

Sequential freeze-in:  
A new phase of dark matter production  
out of equilibrium

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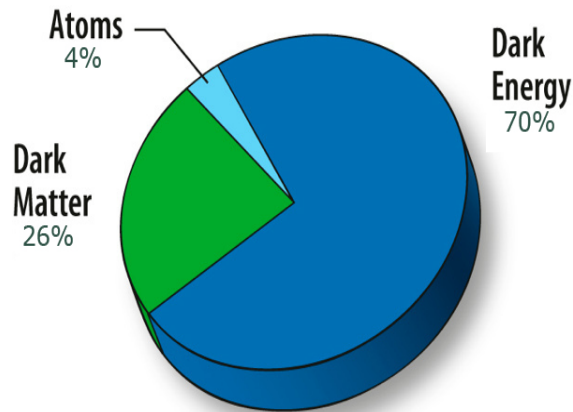
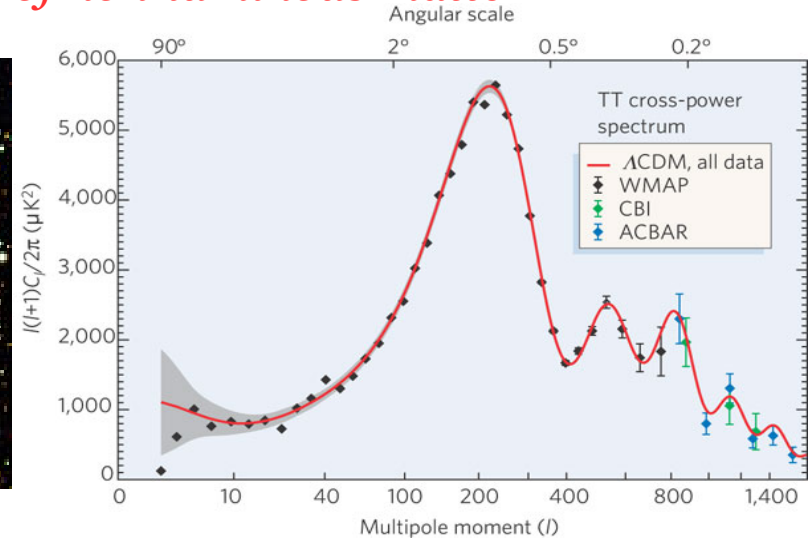
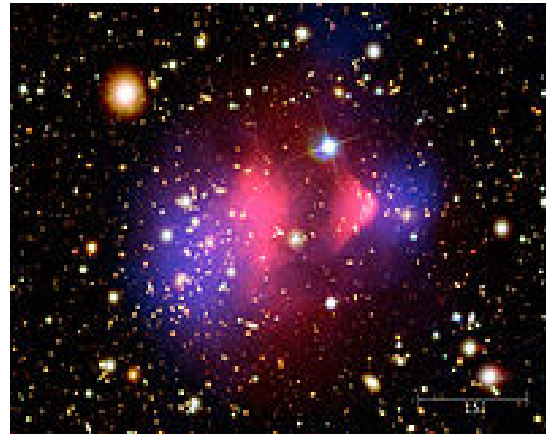
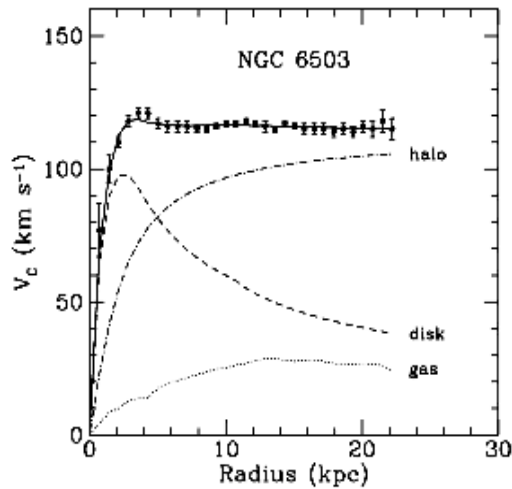
based on: “*Dark Matter Abundance from Sequential Freeze-in Mechanism*”  
arXiv: 2005.06294  
in collab. with G. Bélanger, C. Delaunay, A. Pukhov

# Outline

- Generic introduction to dark matter
- DM production regimes
- Sequential freeze-in regime
- Conclusions

# Dark Matter

*Compelling evidence (only gravitational) of non-luminous matter*



**6 times more abundant than visible matter**

## *We know...*

- its abundance
- pressureless
- long-lived enough
- neutral enough

## *We don't know...*

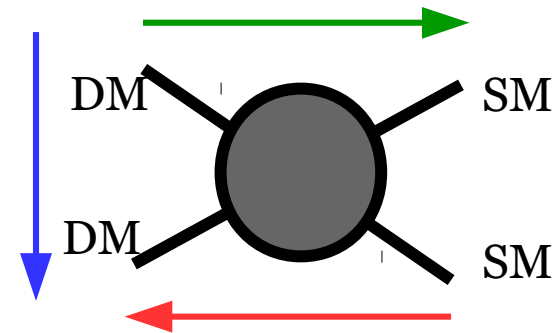
- fundamental particle?
- spin, mass?
- non-gravitational interactions?
- **thermal relic?**
- when was it produced?
- ...

