infty}(t)}$
MCNP Statistical error : ~ 150 pcm

$\hat{k}_{\infty}(t)$ Results of the ANN testing procedure



Mean error : 30 pcm
Std. dev. on error: 200 pcm

MCNP Statistical error : ~ 150 pcm

- Model algorithm

Which Pu content

$$\%Pu =$$

- Model algorithm

Which Pu content to reach a given burnup

$$\%Pu = f(BU_{target},$$

Inputs

BU_{target} : wanted burnup

- Model algorithm

Which Pu content to reach a given burnup with a given batch management,

$$\%Pu = f(BU_{target}, N,$$

Inputs

BU_{target} : wanted burnup

N : # of batches

- Model algorithm

Which Pu content to reach a given burnup with a given batch management, knowing isotopic compositions of Pu et U

$$\boxed{\%Pu = f(BU_{target}, N, \vec{Pu}, \vec{U}, k_{th})}$$

{

}

Inputs

BU_{target} : wanted burnup

N : # of batches

\vec{Pu} : Fissile composition

\vec{U} : Fertile composition

- Model algorithm

Which Pu content to reach a given burnup with a given batch management, knowing isotopic compositions of Pu et U

$$\%Pu = f(BU_{target}, N, \vec{P_u}, \vec{U}, k_{th})$$

```
{
    %Pu = P0           //Initialization
```

```
do
{
    varying BU until <k>(BU/N) = kth
    using eq 1 & 2 : BUmax
```

```
}
```

Inputs

BU_{target} : wanted burnup

N : # of batches

$\vec{P_u}$: Fissile composition

\vec{U} : Fertile composition

eq 1 :

$$\langle k_{\infty} \rangle^{batch}(t) = \frac{1}{N} \sum_i^N k_{\infty}(t + \frac{iT}{N})$$

eq 2 : $\hat{k}_{\infty}(BU, \vec{N})$

$$\vec{N} = \%Pu \vec{P_u} + (1 - \%Pu) \vec{U}$$

PWR-MOX fresh fuel construction

- Model algorithm

Which Pu content to reach a given burnup with a given batch management, knowing isotopic compositions of Pu et U

$$\%Pu = f(BU_{target}, N, \vec{P}_u, \vec{U}, k_{th})$$

```
{
    %Pu = P0           //Initialization

do
{
    varying BU until <k>(BU/N) = kth
    using eq 1 & 2 : BUmax

    if(BUmax > BUtarget)
        decrease %Pu    //%Pu too high
    else
        increase %Pu     //%Pu too low
    }
}
```

Inputs

BU_{target} : wanted burnup

N : # of batches

\vec{P}_u : Fissile composition

\vec{U} : Fertile composition

eq 1 :

$$\langle k_{\infty} \rangle^{batch}(t) = \frac{1}{N} \sum_i^N k_{\infty}(t + \frac{iT}{N})$$

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PWR-MOX fresh fuel construction

- Model algorithm

Which Pu content to reach a given burnup with a given batch management, knowing isotopic compositions of Pu et U

$$\%Pu = f(BU_{target}, N, \vec{P}_u, \vec{U}, k_{th})$$

```
{
    %Pu = P0           //Initialization

do
{
    varying BU until <k>(BU/N) = kth
    using eq 1 & 2 : BUmax

    if(BUmax > BUtarget)
        decrease %Pu    //%Pu too high
    else
        increase %Pu    //%Pu too low
    }
    while ( BUmax != BUtarget ) //accept %Pu or
                                continue looping
return %Pu
}
```

