

Impact of the mean pressure profile of galaxy clusters on tSZ cosmological constraints

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Observing the millimeter Universe with the NIKA2 camera

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Content

- I - Cosmology from the tSZ power spectrum**
- II - Current status of tSZ cosmology**
- III - Mean pressure profile of the cluster population**
- IV - Analysis of the *Planck* tSZ power spectrum**
- V - Impact of a pressure profile modification on σ_8 and Ω_m**

Content

I - Cosmology from the tSZ power spectrum

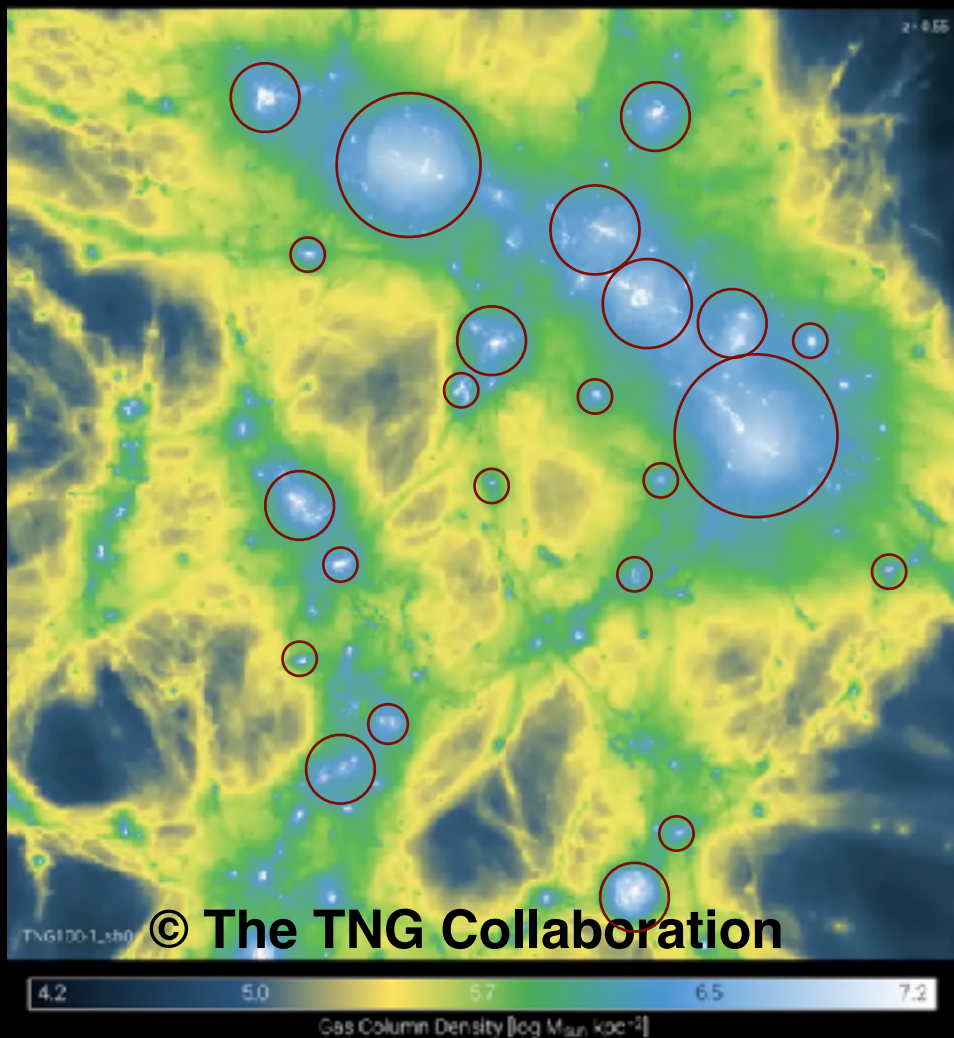
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Cosmology from the tSZ power spectrum



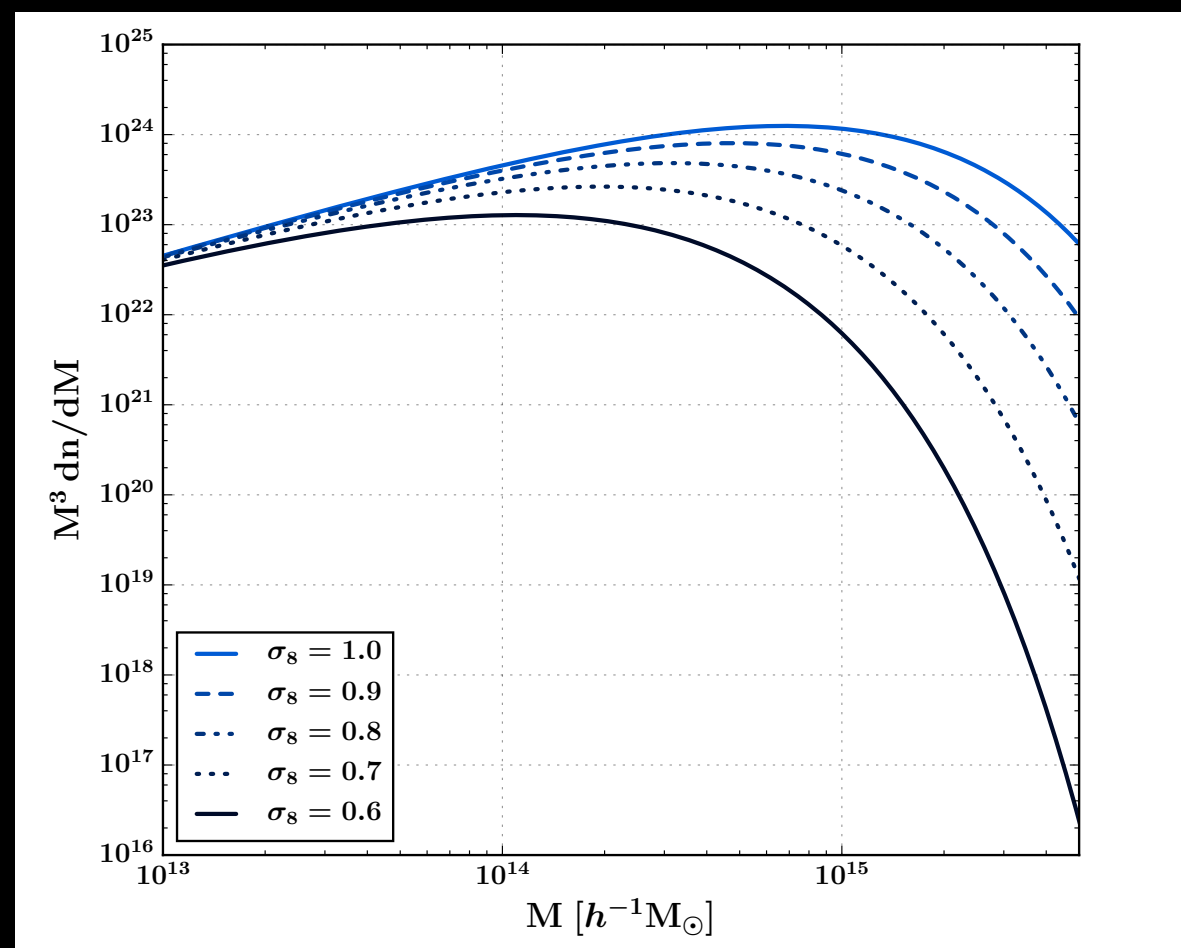
Hierarchical structure formation:

- Little things collapse first, big things collapse later
- The Halo model: spherical collapse + virialization
- Self-similar model: cluster properties given by gravitational physics

Distribution of galaxy clusters:

- Mass function $\frac{d^2n}{dMdz}$
Number density of clusters per unit of mass and redshift
- Large amplitude variations for different σ_8 and Ω_m values

Halo mass function



Cosmology from the tSZ power spectrum

• Power spectrum of the tSZ effect: $C_\ell^{\text{tSZ}} = \int \frac{dV}{dzd\Omega} dz \int \frac{dn}{dM_{500}} \left| \frac{4\pi R_{500}}{\ell_{500}^2} \frac{\sigma_T}{m_e c^2} P_{500} I_{\mathcal{P}(\ell_{500})} \right|^2 dM_{500}$

Volume element
Mass function
Scaling parameter

2D Fourier transform of the mean pressure profile

With $I_{\mathcal{P}(\ell_{500})} = \int x^2 \frac{\sin(\ell x / \ell_{500})}{\ell x / \ell_{500}} \mathcal{P}(x) dx$

And $\mathcal{P}(x)$: the mean pressure profile

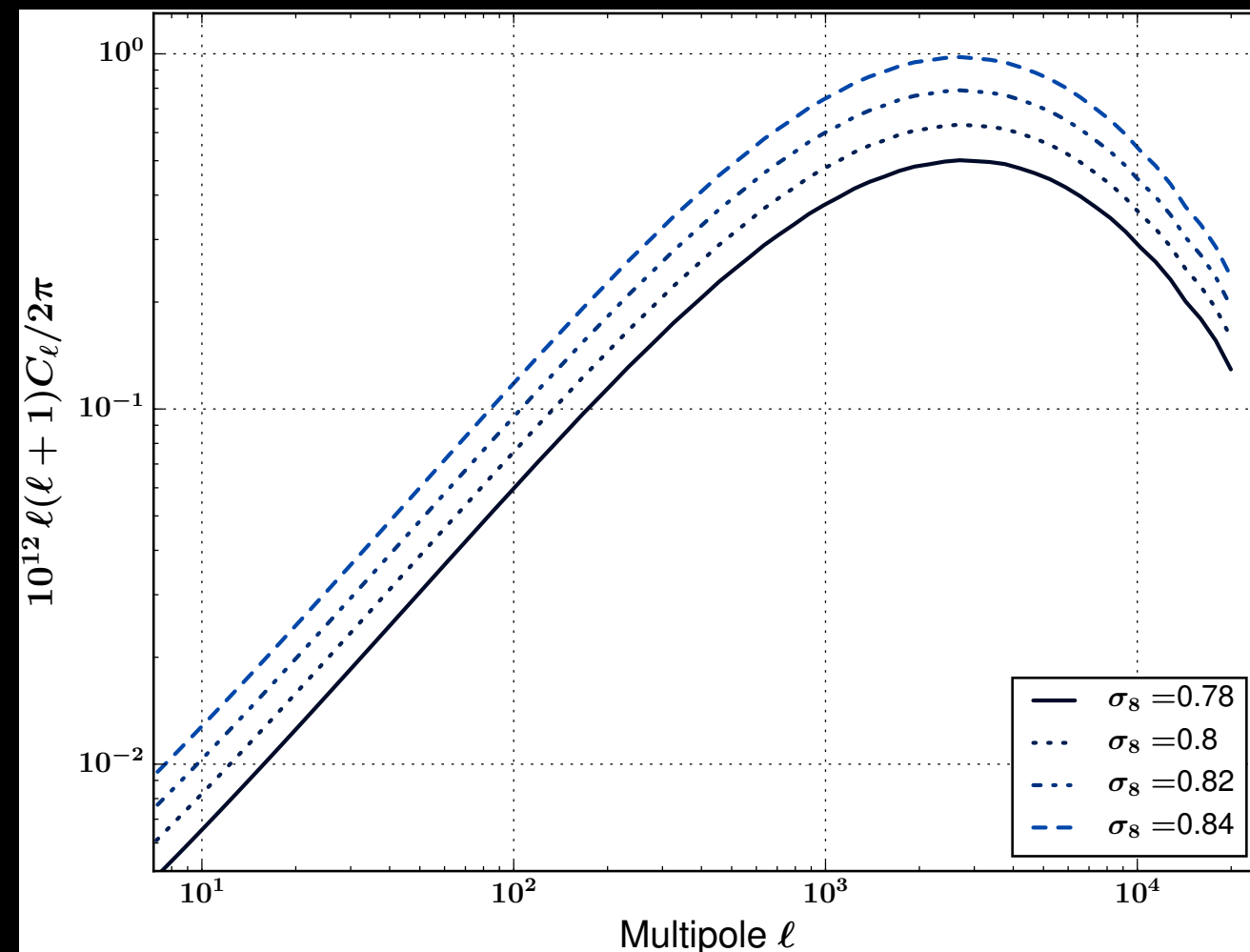
• Amplitude of the tSZ power spectrum depends on:

σ_8 and Ω_m : amplitude of the mass function

Hubble parameter h : volume element

Hydrostatic bias b : included in the scaling parameter

tSZ power spectrum



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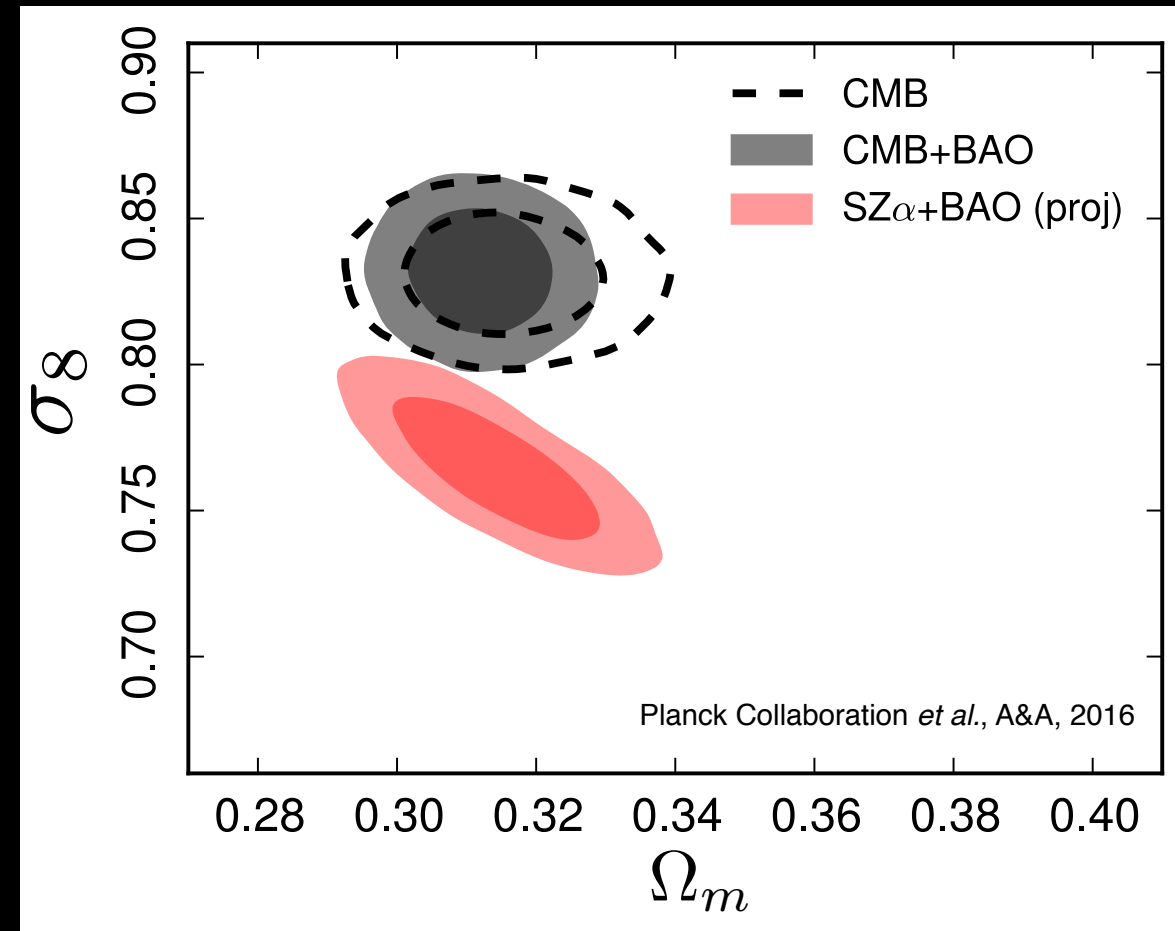
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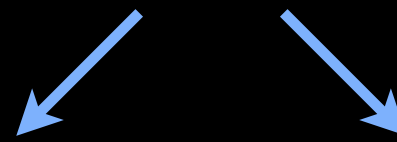
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Current status of tSZ cosmology



