

TOR VERGATA  
UNIVERSITÀ DEGLI STUDI DI ROMA

# Probing the Hubble constant from X-ray and millimetre observations of CHEX-MATE galaxy clusters

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Observing the Universe at millimetre wavelengths - Grenoble 26-30/06/2023

# OVERVIEW

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- Galaxy clusters in the context of the  $H_0$  tension;

## II. Method:

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  - Cosmological rulers;
  - Different inferences of thermodynamical profiles;
  - Hydrodynamical simulations;
- **Data analysis**
  - SZ signal;
  - X-ray signal;
- **The samples**

## III. Results:

- **Observed sample**
  - $\eta_T$  distribution;
- **Simulated sample**
  - New  $\mathcal{B}$  bias;
- **Cosmological inference**
  - $H_0$  posterior;

## IV. Discussion & Conclusion

# Galaxy clusters in the context of the $H_0$ tension

During the last decades,  $H_0$  measurements became remarkably precise, especially for early-Universe (CMB-driven) and local Universe (SN1a-based) estimates.

However, the two methods start to disagree with a significant bias, at a level of  $4\sigma$  with the latest measurements.

This bias survived several attempts of independent reanalyses or the inclusion of more sophisticated of systematics.

Indications of new physics beyond the concordance  $\Lambda$ CDM?

We need more observables, independent of these two methods, to explore the problem.

# INTRODUCTION

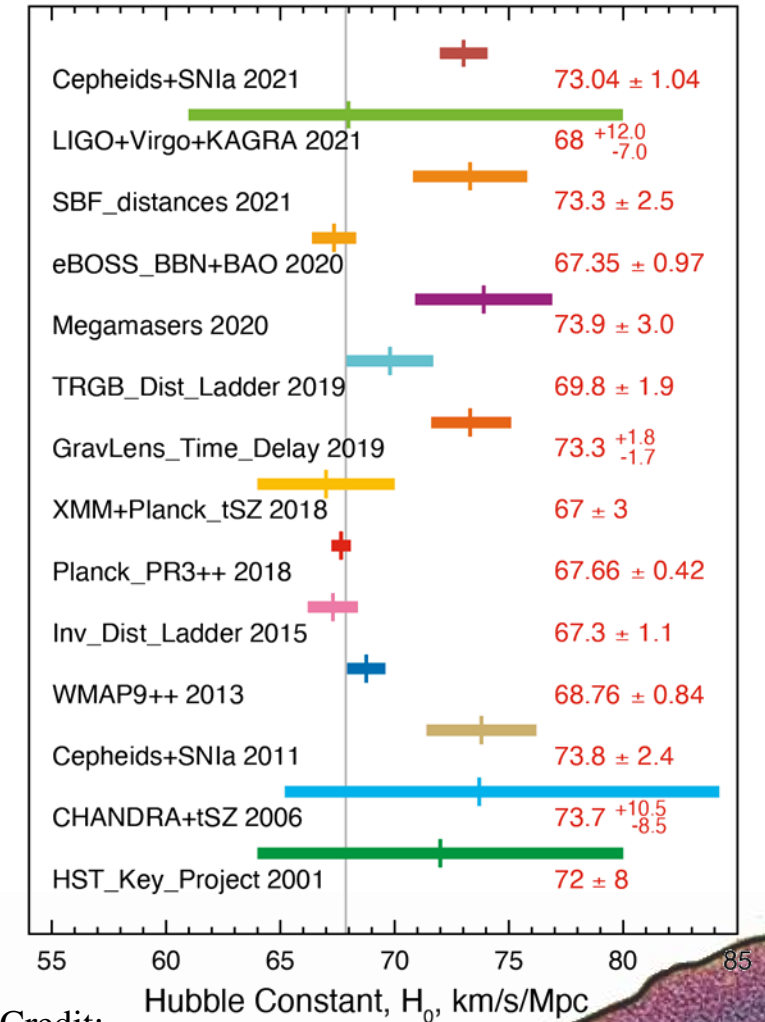


Image Credit:  
NASA / LAMBDA  
Archive Team

# Galaxy clusters as cosmological probes: Cosmological rulers

It is possible to directly extract cosmological information by combining SZ and X-ray observables, as suggested by **Cavaliere et al. (1977)** and **Silk & White (1978)**, with a distance-measuring technique.