Inputs

BU_{target} : wanted burnup

N : # of batches

\vec{P}_u : Fissile composition

\vec{U} : Fertile composition

eq 1 :

$$\langle k_{\infty} \rangle^{batch}(t) = \frac{1}{N} \sum_i^N k_{\infty}(t + \frac{iT}{N})$$

eq 2 : $\hat{k}_{\infty}(BU, \vec{N})$

$$\vec{N} = \%Pu \vec{P}_u + (1 - \%Pu) \vec{U}$$

Benchmark with COSI PWR-MOX Model

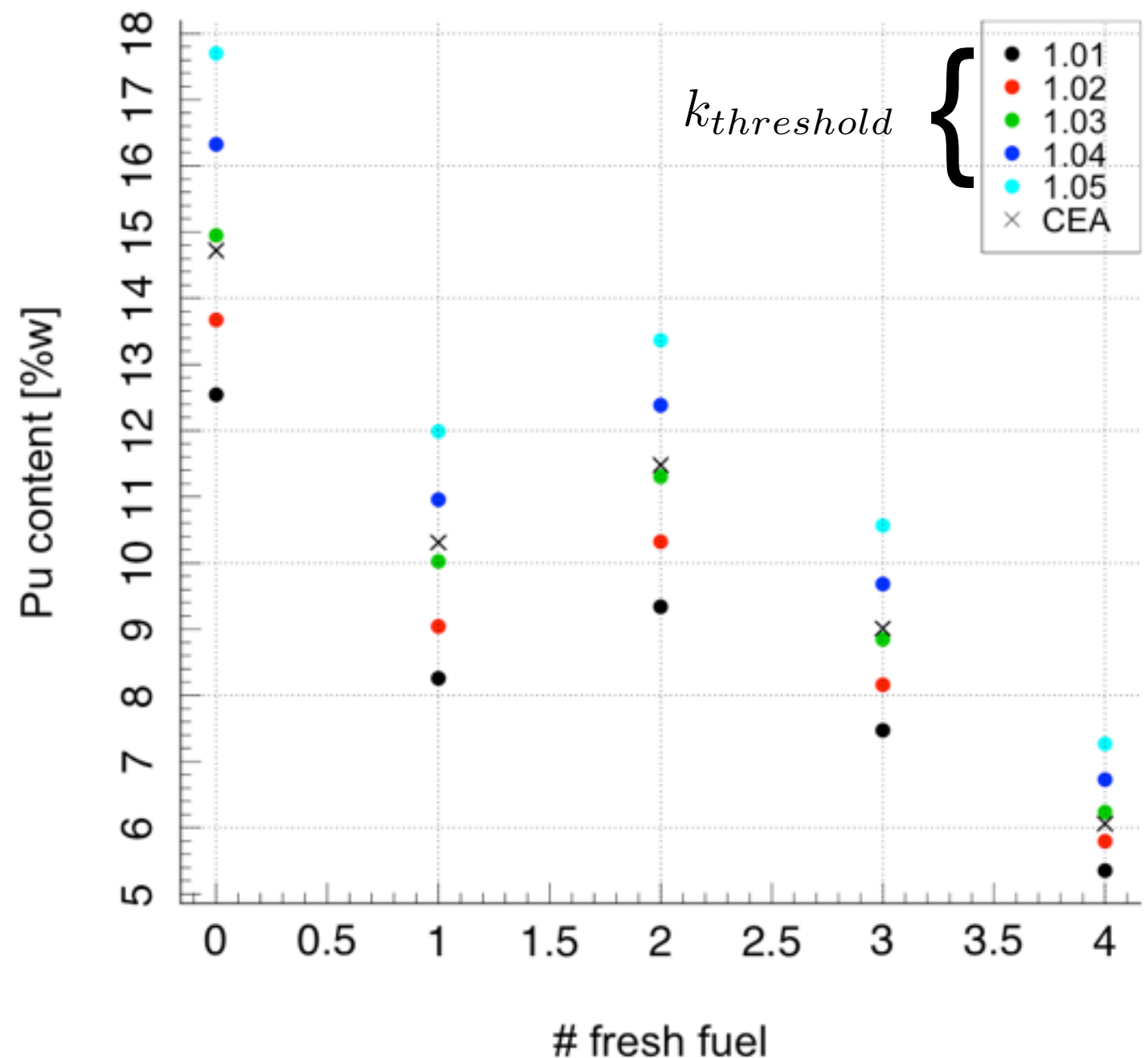
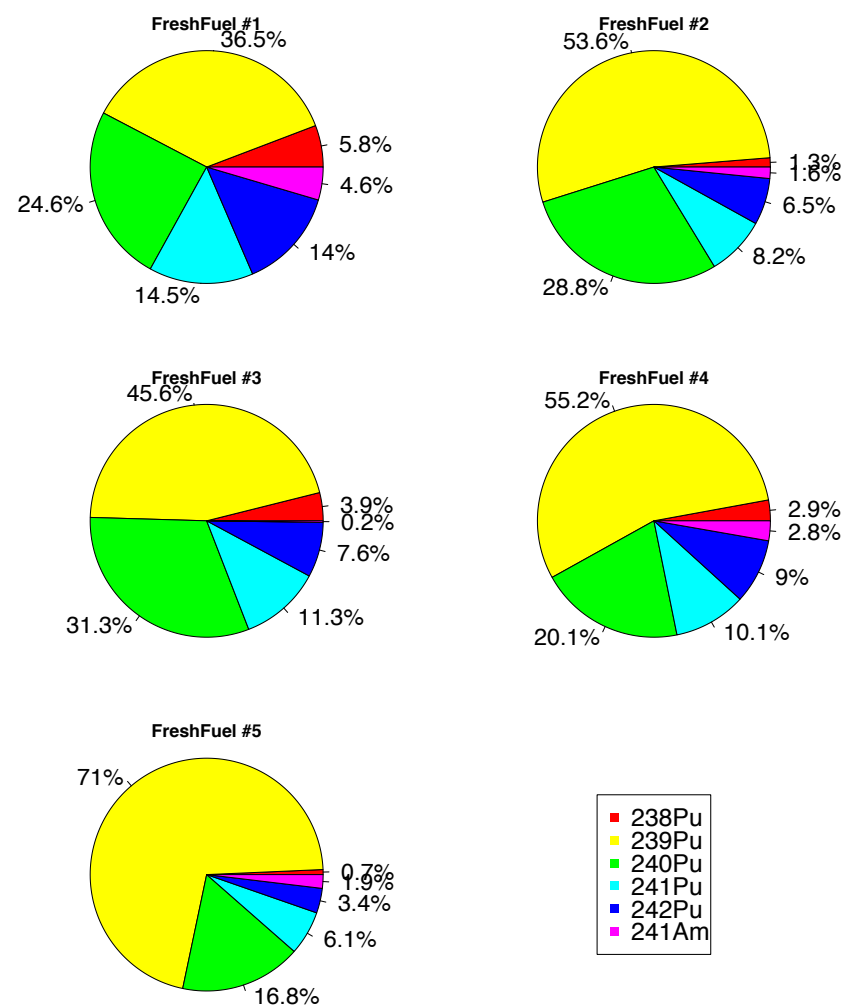
Work accomplished in the framework of a CEA/CNRS collaboration (2014)