Tension between cosmological constraints from CMB and *Planck* cluster catalog for $b = 0.2$



Option 1: Limit in the standard Λ CDM model

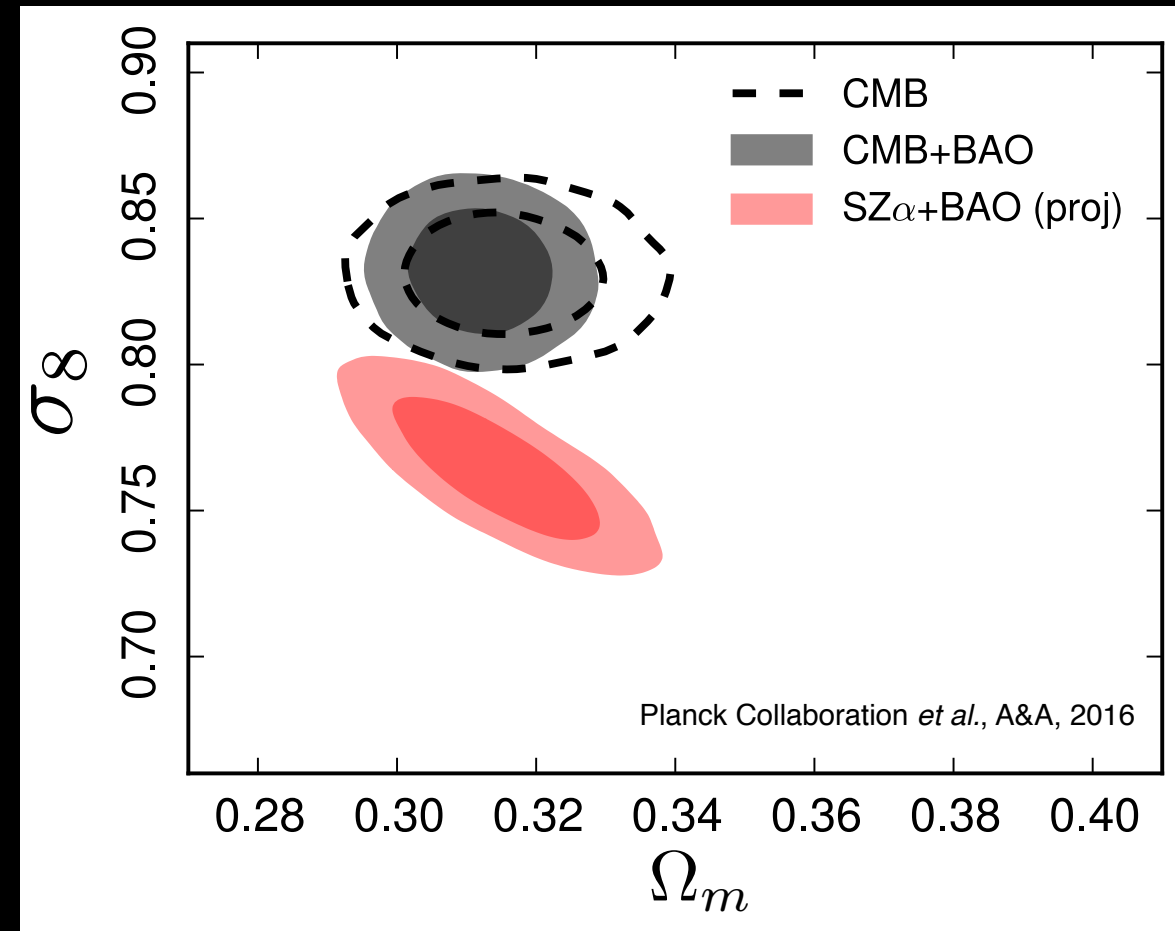
- Neutrino mass
- Modified gravity
- Etc.

Option 2 : Bias and systematic effects

- Wrong estimate of hydrostatic bias
- Pressure profile and scaling relation at $z \gtrsim 0.4$

1st Assumption: tension not due to limit in Λ CDM model

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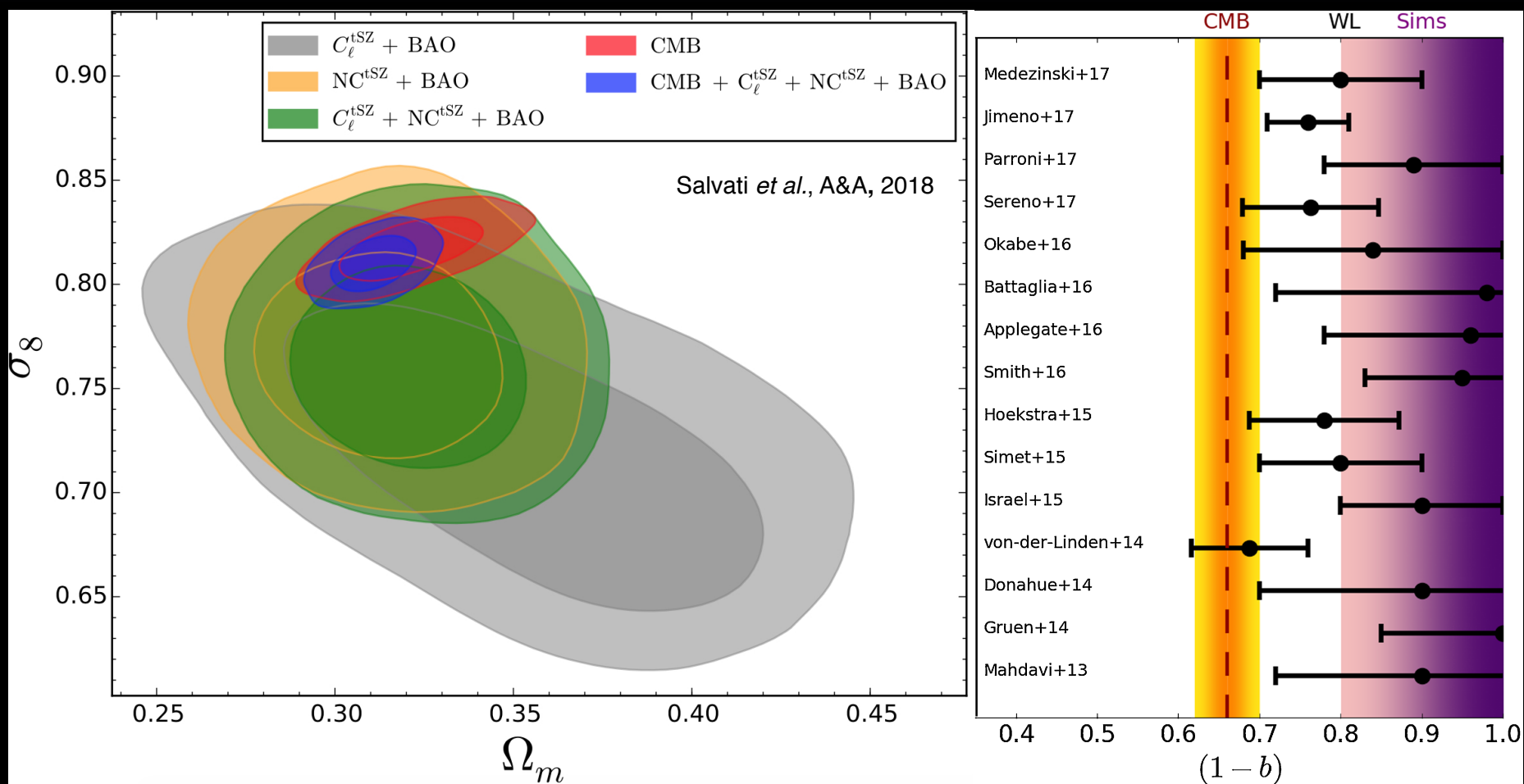
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Current status of tSZ cosmology



- **Most recent analyses:** - take into account new *Planck* cosmology
- take into account uncertainties on mass bias measurements

➔ **Tension between cosmological parameters is not significant**



- **Joint analysis CMB+clusters** ➔ $b \sim 0.4$ in tension with values from observations+simulations

2nd Assumption: tension not fully due to wrong estimate of hydrostatic bias

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Mean pressure profile of the cluster population

1 - Previous results

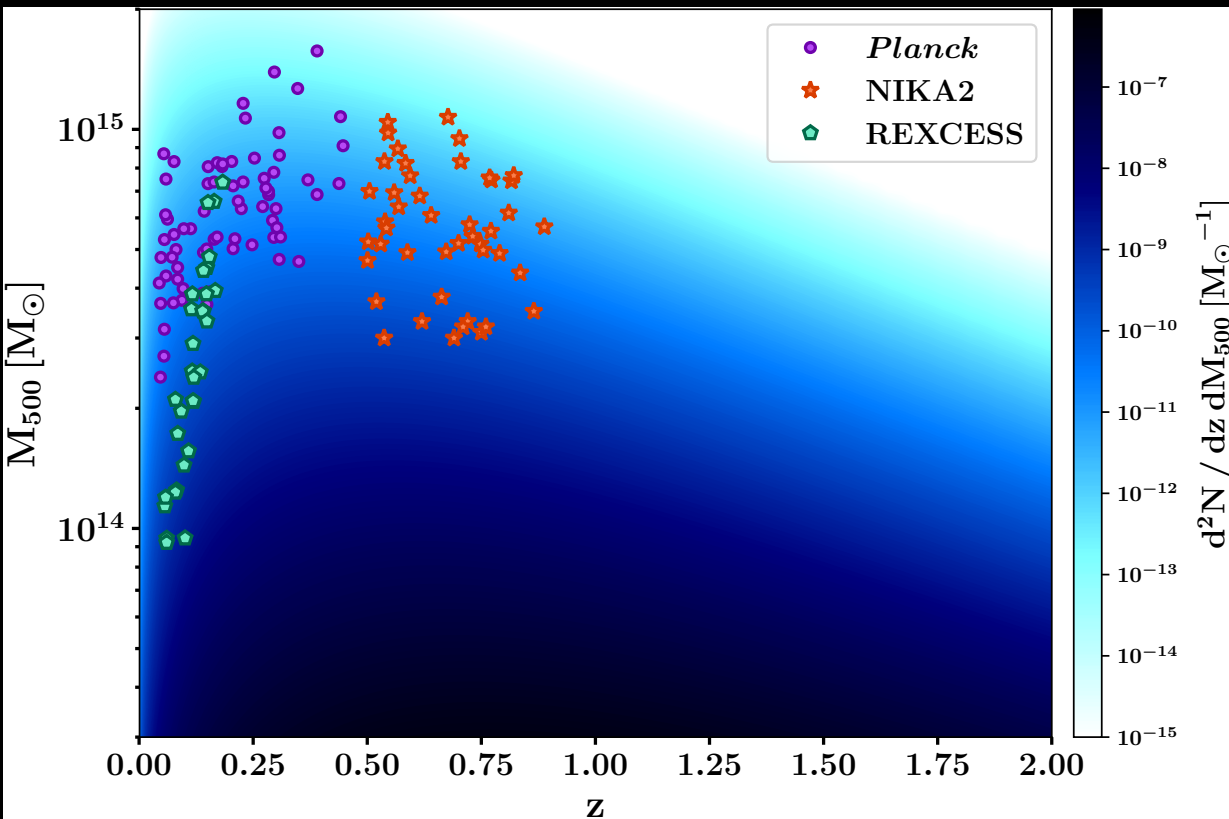
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Mean pressure profile of the cluster population

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Mean pressure profile of the cluster population



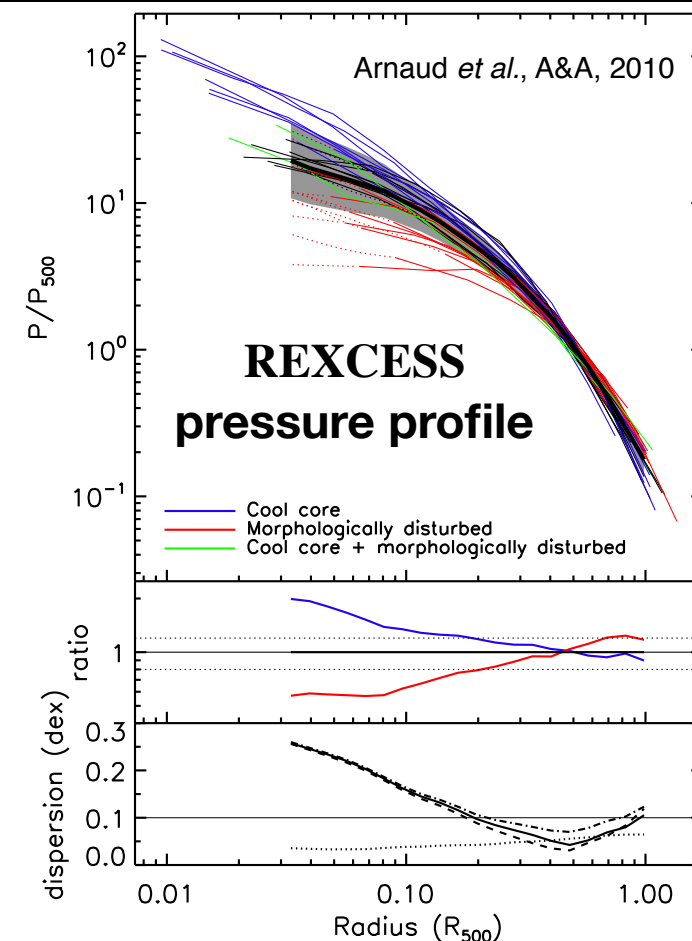
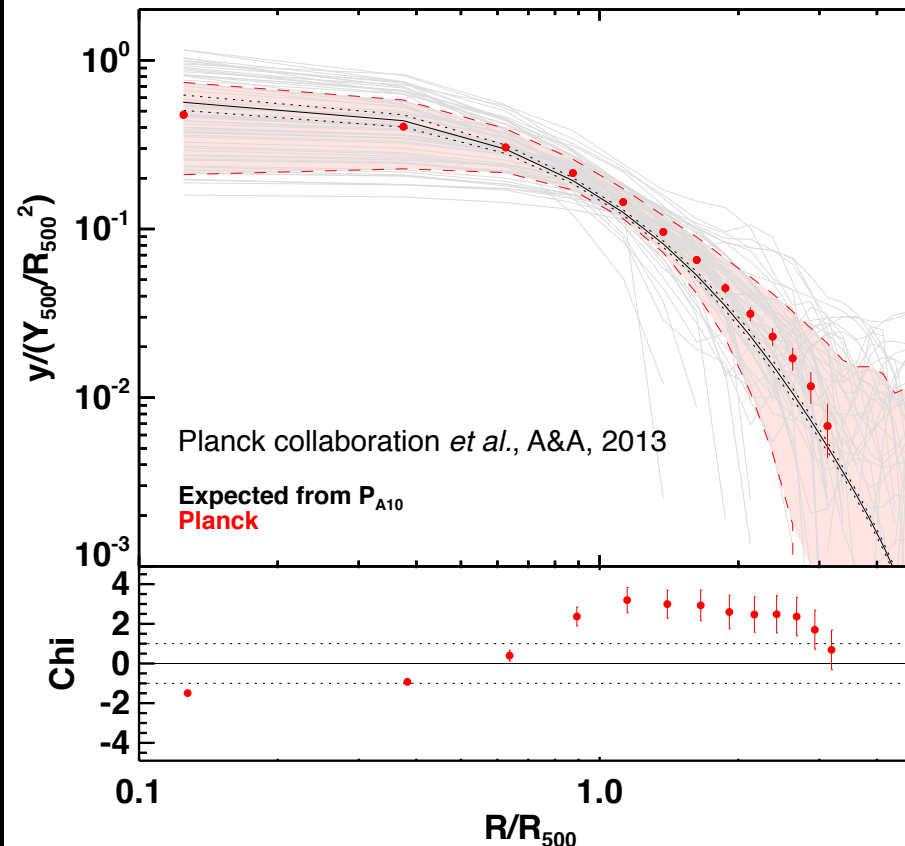
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- **Mean pressure profile:** amplitude of the tSZ power spectrum and shape at high ℓ
- **Most widely used profiles:** computed at high mass and low redshift $z \lesssim 0.4$