**X-ray:**  $\Sigma_X(\theta) = \frac{1}{4\pi(1+z)^4} \int n_e^2 \Lambda_X D_A d\theta \propto n_e^2 D_A \theta_c$

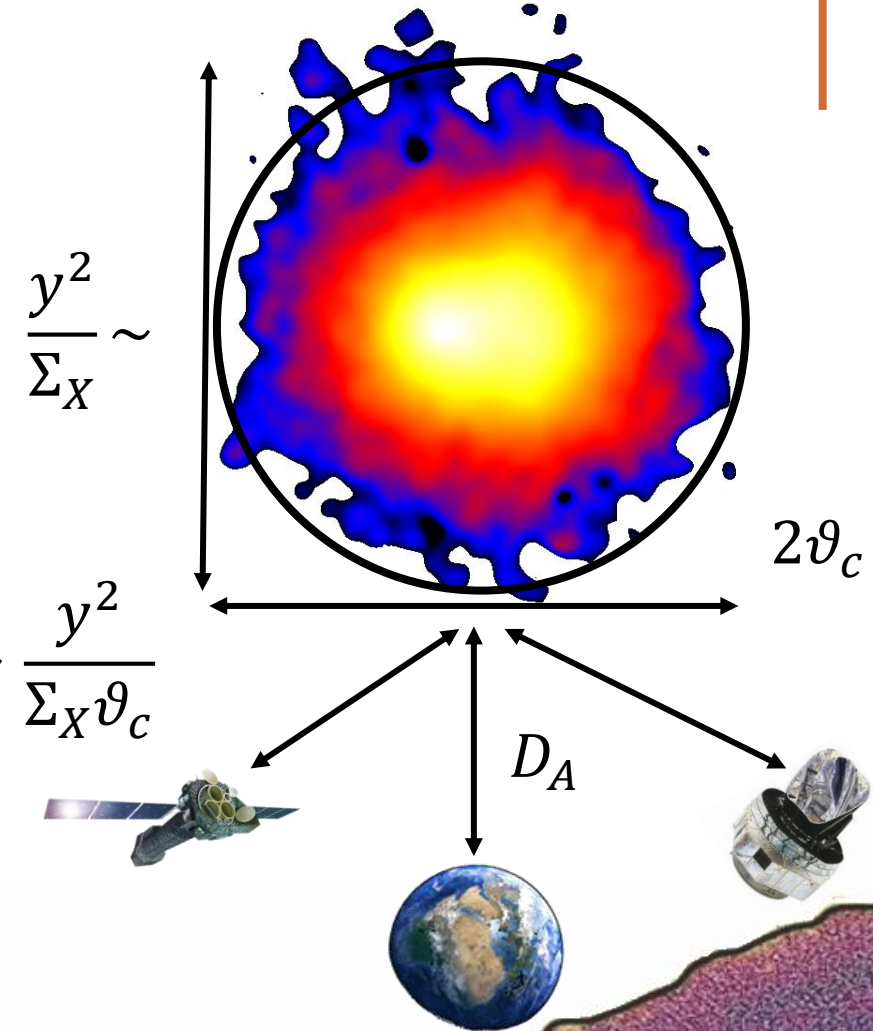
**SZ:**  $y(\theta) = \frac{k\sigma_T}{m_e c^2} \int n_e T_e D_A d\theta \propto n_e D_A \theta_c$

$D_a(z, H_0) \sim \frac{y^2}{\Sigma_X \vartheta_c}$

**Key quantities:**  
 $\Sigma_X, y, \text{redshift}$

$\vartheta_c$ : characteristic scale  
of the cluster

## METHOD



## Galaxy clusters as cosmological probes: Cosmological rulers

Cosmological information in  $D_a(z)$  can be derived from the thermodynamical profile of the ICM by combining multiwavelength surveys of galaxy clusters, as done in [Kozmanyán<sup>1</sup> et al. \(2019\)](#).

$$\Sigma_X(\theta) = \frac{1}{4\pi(1+z)^4} \int n_e^2(r(\theta)) \Lambda_X dr$$

$$T_X(\theta) = \frac{\int w T(r(\theta)) dr}{\int w dr}$$

$$\eta_T = T_X / T_{SZ} = \frac{T_X}{(P_e/n_e)}$$

$$y(\theta) = \frac{\sigma_T}{m_e c^2} \int \eta_T \cdot P_e(r(\theta)) dr$$

$$= \frac{\sigma_T}{m_e c^2} \int \eta_T \cdot n_e(r(\theta)) \cdot k T_{SZ}(r(\theta)) dr$$