Pu content predicted by the two codes for 5 different Pu isotopy :

$$N = 3$$

$$k_{threshold} = [1.01; 1.05] \quad \vec{P}_u = \text{variable}$$

$$BU_{target} = 50 \text{ GWd/t} \quad \vec{U} = 0.25\% {}^{235}\text{U}$$



Conclusions & outlooks

Mean cross sections interpolation :

- ➔ Good precision of the ANN approach on $\langle \sigma \rangle$ prediction. For PWR-MOX :
 - (n,f) : std. dev. on error < 1 %
 - (n, γ) : std. dev. on error < 2 %
 - (n,2n) : std. dev. on error < 5 % (for actinides)Discrepancy due to Monte Carlo statistical error
- ➔ Performances in a depletion calculation:
 - Error (compared as MURE calc.) ~3% max @ EOC for main actinides
 - Computational time ~30 s

This methodology is used for all reactor description in CLASS

Conclusions & outlooks

Fresh fuel construction

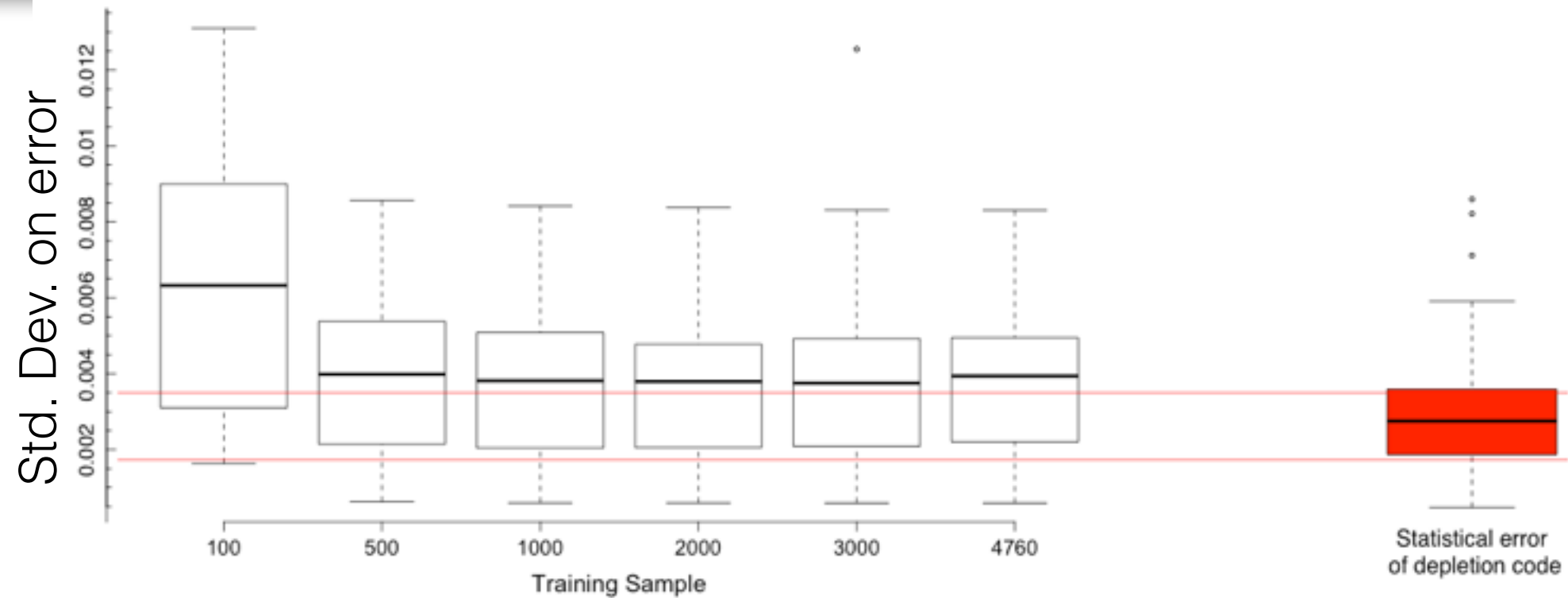
➔ PWR-MOX model :

- Based on batch averaged k_{infinite} .
- $k_{\text{infinite}}(t)$ prediction using MLP (std. dev. 200pcm)
- Flexible : possibility to change $k_{\text{threshold}}$ and number of batches
- Pu content prediction close to COSI(CEA) with $k_{\text{threshold}} = 1.03$

