# Detection of Thermal SZ — CMB Lensing Cross-Correlation in *Planck* Legacy Data

## Colin Hill

Columbia University

mm Universe Grenoble - LPSC 26 June 2023







to appear w/ F. McCarthy (arXiv: this week) to appear w/ F. McCarthy (arXiv: next week)

## Columbia/CCA Talks This Week

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 Ola Kusiak: Probing the Ionized Gas Thermodynamics in unWISE Galaxies with the Sunyaev-Zel'dovich Effect Wednesday, 2:10 pm, Room 9



 Kristen Surrao: Enhancing Kinematic Sunyaev-Zel'dovich Power Spectrum Measurements by Removing CIB Contamination Using unWISE Galaxies



Wednesday, 2:20 pm, Amphitheatre

 Alina Sabyr: Compton-y distortion: CMB constraints and new prospects with CIB

Thursday, 4:20 pm, Room 9



 Fiona McCarthy: Constraints on primordial non-Gaussianity from halo bias measured through CMB lensing cross-correlations

Wednesday, 3:00 pm, Amphitheater



 Boris Bolliet (now @Cambridge): class\_sz: a fast and accurate code for SZ and cross-correlations

Monday, 3:30 pm, Amphitheatre



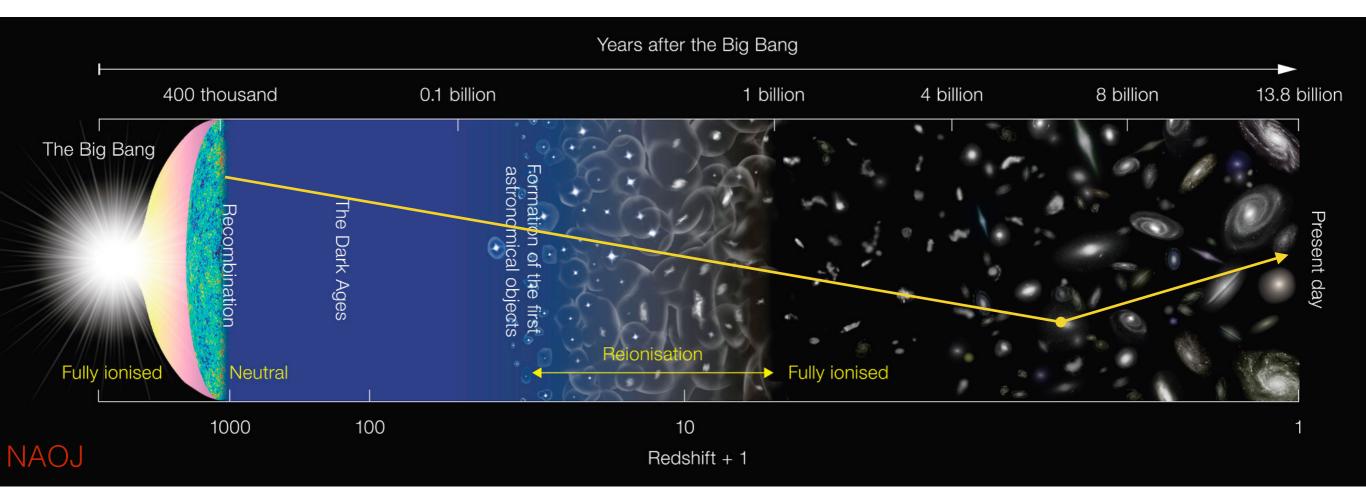
## Outline

- New Compton-y Maps from Planck PR4
  - Flexible CIB Deprojection
  - Public Code: pyilc
- Robust Detection of Thermal SZ CMB Lensing Cross-Correlation
- New Compton-y Maps from ACT DR6 + Planck

# Cosmic Microwave Background Backlight

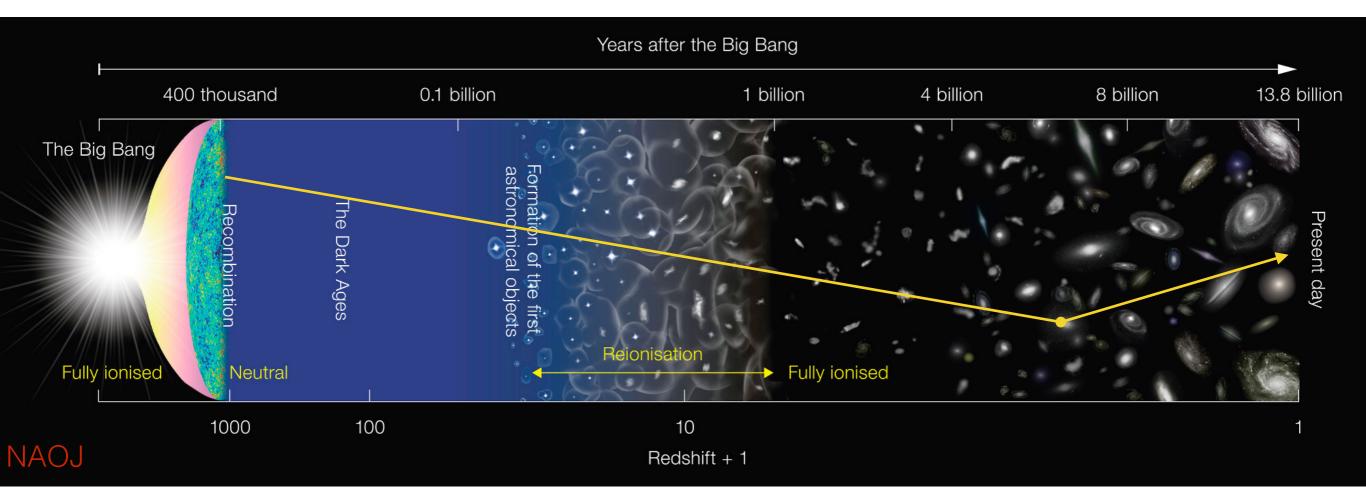
## Cosmic Microwave Backlight

Secondary Anisotropies



## Cosmic Microwave Backlight

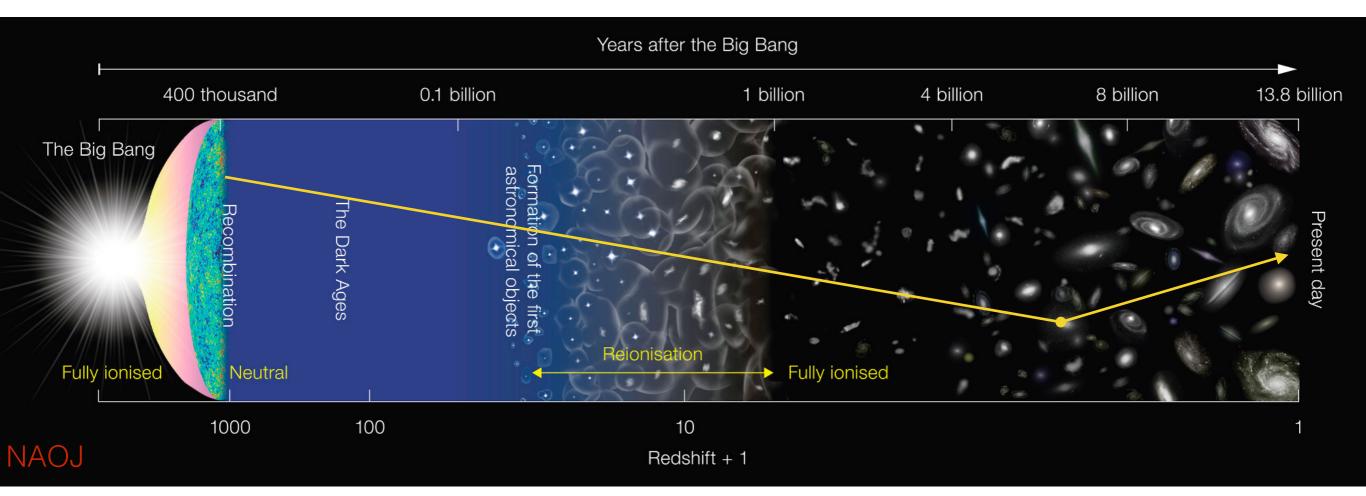
Secondary Anisotropies



- Scattering: thermal / kinematic Sunyaev-Zel'dovich effect redshift-independent

## Cosmic Microwave Backlight

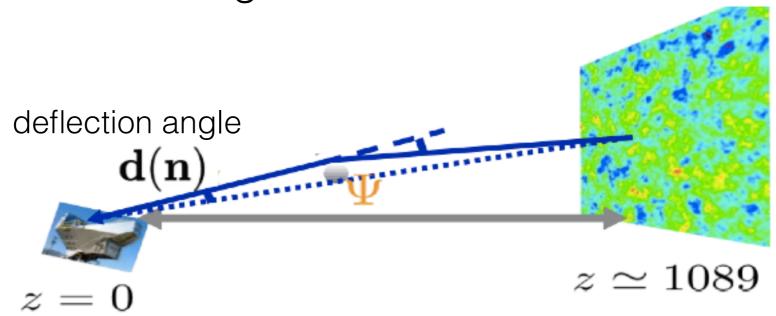
Secondary Anisotropies



- Scattering: thermal / kinematic Sunyaev-Zel'dovich effect
- Deflection: gravitational lensing

Re-mapping of CMB fluctuations (preserves blackbody form)

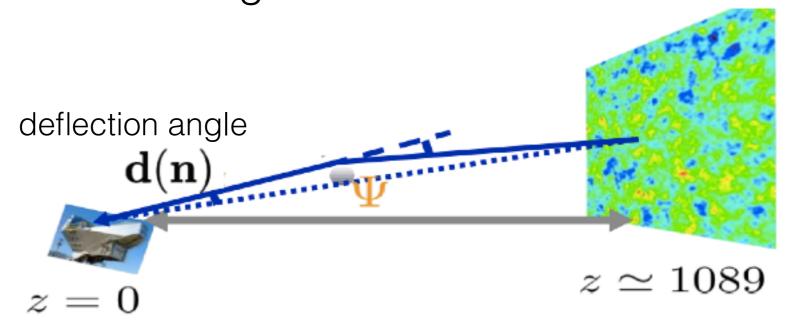
Many (~50) small random deflections lead to a net deflection (~2-3 arcmin), coherent on ~deg scales



$$T(\hat{\mathbf{n}})_{\text{lensed}} = T(\hat{\mathbf{n}} + \mathbf{d}(\hat{\mathbf{n}}))_{\text{unlensed}}$$

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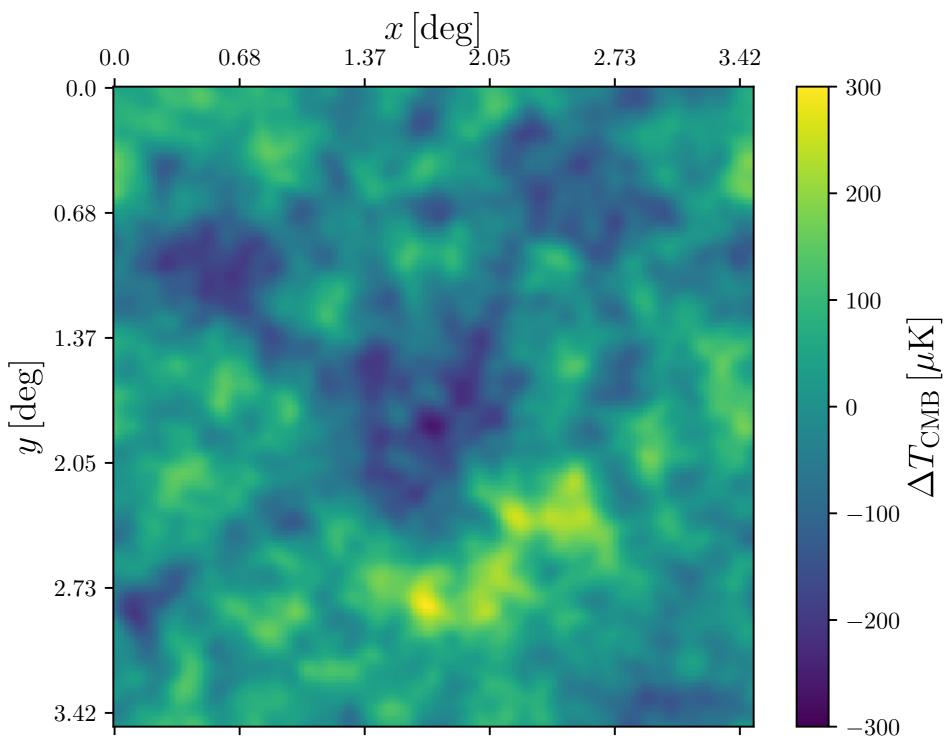
$$T(\hat{\mathbf{n}})_{\text{lensed}} = T(\hat{\mathbf{n}} + \mathbf{d}(\hat{\mathbf{n}}))_{\text{unlensed}}$$

Quadratic reconstruction:

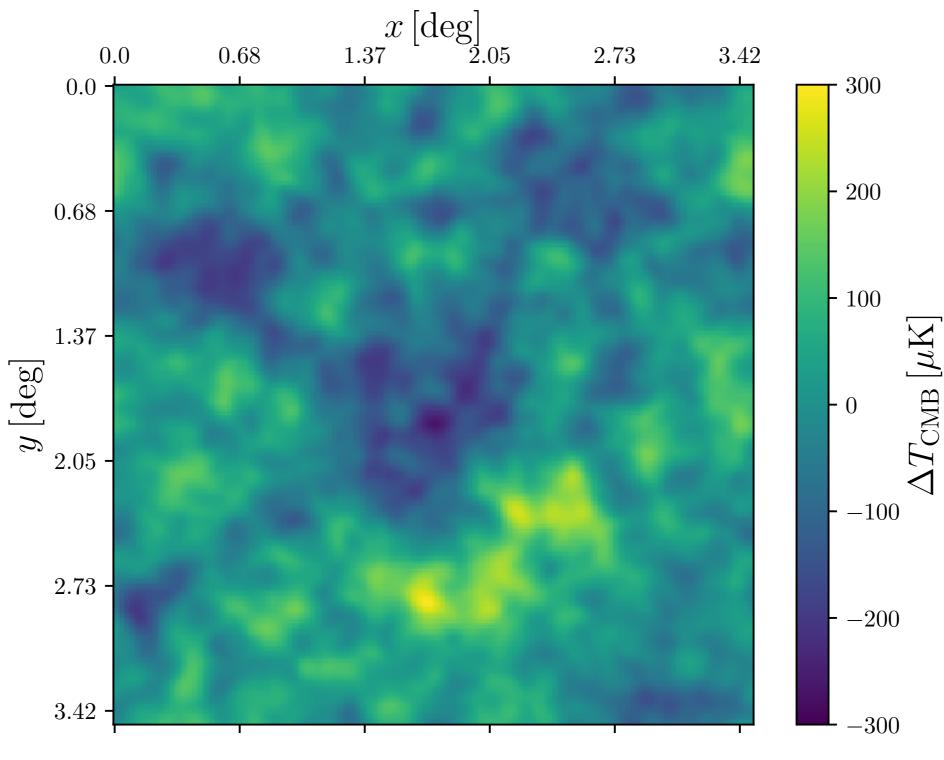
$$\phi(\vec{\mathbf{L}}) \sim T(\vec{\ell})T(\vec{\mathbf{L}} - \vec{\ell})$$

