Modern Tools for

Reusable Publications and Data Products

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LPSC Grenoble Colloquium

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HEPHY ÖAW



Gaël Alguero

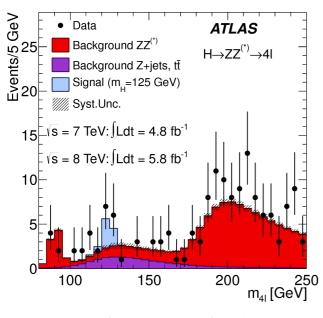
LPSC, Grenoble

Goals for today's discussion

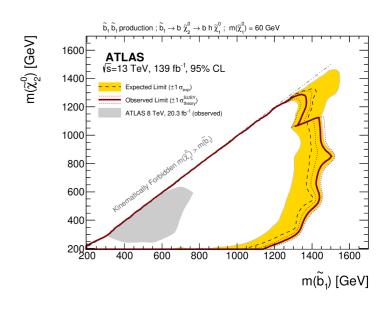
Open and reusable data products are valuable to everyone, especially you!

Show live (toy) example of how easy it can be to get started

Goals of physics analysis at the LHC



CMS Preliminary Run 1: 5.1 fb⁻¹ (7 TeV) + 19.7 fb⁻¹ (8 TeV) Stat. Only 2016: 35.9 fb⁻¹ (13 TeV) Total (Stat. Only) 124.70 ± 0.34 (± 0.31) GeV Run 1 H→ ZZ*→ 4I 125.59 ± 0.46 (± 0.42) GeV Run 1 Combined 125.06 ± 0.29 (± 0.27) GeV 2016 H→γγ 125.78 ± 0.26 (± 0.18) GeV 2016 H→ ZZ*→ 4I 125.26 ± 0.21 (± 0.19) GeV 2016 Combined 125.46 ± 0.17 (\pm 0.13) GeV Run 1 + 2016



Search for new physics

Make precision measurements

Provide constraints on models through setting best limits

- The results of these analyses are **data products** (plots, tables, likelihoods)
- For these data products to be useful need to be shared and reusable with experiments and theory
- Requires the data products to be archived, easily findable, and machine readable (and human understandable)

Easy, just make them open...?

- Making data products open is a great first start, but not enough!
- If just the code and data were made public, would be **largely useless** to anyone but the authors
 - o Millions of lines in codebases, hundreds of TB of data
- Experiments are complex and code and workflows are complicated
- For data products to be useful they need to be able to be understood and used by the scientific community
 - Relationship of the data and the analysis needs to be made clear/available as well

Perspective | Open Access | Published: 15 November 2018

Open is not enough

Xiaoli Chen, Sünje Dallmeier-Tiessen ⊡, Robin Dasler, Sebastian Feger, Pamfilos Fokianos, Jose Benito Gonzalez, Harri Hirvonsalo, Dinos Kousidis, Artemis Lavasa, Salvatore Mele, Diego Rodriguez Rodriguez, Tibor Šimko ⊡, Tim Smith, Ana Trisovic ⊡, Anna Trzcinska, Ioannis Tsanaktsidis, Markus Zimmermann, Kyle Cranmer, Lukas Heinrich, Gordon Watts, Michael Hildreth, Lara Lloret Iglesias, Kati Lassila-Perini & Sebastian Neubert

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Nature Physics 15, 113-119(2019) | Cite this article

14k Accesses | 26 Citations | 161 Altmetric | Metrics
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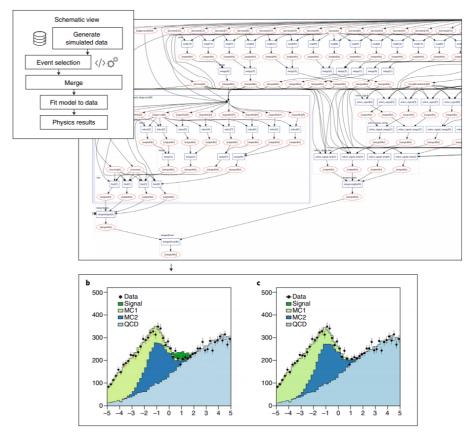
Challenging, but possible

In this paper we have discussed how open sharing enables certain types of data and software reuse, arguing that simple compliance with openness is not sufficient to foster reuse and reproducibility in particle physics. Sharing data is not enough; it is also essential to capture the structured information about the research data analysis workflows and processes to ensure the usability and longevity of results.

...other extreme: Preserving analyses in full

Ideally preserve the *entire* analysis workflow

- RECAST, REANA: Reproducible research data analysis platform
 - Infrastructure for lossless analysis preservation
 - 1. Capture software
 - 2. Capture commands
 - 3. Capture workflow
- This is great for the LHC experiments (pioneered in ATLAS), but requires huge amounts of resources
 - Hard to scale out for everyone in science
 - Currently still an internal service for CERN
- While the LHC experiments are making this a standard what can be done now?