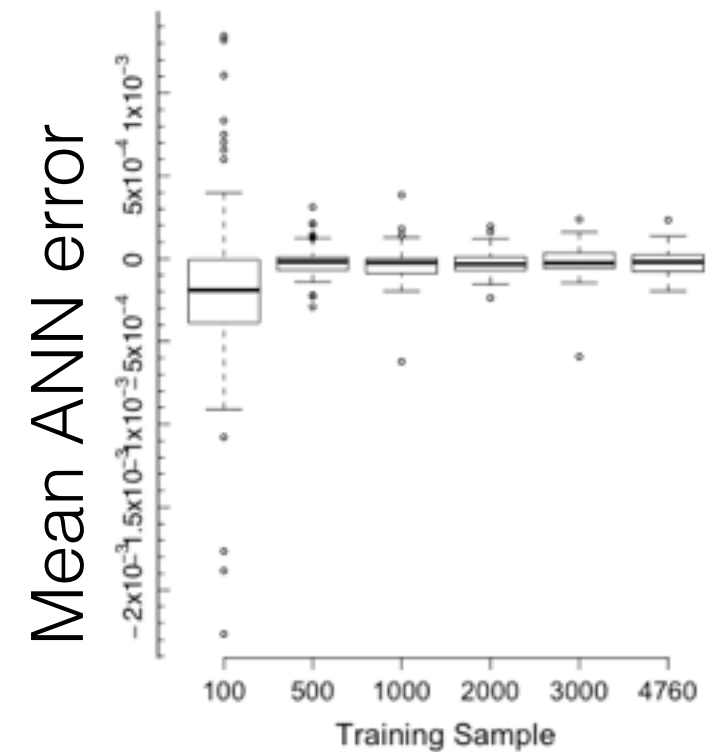
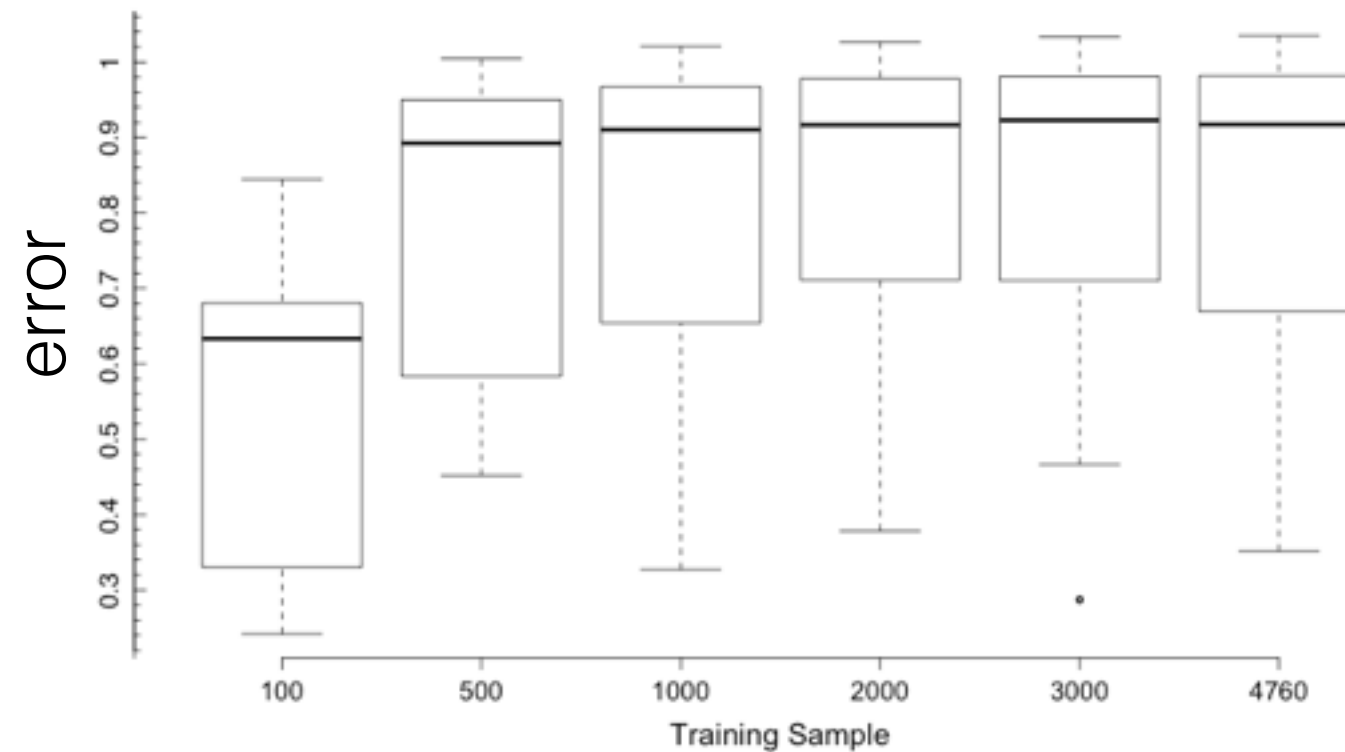
➔ List of CLASS equivalence models :