$$\vec{\mathbf{d}} = \nabla \phi$$

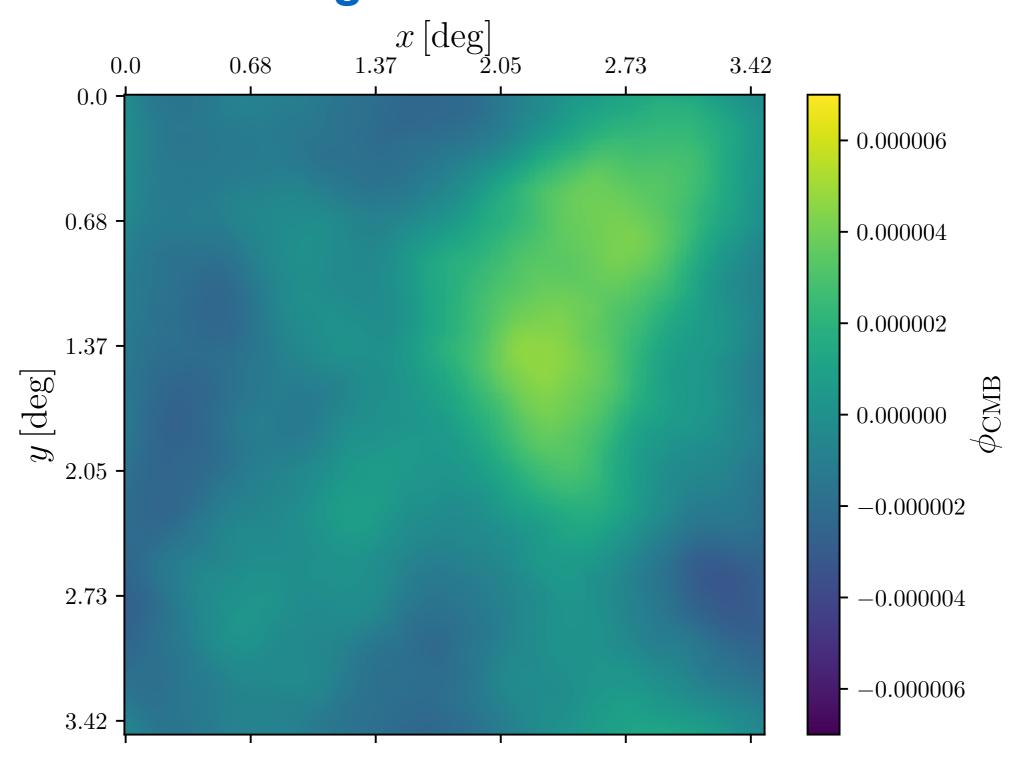
lensing potential



unlensed



lensed



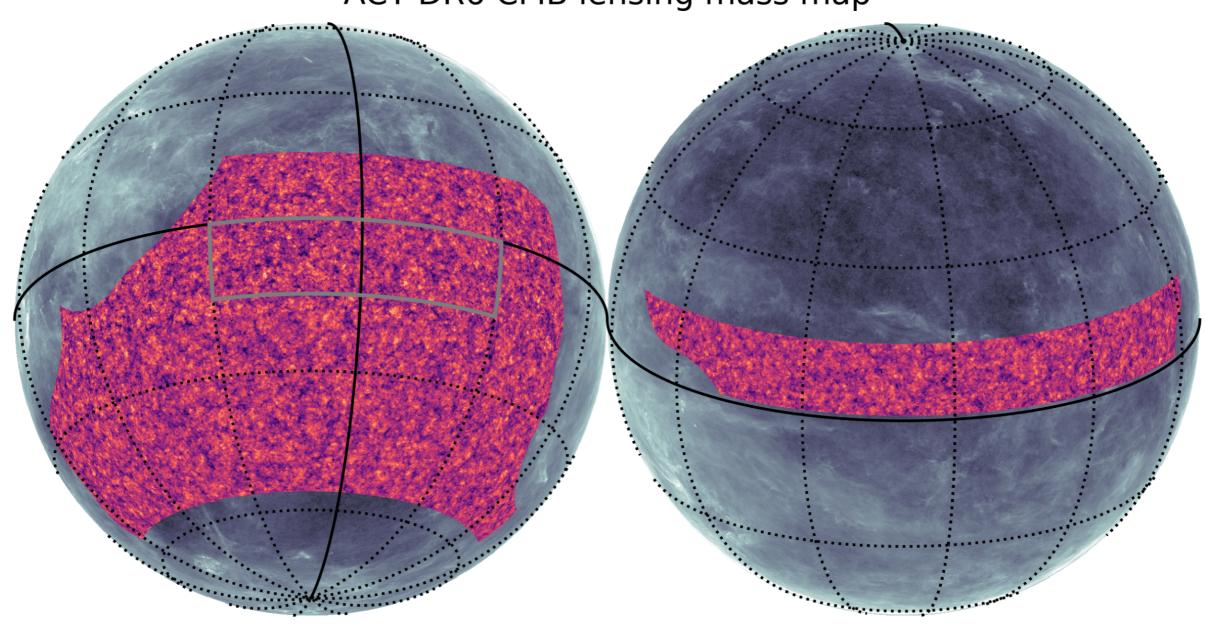
input lensing potential

$$\phi(\hat{\boldsymbol{n}}) = -2 \int_0^{\chi_*} d\chi \frac{f_K(\chi_* - \chi)}{f_K(\chi_*) f_K(\chi)} \Psi(\chi \hat{\boldsymbol{n}}; \eta_0 - \chi)$$

## CMB Lensing

State of the art: ACT DR6

ACT DR6 CMB lensing mass map

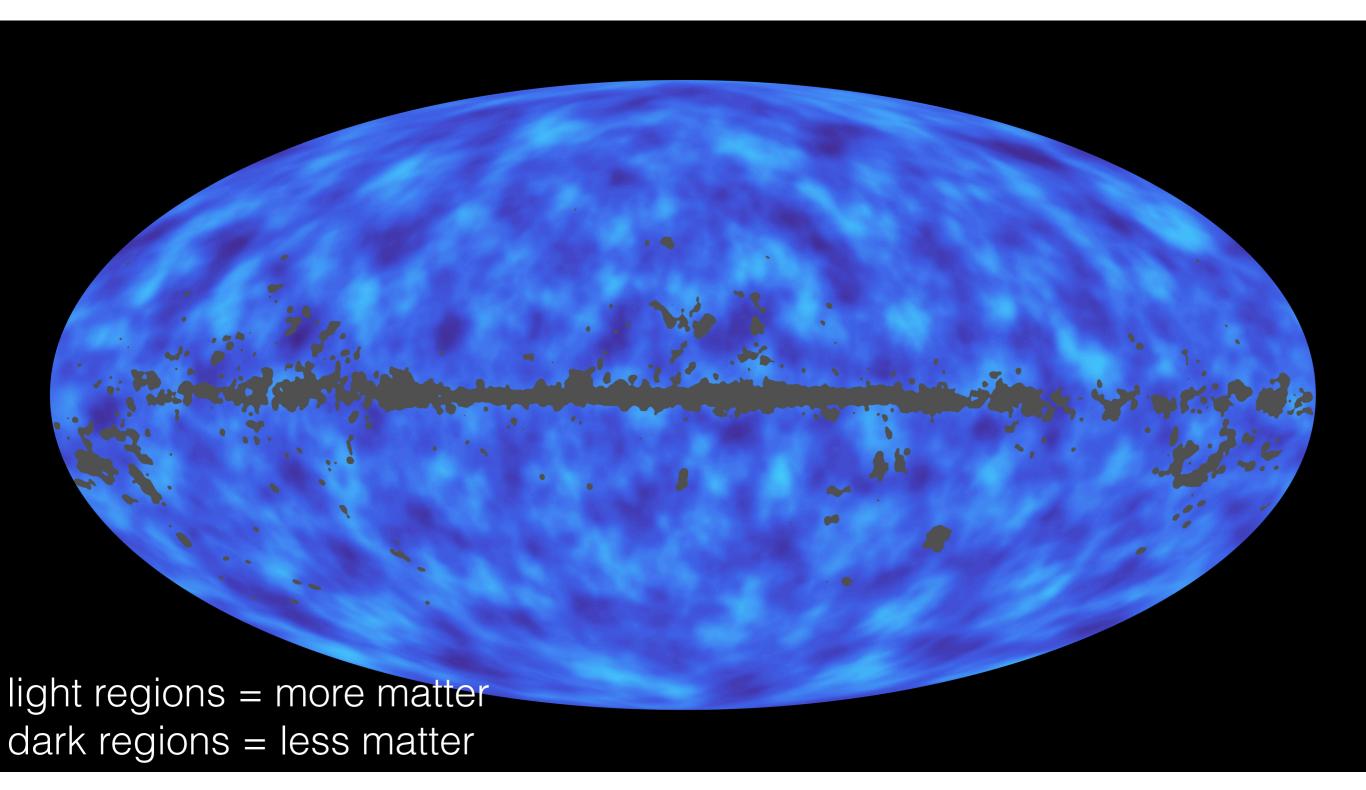


light regions = more matter; dark regions = less matter

Qu et al. (2023); Madhavacheril et al. (2023); MacCrann et al. (2023)

## CMB Lensing

State of the art: *Planck* 

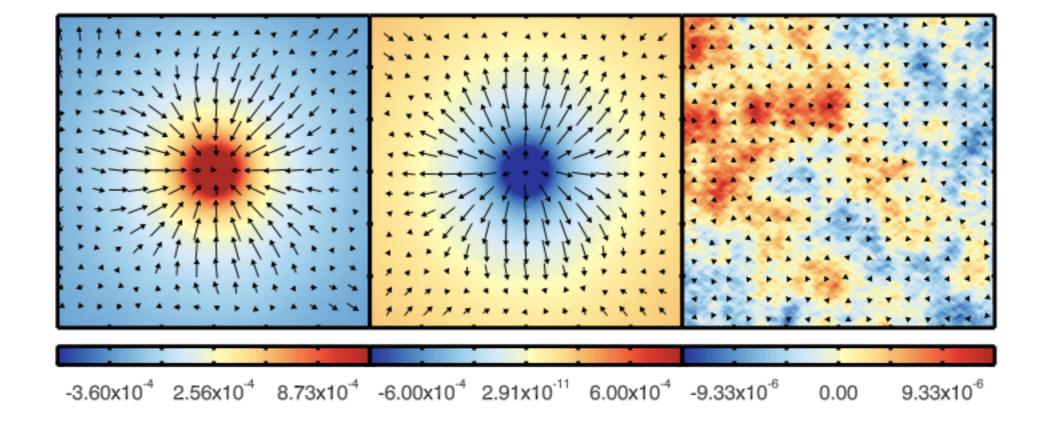


## Cosmic Infrared Background

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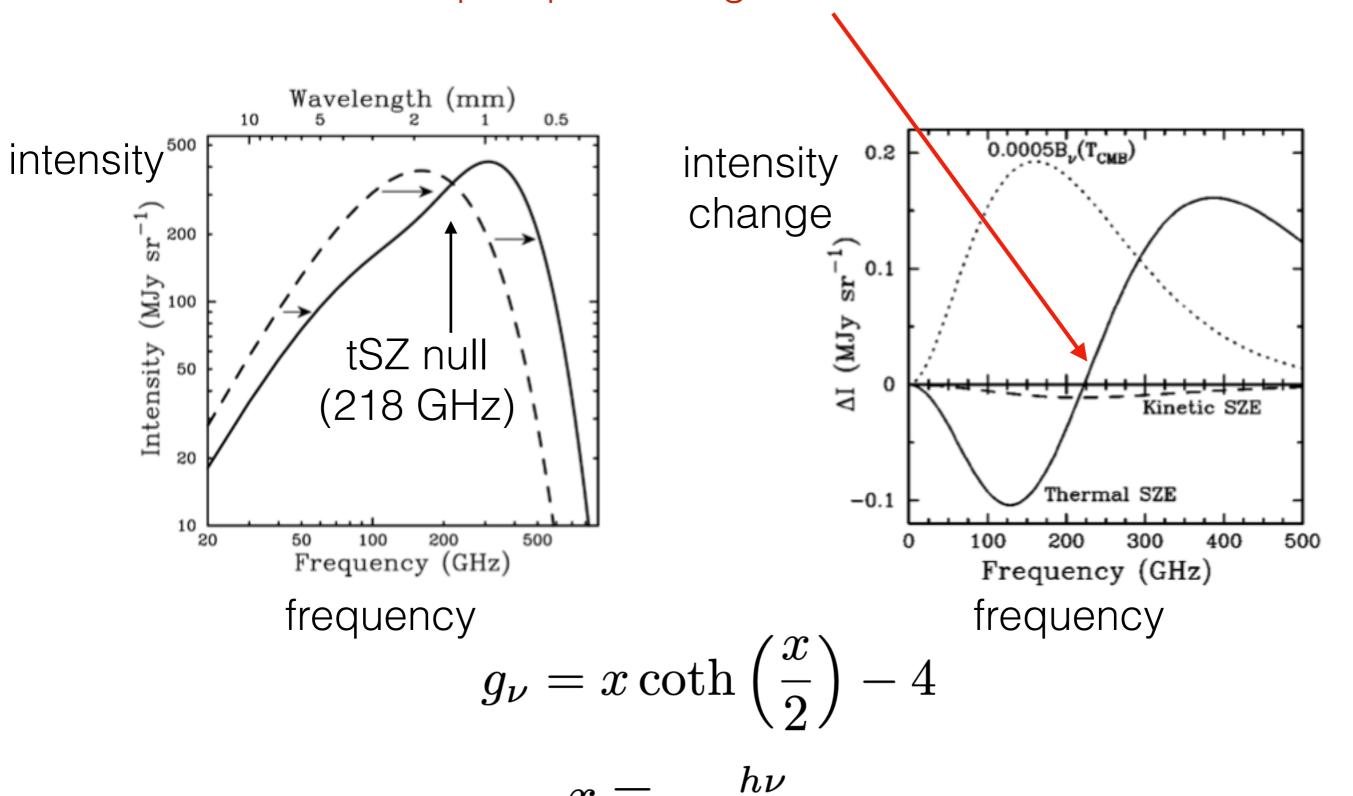
cumulative emission of dusty, star-forming galaxies over cosmic time strongly correlated with CMB lensing (and partially correlated w/ tSZ and other fields)





# Compton-y Maps from Planck PR4 with pyilc

Utilize unique spectral signature of tSZ effect



Figures: Carlstrom+ (2002)

#### Internal Linear Combination

relatively agnostic approach, flexible choice of domain

$$\Delta T_i(p) = a_i y(p) + n_i(p)$$

i←→frequency

observed temperature fluctuation

component of interest

noise+ contaminants

#### Internal Linear Combination

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$$\Delta T_i(p) = a_i y(p) + n_i(p)$$
 i frequency

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minimum-variance estimator with unit response to desired component:

$$\hat{y}(p) = w_i \Delta T_i(p)$$
  $w_j = \frac{a_i (\hat{R}^{-1})_{ij}}{a_k (\hat{R}^{-1})_{kl} a_l}$ 

$$\hat{R}_{ij} = N_{\text{pix}}^{-1} \sum_{p} \Delta T_i(p) \Delta T_j(p)$$

flexibility = choice of domain on which to compute freq.-freq. covariance

#### Constrained Internal Linear Combination

extension: explicitly remove other component(s) as well

$$\Delta T_i(p) = a_i y(p) + b_i s(p) + n_i(p)$$

observed temperature fluctuation

component of interest

component to remove

noise + other contaminants

#### Constrained Internal Linear Combination

extension: explicitly remove other component(s) as well

$$\Delta T_i(p) = a_i y(p) + b_i s(p) + n_i(p)$$

observed temperature fluctuation

component of interest

component to remove

noise + other contaminants

minimum-variance estimator with unit response to desired component and zero response to undesired component:

$$w_j = \frac{\left(b_k(\hat{R}^{-1})_{kl}b_l\right)a_i(\hat{R}^{-1})_{ij} - \left(a_k(\hat{R}^{-1})_{kl}b_l\right)b_i(\hat{R}^{-1})_{ij}}{\left(a_k(\hat{R}^{-1})_{kl}a_l\right)\left(b_m(\hat{R}^{-1})_{mn}b_n\right) - \left(a_k(\hat{R}^{-1})_{kl}b_l\right)^2}$$