# DM non-gravitational interactions?

- ◆ DM annihilating/decaying into SM particles?  
(Gunn, Lee, Lerche, Schramm and Steigman  
1978, Astrophys.J. 223, 1015)

(DM not mentioned explicitly here)

**DM indirect detection**



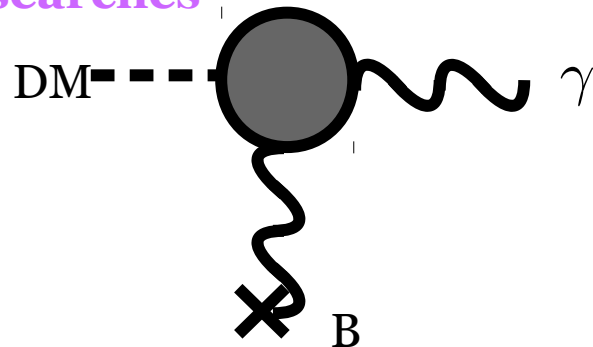
- ◆ DM scattering off nuclei ?  
(Goodman & Witten  
1985, Phys.Rev. D31, 3059)  
**DM direct detection**

- ◆ DM produced in particle collisions  
(Ellis, Frère, Hagelin, Kane, Petcov,  
1983, Phys.Lett.B 132 436-442)  
(DM not mentioned explicitly here)  
**DM collider searches**

(not sure if  
this is the very  
first paper)

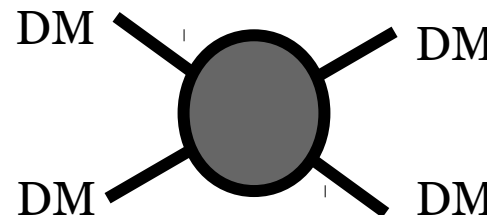
- ◆ Axion DM experiments  
(Sikivie, P., 1983,  
Phys.Rev.Lett. 51, 1415.)

**Axion searches**



- ◆ DM self-interactions (Spergel and Steinhardt,  
1999, Phys.Rev.Lett. 84, 3760-3763)

**Gravitational lensing**



# Thermal vs. Non-thermal DM

...whether or not the DM particles have been in thermal equilibrium with the SM bath

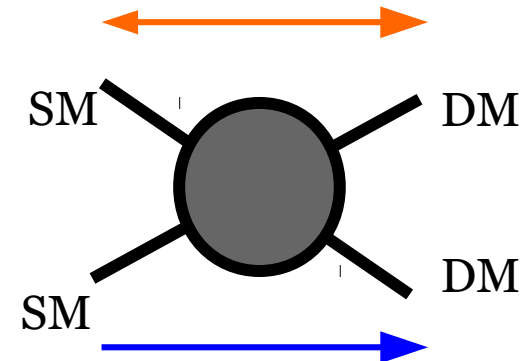
At early times...

If thermal DM:

$$H < \Gamma(\text{DM} + \text{DM} \rightarrow \text{SM} + \text{SM}) = \Gamma(\text{SM} + \text{SM} \rightarrow \text{DM} + \text{DM})$$

$H$  : expansion rate

$\Gamma$  : reaction rate



If non-thermal DM:

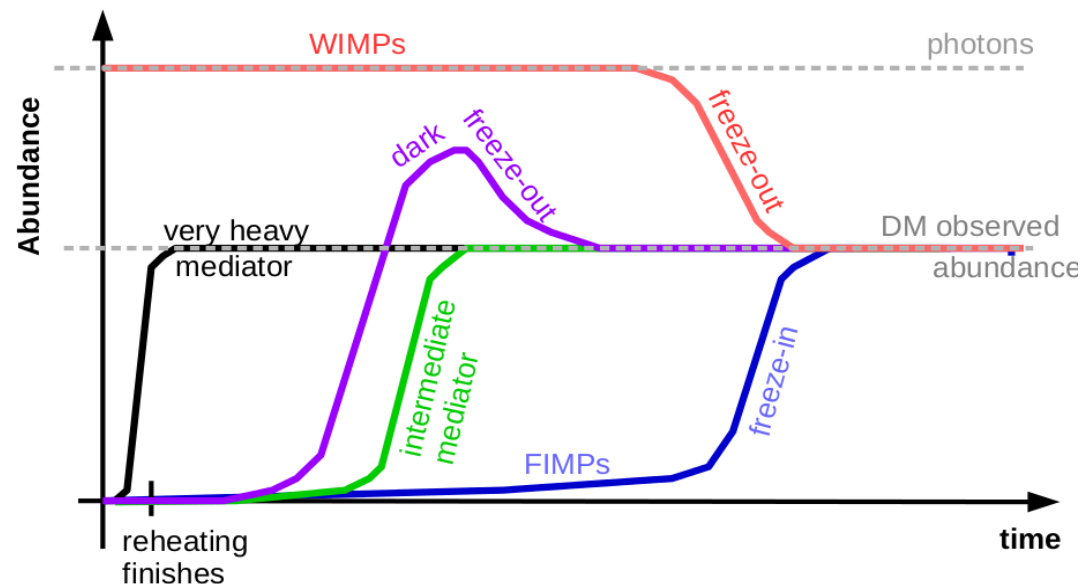
$$\Gamma(\text{DM} + \text{DM} \rightarrow \text{SM} + \text{SM}) < H < \Gamma(\text{SM} + \text{SM} \rightarrow \text{DM} + \text{DM})$$