Model Name	Reactor	Fuel	Spectrum	Target Burnup	Batch Management	Regression Method	Predicted value	Input parameters
PWR_POL_UO2	PWR	UOX	Thermal	any	fixed	Polynomial	% 235U	Target burnup
PWR_MLP_MOX	PWR	MOX	Thermal	any	fixed	MLP	Pu content	Target burnup
PWR_MLP_MOXAm	PWR	MOX-Am	Thermal	any	fixed	MLP	(Pu+Am) content	Target burnup
MLP_Kinf	any (not breeder)	any		any	any	MLP	K_{∞}	Target BU / Kthreshold/ N Batch
PWR_MLP_MOXEUS	PWR	MOX EUS	Thermal	any	any	MLP	K_{∞}	Target BU / Kthreshold/ N Batch/ Max Pu Content
FBR_BakerAndRoss	any (breeder)	MOX	fast	fixed	none	Linear (pert. theory)	Pu content	reactivity weights
FBR_MLP_Keff	any (breeder)	any	fast	fixed	none	MLP	keff(t=0)	none

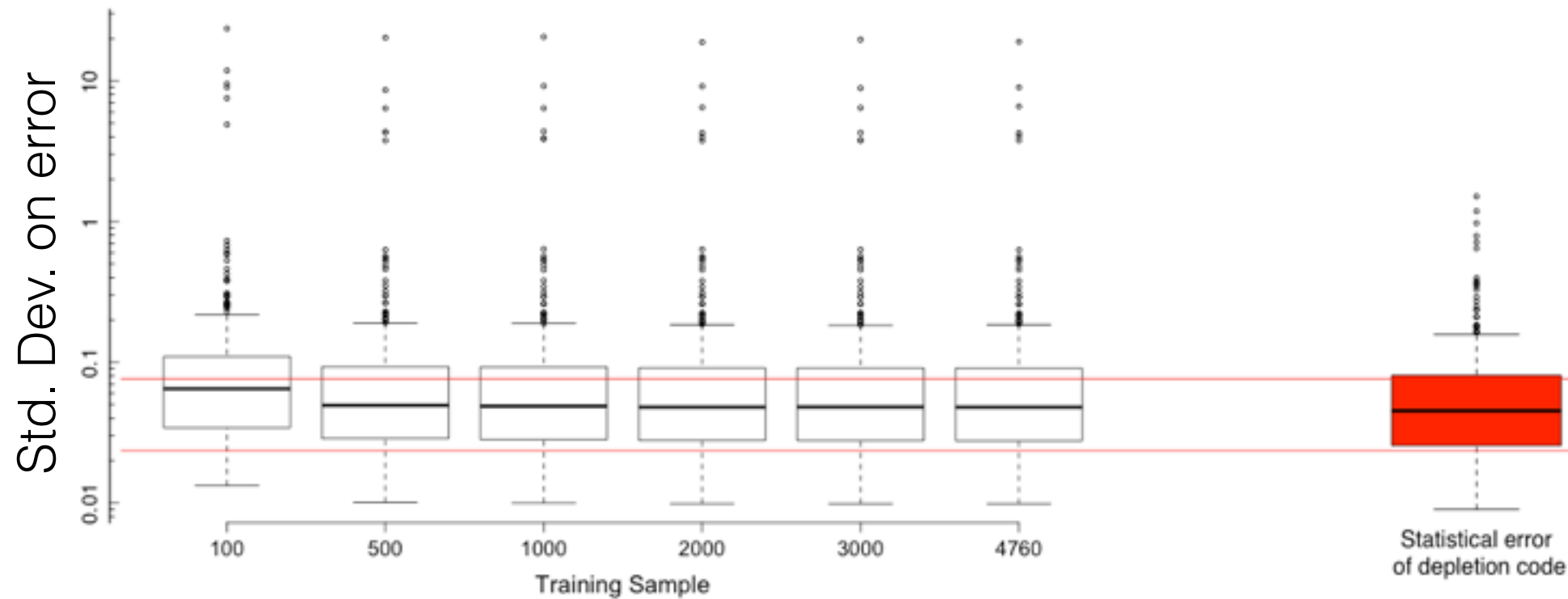
Testing performances : Fission prediction