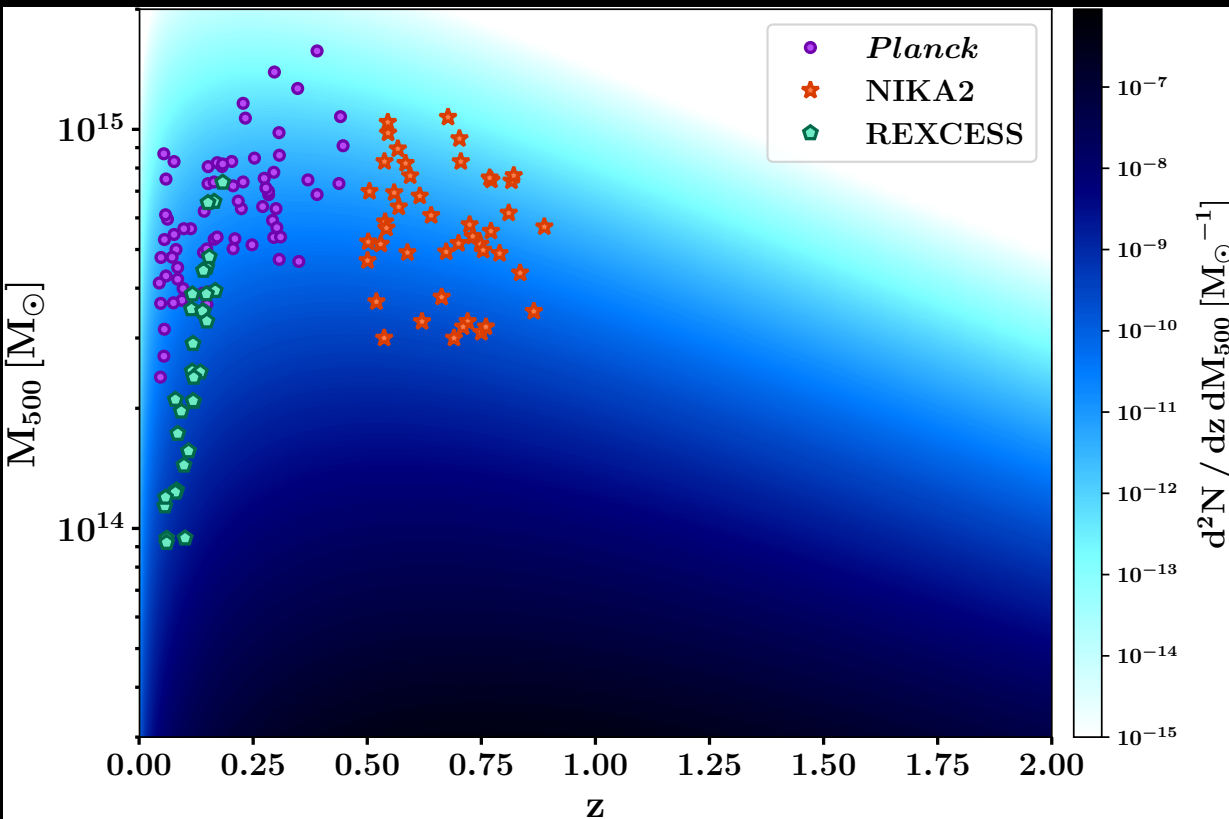
Potentially not representative of the cluster population

- Slight difference between outer slopes of *Planck* and REXCESS profiles
 → ICM thermodynamics in X and SZ
- **Redshift evolution:**
 - relaxed VS disturbed cores/morphologies
- **Importance of the intrinsic scatter:**
 - selection function, distribution skewness

Planck pressure profile



Mean pressure profile of the cluster population



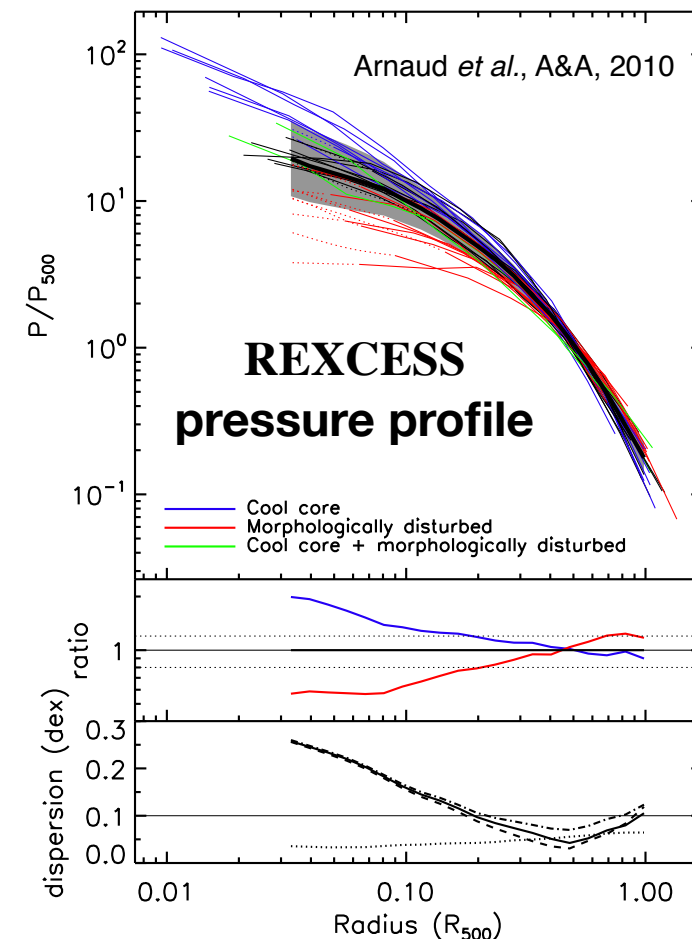
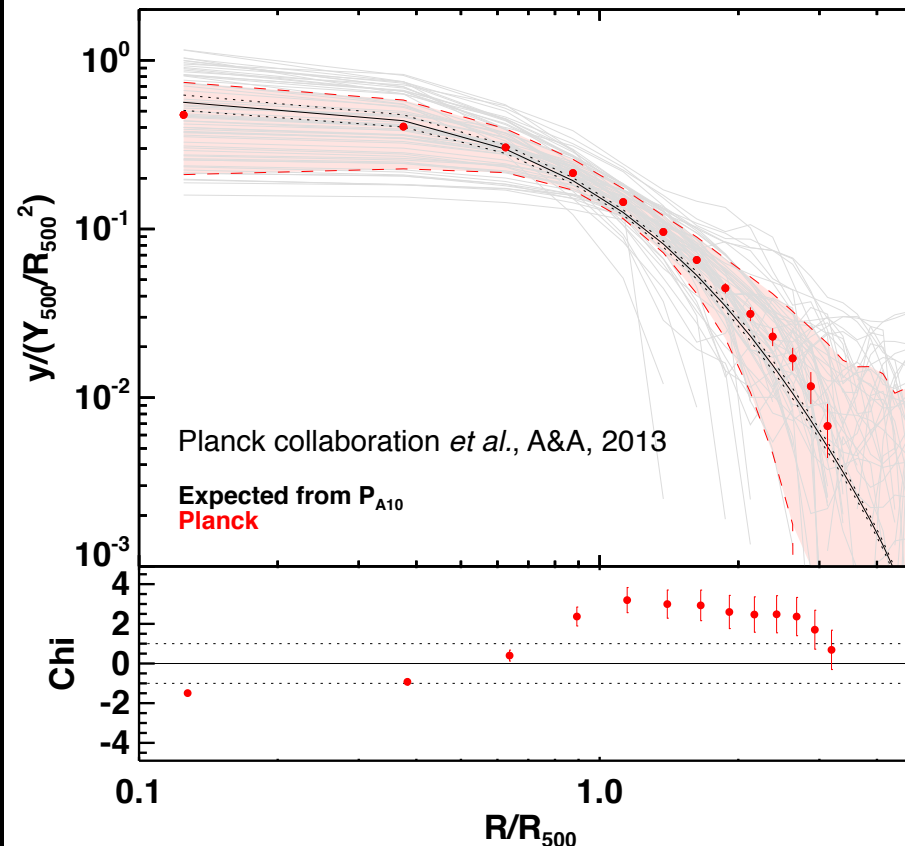
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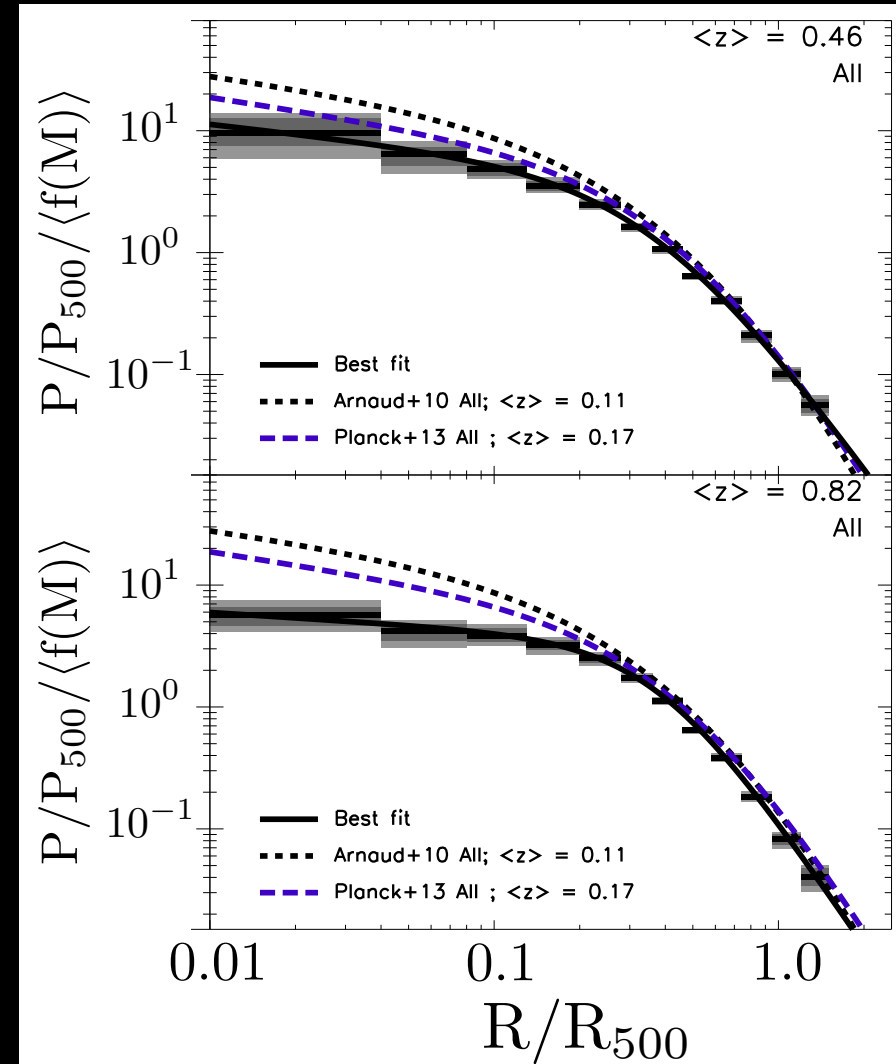
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Planck pressure profile



Mean pressure profile of the cluster population

Mean normalized pressure profiles



Eckert et al., A&A, 2013

Eckert et al., A&A, 2019

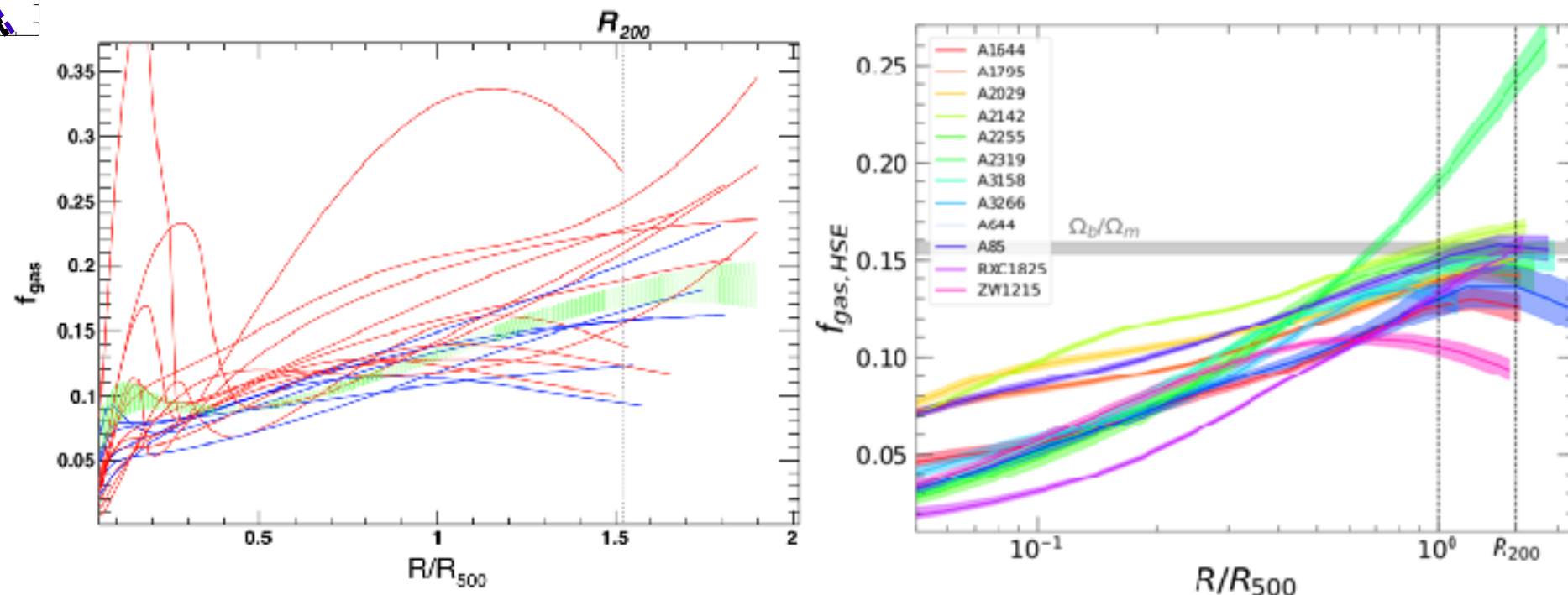
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 - In X-ray: ICM seems slightly cooler at high z (McDonald et al., ApJ, 2014)
 - In SZ: on-going NIKA2 SZ large program, 45 clusters at $0.5 < z < 0.9$
- Importance of the gas mass fraction:

$$\text{Hydrostatic mass: } M_{HSE}(r) \propto \frac{r^2}{n_e(r)} \times \frac{dP_e(r)}{dr}$$