At later times...

$$\Gamma(\text{SM} + \text{SM} \rightarrow \text{DM} + \text{DM}) < H \quad (\text{thermal})$$

At the end of the day....

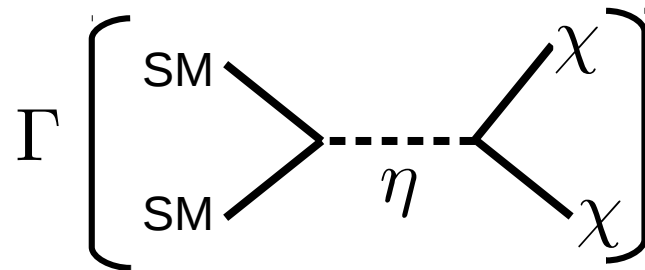
$$\Gamma \ll H \quad \dots \text{so DM freezes-out (in)}$$



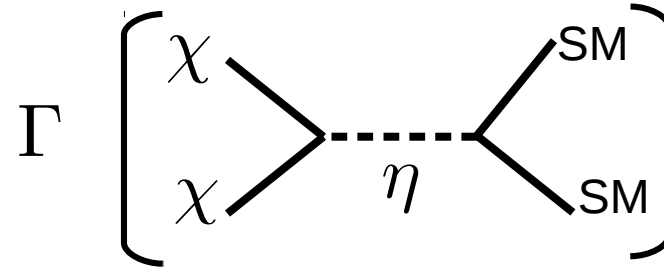
# ...it is mostly about couplings...

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{HS}} \left( \begin{array}{c} \chi \\ \chi \end{array} \right) \begin{array}{c} g_\chi \\ \bullet \end{array} \text{---} \eta + \begin{array}{c} \text{SM} \\ \text{SM} \end{array} \begin{array}{c} g_v \\ \bullet \end{array} \text{---} \eta \right)$$

If  $g_\chi \cdot g_v$   
very tiny



If  $g_\chi \cdot g_v$   
sizeable



If  $g_\chi \gg g_v$

dynamics is more complex, mix between freeze-in and freeze-out

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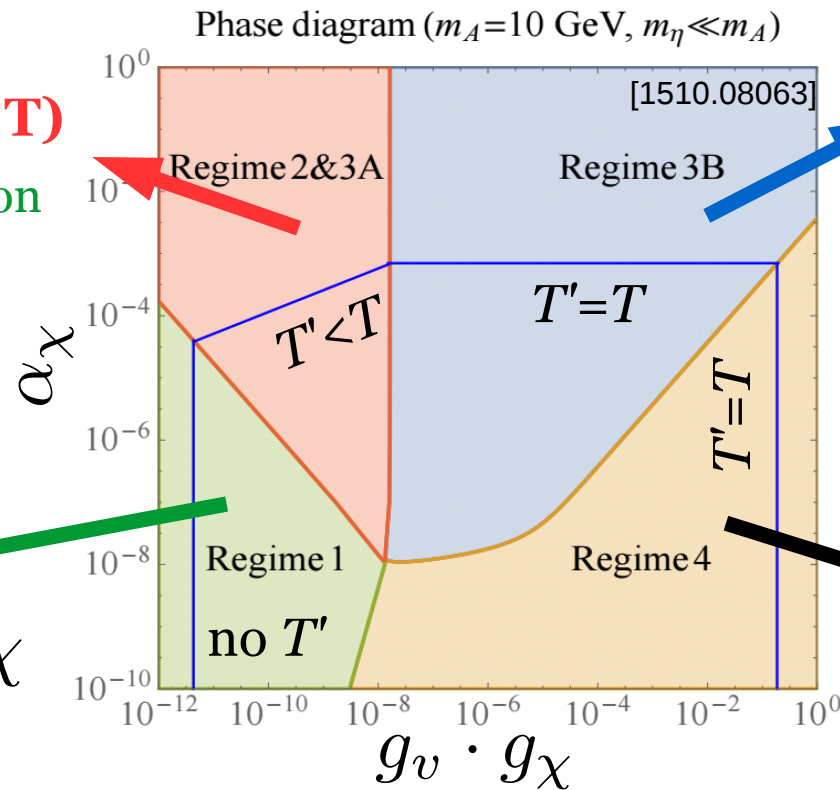
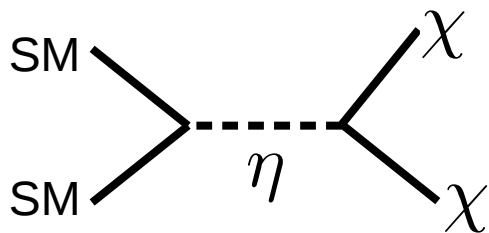
# Different thermal histories of DM