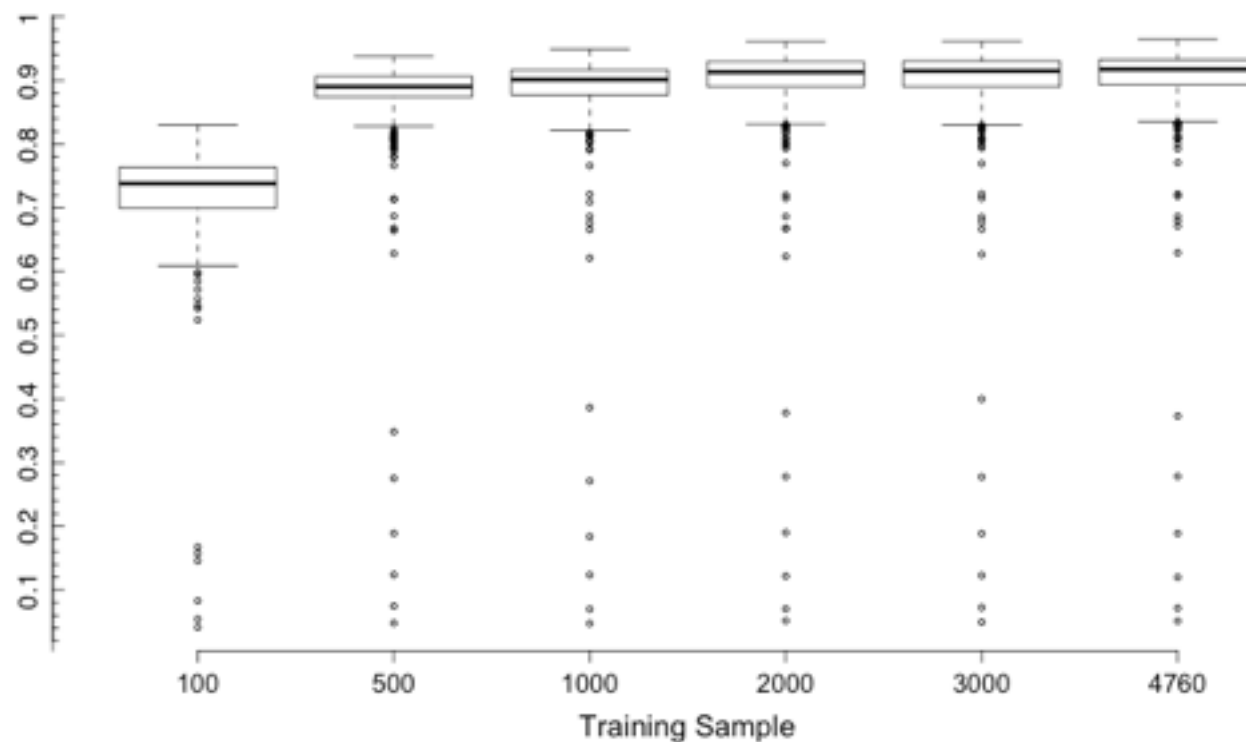
Proportion of error
due to statistical
error



Testing performances : (n,2n) prediction



Proportion of error
due to statistical
error



Mean ANN error