ICM pressure
ICM density

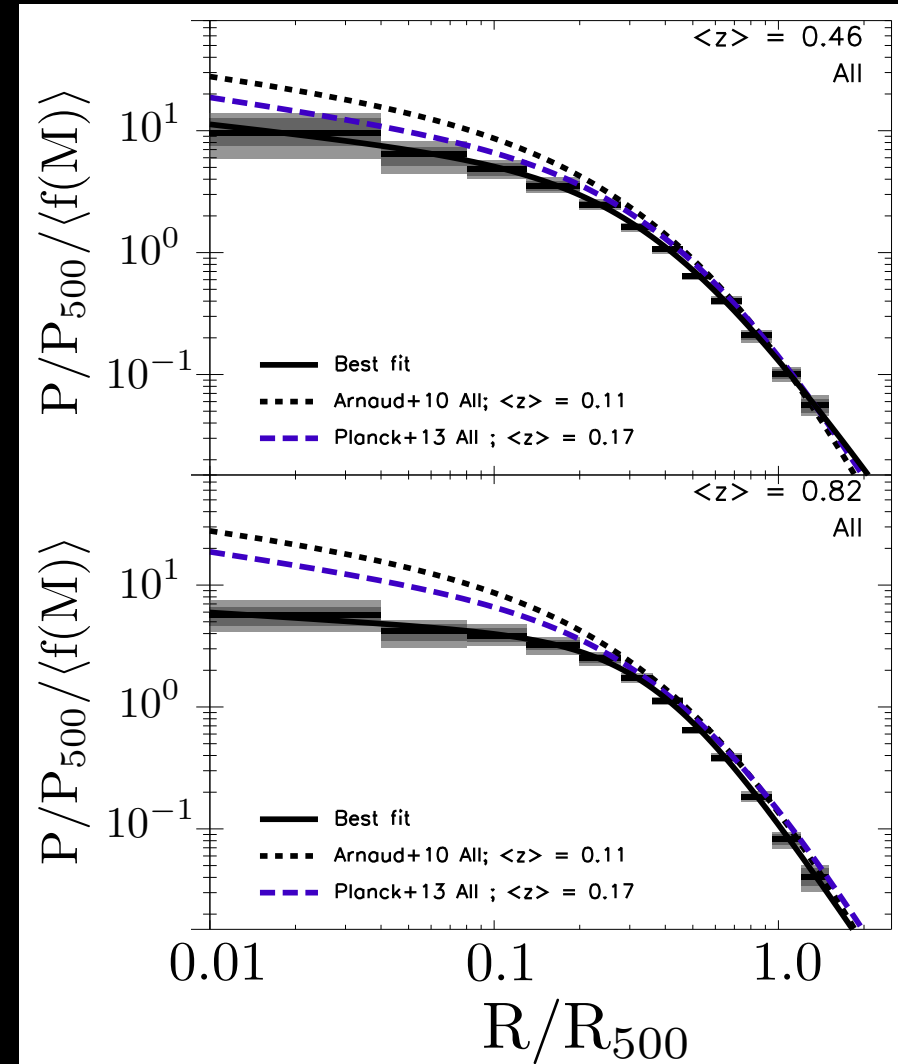
For a given cluster mass: less gas \rightarrow less thermal pressure