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{HS}} \left( \chi \begin{array}{c} \nearrow g_\chi \\ \searrow \end{array} \eta + \begin{array}{c} \text{SM} \\ \nearrow g_\nu \\ \searrow \text{SM} \end{array} \eta \right)$$

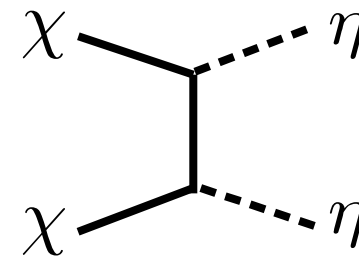
**Dark Freeze-out ( $T' < T$ )**

- Freeze-in production  
+ dark annihilation

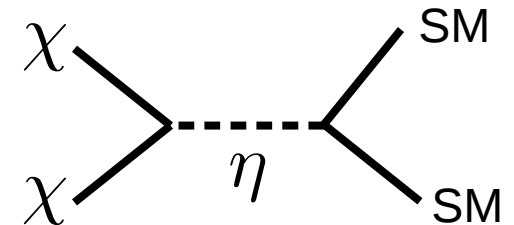
**Freeze-in**



**Dark Freeze-out ( $T' = T$ )**



**usual Freeze-out**



So what is 2005.06294 about?

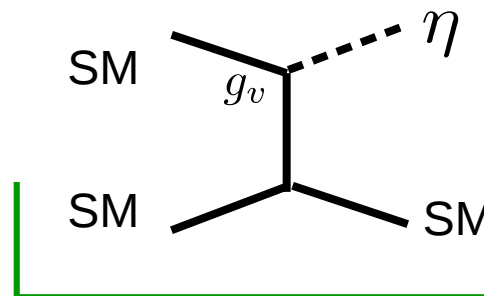
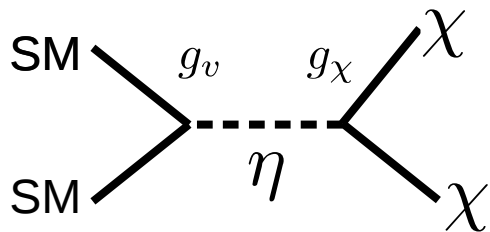
Note: we work in the framework of a particular model  
(up-philic scalar mediator, lighter than fermionic DM),  
however the mechanism is pretty generic



# “Sequential freeze-in”

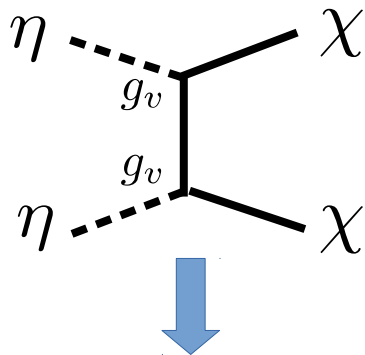
[Hambye, Tytgat, Vandecasteele, Vanderheyden, 1908.09864]  
[this work]

At the beginning... (assuming zero abundance of both mediator & DM)