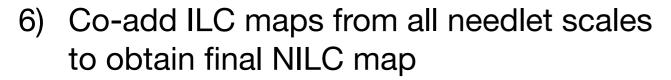
- can be extended to explicitly remove N components
- advantage: can remove contaminants that could bias some analysis
- disadvantage: variance in final ILC map is larger

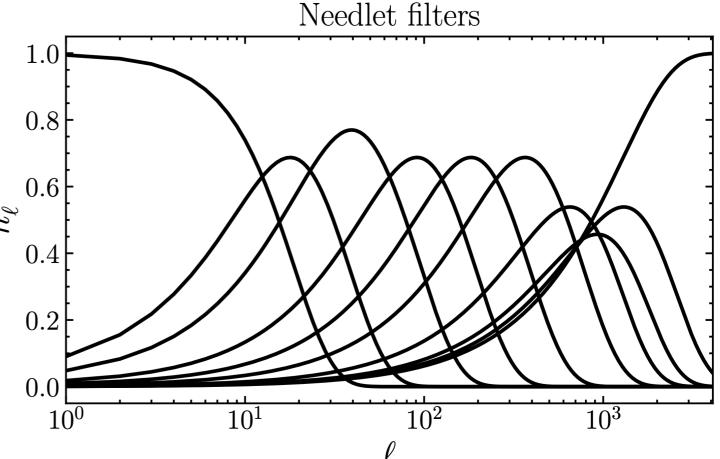
#### Needlet Internal Linear Combination

Needlets allow localization of ILC weights in both harmonic and pixel space

#### Steps:

- Filter each frequency map with each harmonic-space needlet filter
- 2) Compute the freq.-freq. covariance matrix in real-space domain of specified size centered on each pixel (for maps at each needlet scale)
- 3) Compute ILC weights at each pixel (for maps at each needlet scale)
- 4) Obtain per-scale ILC maps
- 5) Filter each per-scale ILC map again with the needlet filters





e.g., Eriksen+(2004); Delabrouille+(2009); Remazeilles+(2011); JCH & Spergel (2014)

pyilc

#### flexible, extensible NILC code in Python

Needlet ILC in Python

#### **Features:**

- Trivial installation, requires only healpy
- Many component SEDs available (CMB, tSZ, CIB, synchrotron, ..) + easy to add more
- Easy to define any type of needlet filters
- Delta-function or realistic passbands can be used
- Gaussian beams or arbitrary ell-dependent beams can be used
- Automatically determines which frequency maps to use at a given needlet scale, given their beams
- Covariances are computed only once and then cached for future use, allowing many constrained ILCs ("deprojections") to be run at ~zero additional computational expense
- Automatically determines the size of the real-space domains to be used in computing the freq.-freq. covariance matrix at each needlet scale, by requiring the number of modes to be large enough to keep the "ILC bias" below a fixed tolerance:

$$\frac{b_{\rm ILC}}{\langle s^2 \rangle} = \frac{|1 + N_{\rm deproj} - N_{\rm freq}|}{N_{\rm modes}}$$

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CIB cleaning: moment deprojection

Idea: suppose the fundamental SED describing dust emission is indeed a modified blackbody (MBB). Variations in the MBB parameters (β,T) across the sky and along the line of sight will generically produce new spectral shapes that are described by higher-order moments in a Taylor expansion of the fundamental SED.

#### CIB cleaning: moment deprojection

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MBB:

$$I_{\nu}^{\text{CIB}}(\hat{n}) = \left(\frac{\nu}{\nu_0}\right)^{\beta+3} \frac{1}{e^{x_{\text{CIB}}} - 1} A^{\text{CIB}}(\hat{n})$$

First-order moments:

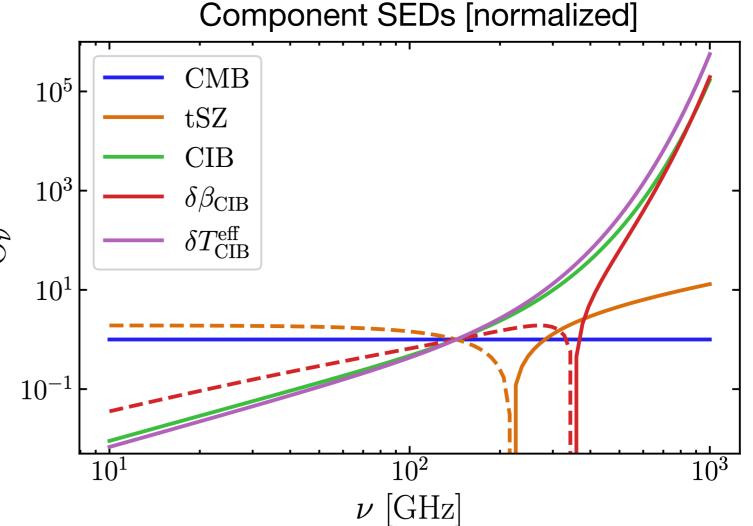
$$\frac{\partial I_{\nu}^{\text{CIB}}(\hat{n})}{\partial \beta} = \ln\left(\frac{\nu}{\nu_0}\right) I_{\nu}^{\text{CIB}}(\hat{n});$$

$$\frac{\partial I_{\nu}^{\text{CIB}}(\hat{n})}{\partial T_{\text{CIB}}^{\text{eff}}} = I_{\nu}^{\text{CIB}}(\hat{n}) \frac{x_{\text{CIB}}}{T_{\text{CIB}}^{\text{eff}}} \frac{e^{x_{\text{CIB}}}}{e^{x_{\text{CIB}}} - 1}$$

$$\stackrel{\wedge}{=} \frac{\partial I_{\nu}^{\text{CIB}}(\hat{n})}{\partial T_{\text{CIB}}^{\text{eff}}} = \frac{e^{x_{\text{CIB}}}}{e^{x_{\text{CIB}}} - 1}$$

$$x_{\mathrm{CIB}} \equiv \frac{h\nu}{k_B T_{\mathrm{CIB}}^{\mathrm{eff}}}$$

$$v_0 = 353 \text{ GHz}$$



Chluba, JCH, Abitbol (2017); McCarthy & JCH (to appear)

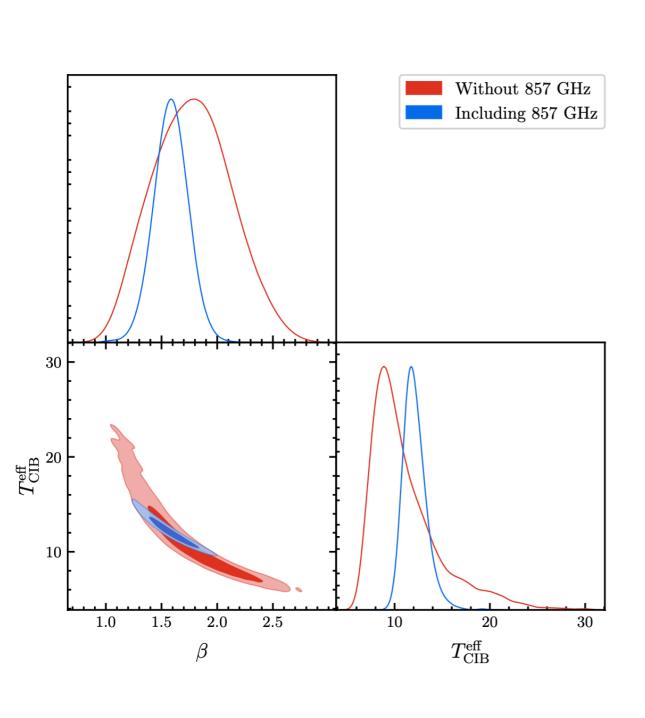
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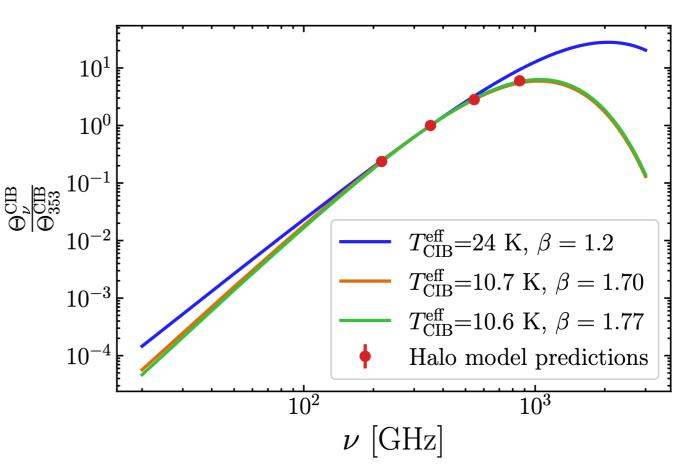
CIB cleaning: moment deprojection

MBB fit to CIB monopole SED predicted by best-fit halo model to CIB power spectra

#### CIB cleaning: moment deprojection

#### MBB fit to CIB monopole SED predicted by best-fit halo model to CIB power spectra



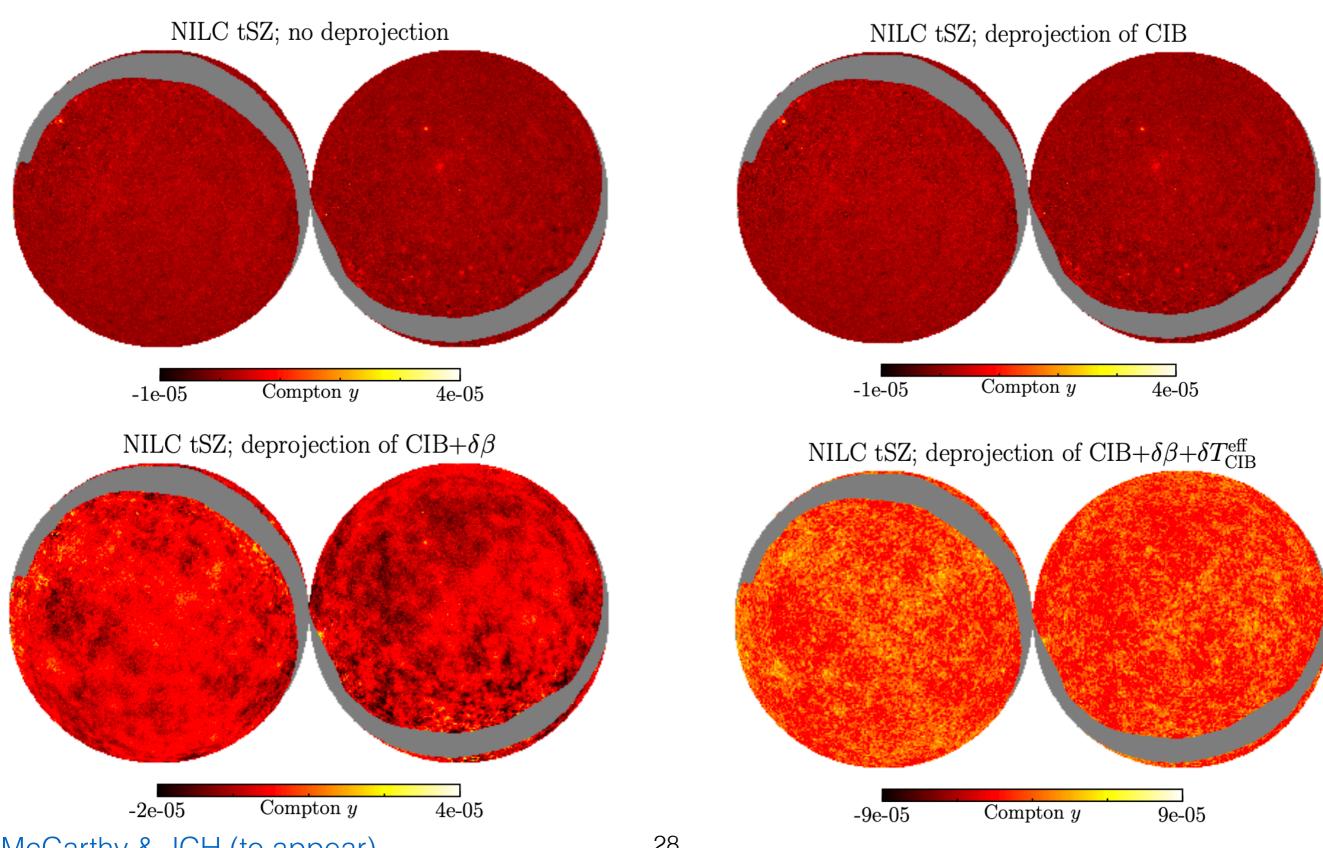


Later in our analysis we will draw (β,Teff) samples from this posterior to test the sensitivity of our CIB deprojections to the assumed MBB SED

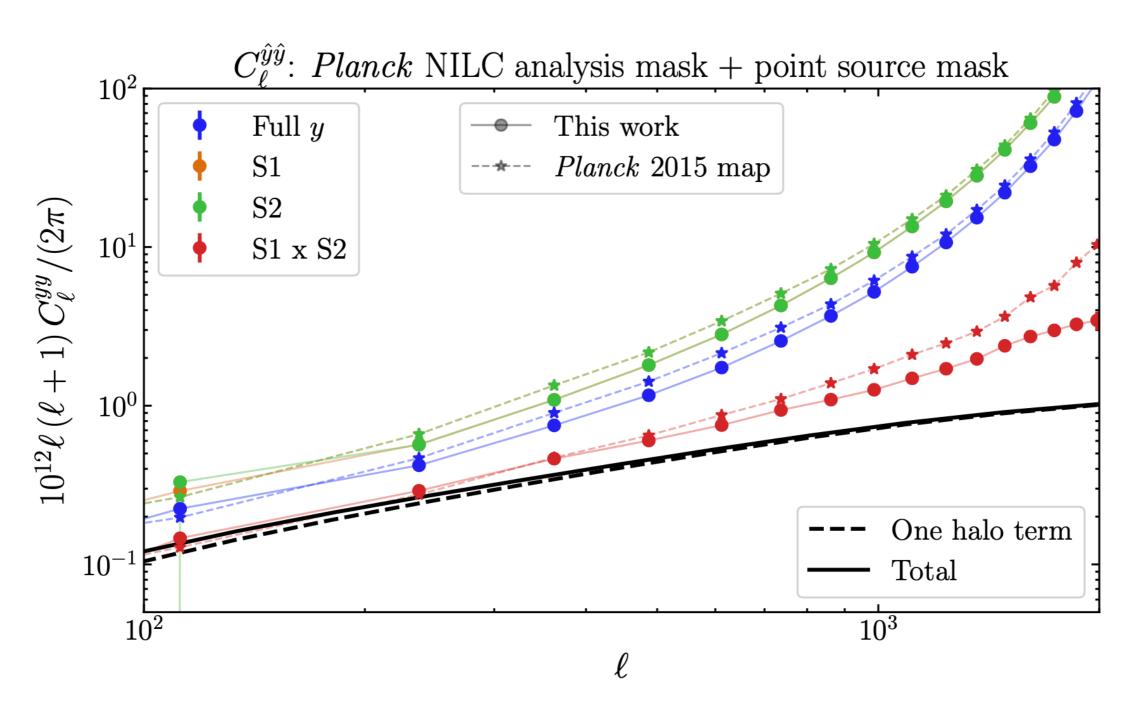
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## Thermal SZ Extraction