REANA computational workflow for a beyond the Standard Model (BSM) full analysis

Making data products FAIR

- For data products to be useful they should follow
 FAIR principles
- **F**indable: Metadata and data should be easy to find for both humans and computers.
 - Unique persistent identifier (digital object identifier (DOI))
 and rich metadata
- Accessible: Retrievable by identifier using a standardised communications protocol
 - HTTPS, public APIs
- Interoperable: Interoperate with applications or workflows for analysis, storage, and processing
 - Schemas and serialization
 - Formal, shared, broadly applicable
- Reuseable: Well-described so can be replicated and/or combined in different settings
 - Annotated metadata (Codemeta JSON-LD)

Open Access | Published: 15 March 2016

The FAIR Guiding Principles for scientific data management and stewardship

Mark D. Wilkinson, Michel Dumontier, [...] Barend Mons ⊡

Scientific Data 3, Article number: 160018 (2016) | Cite this article

158k Accesses | 1993 Citations | 1610 Altmetric | Metrics

DOE AWARDS \$2.2M TO PROJECT AT THE INTERSECTION OF AI AND HIGH-ENERGY PHYSICS LED BY NCSA'S CENTER FOR ARTIFICIAL INTELLIGENCE INNOVATION

08.11.20 - @ Permalink

The United States Department of Energy (DOE) awards \$2.2 million to the FAIR Framework for Physics-Inspired Artificial Intelligence in High Energy Physics project, spearheaded by the National Center for Supercomputing Applications' Center for Artificial Intelligence Innovation (CAII) and the University of Illinois at Urbana-Champaign (UIUC). The primary focus of this project is to advance our understanding of the relationship between data and artificial intelligence (AI) models by exploring relationships among them through the development of FAIR (Findable, Accessible, Interoperable, and Reusable) frameworks. Using high-energy physics (HEP) as the science driver, this project will develop a FAIR framework to advance our understanding of AI, provide new insights to apply AI techniques, and provide an environment where novel approaches to AI can be explored.

Large interest in FAIR data across all levels

Case study:

publishing LHC experiment full likelihoods



ATLAS PUB Note

ATL-PHYS-PUB-2019-029

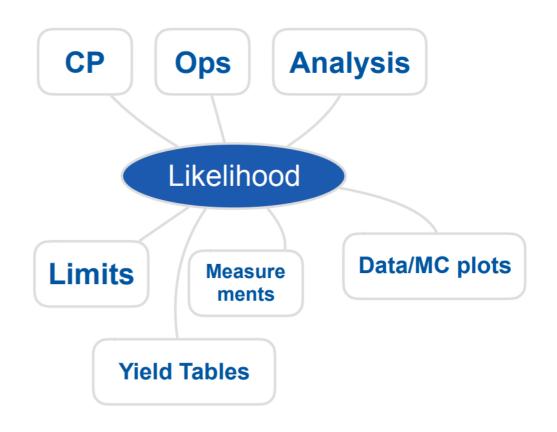
21st October 2019



Reproducing searches for new physics with the ATLAS experiment through publication of full statistical likelihoods

Why is the likelihood important?

- High information-density summary of analysis
- Almost everything we do in the analysis ultimately affects the likelihood and is encapsulated in it
 - Trigger
 - Detector
 - Combined Performance / Physics Object Groups
 - Systematic Uncertainties
 - Event Selection
- Unique representation of the analysis to reuse and preserve



Importance of public likelihoods

- The statistical model of an experimental analysis provides the complete mathematical description of that analysis
 - $p\left(x|ec{lpha}
 ight)$ relating the observed quantities x to the parameters $ec{lpha}$
- Given the likelihood, can employ standard statistical approaches for extracting information from it
- **Essential information** for any detailed interpretation of experimental results
 - Determining the compatibility of theoretical predictions with the observations!

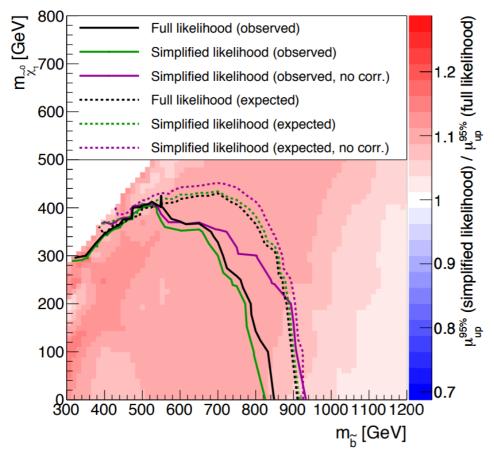
- Requested in Les Houches Recommendations (2012)
- **3b:** When feasible, provide a mathematical description of the final likelihood function in which experimental data and parameters are clearly distinguished, either in the publication or the auxiliary information. Limits of validity should always be clearly specified.
- **3c:** Additionally provide a digitized implementation of the likelihood that is consistent with the mathematical description.