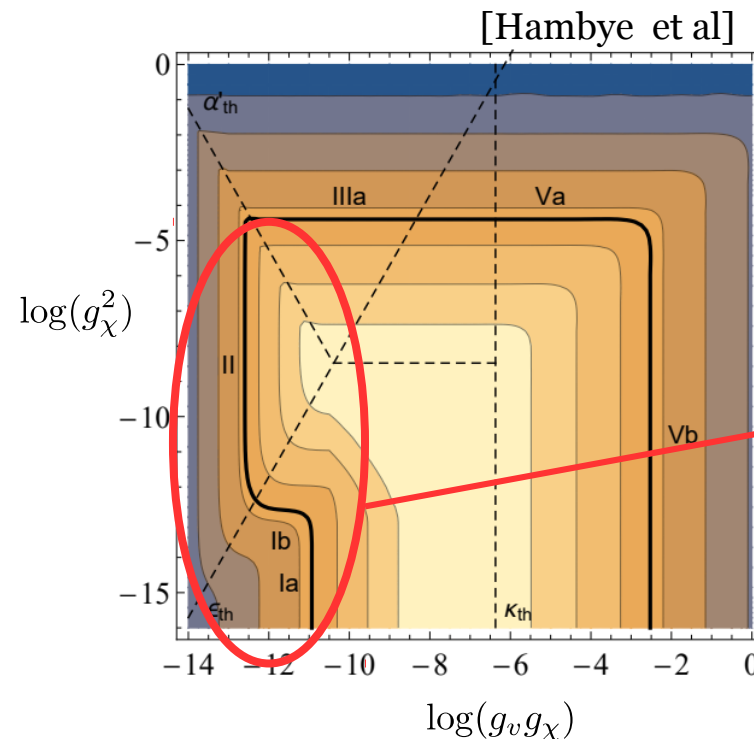


$\eta$  in thermal eq.  
with SM or not, depending  
on size of  $g_v$

Soon after... if  $g_\chi \gg g_v$

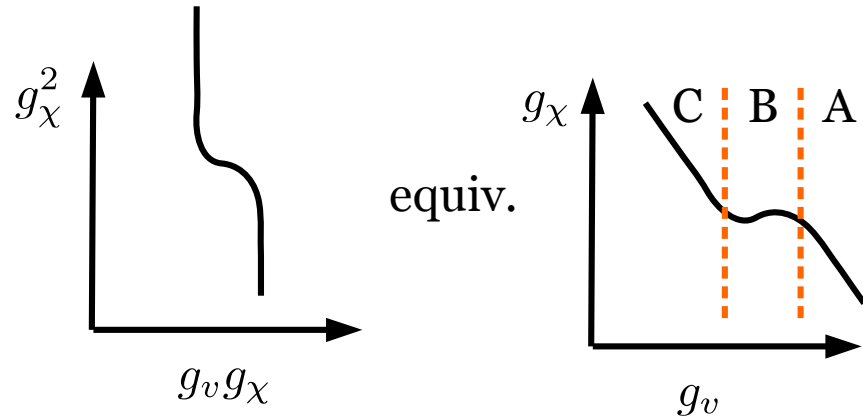


becomes the dominant  
DM production mode  
even if  $\eta$  is not in thermal eq.!



“mooring bollard”  
shape  
due to the  
production from  
mediators

# “Sequential freeze-in”

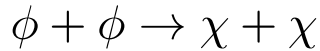


## A) standard freeze-in



$$\Gamma \propto n_{\text{SM}}^2 \langle \sigma v \rangle_A \sim 1 \cdot (g_v g_\chi)^2$$

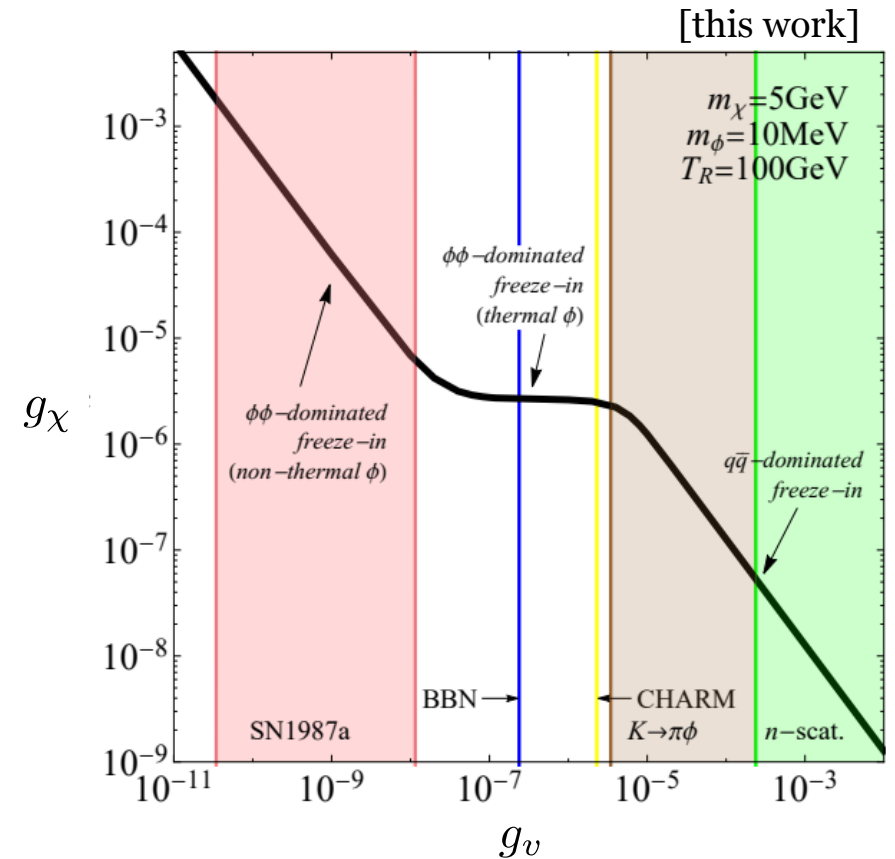
## B) mediator-dom. freeze-in (med. is thermal)



$$\Gamma \propto n_\phi^2 \langle \sigma v \rangle_B \sim 1 \cdot (g_\chi)^4$$

## C) mediator-dom. freeze-in (med. is not thermal) $\phi + \phi \rightarrow \chi + \chi$

$$\Gamma \propto n_\phi^2 \langle \sigma v \rangle_C \sim (n_{\text{SM}}^2 \langle \sigma v \rangle_\phi)^2 \langle \sigma v \rangle_C \sim 1 \cdot (g_v)^4 \cdot (g_\chi)^4$$