Gas mass fraction profiles



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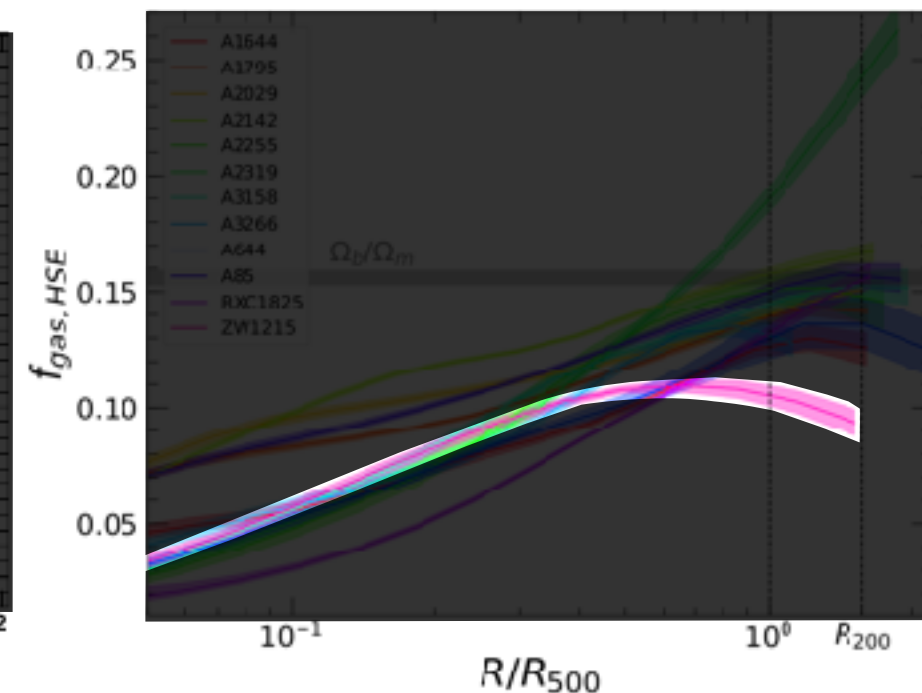
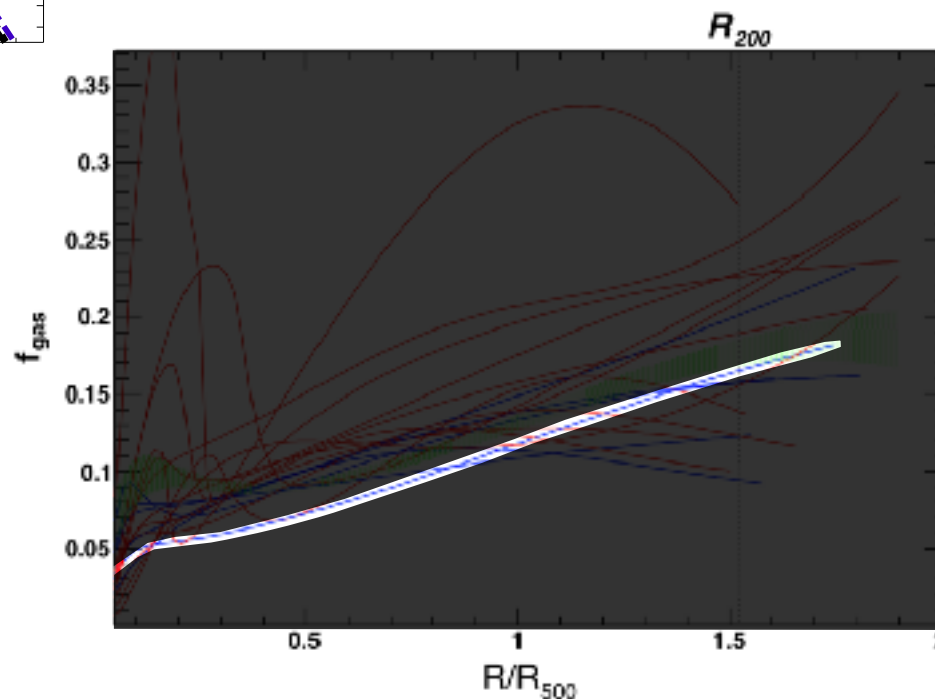
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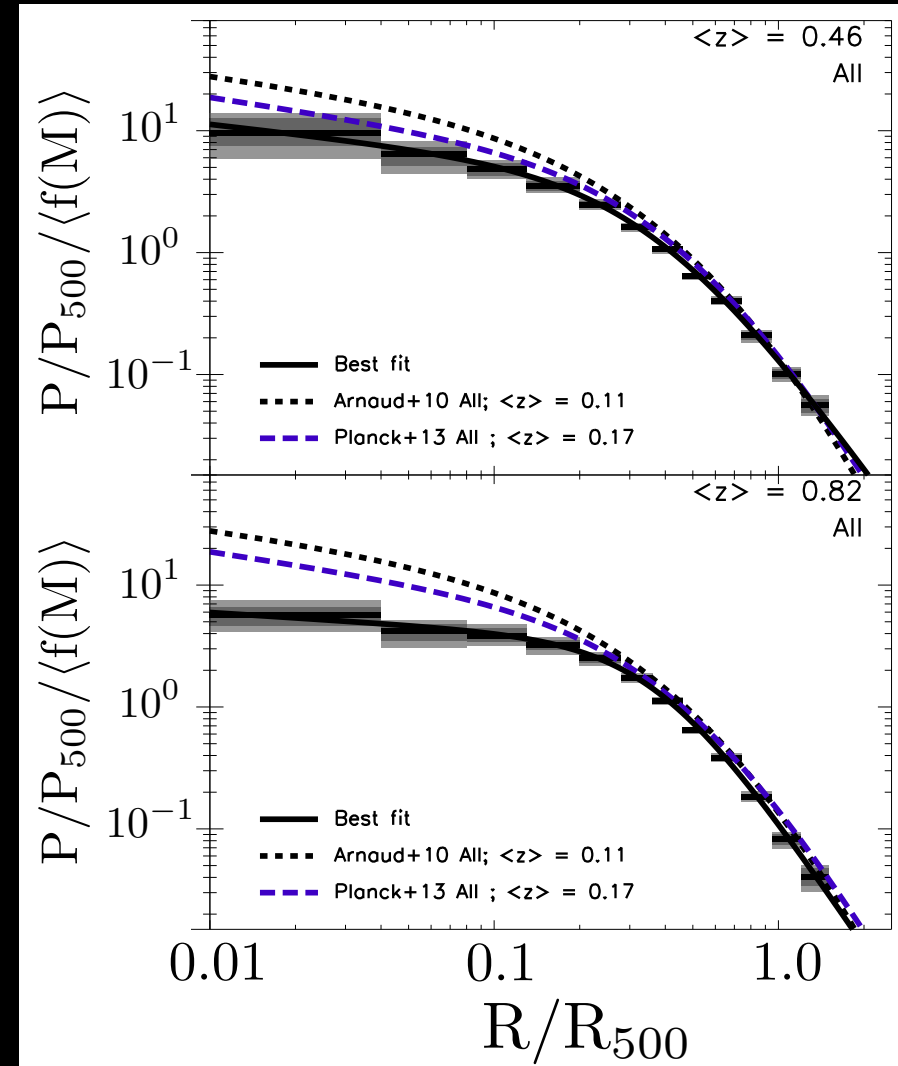
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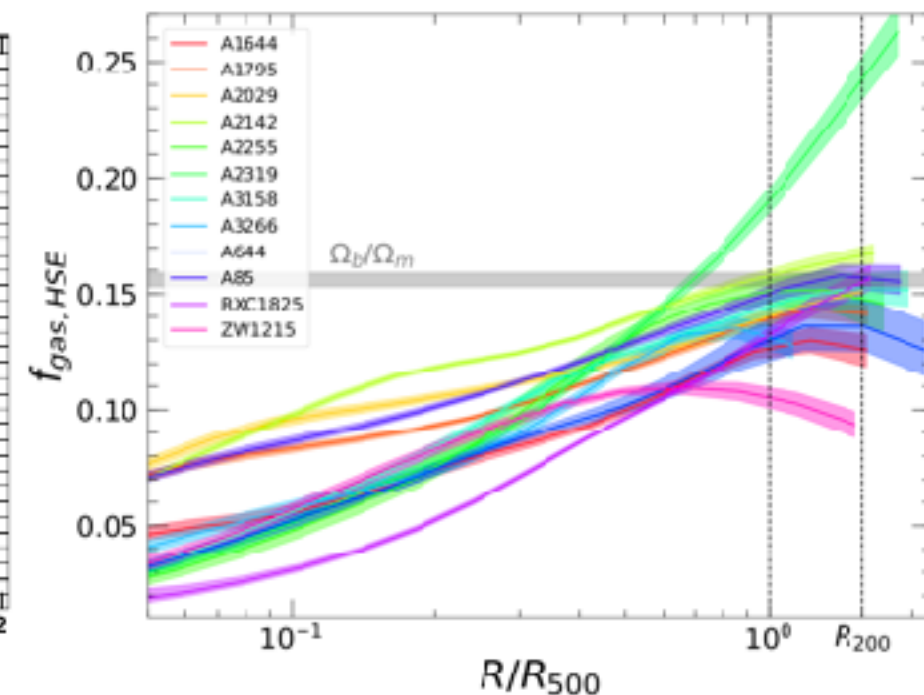
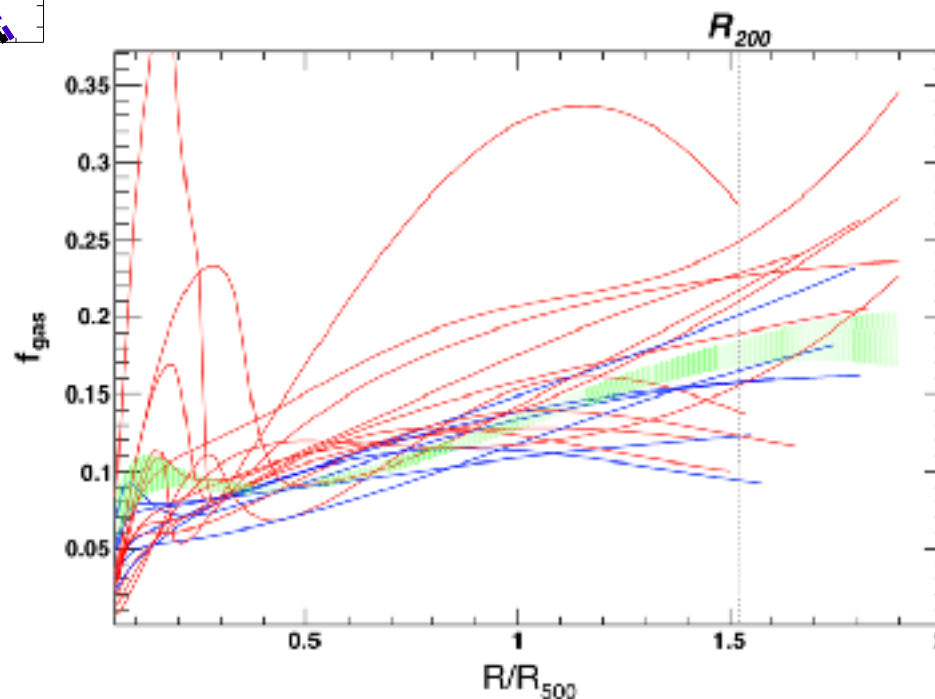
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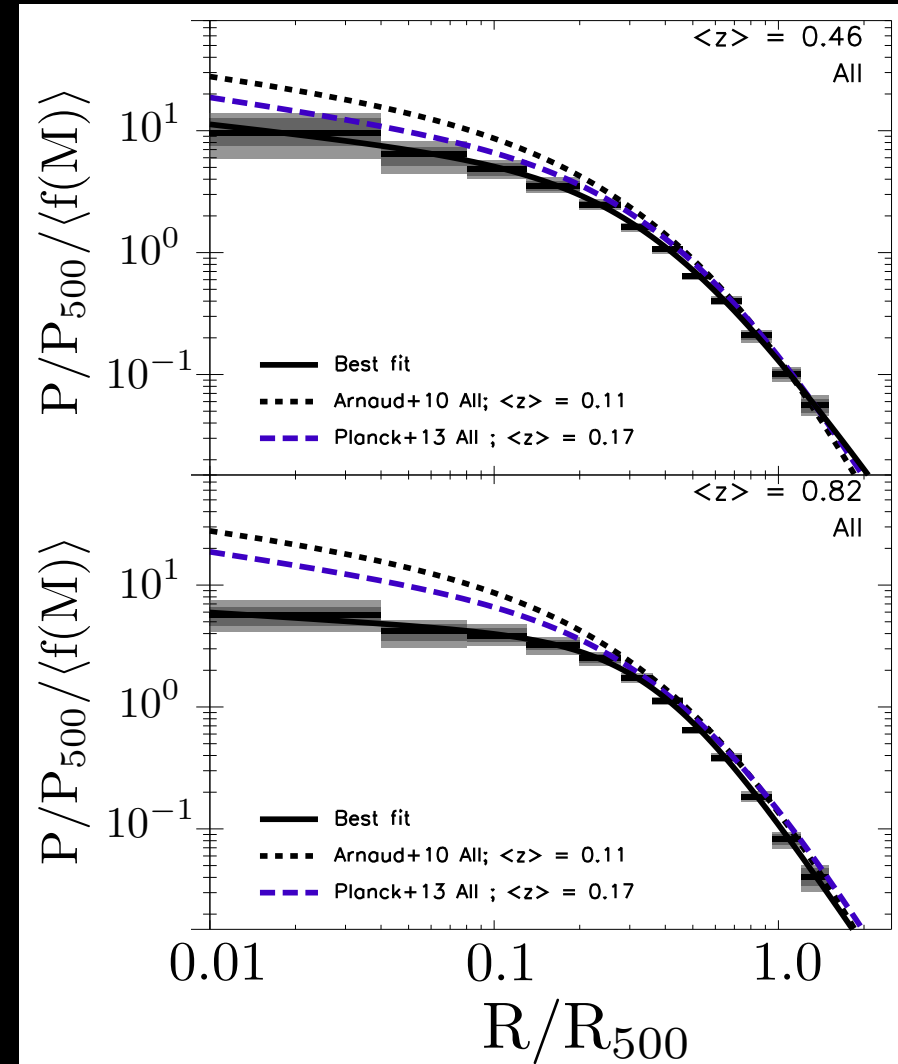
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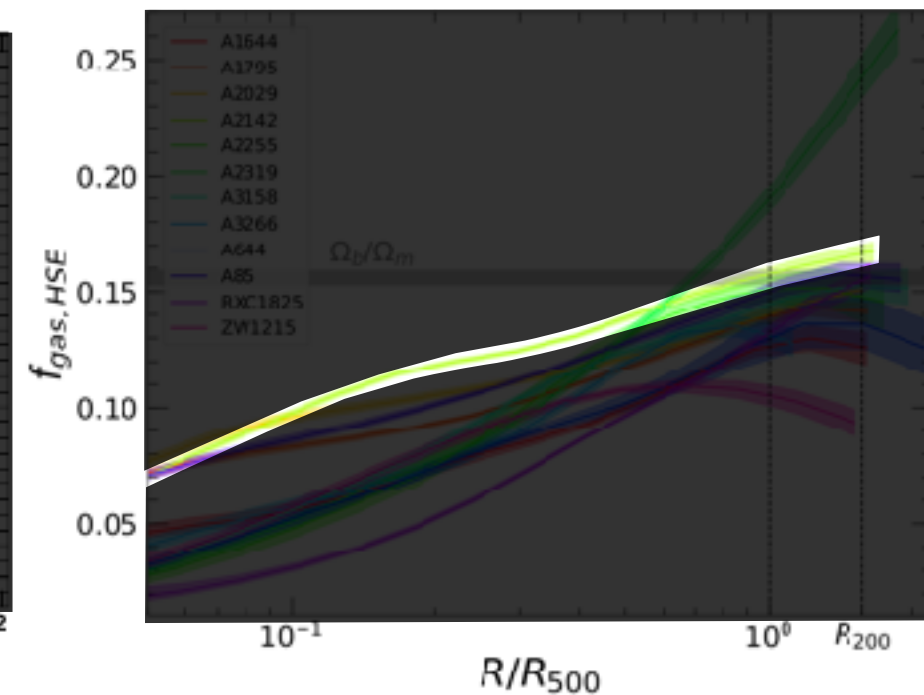
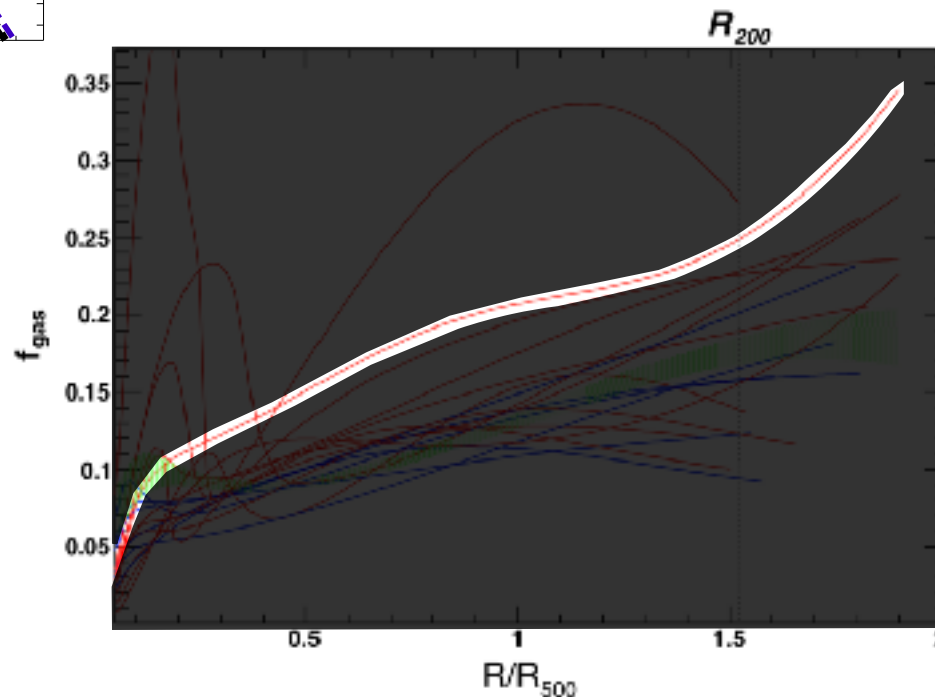
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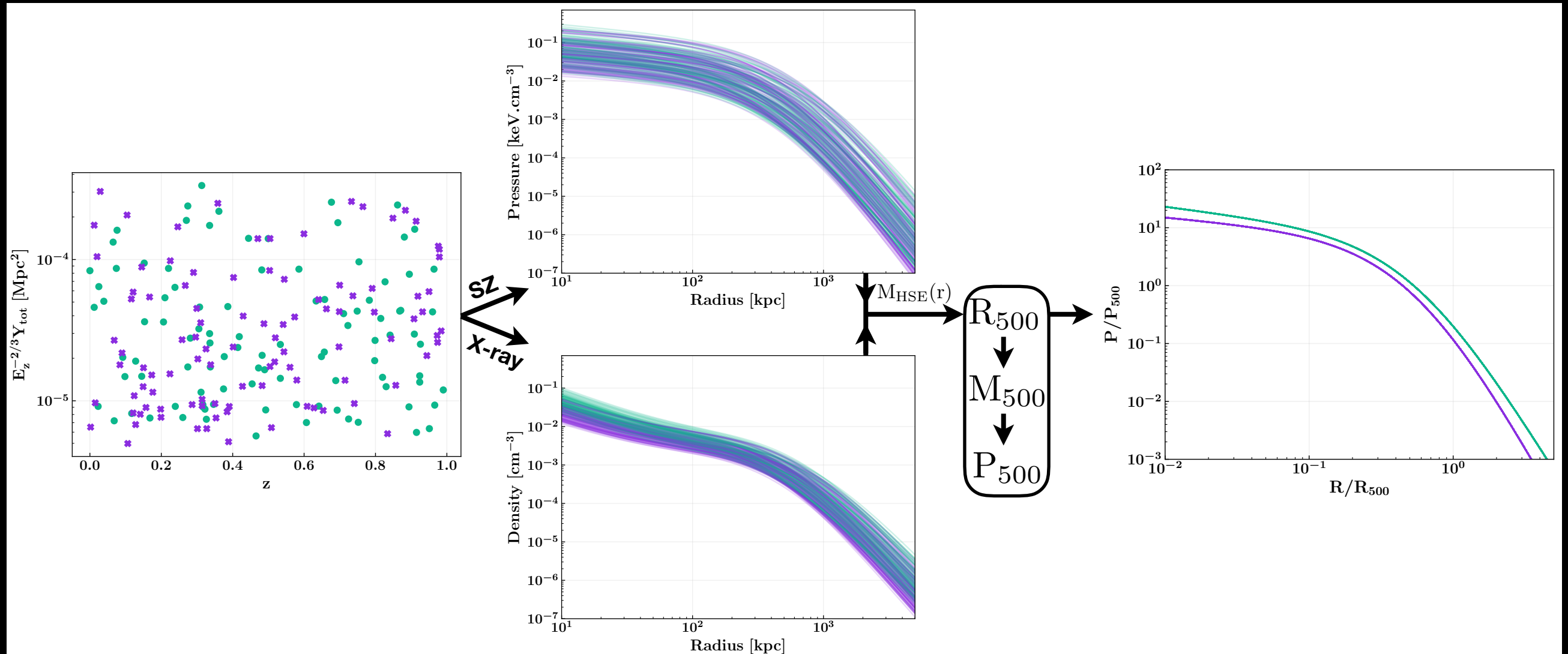


Mean pressure profile of the cluster population

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Mean pressure profile of the cluster population



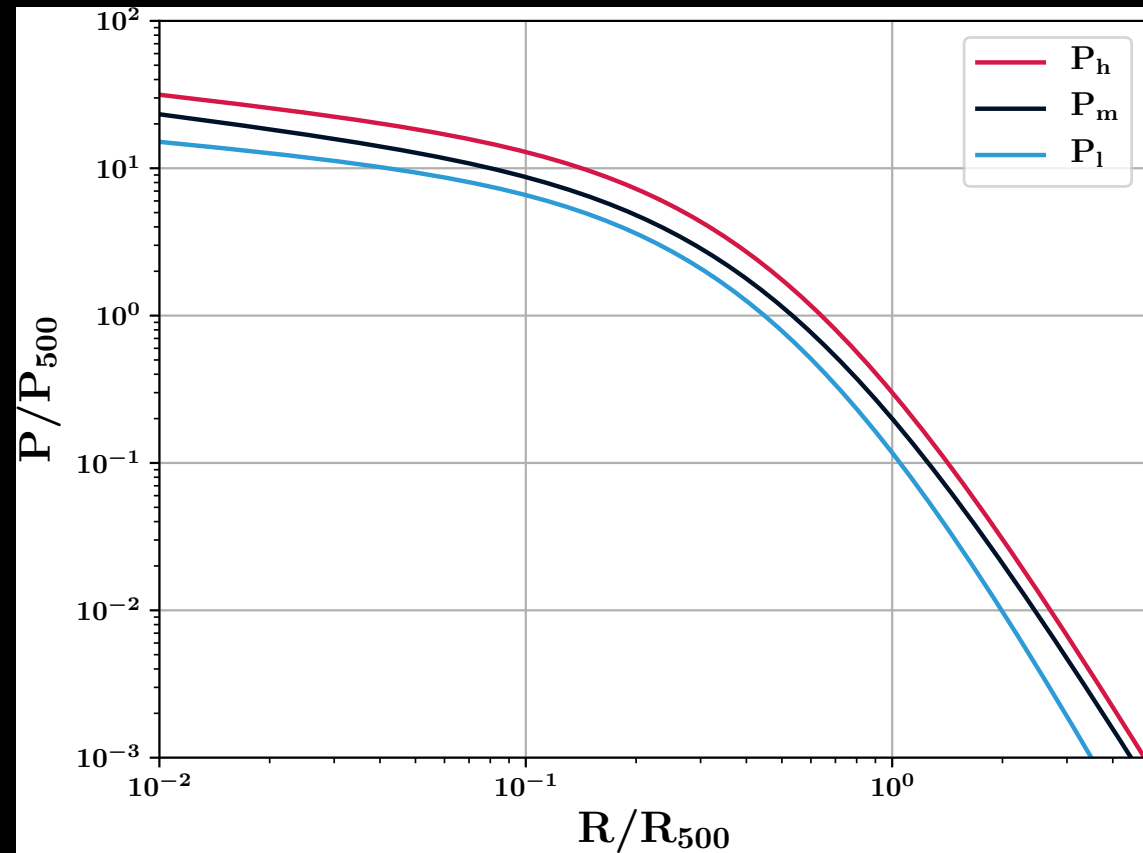
- **Impact of gas mass fraction on mean pressure profile:**

- Similar distributions of clusters in $Y_{tot} - z$ plane
- Pressure profiles and density profiles with different gas mass fractions \rightarrow hydrostatic mass profiles
- Scale pressure profiles using same definition of $P_{500} \propto E_z^{8/3} M_{500}^{2/3+0.12}$