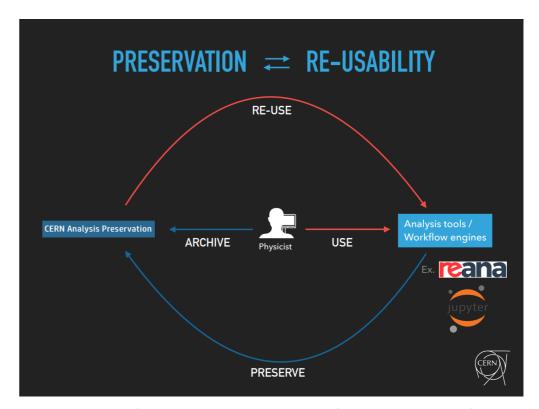
Searches for New Physics: Les Houches Recommendations for the Presentation of LHC Results

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S. Kraml<sup>1</sup>, B.C. Allanach<sup>2</sup>, M. Mangano<sup>3</sup>, H.B. Prosper<sup>4</sup>, S. Sekmen<sup>3,4</sup> (editors), C. Balazs<sup>5</sup>, A. Barr<sup>6</sup>, P. Bechtle<sup>7</sup>, G. Belanger<sup>8</sup>, A. Belyaev<sup>9,10</sup>, K. Benslama<sup>11</sup>, M. Campanelli<sup>12</sup>, K. Cranmer<sup>13</sup>, A. De Roeck<sup>3</sup>, M.J. Dolan<sup>14</sup>, T. Eifert<sup>15</sup>, J.R. Ellis<sup>16,3</sup>, M. Felcini<sup>17</sup>, B. Fuks<sup>18</sup>, D. Guadagnoli<sup>8,19</sup>, J.F. Gunion<sup>20</sup>, S. Heinemeyer<sup>17</sup>, J. Hewett<sup>15</sup>, A. Ismail<sup>15</sup>, M. Kadastik<sup>21</sup>, M. Krämer<sup>22</sup>, J. Lykken<sup>23</sup> F. Mahmoudi<sup>3,24</sup>, S.P. Martin<sup>25,26,27</sup>, T. Rizzo<sup>15</sup>, T. Robens<sup>28</sup>, M. Tytgat<sup>29</sup>, A. Weiler<sup>30</sup>
```

Partial likelihoods already published/preserved

CMS Preliminary





CERN Analysis Preservation implements FAIR data

(CERN, CHEP 2019)

(CMS, 2017)

Full likelihood serialization...

...making good on 19 year old agreement to publish likelihoods

Massimo Corradi

It seems to me that there is a general consensus that what is really meaningful for an experiment is *likelihood*, and almost everybody would agree on the prescription that experiments should give their likelihood function for these kinds of results. Does everybody agree on this statement, to publish likelihoods?

Louis Lyons

Any disagreement? Carried unanimously. That's actually quite an achievement for this Workshop.

(1st Workshop on Confidence Limits, CERN, 2000)

This hadn't been done in HEP until 2019

- In an "open world" of statistics this is a difficult problem to solve
- What to preserve and how? All of ROOT?
- Idea: Focus on a single more tractable binned model first

Enter HistFactory and pyhf

$$f\left(ext{data}| ext{parameters}
ight) = f\left(ec{n},ec{a}|ec{\eta},ec{\chi}
ight) = \prod_{c \, \in \, ext{channels}} \prod_{b \, \in \, ext{bins}_c} ext{Pois}\left(n_{cb}|
u_{cb}\left(ec{\eta},ec{\chi}
ight)
ight) \prod_{\chi \, \in \, ec{\chi}} c_{\chi}\left(a_{\chi}|\chi
ight)$$

Use: Multiple disjoint channels (or regions) of binned distributions with multiple samples contributing to each with additional (possibly shared) systematics between sample estimates

HistFactory is used ubiquitously in binned analyses
Focus on this flexible p.d.f. template rather than "open world" of models

This is a mathematical representation! Nowhere is any software spec defined

pyhf: HistFactory in pure Python hardware accelerated with autodiff 10.5281/zenodo.1169739 (how to cite)









Lukas Heinrich Matthew Feickert

Giordon Stark

CERN

Illinois

UCSC SCIPP

JSON spec fully describes the HistFactory model

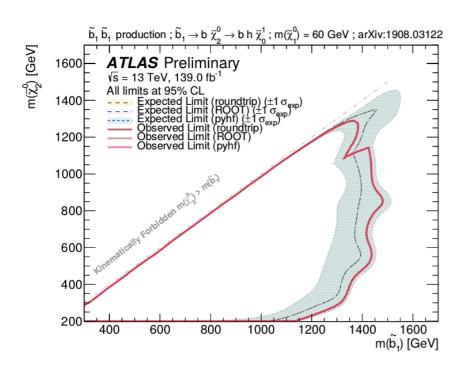
- Human & machine readable declarative statistical models
- Industry standard
 - Will be with us forever
- Parsable by every language
 - Highly portable
 - Bidirectional translation with ROOT
- Versionable and easily preserved
 - JSON Schema describing HistFactory specification
 - Attractive for analysis preservation
 - Highly compressible