Application to Planck PR4 (NPIPE) maps

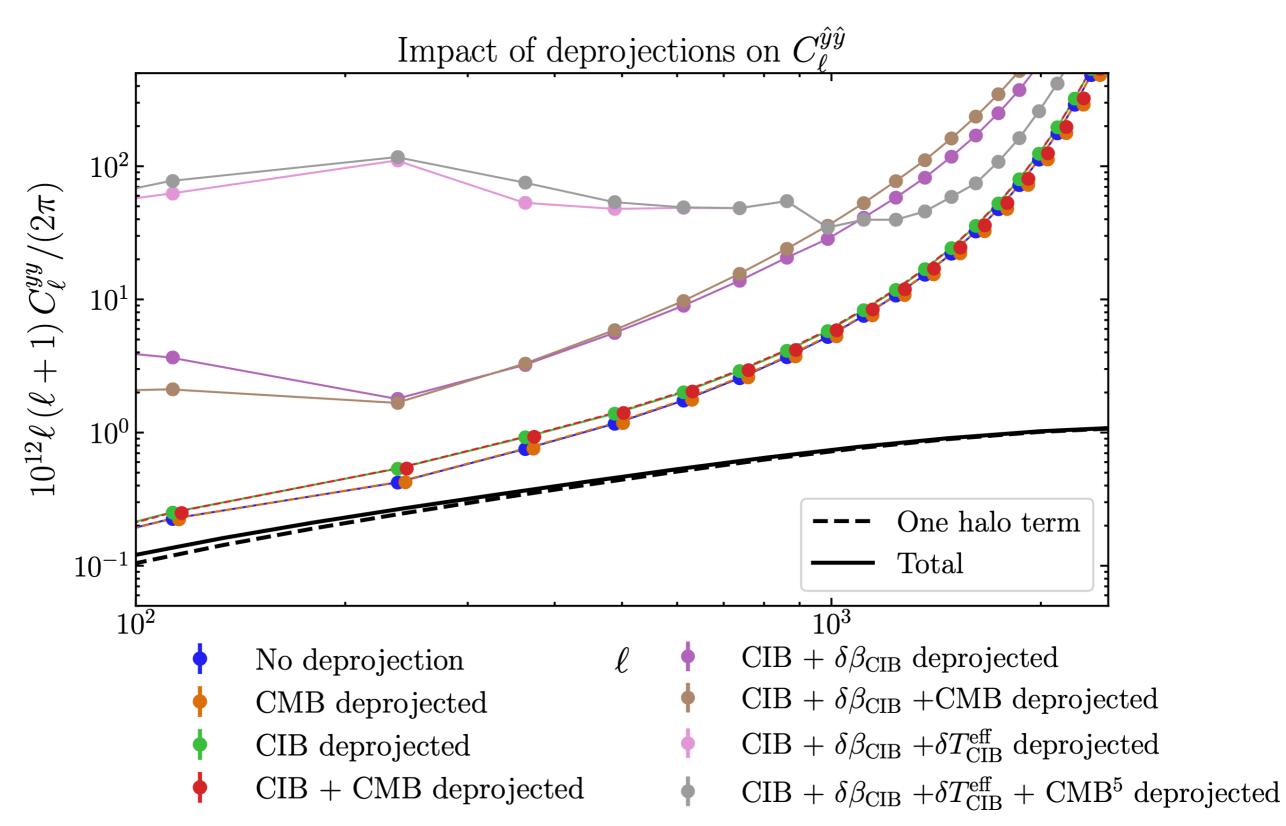


Application to Planck PR4 (NPIPE) maps



~10-20% lower noise visible on small scales in auto-spectrum, and improved foreground cleaning visible in S1xS2 cross-spectrum (free of noise bias)

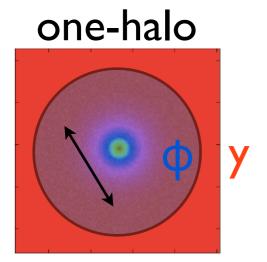
Application to Planck PR4 (NPIPE) maps



# Thermal SZ X CMB Lensing

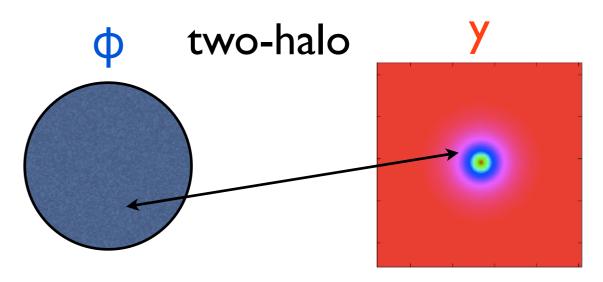
#### Theory: halo model

- Cross-spectrum can be derived similarly to tSZ auto-spectrum
- Need Fourier transform of both the y-profile and φ- (lensing potential) profile (e.g., computed from NFW) for each halo
- Contributions from both one-halo and two-halo terms:



dominates on small scales

sensitive to number of clusters and how gas pressure traces DM in clusters



dominates on large scales

sensitive to how gas traces

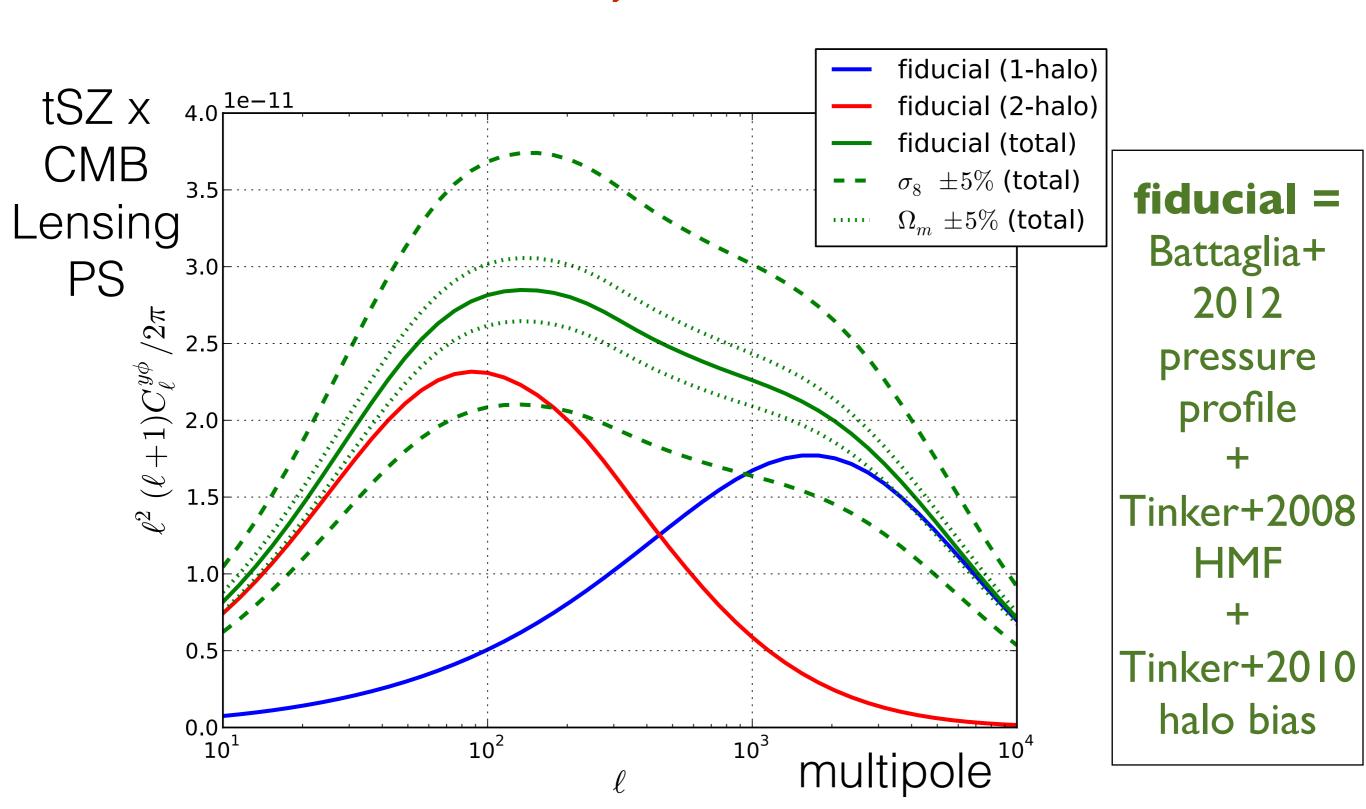
DM on large scales (amongst

many things)

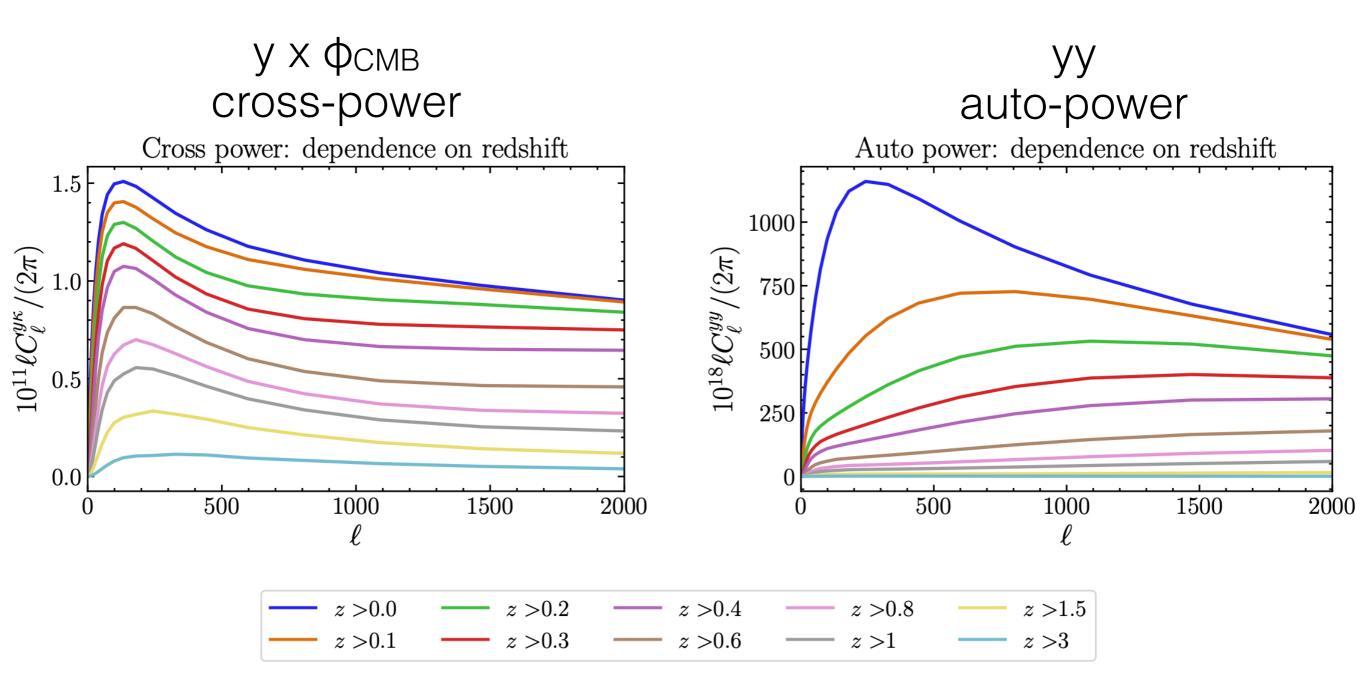
All theory calculations performed with CLASS\_SZ (Bolliet+2022)