Similar distributions in Y_{tot} but different mean normalized pressure profiles

Mean pressure profile of the cluster population

Mean normalized pressure profiles



Definition of three mean pressure profiles

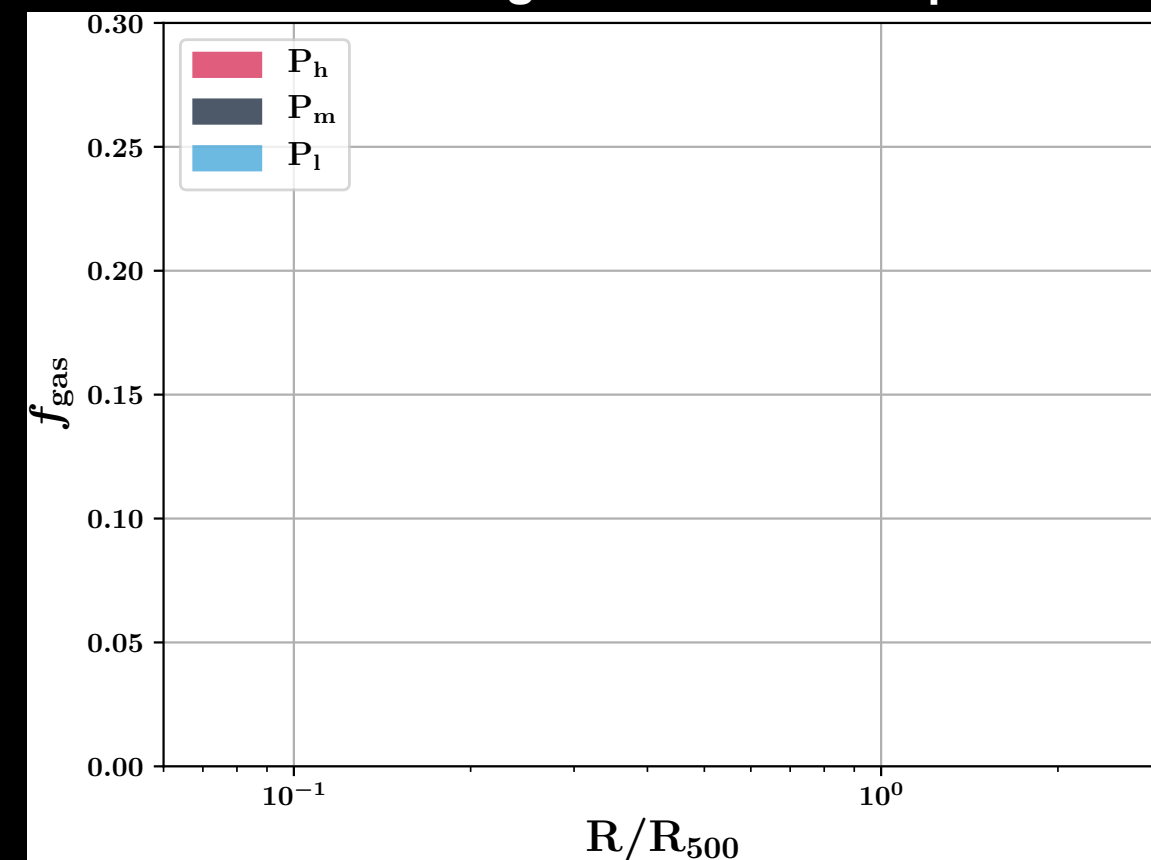
- The mean pressure profile of the *Planck* collaboration
Similar to the A10 profile used for cosmological analyses
- Two extreme cases given:
 - The intrinsic scatter of the profile distributions at low z
 - Current constraints on the gas mass fraction profiles

Gas mass fraction profiles knowing z , M_{500} , and $\mathbb{P}(x)$:

- Assume NFW model for mass profile $M_{\text{tot}}(r)$
- Hydrostatic mass profile:
$$\begin{cases} M_{\text{HSE}}(r) = (1 - b)M_{\text{tot}}(r) \\ b \in [0, 0.4] \end{cases}$$
- Density profile from HSE mass and pressure profile

$$\text{Gas mass fraction: } f_{\text{gas}}(r) = M_{\text{gas}}(r)/M_{\text{tot}}(r)$$

Associated gas mass fraction profiles



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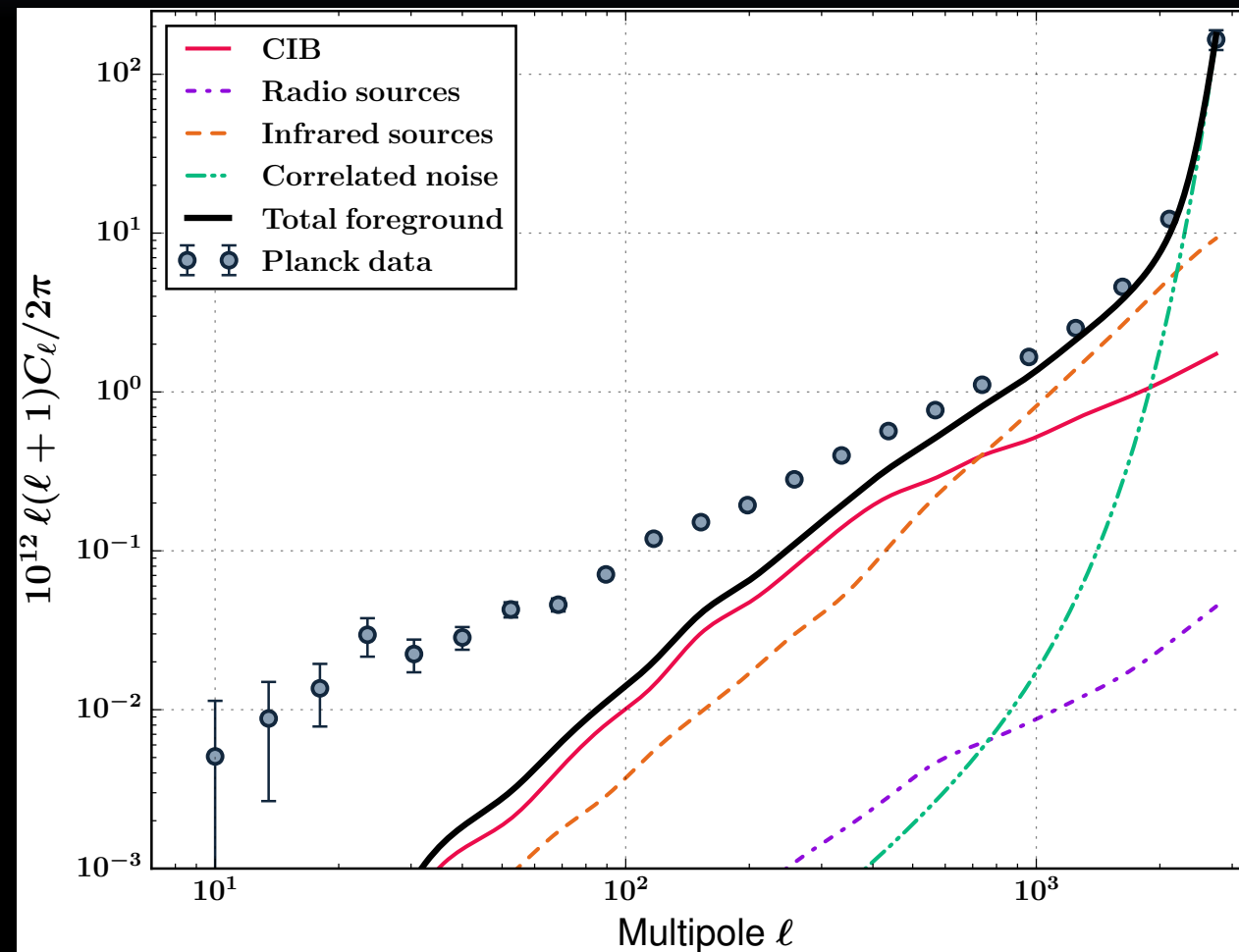
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Analysis of the *Planck* tSZ power spectrum



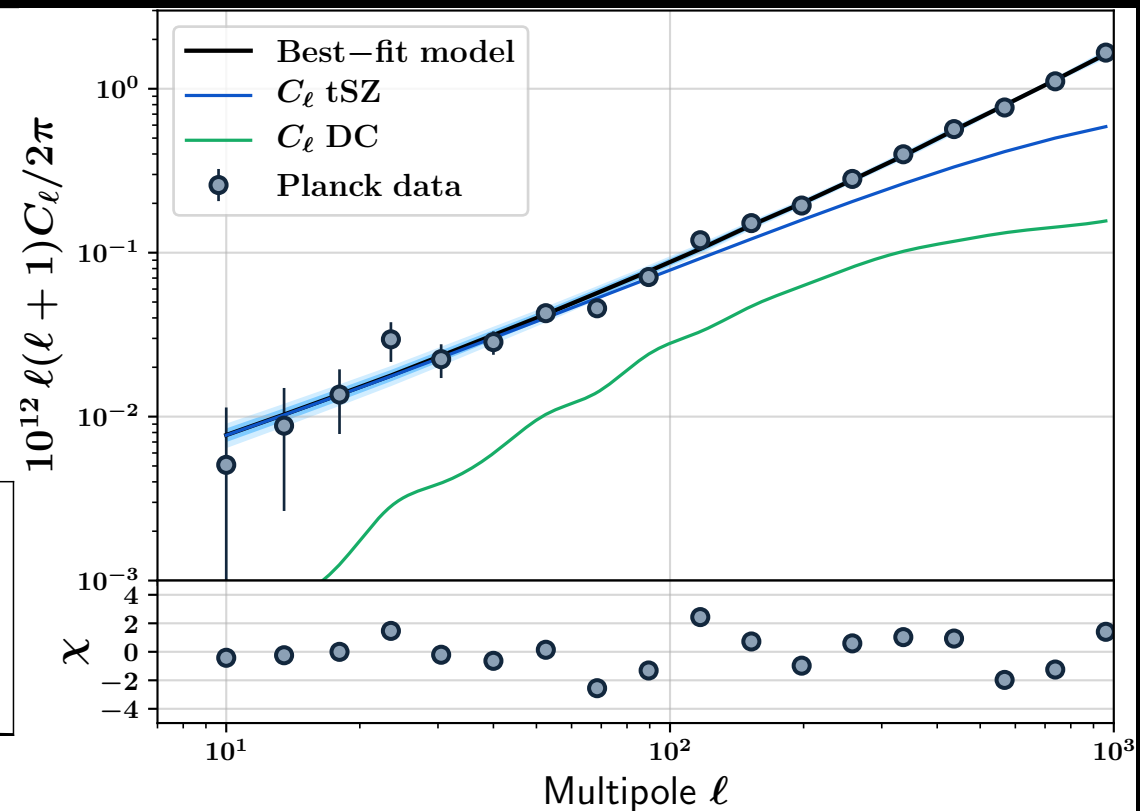
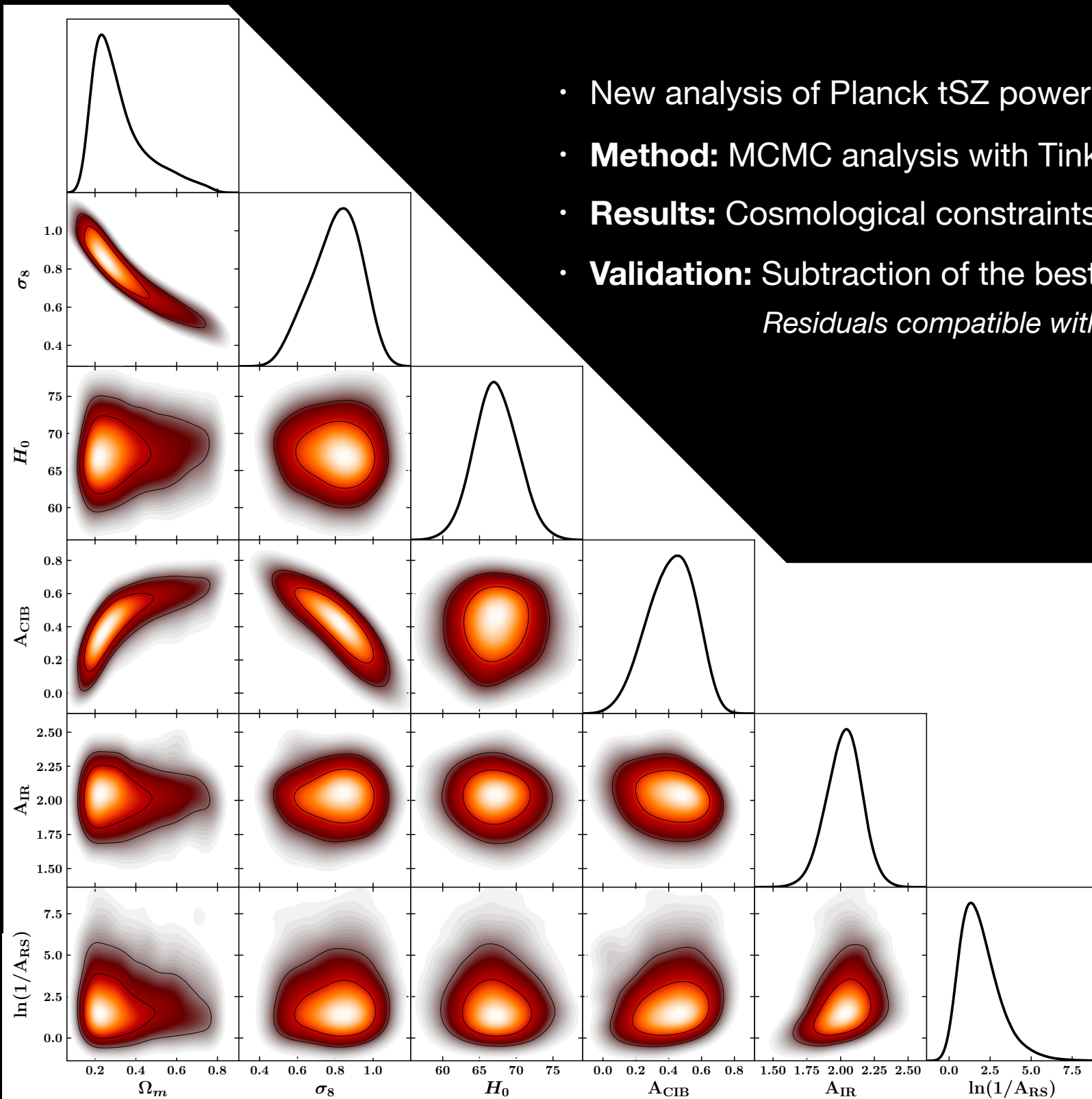
- Use angular power spectrum of the tSZ effect measured by *Planck* *Planck collaboration et al., A&A, 2016*
- **Power spectrum components:**
 - tSZ power spectrum
 - Contaminants:
 - Cosmic Infrared Background (CIB)
 - Radio and Infrared sources
 - Spatially correlated noise

Fit *Planck* power spectrum for $\ell < 1000$

Analysis of the *Planck* tSZ power spectrum

- New analysis of Planck tSZ power spectrum with the three mean pressure profiles
- **Method:** MCMC analysis with Tinker *et al.* mass function
- **Results:** Cosmological constraints + amplitude of contaminant power spectra
- **Validation:** Subtraction of the best-fit model to the Planck data