```
"channels": [ # List of regions
        { "name": "singlechannel",
          "samples": [ # List of samples in region
            { "name": "signal",
              "data": [20.0, 10.0],
              # List of rate factors and/or systematic uncertainties
              "modifiers": [ { "name": "mu", "type": "normfactor", "data": null} ]
            { "name": "background",
              "data": [50.0, 63.0],
              "modifiers": [ {"name": "uncorr bkguncrt", "type": "shapesys", "data": [5.0, 12.0]} ]
    "observations": [ # Observed data
        { "name": "singlechannel", "data": [55.0, 62.0] }
    "measurements": [ # Parameter of interest
        { "name": "Measurement", "config": {"poi": "mu", "parameters": []} }
    "version": "1.0.0" # Version of spec standard
```

JSON defining a single channel, two bin counting experiment with systematics

ATLAS validation and publication of likelihoods

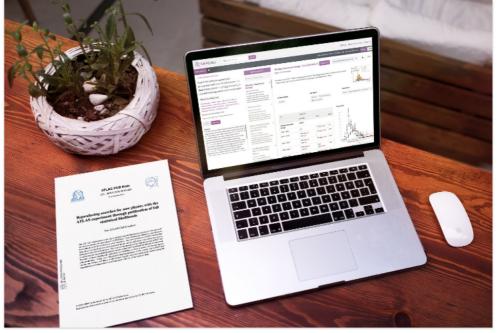
		ATLAS Note
	Report number	ATL-PHYS-PUB-2019-029
Title		$Reproducing \ searches \ for \ new \ physics \ with \ the \ ATLAS \ experiment \ through \ publication \ of full \ statistical \ likelihoods$
	Corporate Author(s)	The ATLAS collaboration



New open release allows theorists to explore LHC data in a new way

The ATLAS collaboration releases full analysis likelihoods, a first for an LHC experiment

9 JANUARY, 2020 | By Katarina Anthony



Explore ATLAS open likelihoods on the HEPData platform (Image: CERN)

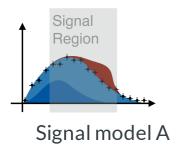
(CERN, 2020)

JSON Patch for signal model (reinterpretation)

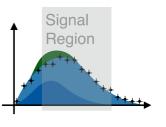
JSON Patch gives ability to **easily mutate model**Think: test a **new theory** with a **new patch**!

(c.f. Lukas Heinrich's RECAST talk from Snowmass 2021 Computational Frontier Workshop)

Combined with RECAST gives powerful tool for **reinterpretation studies**



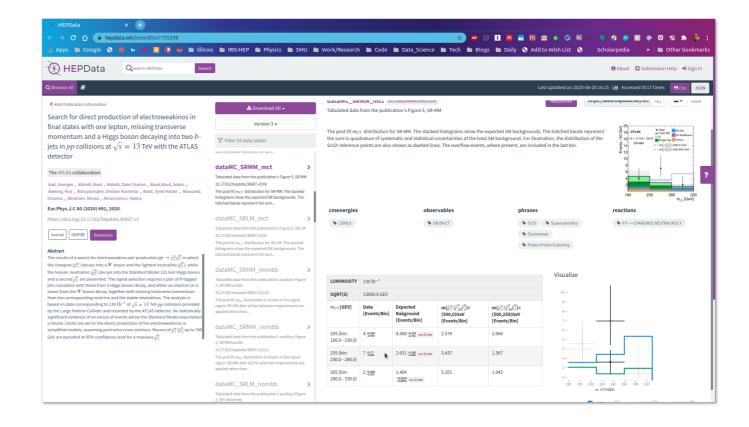
```
$ pyhf cls example.json | jq .CLs_obs
0.053994246621274014
$ cat new_signal.json
    "op": "replace",
    "path": "/channels/0/samples/0/data",
    "value": [10.0, 6.0]
}]
$ pyhf cls example.json --patch new_signal.json | jq .CLs_obs
0.3536906623262466
```



Signal model B

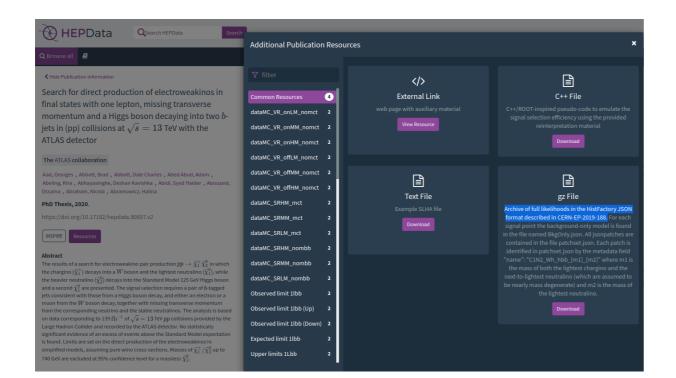


- Repository for publicationrelated High-Energy Physics data
- Allows for publication of data products that accompany papers
 - Extract values for Figures and Tables
 - Serializations in common formats
 - Associated DOI
- Vital resource in the collaboration cycle between experiment and theory



Likelihoods preserved on HEPData

- pyhf pallet:
 - Background-only model JSON stored
 - Hundreds of signal model JSON Patches stored together as a pyhf "patch set" file
- Fully preserve and publish the full statistical model and observations to give likelihood