https://github.com/CLASS-SZ/class\_sz

Theory: halo model

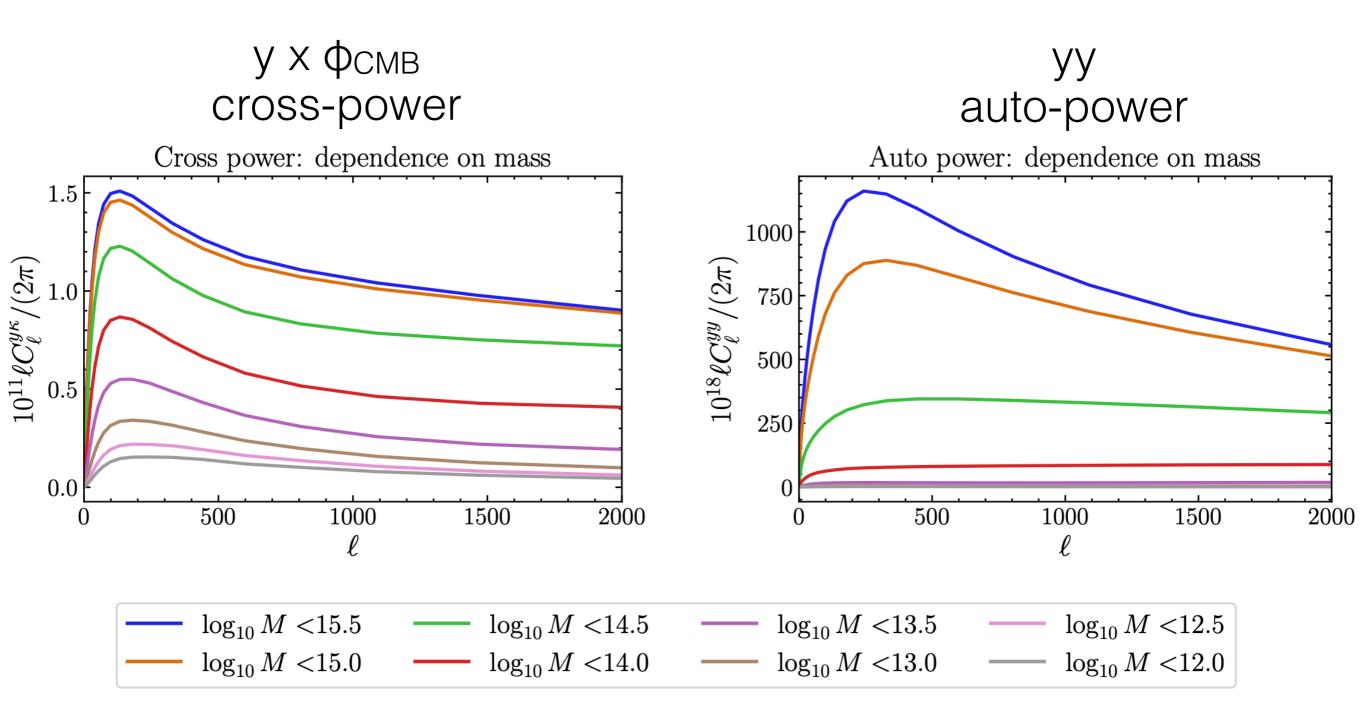


Theory: origin of the signal



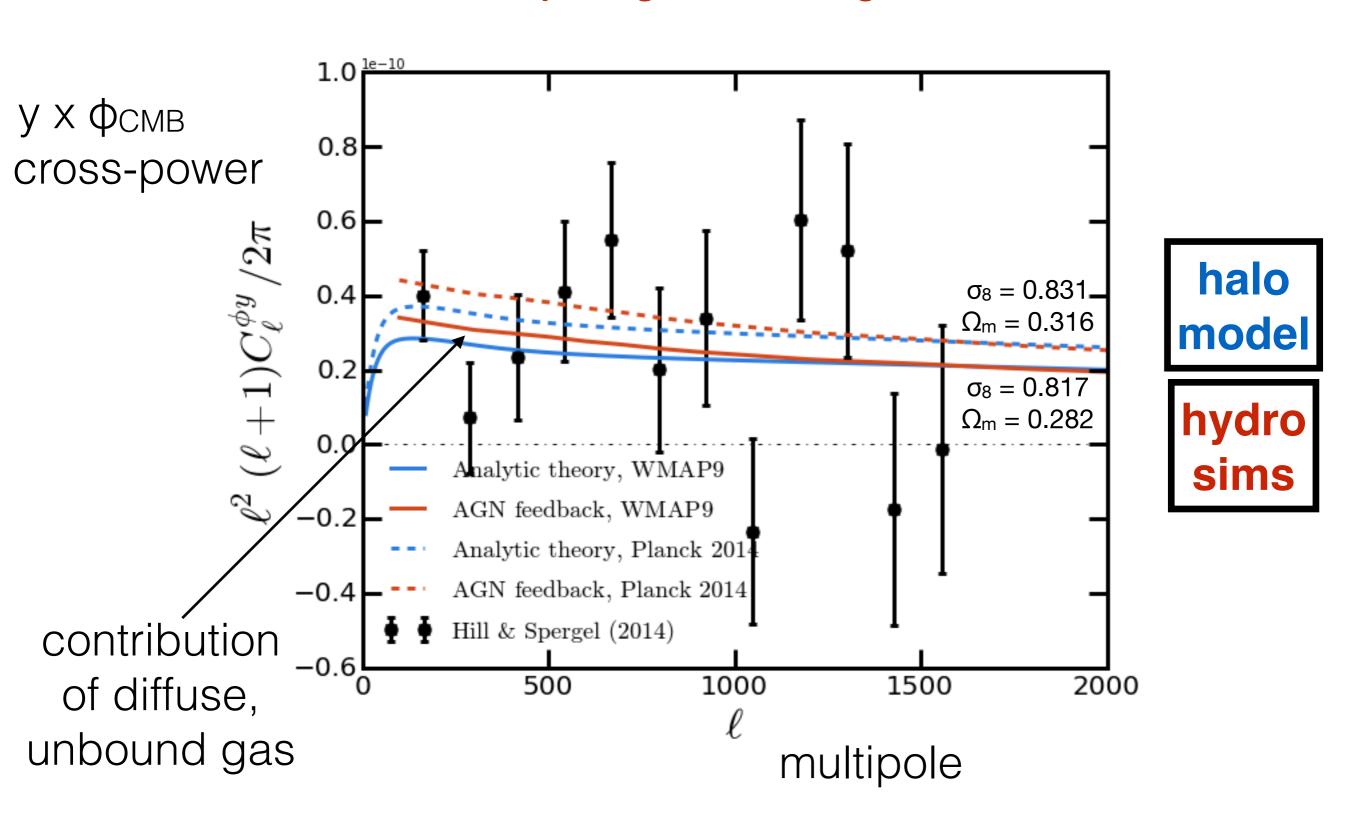
At ell=2000:  $\sim$ 25% of cross-power signal from z > 1 (cf. < 10% of auto-power signal)

Theory: origin of the signal

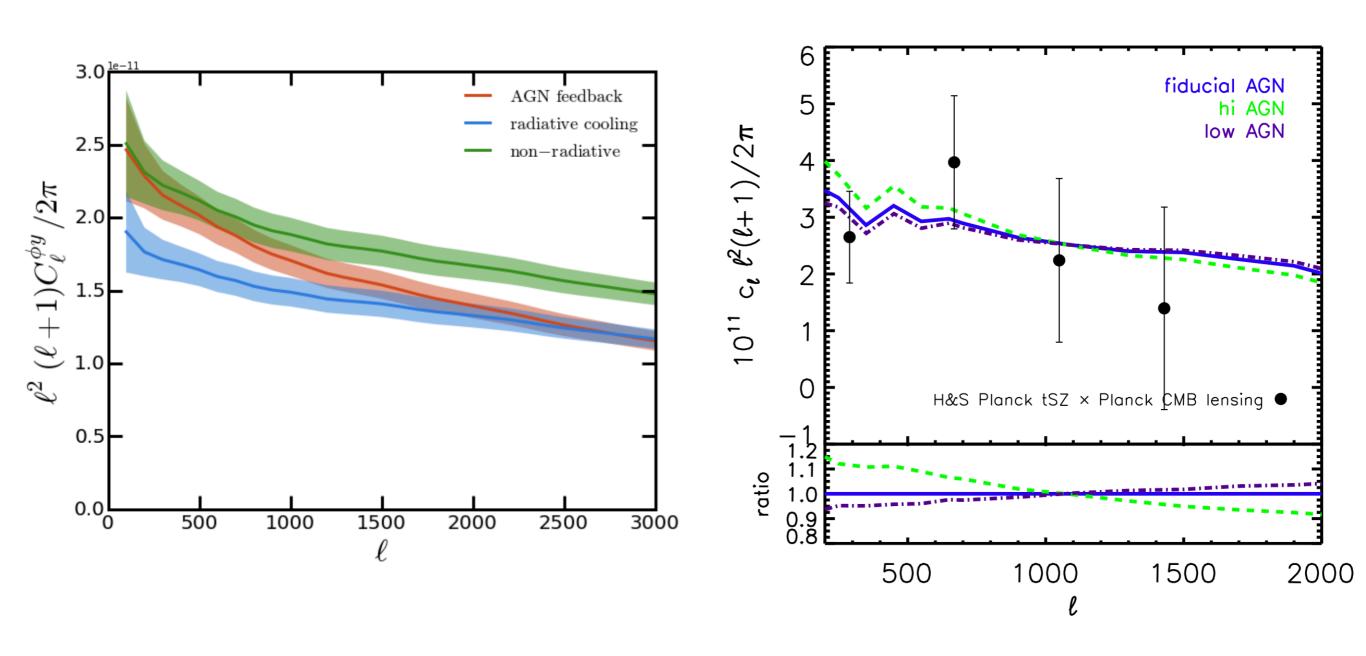


At ell=2000: ~25% of cross-power signal from M <  $10^{13.5}$  M<sub>sun</sub>/h (cf. < 3% of auto-power)

Theory: origin of the signal

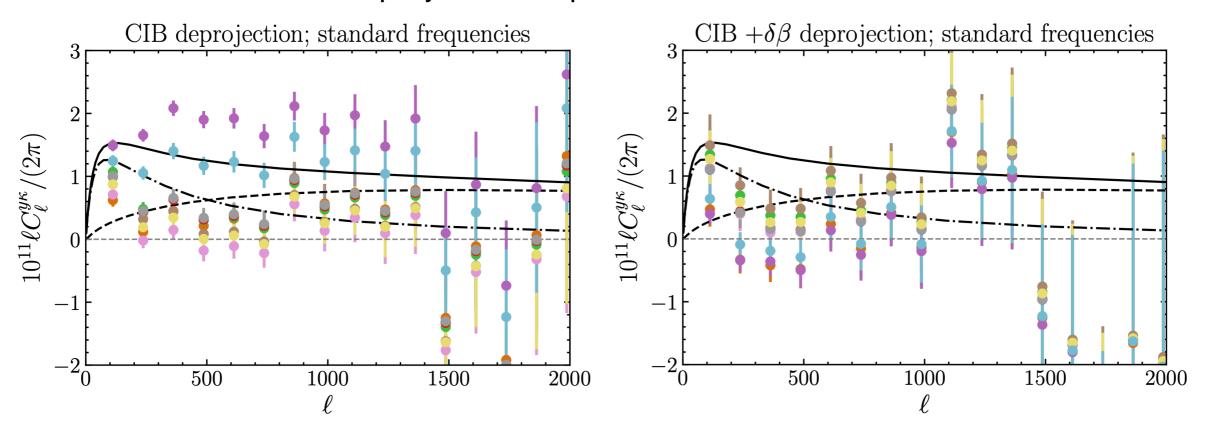


Theory: sensitivity to gastrophysics/feedback modeling



### Cross-correlation of pyilc y-maps with PR4 CMB lensing maps

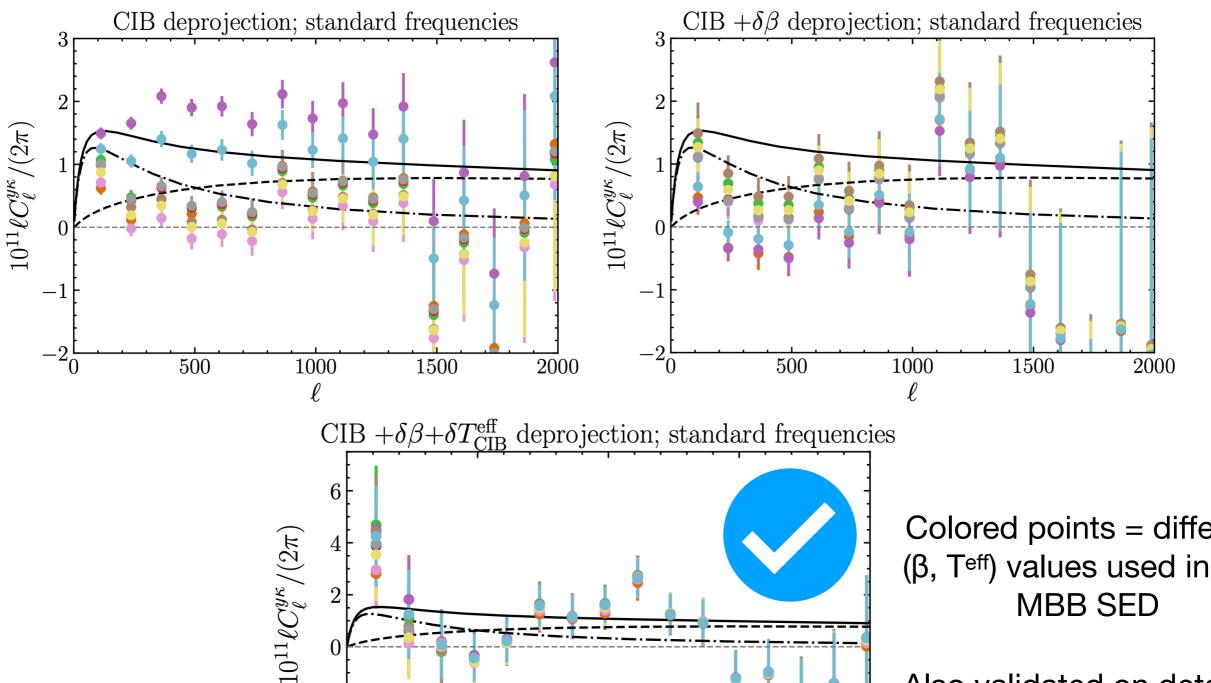
Multi-moment CIB deprojection required to obtain stable/robust measurement



Colored points = different (β, T<sup>eff</sup>) values used in CIB MBB SED

### Cross-correlation of pyilc y-maps with PR4 CMB lensing maps

Multi-moment CIB deprojection required to obtain stable/robust measurement



1000

1500

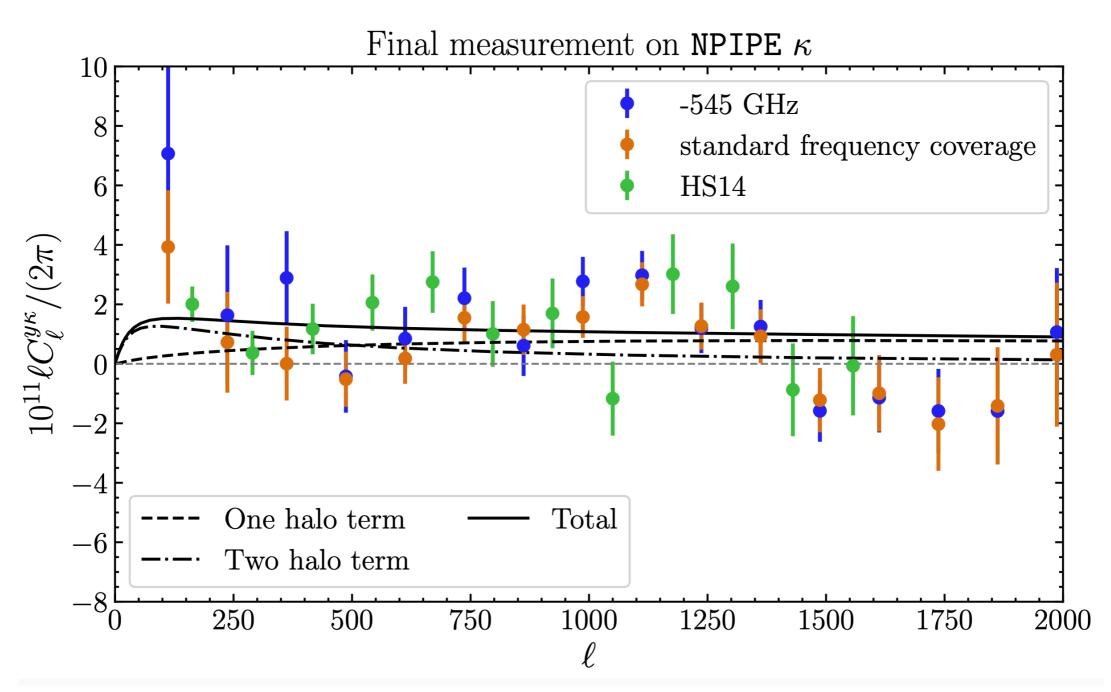
2000

500

Colored points = different (β, Teff) values used in CIB MBB SED

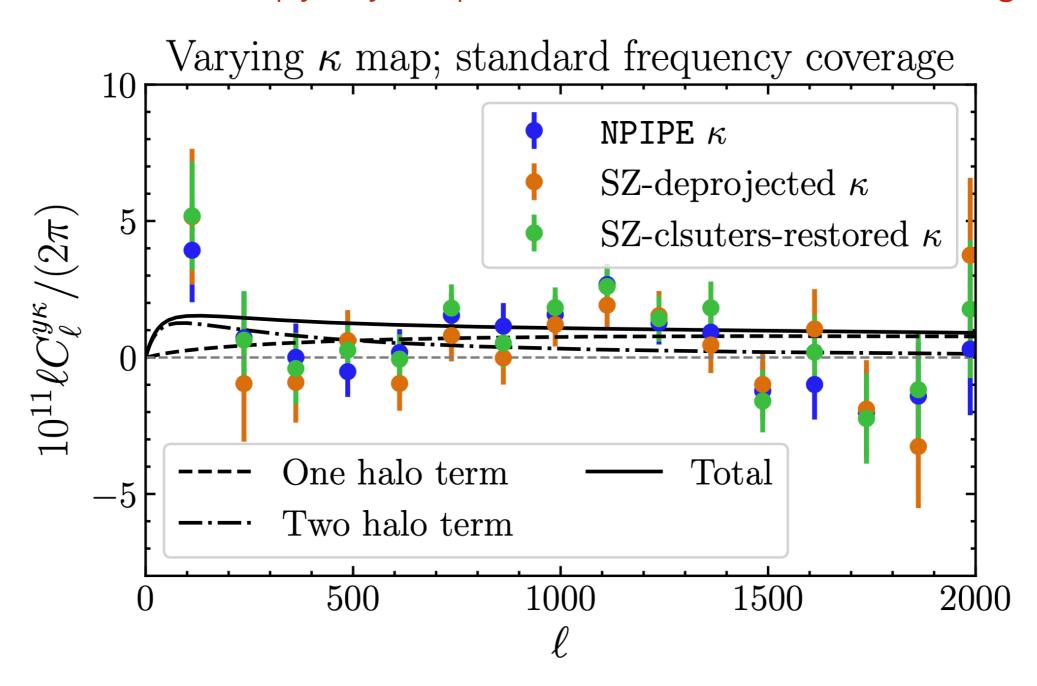
Also validated on detailed mm-wave sky simulations

Cross-correlation of pyilc y-maps with PR4 CMB lensing maps



Robustness comes at a cost: the multiple deprojections in the NILC lead to much larger noise in the *y*-map —> larger error bars in the cross-correlation