**Key quantities:**  
 $\eta_T$ , redshift

$$w = n_e^2 / T^{3/4}$$

<sup>1</sup>DOI: [10.1051/0004-6361/201833879](https://doi.org/10.1051/0004-6361/201833879)

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In the ideal case:  $\eta_T \equiv 1$ . Source of departure from unity:

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$$c = \left(\frac{\overline{D_a}}{D_a}\right)^{1/2} \cdot \left(\frac{n_p/n_e}{\overline{n_p}/\overline{n_e}}\right)^{1/2} \cdot \left(\frac{1 + 4 \frac{n_{He}/n_p}{\overline{n_{He}/\overline{n_p}}}}{1 + 4 \frac{\overline{n_{He}}/\overline{n_p}}{\overline{n_{He}}/\overline{n_p}}}\right)^{1/2}$$

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Emitting ICM distribution property ( $\mathcal{B}$ ):

$$\mathcal{B} = \frac{C_\rho^{1/2}}{e_{LOS}^{1/2}}$$

$e_{LOS}$ : Elongation along  
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$$\eta_T = b_n \times \mathcal{C} \times \mathcal{B}$$

$b_n$ : all other possible systematics

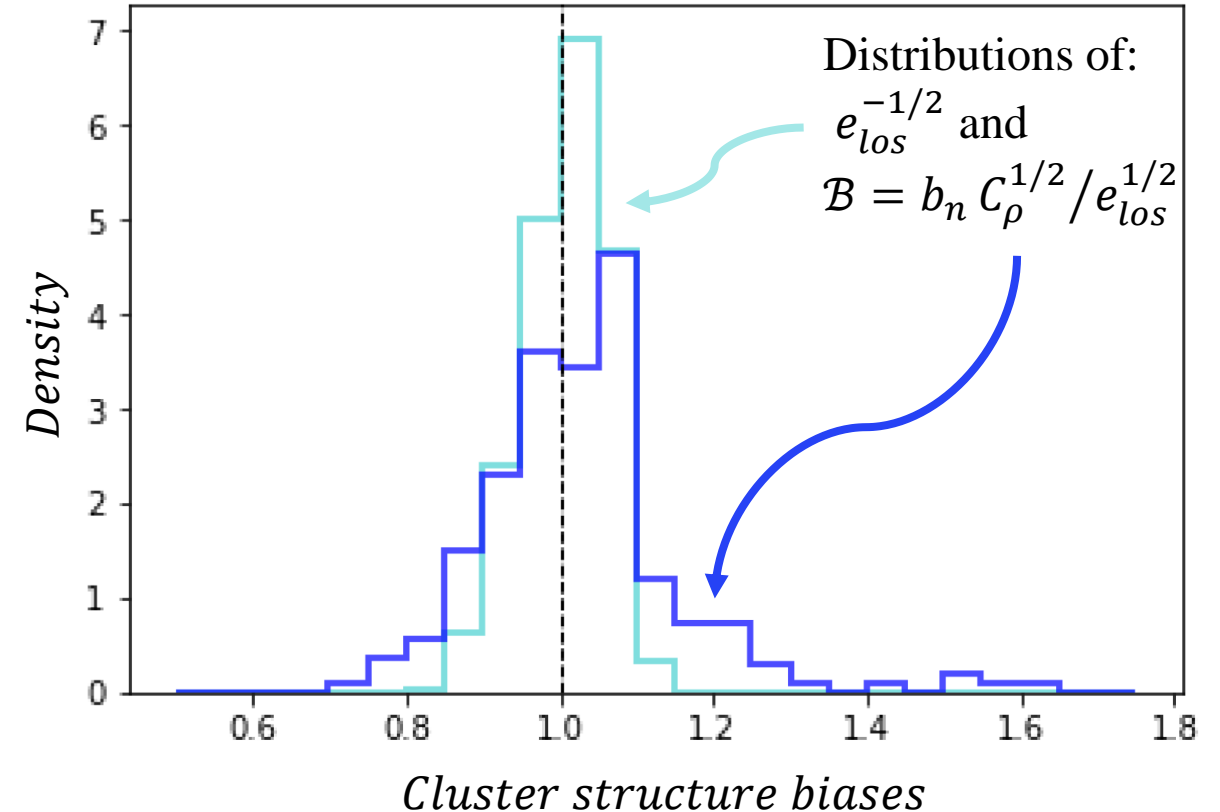
# METHOD

## Galaxy clusters as cosmological probes: Hydrodynamical simulations

We need hydrodynamical simulations to disentangle the cosmological information from the cluster structure bias.