 - with own DOI! DOI 10.17182/hepdata.90607.v3/r3





...can be used from HEPData

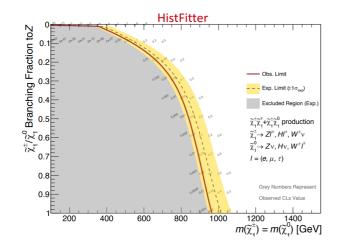
- pyhf pallet:
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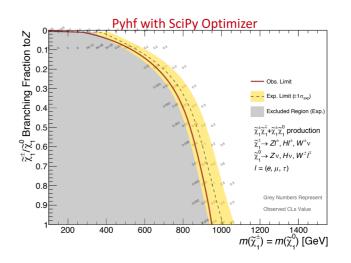
```
$ pyhf contrib download https://doi.org/10.17182/hepdata.90607.v3/r3 1Lbb-pallet && cd 1Lbb-pallet
$ pyhf patchset verify BkgOnly.json patchset.json
All good.
$ cat BkgOnly.json | \
  pyhf cls --patch <(pyhf patchset extract --name C1N2_Wh_hbb_900_300 patchset.json) | \</pre>
  jq .CLs_obs
0.5004165245329418
$ pyhf patchset extract --name C1N2_Wh_hbb_900_400 --output-file C1N2_Wh_hbb_900_400_patch.json patchset.json
$ pyhf cls --patch C1N2 Wh hbb 900 400 patch.json BkgOnly.json | jg .CLs obs
0.5735007268333779
```

Rapid adoption in ATLAS...

- Five ATLAS analyses with full likelihoods published to HEPData
- ATLAS SUSY will be continuing to publish full Run 2 likelihoods
- More FAIR than traditional ROOT workspaces

- direct staus, doi:10.17182/hepdata.89408 (2019)
- sbottom multi-b, doi:10.17182/hepdata.91127 (2019)
- 1Lbb, doi:10.17182/hepdata.92006 (2019)
- 3L eRJR, doi:10.17182/hepdata.90607 (2020)
- ss3L search, doi:10.17182/hepdata.91214 (2020)



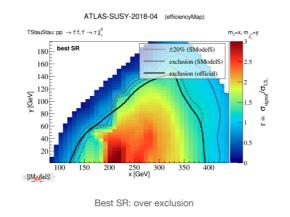


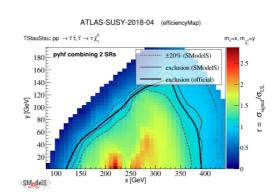
...and by theory

- pyhf likelihoods discussed in
 - Les Houches 2019 Physics at TeV Colliders: New Physics Working Group Report
 - Higgs boson potential at colliders: status and perspectives
- SModelS team has implemented a SModelS/pyhf interface [arXiv:2009.01809]
 - tool for interpreting simplifiedmodel results from the LHC
 - designed to be used by theorists
 - SModels authors gave tutorial at TOOLS 2020 workshop

Validation & impact

ATLAS-SUSY-2018-04: TStauStau





Gaël Alguero, SK, Wolfgang Waltenberger,

Full likelihood: very good agreement with official ATLAS result

The remaining small difference is probably due to the (interpolated) $A\times\epsilon$ values from the simplified model efficiency maps not exactly matching the "true" ones of the experimental analysis.

S. Kraml - Feedback on use of public likelihoods - 24 Sep 2020

1

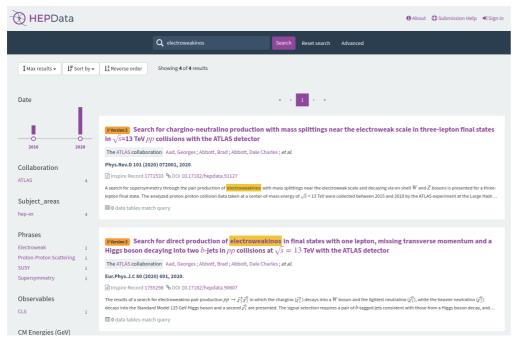
Feedback on use of public Likelihoods, Sabine Kraml (ATLAS Exotics + SUSY Reinterpretations Workshop)

- Have produced three comparisons to published ATLAS likelihoods: ATLAS-SUSY-2018-04, ATLAS-SUSY-2018-31, ATLAS-SUSY-2019-08
 - Compare simplified likelihood (bestSR) to full likelihood (pyhf) using SModelS

FAIR summary for likelihoods: Findable

Metadata and data should be easy to find for both humans and computers

Searchable database



Transparent data products



FAIR summary for likelihoods: Accessible

Once found metadata and data need to be easily accessed

Clickable buttons to download