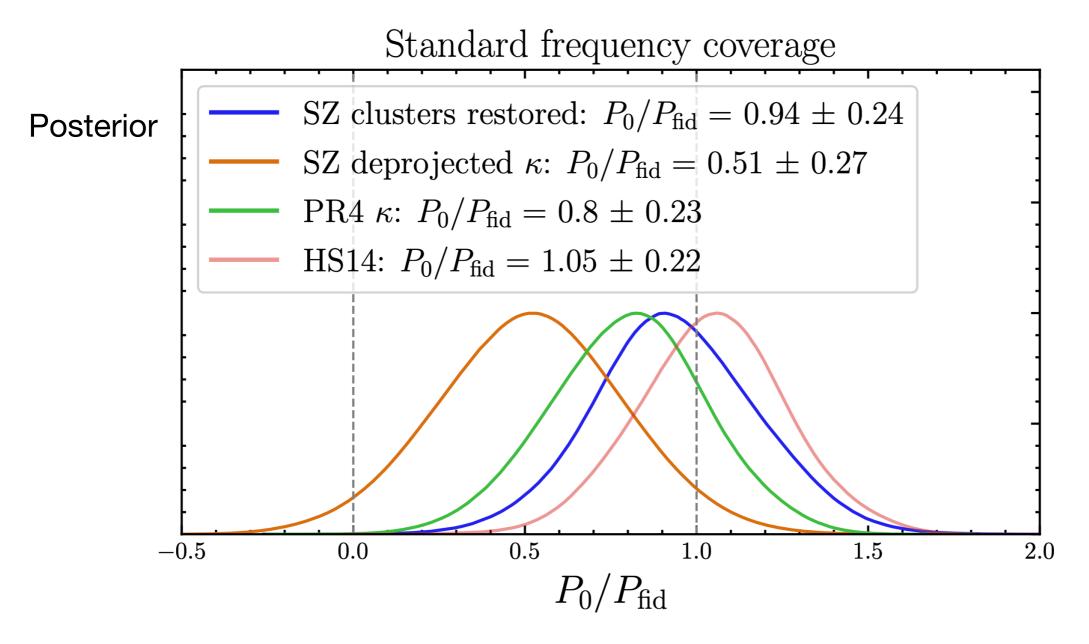
Cross-correlation of pyilc *y*-maps with PR4 + PR3 CMB lensing maps



#### Measurement is also robust to analysis variations in the κ reconstruction:

- Reconstruction on tSZ-deprojected CMB map (avoids <yyy> bias in cross-correlation)
- Reconstruction with signal restored at location of tSZ-detected clusters (masked by default)

Interpretation: amplitude of pressure-mass relation



Data are consistent with fiducial theoretical model (Battaglia+12 pressure profile) extrapolated into high-z, low-mass regime

Detection SNR ~ 4 (similar to HS14 due to enormous CIB deprojection penalty)

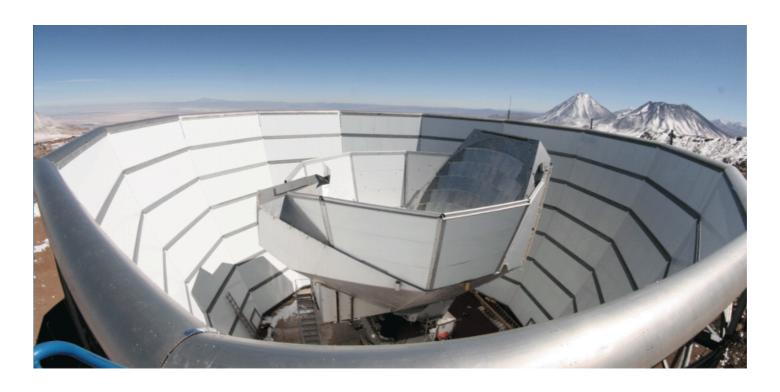
### Summary/Outlook

- We have learned an enormous amount about how to clean the CIB robustly and modelindependently in tSZ cross-correlation measurements
- Implication: significant high-frequency coverage is needed in such measurements
- Use of 857 GHz can decrease the error bars, but we find that the final data points are not as stable/robust to CIB MBB SED variations
- Results are consistent with those of JCH & Spergel (2014), but *much* more robust (entire analysis pipeline validated on detailed sky simulations)
- Current gas pressure profile models calibrated at lower redshift and higher mass adequately describe tSZ x CMB lensing cross-correlation (and no sign of low S<sub>8</sub>)

$$A = 0.80 \pm 0.23$$

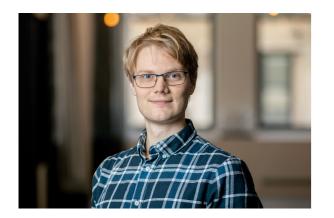
 What's next: higher SNR measurement with ACT DR6 [Bolliet, Coulton, McCarthy, JCH, ++]

# ACT DR6: Compton-y Maps



The Atacama Cosmology Telescope: High-resolution component-separated maps across one-third of the sky

William Coulton, Mathew S. Madhavacheril, Adriaan J. Duivenvoorden, J. J. Colin Hill, 5, 1



+ ACT Collaboration

## ACT Data Release 6

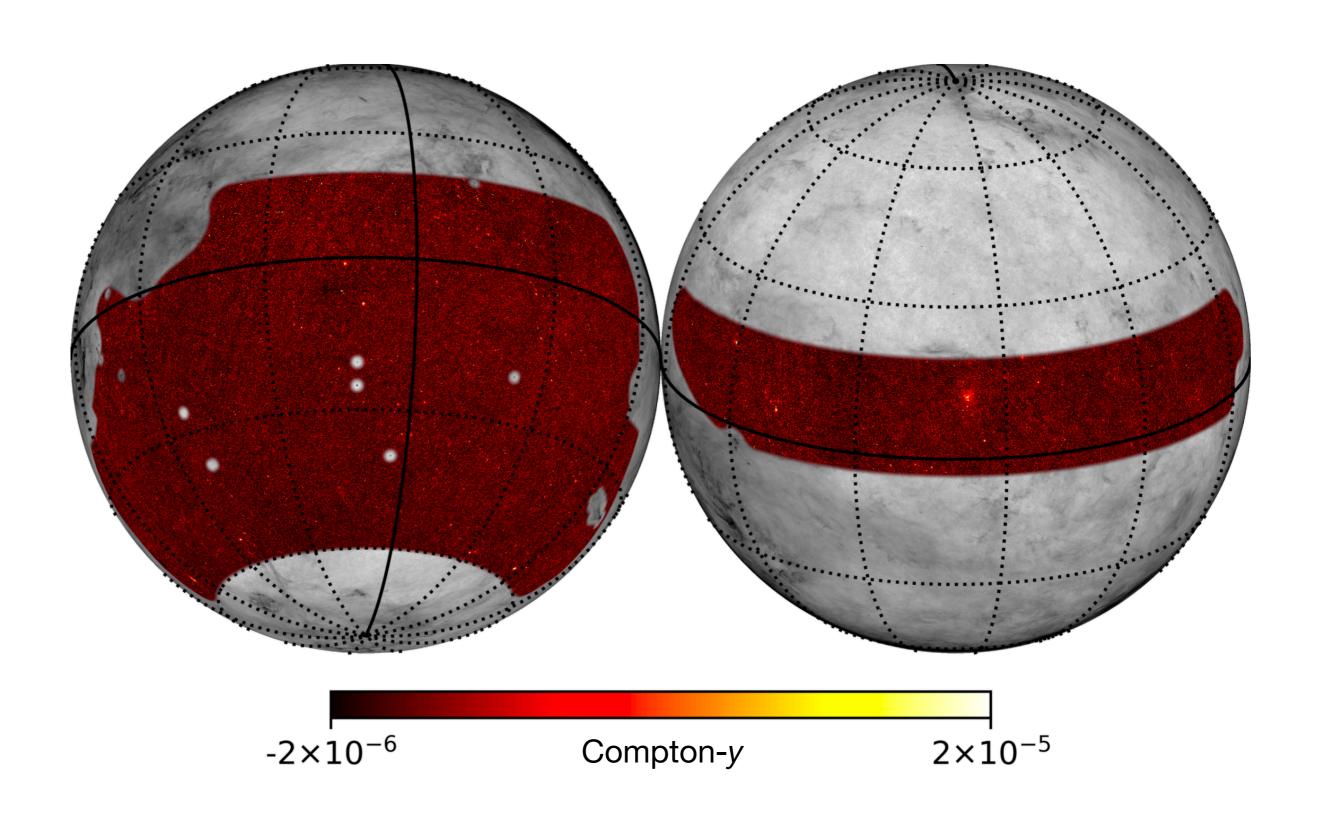
High-sensitivity, arcminute-resolution maps at 90/150/220 GHz covering ~17,000 deg<sup>2</sup>

- Qu et al. (2023): Reconstructed CMB lensing maps
- Madhavacheril et al. (2023): Cosmology from CMB lensing
   S<sub>8</sub> = 0.840 ± 0.028
- MacCrann et al. (2023): Foreground mitigation for CMB lensing
- Coulton et al. (2023): Component-separated maps (y, T, E)
- Much more still to come, including:
  - Frequency map characterization and data release
  - Primary CMB TT, TE, EE power spectra
  - Cosmological constraints from CMB power spectra
  - Expanded tSZ cluster catalog
  - Cosmological constraints from cluster abundances (with DES and HSC weak lensing mass calibration)
  - and more

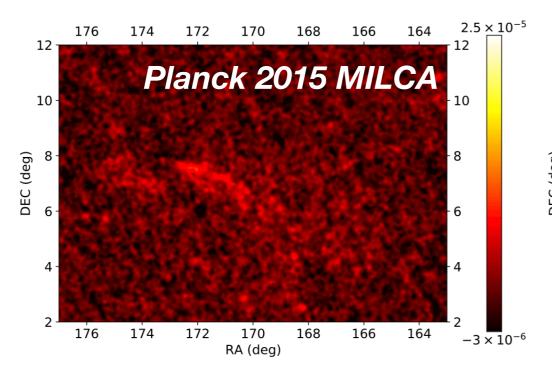
https://lambda.gsfc.nasa.gov/product/act/

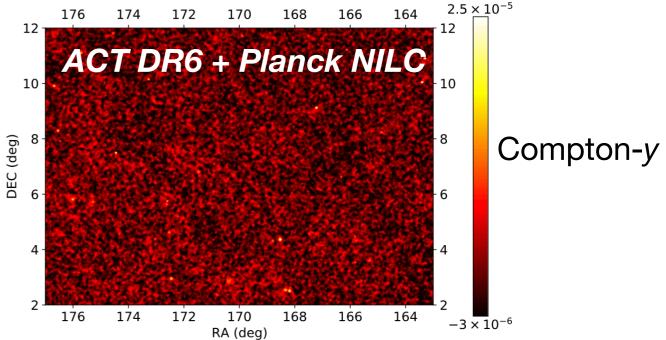
# ACT DR6 NILC y-map

ACT + Planck NPIPE



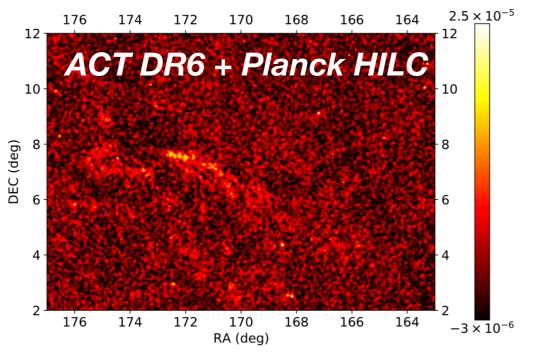
#### ACT + Planck NPIPE

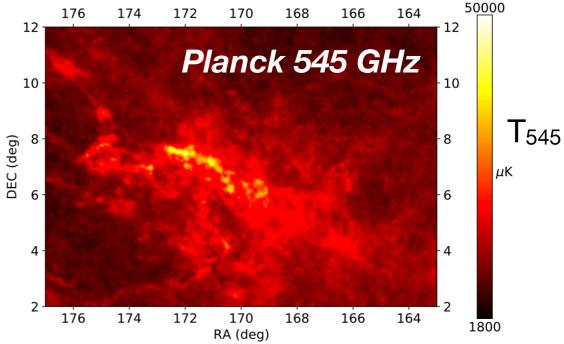




(a) Planck MILCA Compton-y map

(b) ACT & Planck NILC Compton-y map





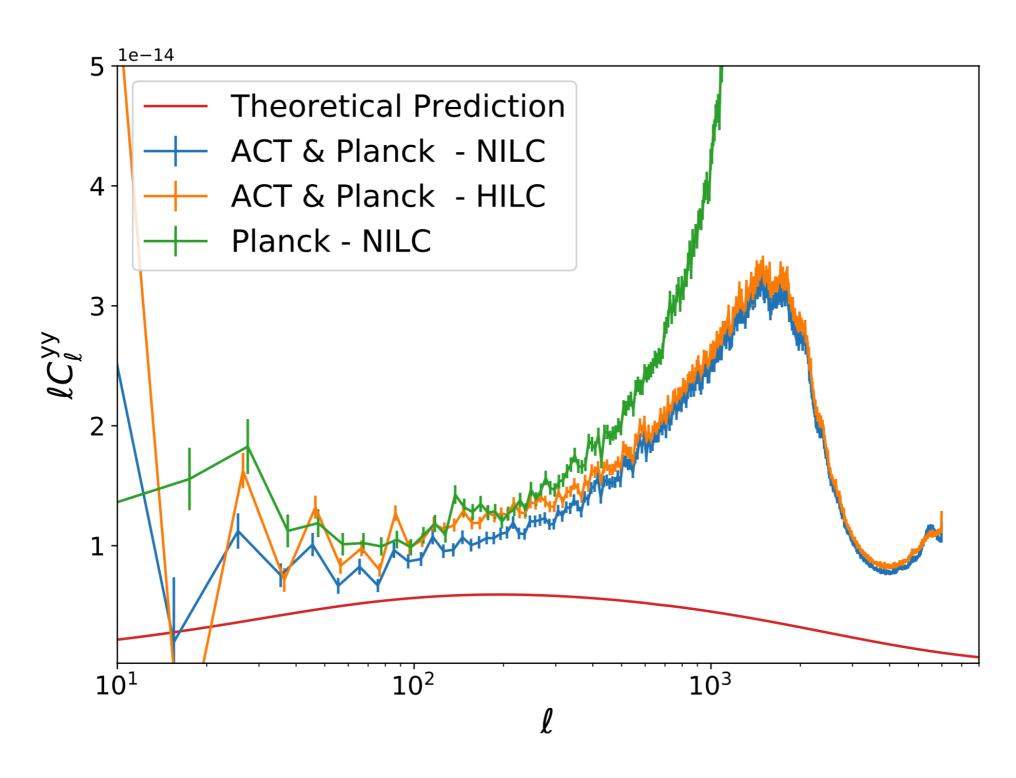
(c) ACT & Planck Harmonic ILC Compton-y map