# Mediator production

Boltzmann Equation  $\hat{L}[f_\phi] = C[f_\phi]$

Liouville operator, dealing with  
the expansion rate and gravity

collision term, where the reaction rates  
enter

$f_\phi$  : mediator's distribution function

For FRW universe

$$E(\partial_t - Hp\partial_p)f_\phi = C[f_\phi] \quad (\text{I})$$

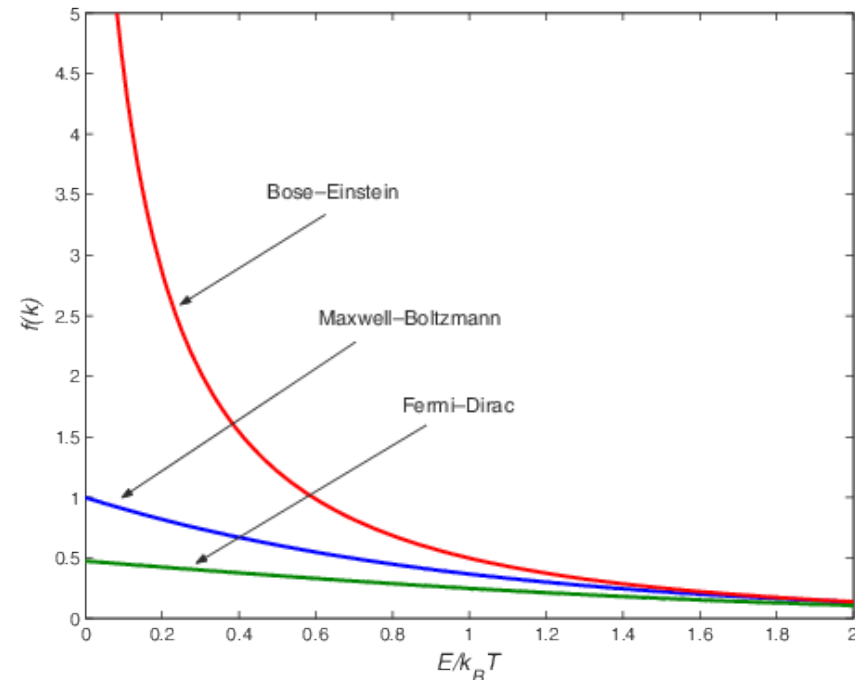
For species in thermal eq.,  $f$  has a known shape, completely  
determined by the temperature and the energy

So it is convenient to integrate the Boltzmann  
Eq. to get an Eq. for number density  $n$