DOI 10.17182/hepdata.90607.v3/r3

CLI tools and Python API



\$ pyhf contrib download --verbose https://doi.org/10.17182/hepdata.90607.v3/r3 1Lbb-pallet
1Lbb-pallet/patchset.json
1Lbb-pallet/README.md
1Lbb-pallet/Bkg0nly.json

FAIR summary for likelihoods: Interoperable

Interoperate with applications for analysis, storage, and processing

JSON spec

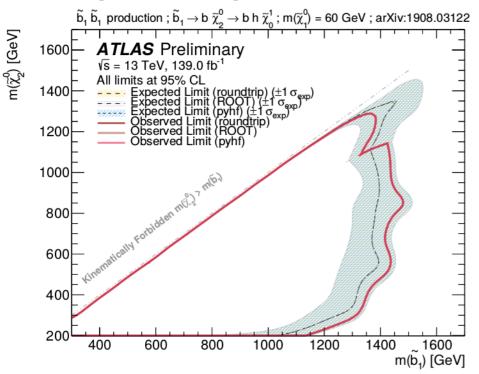
```
"channels": [
        { "name": "singlechannel",
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              "data": [50.0, 60.0],
              "modifiers": [ {"name": "uncorr_bkguncrt", "type": "shapesys", "data": [5.0, 12.0]} ]
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    "measurements": [
        { "name": "Measurement", "config": {"poi": "mu", "parameters": []} }
    "version": "1.0.0"
```

FAIR summary for likelihoods: Reusable

Well-described so can be replicated and/or combined in different settings

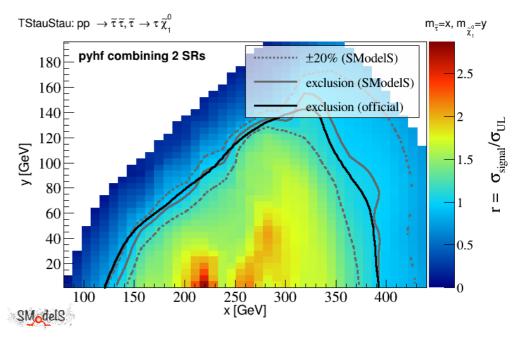
HEPData platform and rich metadata make possible

Replication of published results



New applications and reinterpretation

ATLAS-SUSY-2018-04 (efficiencyMap)



Tools for making data products FAIR





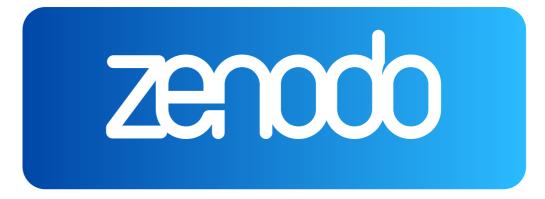
- HEP centric by design (FAIR data core tool)
- Open source
- HEP data products:
 - o table source data
 - o figure source data
 - likelihoods

- Open science resource for all fields
- Open source (but your files can be closed access)
- Versioned archival of everything:
 - code
 - documents
 - data products
 - data sets

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Why use Zenodo?

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- GitHub integration Easily preserve your GitHub repository in Zenodo.
- Usage statisics All uploads display standards compliant usage statistics



October 20, 2020



Open Access

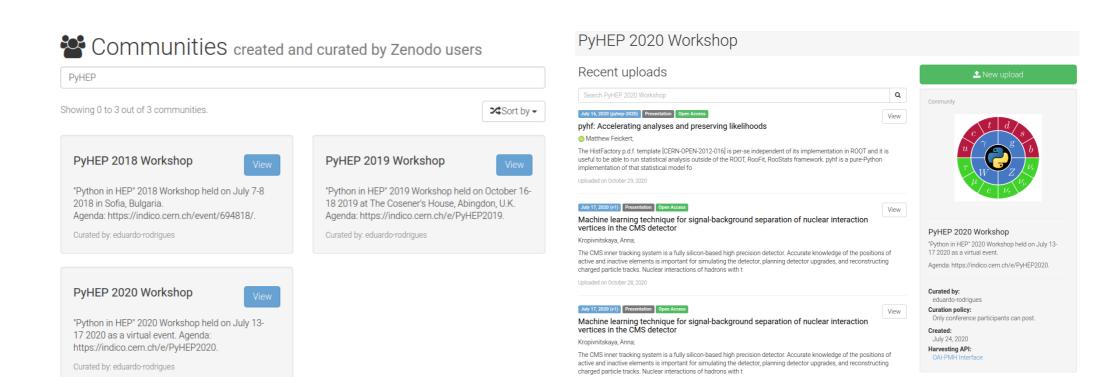
scikit-hep/pyhf: v0.5.3

(b) Lukas Heinrich; **(b)** Matthew Feickert; **(b)** Giordon Stark pure-Python HistFactory implementation with tensors and autodiff

DOI

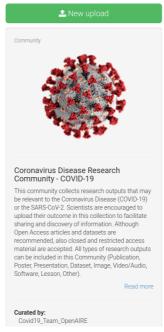
10.5281/zenodo.1169739

Communities allow for archival of collections

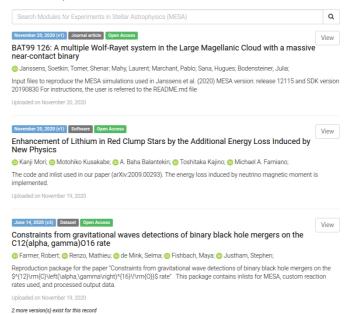


...and finding topical data sets

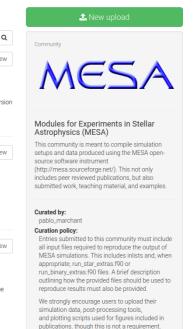




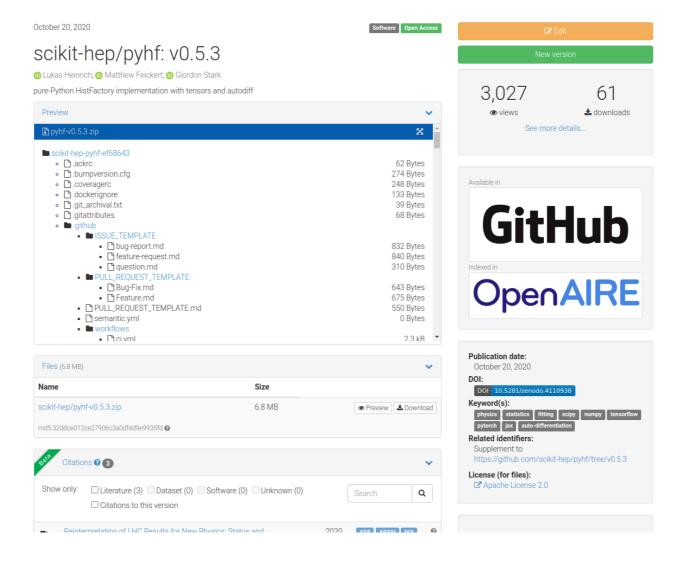
Modules for Experiments in Stellar Astrophysics (MESA)



Recent uploads



Anatomy of a Zenodo archive



Zenodo DOI \rightarrow reproducible examples



Turn a Git repo into a collection of interactive notebooks

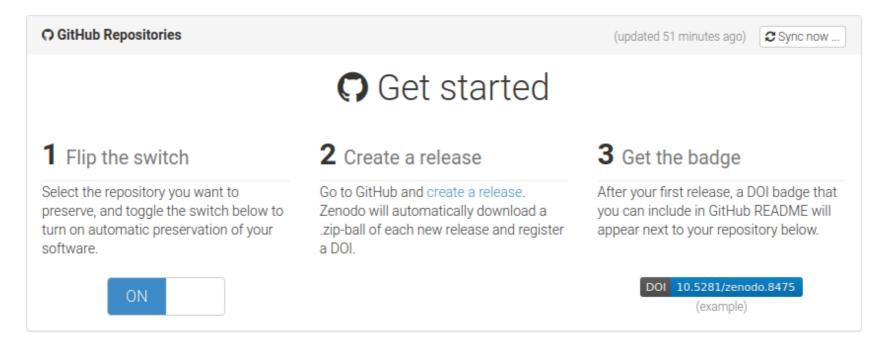
Have a repository full of Jupyter notebooks? With Binder, open those notebooks in an executable environment, making your code immediately reproducible by anyone, anywhere.