Residuals compatible with noise at all ℓ



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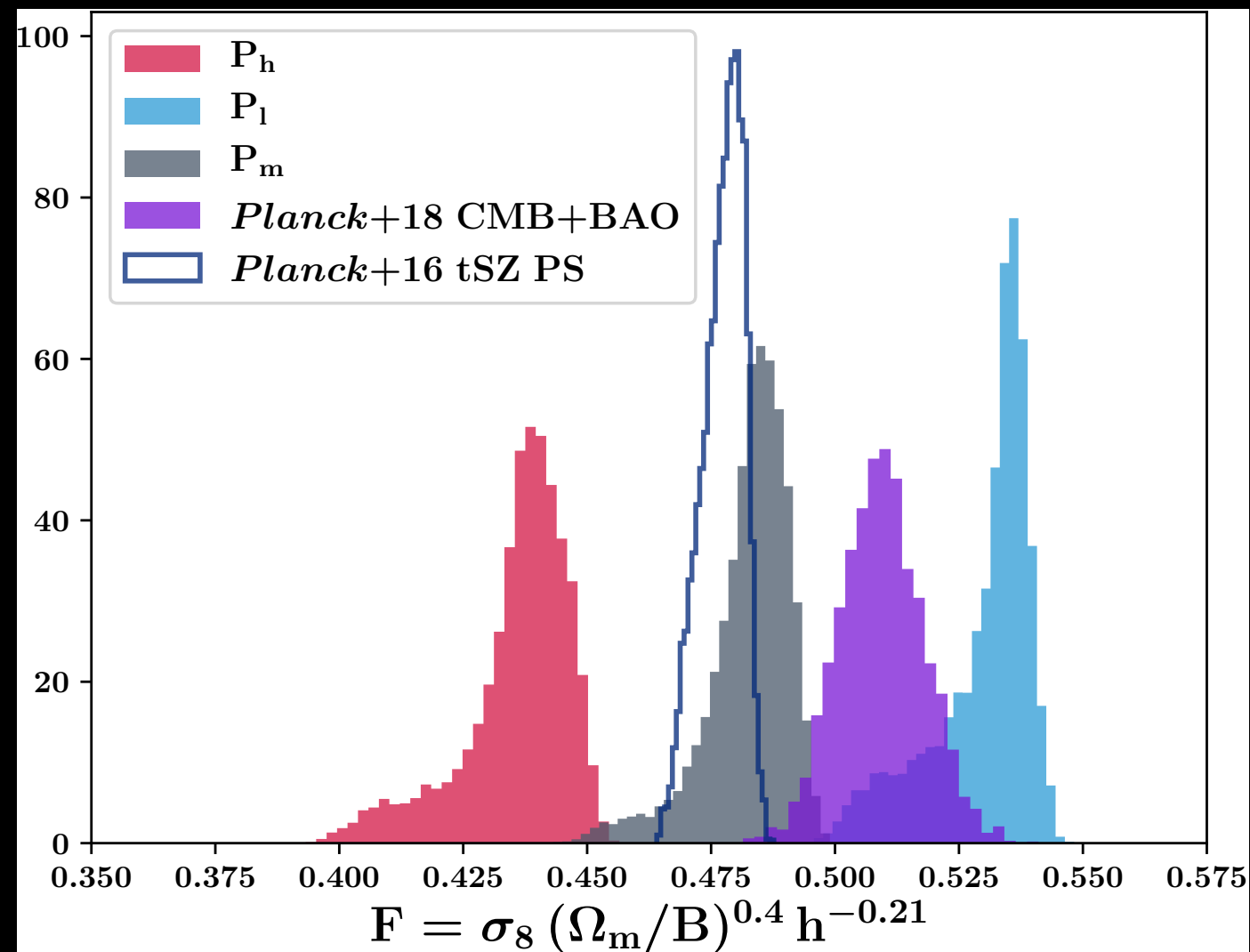
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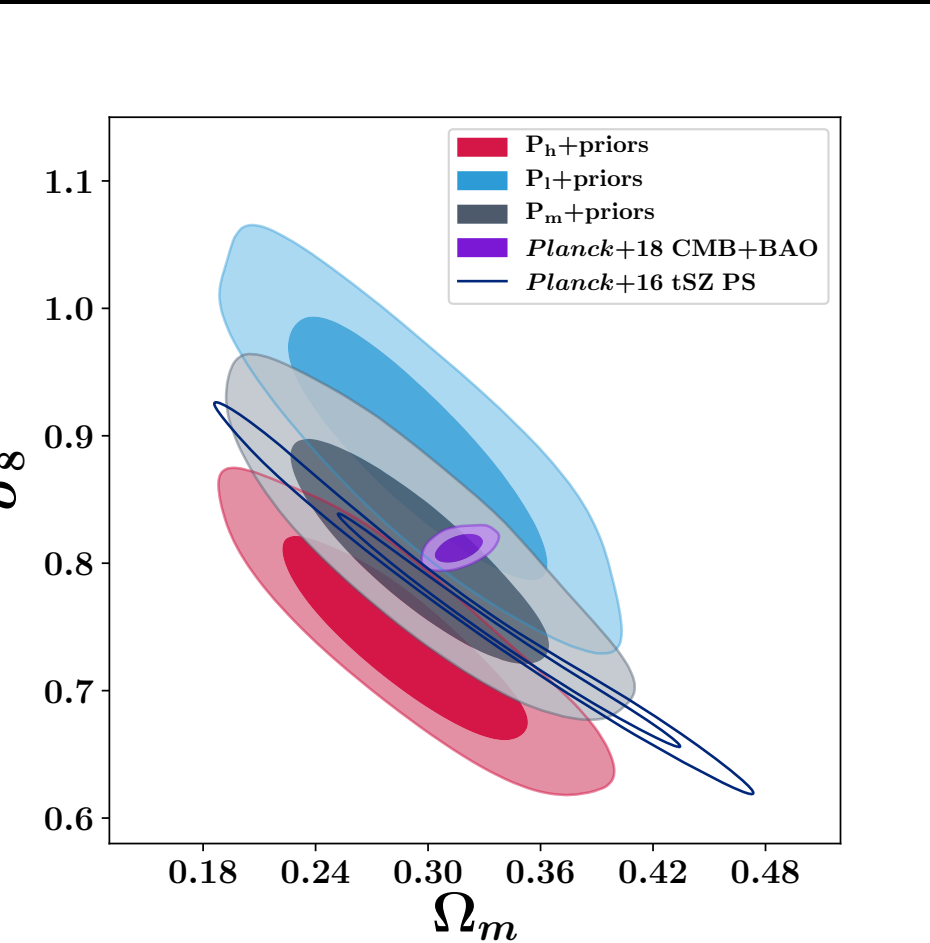
Impact of the pressure profile on tSZ cosmology



- **Cosmological constraints:** significant differences for the three mean pressure profiles
- Estimates obtained with \mathbb{P}_m profile compatible with previous constraints
- CMB constraints enclosed between the ones obtained with \mathbb{P}_m and \mathbb{P}_l profiles

Cosmological tension can be solved with mean pressure profile variations

Impact of the pressure profile on tSZ cosmology



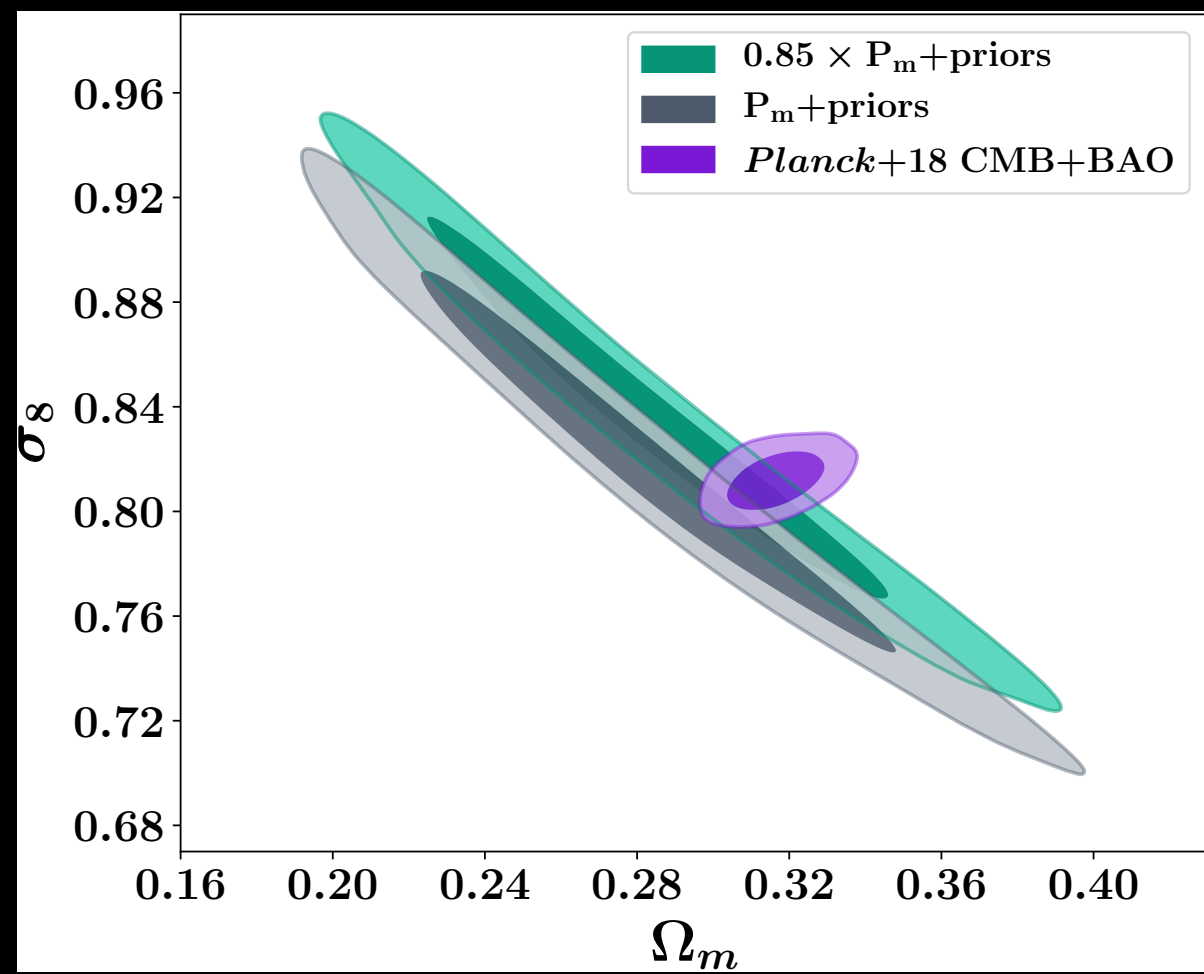
- Prior on:
 - b Lensing VS X-ray/SZ mass $\rightarrow b = 0.2 \pm 0.08$
 - Ω_m Baryon acoustic oscillations (BAO) $\rightarrow \Omega_m = 0.3 \pm 0.05$
- Cosmological constraints on σ_8 and Ω_m

No significant tension between CMB and tSZ PS constraints with P_m

• Possible future?

Prior on hydrostatic bias $b = 0.2 \pm 0.01$
 Better lensing mass estimates with e.g. Euclide
 \rightarrow Tension with current CMB constraints

15% decrease of mean pressure profile \rightarrow tension canceled

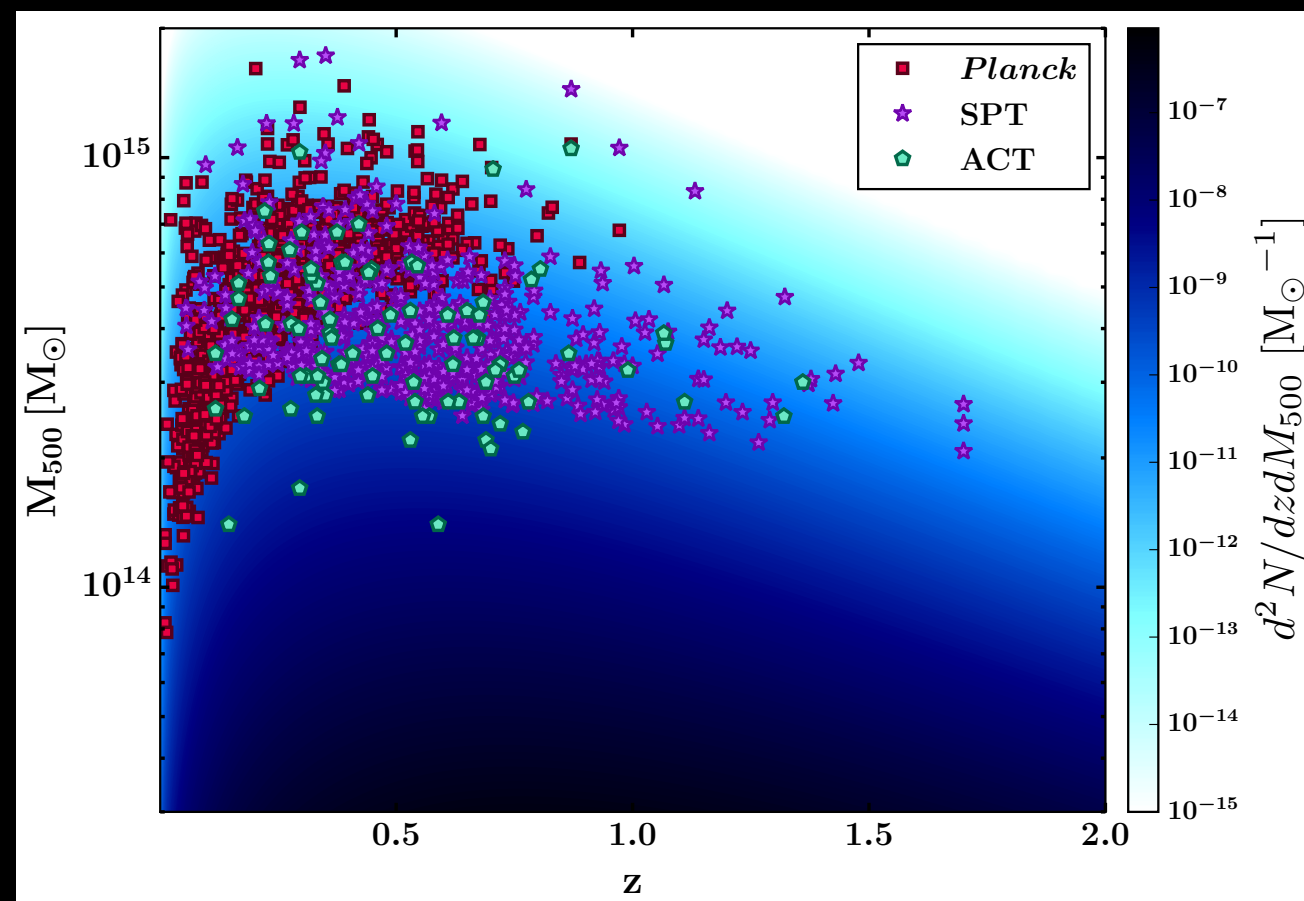


Conclusions / Perspectives

- If everything is taken into account: no cosmological tension **BUT** issue with hydrostatic bias value
→ Need to explore other sources of bias in tSZ cosmological analyses
- Mild indications of redshift evolution of ICM profiles
→ Wrong calibration of mean normalized pressure profile = potential source of bias
- New analysis of *Planck* tSZ power spectrum using extreme cases for mean pressure profile
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Perspectives:

- Need to estimate cluster thermodynamic properties at high z *X-ray/SZ analyses*
- Need to understand progenitor physics *low mass systems*