For a simulated sample of galaxy clusters, the cosmological framework is set from the beginning:  $\mathcal{C} \equiv 1$  and  $\eta_T = b_n \mathcal{B}$ .

From Kozmanyán et al. (2019)



# METHOD

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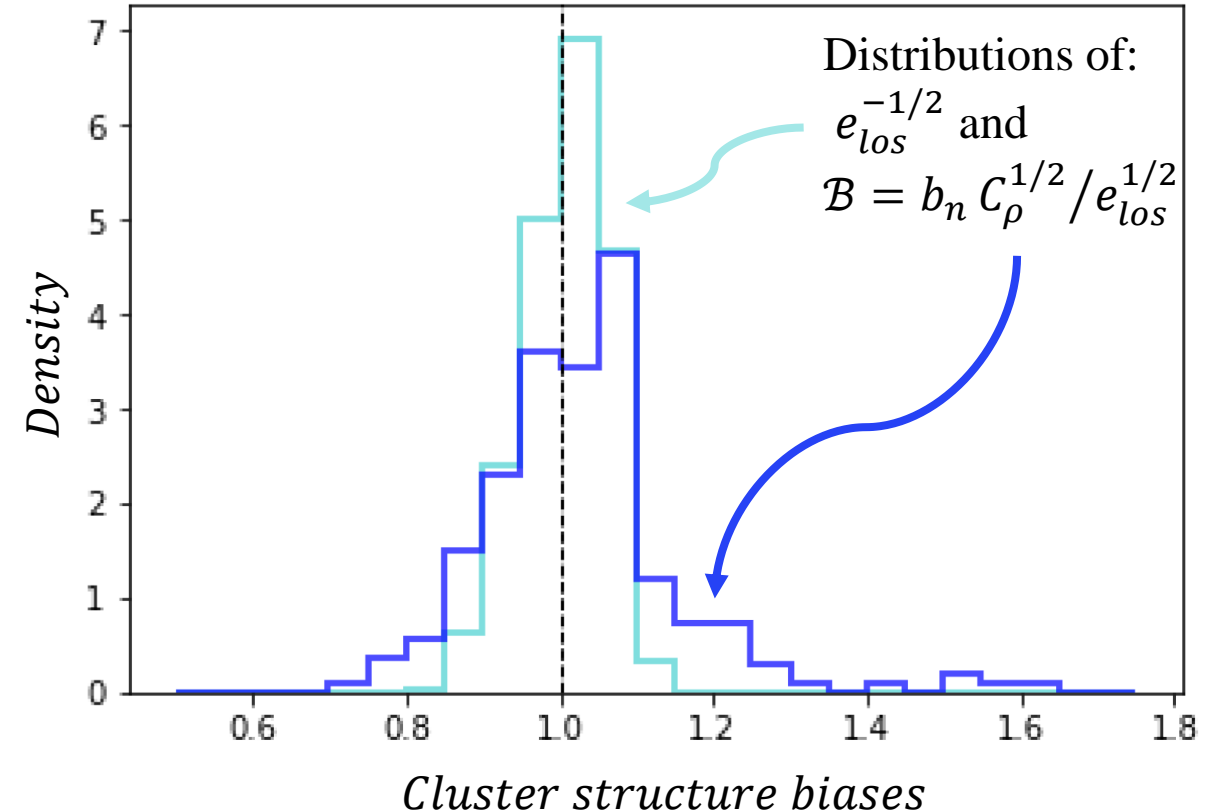
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Thus, it is possible to use the  $\mathcal{B}$  distribution in the  $H_0$  derivation with a Bayesian approach:

$$P(H_0) = \int \mathcal{L} \left( \left\{ \eta_T^{(i)} \right\} \mid H_0, \Omega_m, Y, \{ \mathcal{B}_i \} \right) p(\{ \mathcal{B}_i \}) p(H_0) p(\Omega_m) p(Y) d\Omega_m dY d\mathcal{B}_1 \dots d\mathcal{B}_N$$