New to Binder? Get started with a Zero-to-Binder tutorial in Julia, Python or R.

Zenodo DOI ▼	10.5281/zenodo.41	52915		
Git ref (branch, tag, or commit)		Path to a notebook file (optional)		
		Path to a notebook file (optional)	File →	
.,	elow and share your Bi	o/10.5281/zenodo.4152915/		

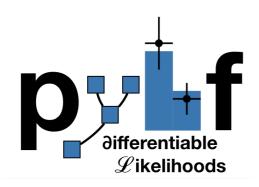
DOI minting made easy

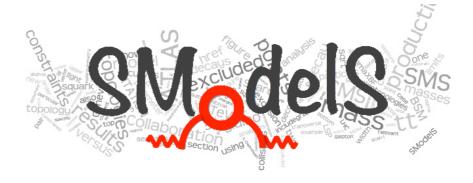
- Everything on Zenodo has a DOI
- You can upload directly to Zenodo or can enable it to automatically preserve work from GitHub
- We're going to do so now



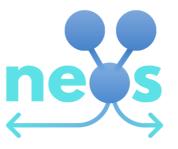
Open data creates space for open ecosystems

All these tools are able to make use of public likelihoods









simplify

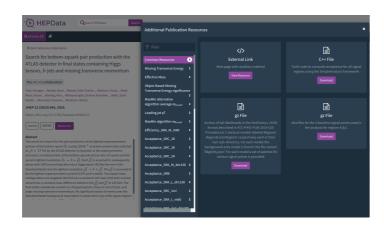
CI passing docs unknown Codecov 82% pypi package 0.1.1 python 3.6 | 3.7 | 3.8 code style bl

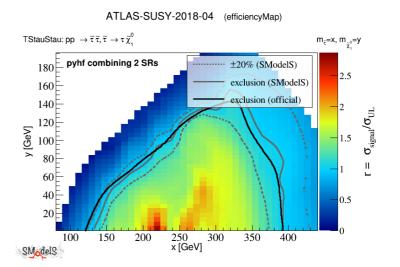
A package that creates simplified likelihoods from full likelihoods. Currently, only one form of simplified likelihoods is implemented, but the idea is to implement additional versions of the simplified likelihoods, such that the user can chose the one he likes the most (or needs the most).

FAIR data products are able to expand and accelerate research and tooling

Summary

- Application of Findable, Accessible, Interoperable, and Reuseable data principles extends the usefulness of data far beyond the publication
 - Case study of FAIR open likelihoods increasing the communication and sharing of data products between HEP experiment and theory
 - Expanding scope of existing work and creating new
- Democratizing process
 - Data products in open common formats ensures accessible to everyone, regardless of resources
 - Breeds best practices and open ecosystem growth
- Existing infrastructure makes FAIR data practices easy and smart to do
 - Archival, storage hosting, DOI/citation





Backup

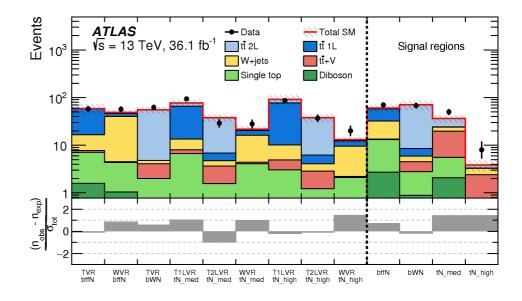
HistFactory Template

$$f\left(ext{data}| ext{parameters}
ight) = f\left(ec{n},ec{a}|ec{\eta},ec{\chi}
ight) = \prod_{c \, \in \, ext{channels}} \prod_{b \, \in \, ext{bins}_c} ext{Pois}\left(n_{cb}|
u_{cb}\left(ec{\eta},ec{\chi}
ight)
ight) \prod_{\chi \, \in \, ec{\chi}} c_{\chi}\left(a_{\chi}|\chi
ight)$$

Use: Multiple disjoint channels (or regions) of binned distributions with multiple samples contributing to each with additional (possibly shared) systematics between sample estimates

Main pieces:

- Main Poisson p.d.f. for simultaneous measurement of multiple channels
- Event rates ν_{cb} (nominal rate ν_{scb}^0 with rate modifiers)
- Constraint p.d.f. (+ data) for "auxiliary measurements"
 - encode systematic uncertainties (e.g. normalization, shape)
- \vec{n} : events, \vec{a} : auxiliary data, $\vec{\eta}$: unconstrained pars, $\vec{\chi}$: constrained pars