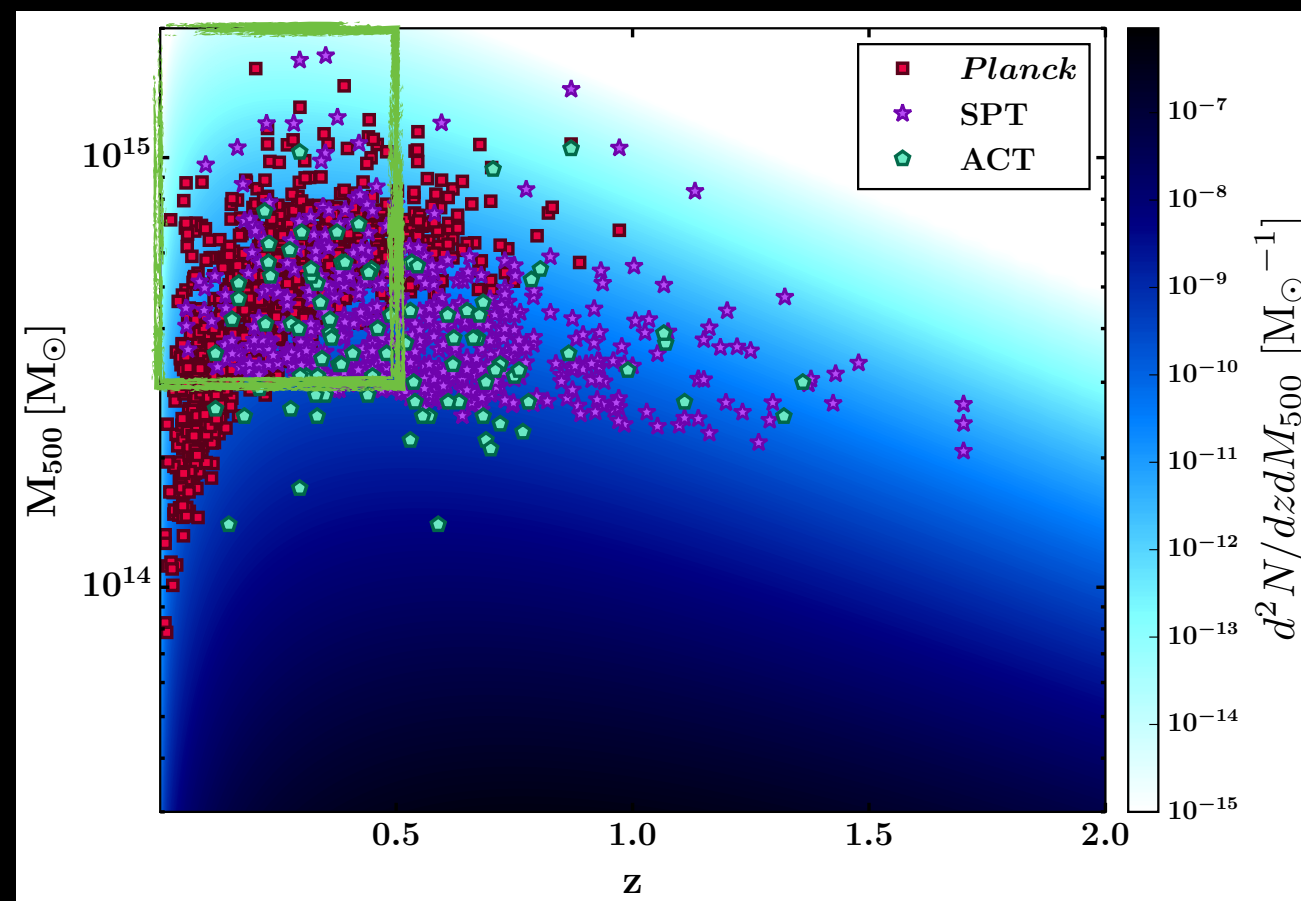


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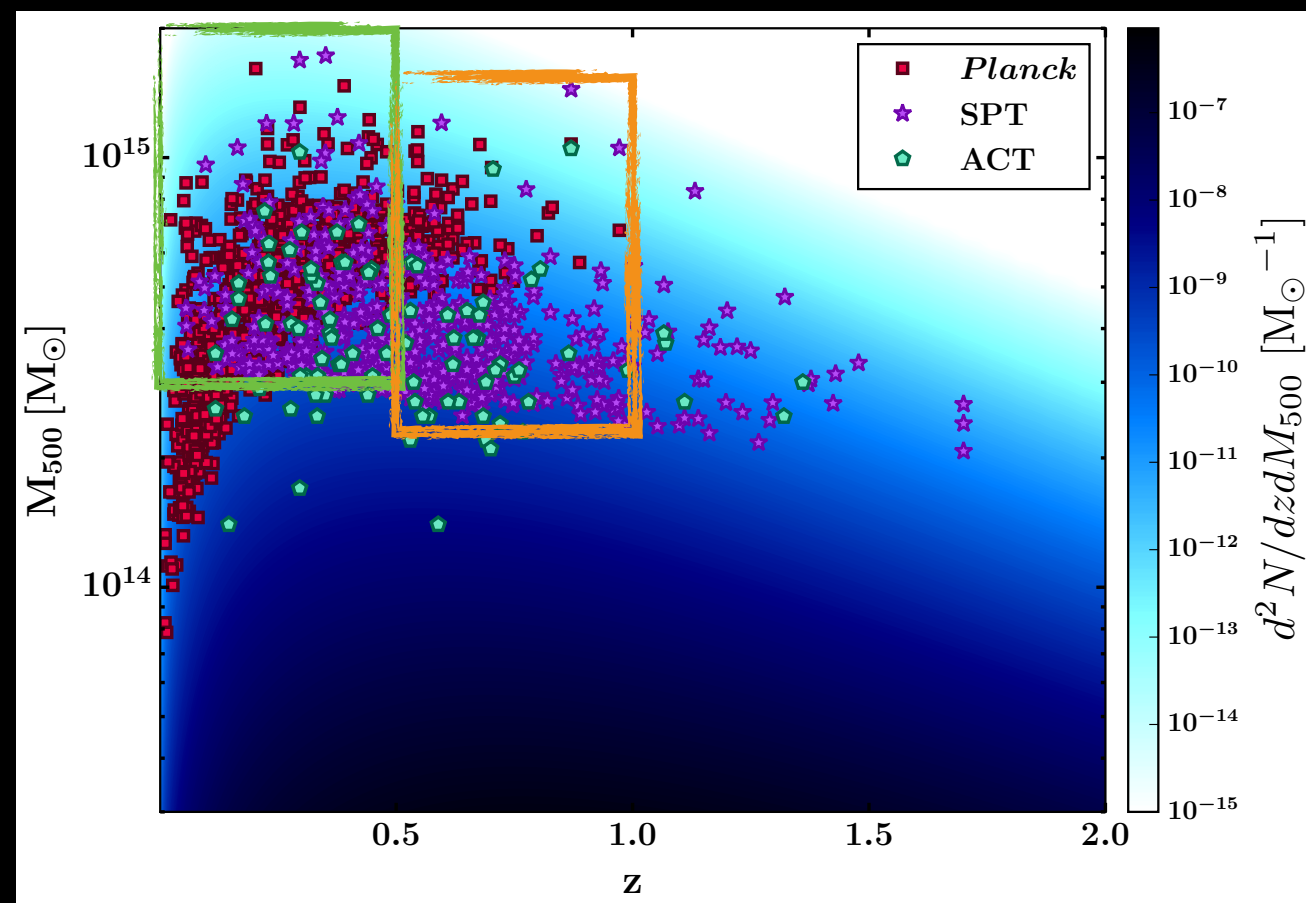


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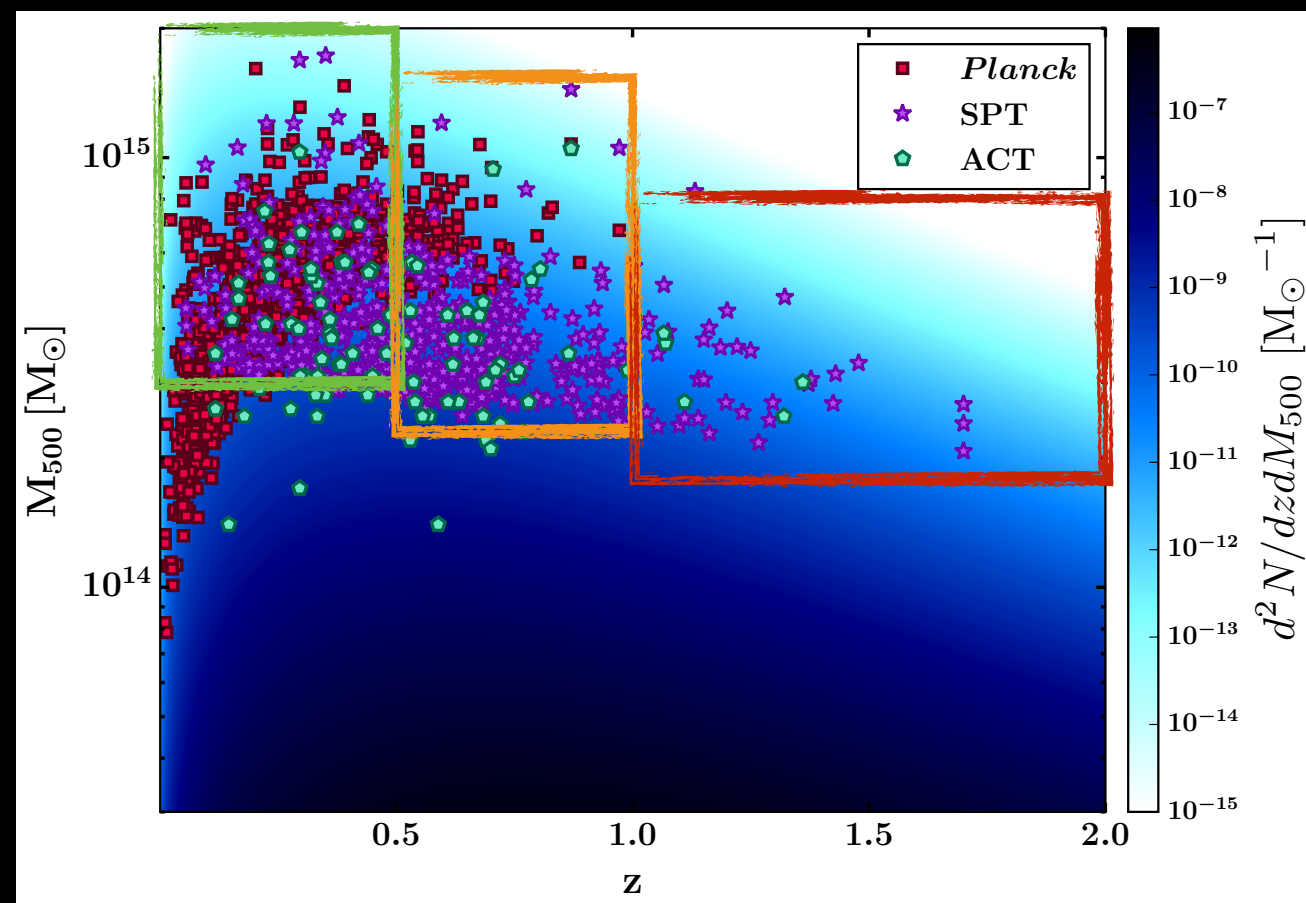


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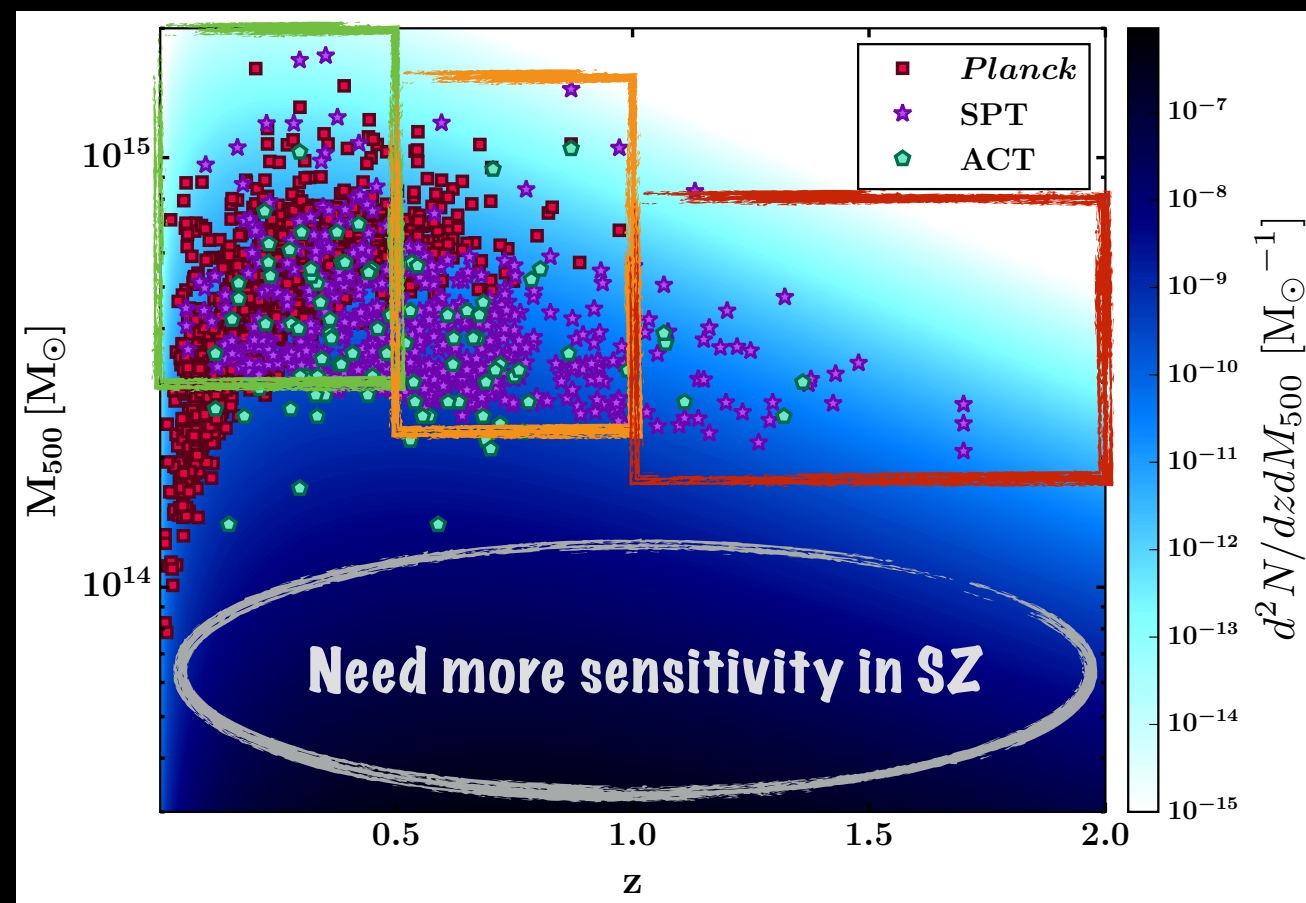


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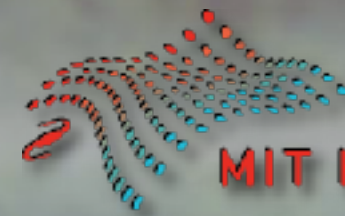
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Thank you



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