(d) Planck 545 GHz map

## ACT DR6 NILC y-map

#### ACT + Planck NPIPE

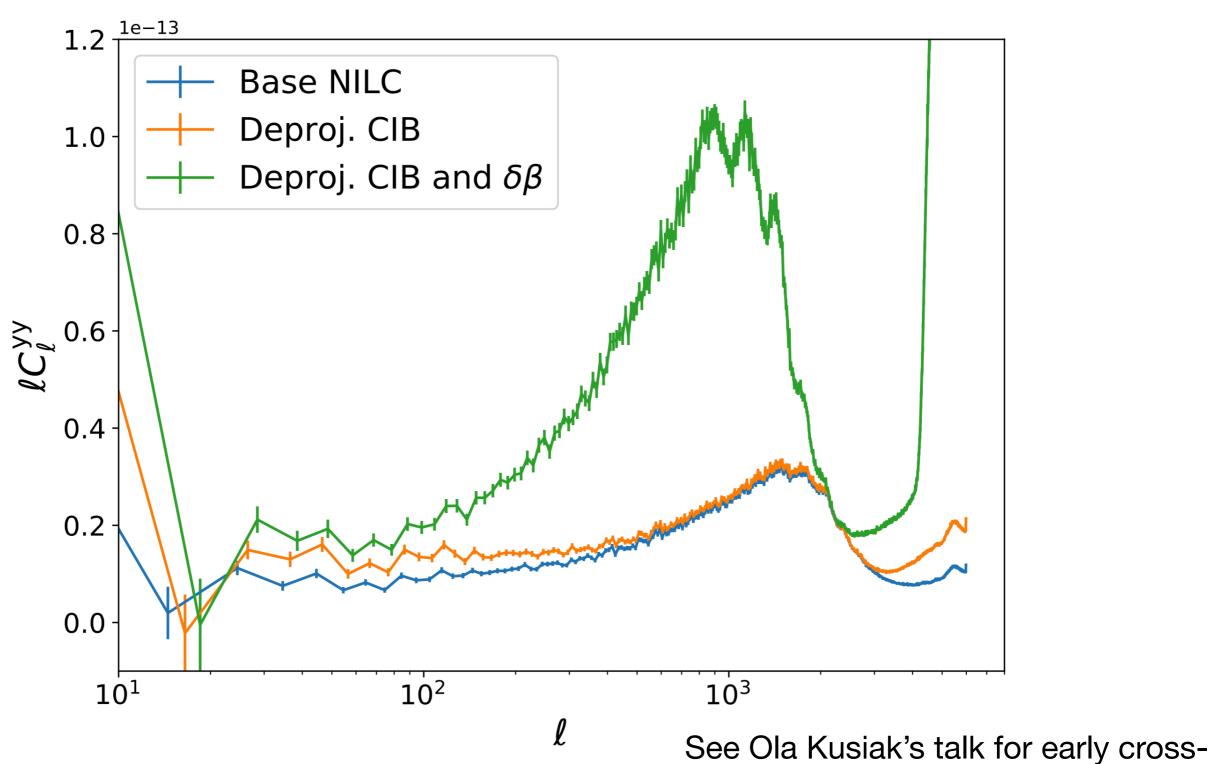
Auto-power spectra of y-maps: enormous gains in SNR over *Planck*-only maps



## ACT DR6 NILC y-map

#### ACT + Planck NPIPE

#### Various CIB deprojection options also implemented



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## Take-Home Messages

- 1) Flexible, robust NILC pipeline now publicly available: pyilc
- 2) CIB-deprojected *y*-maps from PR4 NPIPE data now publicly available
- 3) Robust PR4 tSZ x CMB lensing measurement is consistent with extrapolation of existing gastrophysics models to high-z, low-mass regime
- 4) ACT DR6 (+PR4) y-maps soon unprecedented resolution and signal-to-noise across ~14,000 deg<sup>2</sup>

# Bonus

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### Cross-correlation of pyilc y-maps with PR4 CMB lensing maps

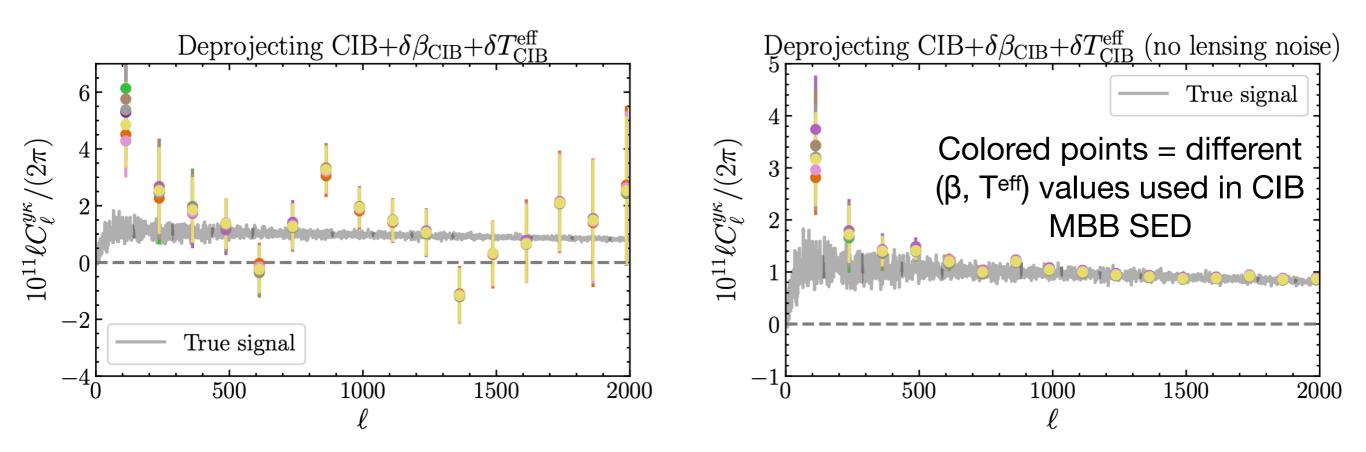
Validation of pipeline on detailed mm-wave sky simulations

- Simulations: Websky CMB+tSZ+CIB + PySM dust+synch+free-free+AME + Planck noise
- Processed through pyilc pipeline with various CIB deprojection choices
- Cross-correlated with true Websky κ map (with or without noise)

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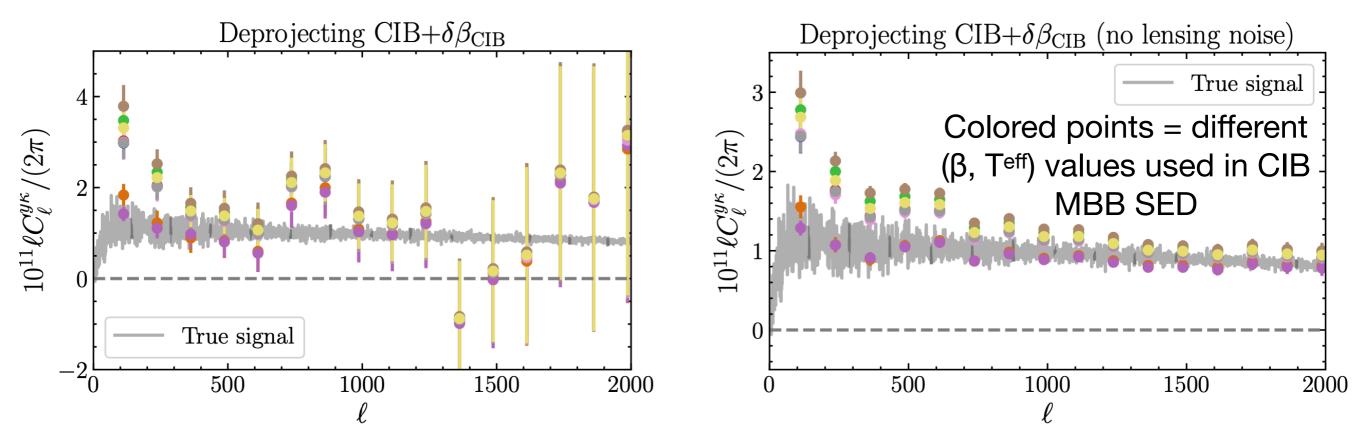
Only by deprojecting the CIB + both first moment SEDs is the measurement stable/robust to the assumed MBB parameters of the CIB (β, Teff)

CMB is also deprojected in first five needlet scales (to mitigate potential ISW-lensing contribution)

### Cross-correlation of pyilc y-maps with PR4 CMB lensing maps

Validation of pipeline on detailed mm-wave sky simulations

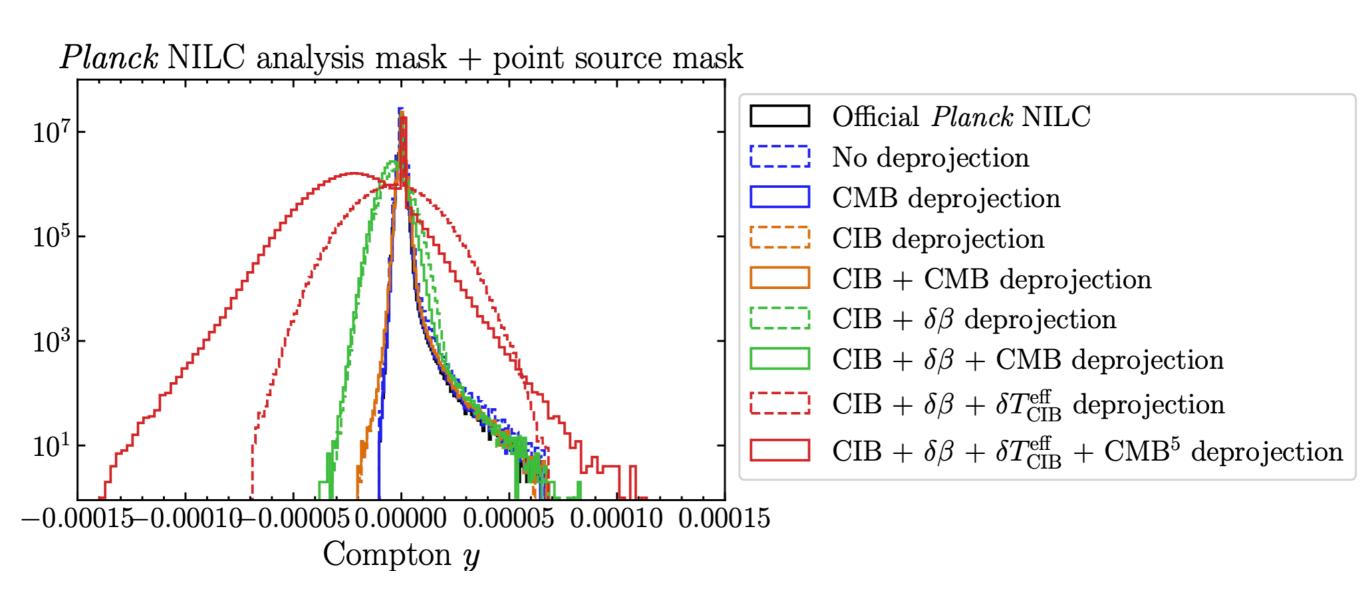
- Simulations: Websky CMB+tSZ+CIB + PySM dust+synch+free-free+AME + Planck noise
- Processed through pyilc pipeline with various CIB deprojection choices
- Cross-correlated with true Websky κ map (with or without noise)



Even deprojecting the CIB +  $\beta$  first moment SED is not sufficient to yield a measurement stable/robust to the assumed MBB parameters of the CIB ( $\beta$ , T<sup>eff</sup>)

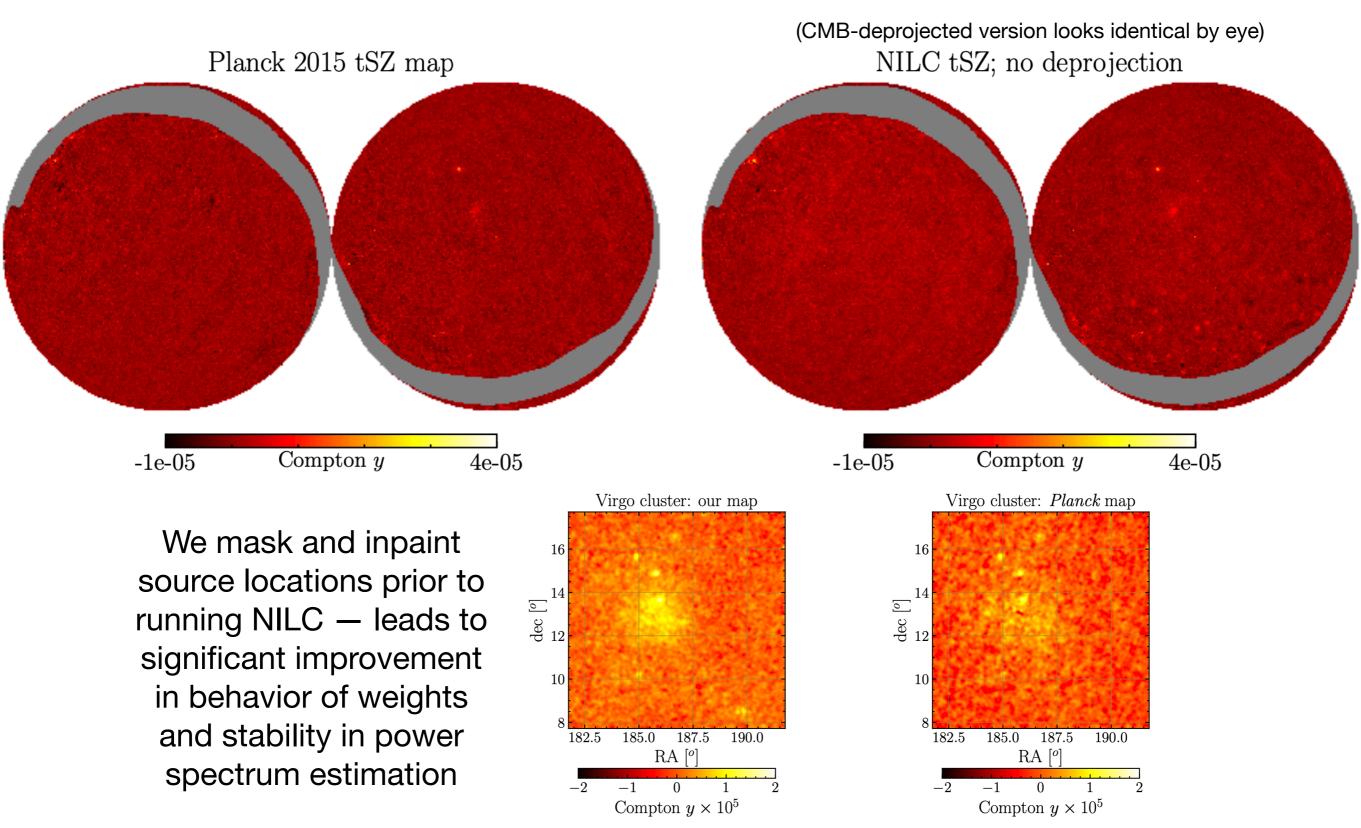
## Thermal SZ Extraction

Application to Planck PR4 (NPIPE) maps



### Thermal SZ Extraction

### Comparison to official PR2 y-map

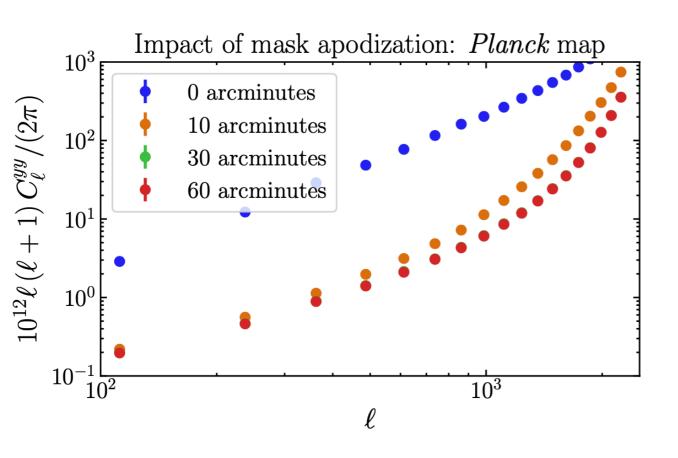


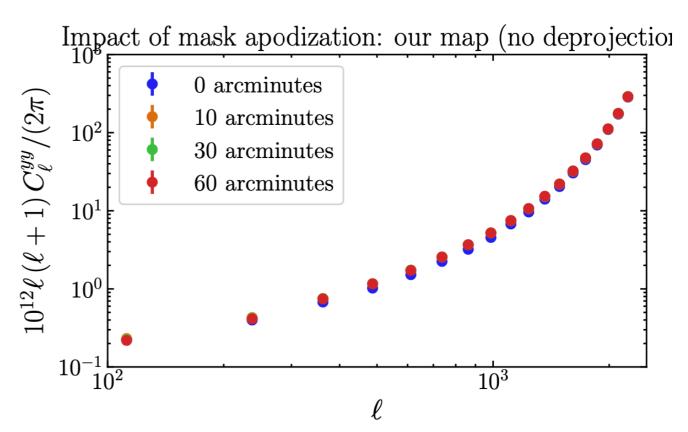
McCarthy & JCH (to appear); see also Tanimura+(2022) and Chandran+(2023)