Example: **Each bin** is separate (1-bin) channel, each **histogram** (color) is a sample and share a **normalization systematic** uncertainty

HistFactory Template

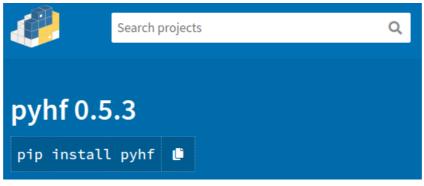
$$f\left(ec{n},ec{a}|ec{\eta},ec{\chi}
ight) = \prod_{c \,\in\, ext{channels } b \,\in\, ext{bins}_c} ext{Pois}\left(n_{cb}|
u_{cb}\left(ec{\eta},ec{\chi}
ight)
ight) \prod_{\chi \,\in\, ec{\chi}} c_\chi\left(a_\chi|\chi
ight)$$

Mathematical grammar for a simultaneous fit with

- multiple "channels" (analysis regions, (stacks of) histograms)
- each region can have multiple bins
- coupled to a set of constraint terms

This is a mathematical representation! Nowhere is any software spec defined **Until now** (2018), the only implementation of HistFactory has been in ROOT

pyhf: HistFactory in pure Python



Full likelihood plans and ideas

Besides allowing us to better reproduce the official limits of each analysis, the full likelihoods

- will greatly improve global fits
- offer interesting possibilities to explore cross-analysis correlations
 - Systematic naming of nuisances?



for this great step forward to publish full likelihoods!

- extremely useful for long-term preservation
- opens the door for much better reinterpretation studies

I'm sure lots of interesting work is to follow



Please keep doing this systematically for all new analyses

(and please also keep providing ample simplified model Axe maps 👍)



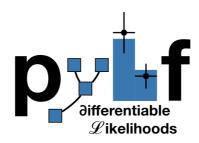
S. Kraml - Feedback on use of public likelihoods - 24 Sep 2020

What is pyhf?

Please checkout the many resources we have starting with the website and the SciPy 2020 talk!









References

- 1. F. James, Y. Perrin, L. Lyons, Workshop on confidence limits: Proceedings, 2000.
- 2. ROOT collaboration, K. Cranmer, G. Lewis, L. Moneta, A. Shibata and W. Verkerke, *HistFactory: A tool for creating statistical models for use with RooFit and RooStats*, 2012.
- 3. L. Heinrich, H. Schulz, J. Turner and Y. Zhou, Constraining A_4 Leptonic Flavour Model Parameters at Colliders and Beyond, 2018.
- 4. A. Read, Modified frequentist analysis of search results (the ${
 m CL}_s$ method), 2000.
- 5. K. Cranmer, CERN Latin-American School of High-Energy Physics: Statistics for Particle Physicists, 2013.
- 6. ATLAS collaboration, Search for bottom-squark pair production with the ATLAS detector in final states containing Higgs bosons, b-jets and missing transverse momentum, 2019
- 7. ATLAS collaboration, *Reproducing searches for new physics with the ATLAS experiment through publication of full statistical likelihoods*, 2019
- 8. ATLAS collaboration, Search for bottom-squark pair production with the ATLAS detector in final states containing Higgs bosons, b-jets and missing transverse momentum: HEPData entry, 2019

The end.