$$n \propto \int f_\phi d^3p$$

$$\dot{n} + 3Hn \propto \int C[f_\phi] d^3p/E \quad (\text{II})$$

When med. is not in eq., a priori (I) should be used



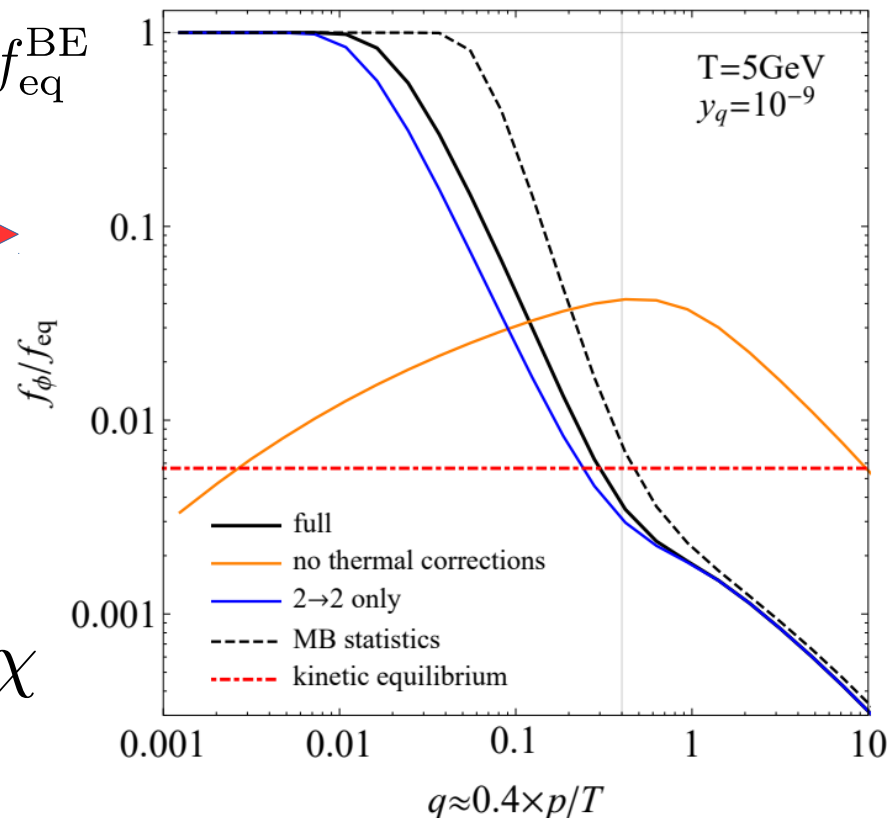
# Mediator production for DM

Sometimes in the literature it is assumed  $f_\phi \propto f_{\text{eq}}^{\text{BE}}$  so as to avoid solving (I) (kinetic eq. approx.)

As for med. itself, this is far from correct  $\rightarrow$

If assuming MB distrib. for the SM particles

$$\frac{f_\phi}{f_{\text{eq}}} \sim 1 - \exp \left[ -\frac{g_v^2 M_{\text{Pl}}}{p} \left( 1 + \log \frac{p}{T} \right) \right]$$

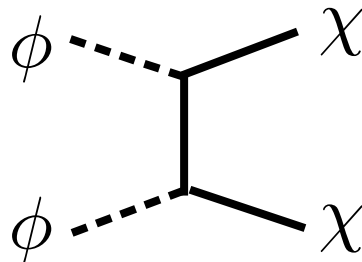


DM production from mediator:

$$\Gamma_{\phi\phi \rightarrow \chi\chi} \propto f_\phi(p_1) f_\phi(p_2)$$

since  $m_\chi \gg m_\phi$

$p_1 + p_2$  should be sizeable  $\rightarrow$  DM prod. is maximised for  $p_1 \gg p_2$



Thus, as for DM is concerned, kinetic eq. approx. actually gives correct order of magnitude [off by factor  $\sim 2$  for low coupling  $g_v$ ]

# About thermal corrections

Since “freeze-in” was first proposed (Hall et al, 2009, although see McDonald 2001) thermal corrections were neglected until few years ago

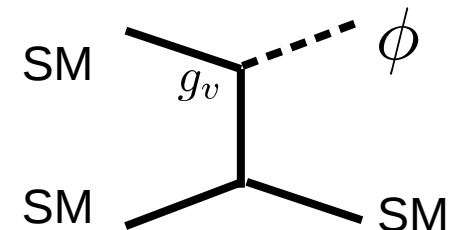
Here thermal corrections are *a priori* relevant, since DM production is out of eq., (so no washout of initial conditions) starting from very high temperatures

In finite-temperature QFT:

- particles acquire temperature-dependent masses
- interaction vertices are also temperature-dependent
- other effects apparently less relevant...

As for the mediator-production is concerned:

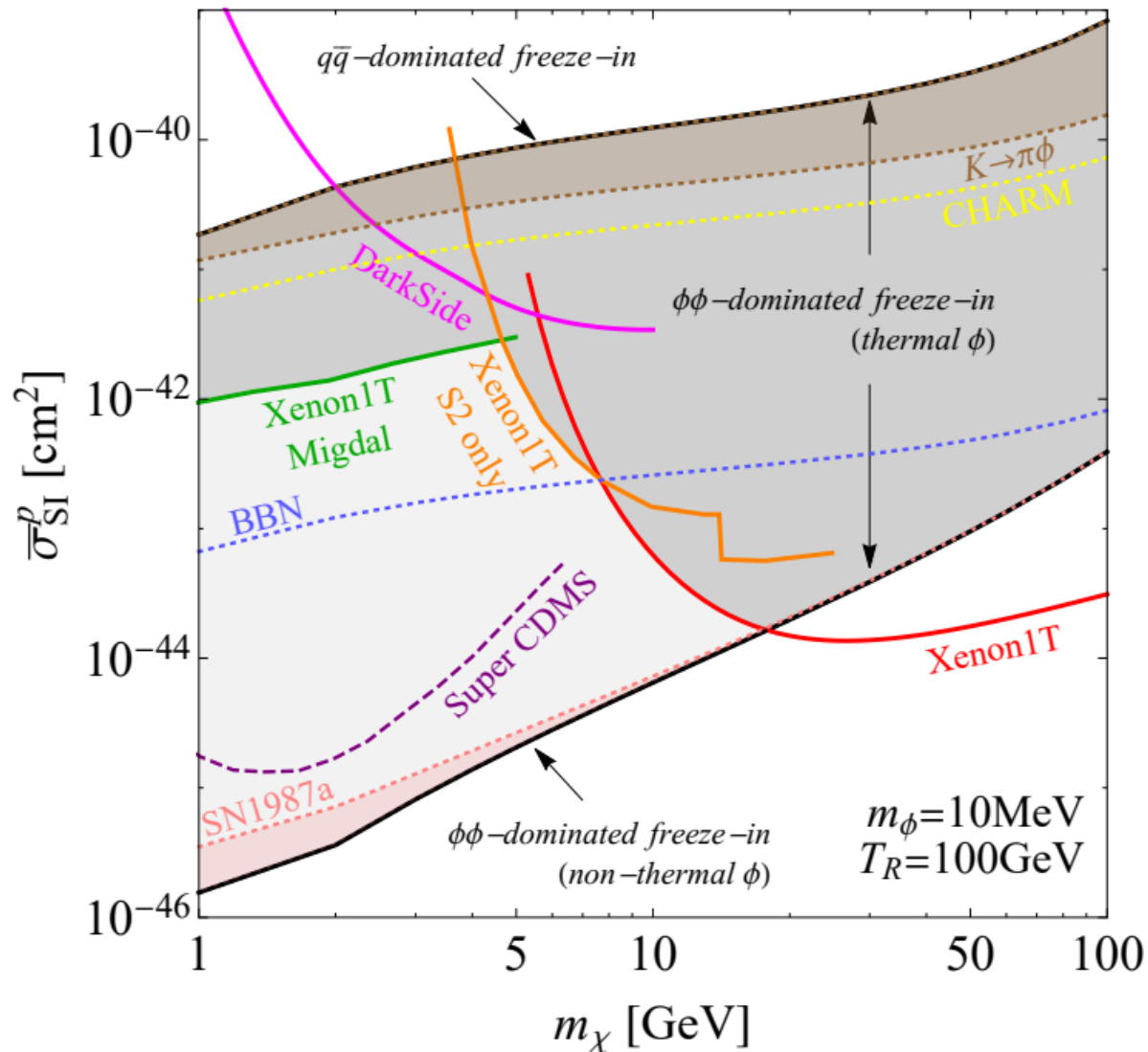
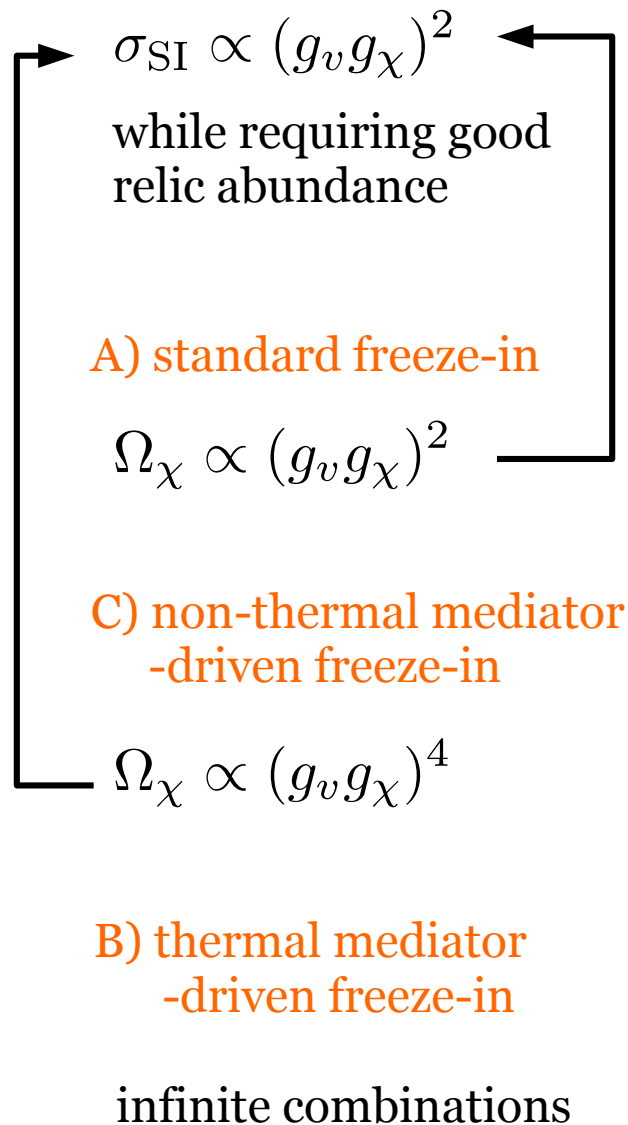
- cross-section's forward divergence regulated by thermal masses at **high momenta**
- Enhancement of med. production at **low momenta** (soft  $\phi$ ), which is absent when no thermal corr. are included



As for DM production is concerned:

**O(1) change in the abundance**, wrt not considering such corrections

# Probes with Direct Detection experiments



# Summary

- Sequential freeze-in is a recently discovered DM production regime at work when  $g_\chi \gg g_v$
- Interestingly, values of coupling combinations much smaller than the standard freeze-in can still deliver good relic abundance
- Case of mediator out of equilibrium is very important, although a priori technically challenging (still, some assumptions may give reasonable results)
- Thermal corrections are very important a priori, but do not change the order of magnitude of the DM abundance
- Direct Detection experiments are able to probe a large part of the parameter space of sequential freeze-in