## Thermal SZ Extraction

#### Comparison to official PR2 y-map

We mask and inpaint source locations prior to running NILC — leads to significant improvement in behavior of weights and stability in power spectrum estimation





### Theory: halo model

- Cross-spectrum can be derived similarly to tSZ auto-spectrum
- Need Fourier transform of convergence profile of each halo:

$$\tilde{\kappa}_\ell(M,z) = \frac{4\pi r_s}{\ell_s^2} \int dx \, x^2 \frac{\sin((\ell+1/2)x/\ell_s)}{(\ell+1/2)x/\ell_s} \frac{\rho(x;M,z)}{\Sigma_{crit}(z)} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{\det \chi_s(M,z)} = \frac{4\pi r_s}{\ell_s^2} \int dx \, x^2 \frac{\sin((\ell+1/2)x/\ell_s)}{(\ell+1/2)x/\ell_s} \frac{\rho(x;M,z)}{\Sigma_{crit}(z)} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{(NFW)} = \frac{1}{2} \frac{\det \chi_s(M,z)}{(NFW)} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{(NFW)} = \frac{1}{2} \frac{\det \chi_s(M,z)}{(NFW)} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{(NFW)} = \frac{1}{2} \frac{\det \chi_s(M,z)}{(NFW)} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{(\ell+1/2)x/\ell_s} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{(NFW)} = \frac{1}{2} \frac{\det \chi_s(M,z)}{(NFW)} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{(NFW)} = \frac{1}{2} \frac{\det \chi_s(M,z)}{(NFW)} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{(NFW)} = \frac{1}{2} \frac{\det \chi_s(M,z)}{(NFW)} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{(NFW)} = \frac{1}{2} \frac{\det \chi_s(M,z)}{(NFW)} \underbrace{\qquad \qquad }_{\text{critical surface density for lensing}} \frac{\det \chi_s(M,z)}{(NFW)} = \frac{1}{2} \frac{\det \chi_s($$

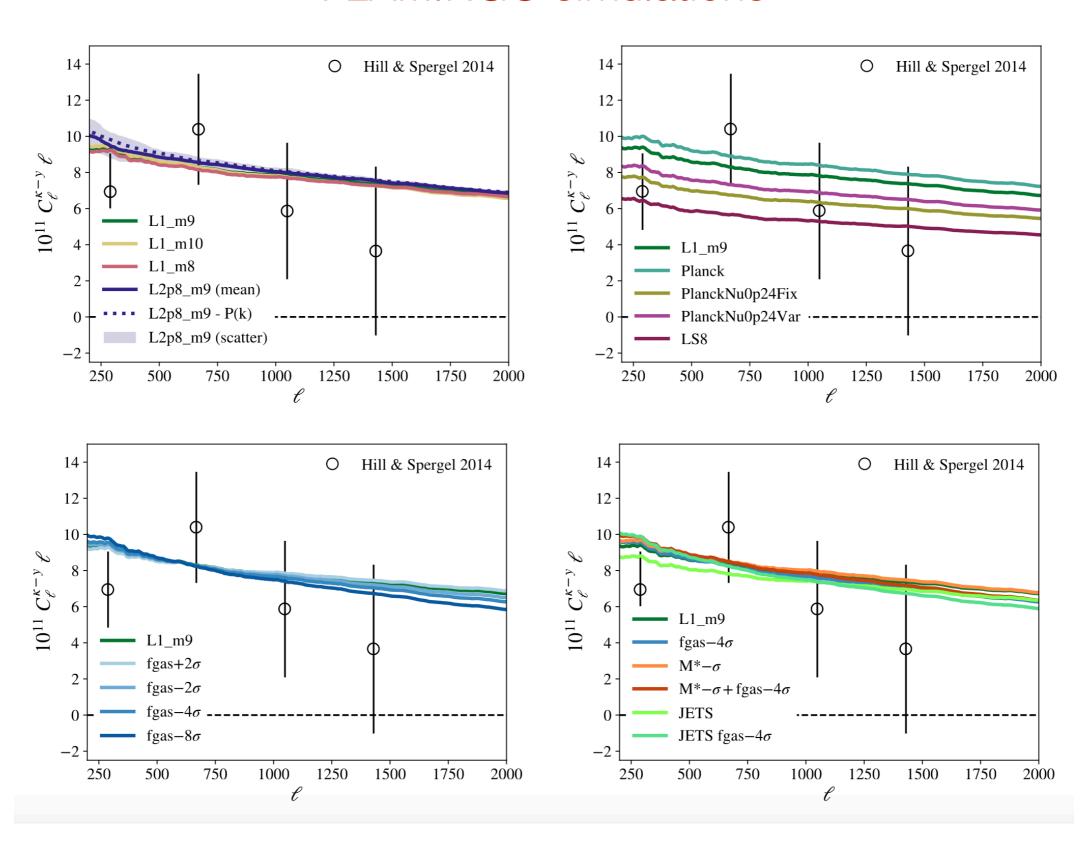
One-halo term:

$$C_{\ell}^{y\kappa,1h} = \int dz \frac{d^2V}{dzd\Omega} \int dM \frac{dn}{dM} \tilde{y}_{\ell}(M,z) \tilde{\kappa}_{\ell}(M,z)$$

Two-halo term:

$$C_{\ell}^{y\kappa,2h} = \int dz \frac{d^2V}{dzd\Omega} P_{lin}(\ell/\chi,z) \left[ \int dM_1 \frac{dn}{dM_1} b(M_1,z) \tilde{y}_{\ell}(M_1,z) \right] \times \left[ \int dM_2 \frac{dn}{dM_2} b(M_2,z) \tilde{\kappa}_{\ell}(M_2,z) \right], \quad \text{halo bias}$$

#### FLAMINGO simulations



# Next: ACT DR6

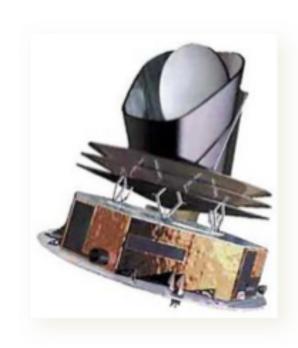
(target: later this year)

		SO-Pre		SO-N	Nominal Ope	rations		00
2020	2021	2022	2023	2024	2025	2026	2027	2028

Planck

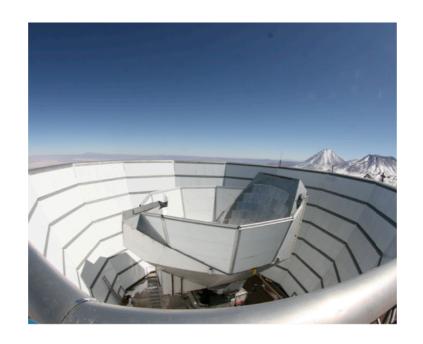


#### **Advanced ACT**



Final data 2018 100% sky

0.35 — 10 mm (9 bands) 5 — 33' resolution



Observations until 2022 40% sky

Noise ~3 times < Planck

1.4 — 10 mm (5 bands)

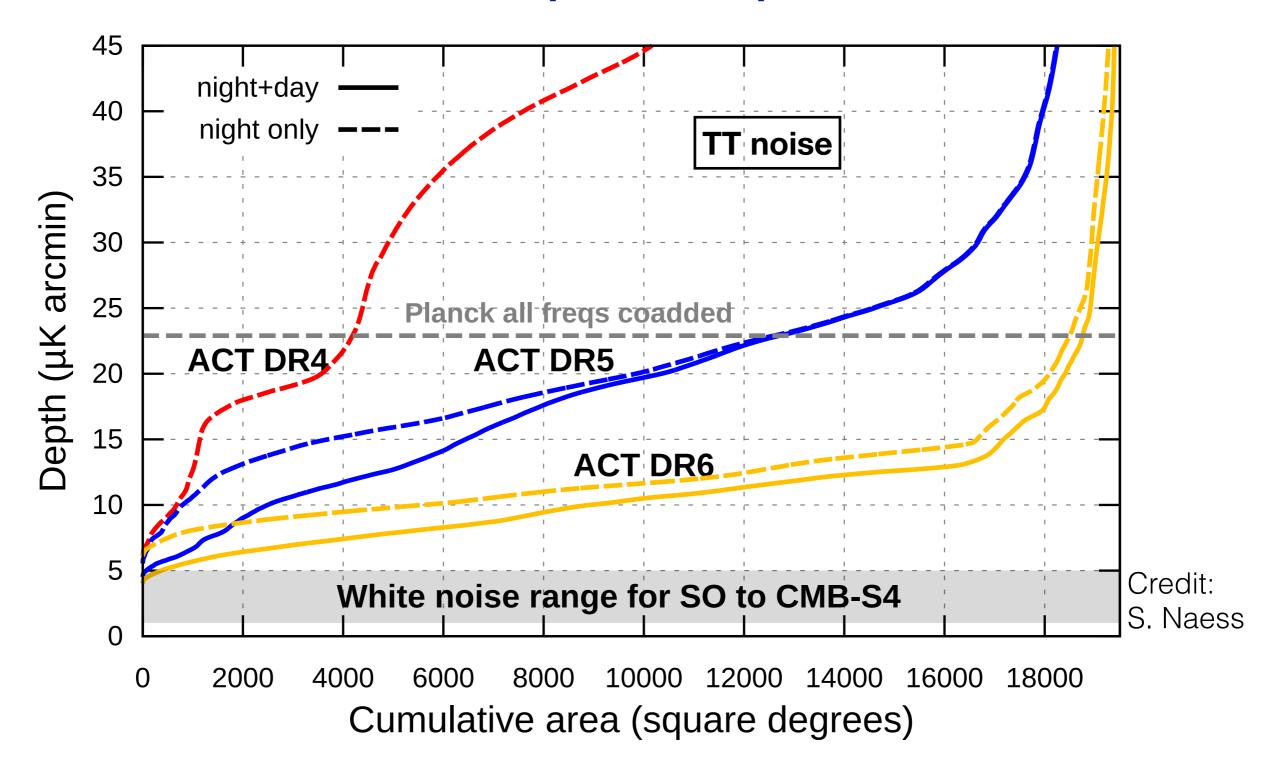
I — 7' resolution

[South Pole Telescope - same timeframe]

ACT DR4 only comprises data collected through 2016 — we have >5x as much data already on disk, collected through 2022

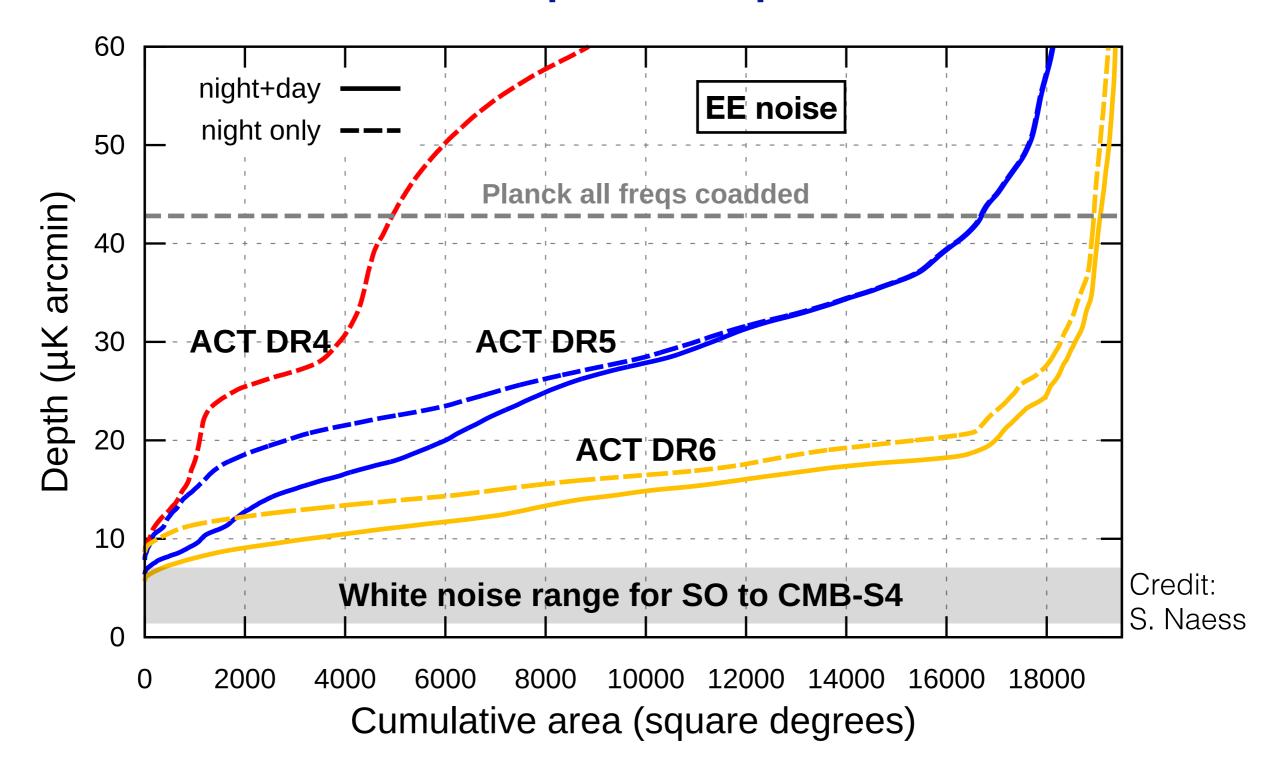
 $\sigma(H_0) \sim 0.5 \text{ km/s/Mpc}$  in  $\Lambda CDM$ 

# DR6 Map Depth: T



ACT DR6 maps are significantly deeper (i.e., more sensitive) than Planck on nearly 40% of the sky, with >5x higher angular resolution

# DR6 Map Depth: E



ACT DR6 maps are significantly deeper (i.e., more sensitive) than Planck on nearly 40% of the sky, with >5x higher angular resolution

## ACT DR6 Forecasts

### ACT TT + TE + EE : precision cosmology beyond Planck

	ACT DR4	ACT DR4 + WMAP	Planck	Planck + ACT DR6	
σ(H <sub>0</sub> )	1.5	1.1	0.5	0.4	
σ(n <sub>s</sub> )	0.015	0.006	0.004	0.003	
σ(N <sub>eff</sub> )	0.4	0.3	0.2	0.1	

Large improvements in beyond-ΛCDM parameters: ~2x increase in sensitivity to new light relic particles



Upcoming ACT DR6 precision cosmology constraints will surpass those from Planck (H<sub>0</sub>, N<sub>eff</sub>, Σm<sub>v</sub>, σ<sub>8</sub>, + beyond-ΛCDM models) — stay tuned!