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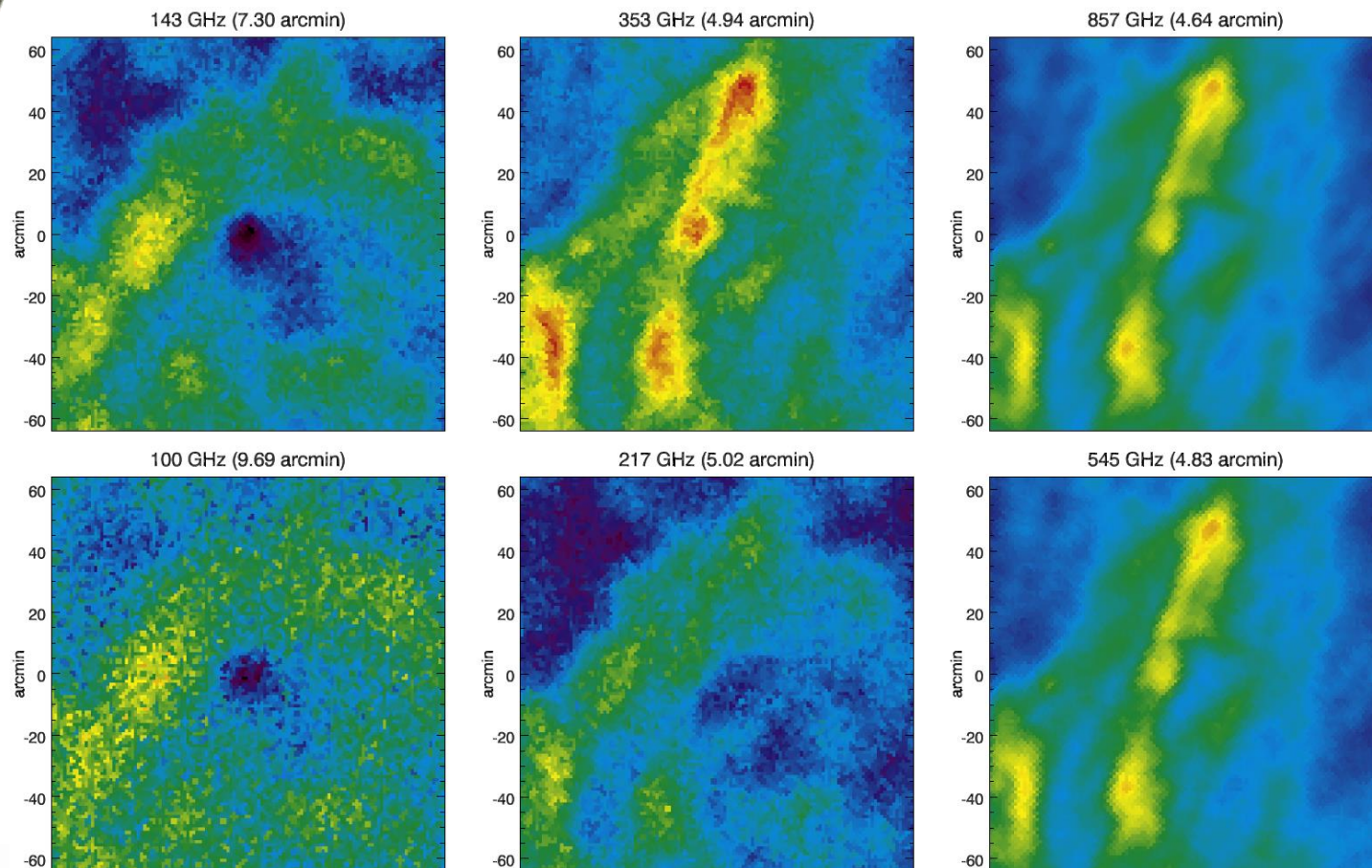
## Data analysis: SZ signal

The SZ and X-ray signals are extracted with an optimised application of the [Bourdin<sup>2</sup> et al. \(2017\)](#) work.

- Instrument: *Planck*-HFI data;
- Wavelet denoising and reconstruction of HFI maps;
- Parametric component separation;
- Forward modelling of [Nagai et al. \(2006\)](#) pressure profile.

<sup>2</sup>DOI: [10.3847/1538-4357/aa74d0](https://doi.org/10.3847/1538-4357/aa74d0)

# METHOD



*Planck*-HFI frequency maps of A2163 from [Bourdin et al. \(2017\)](#).



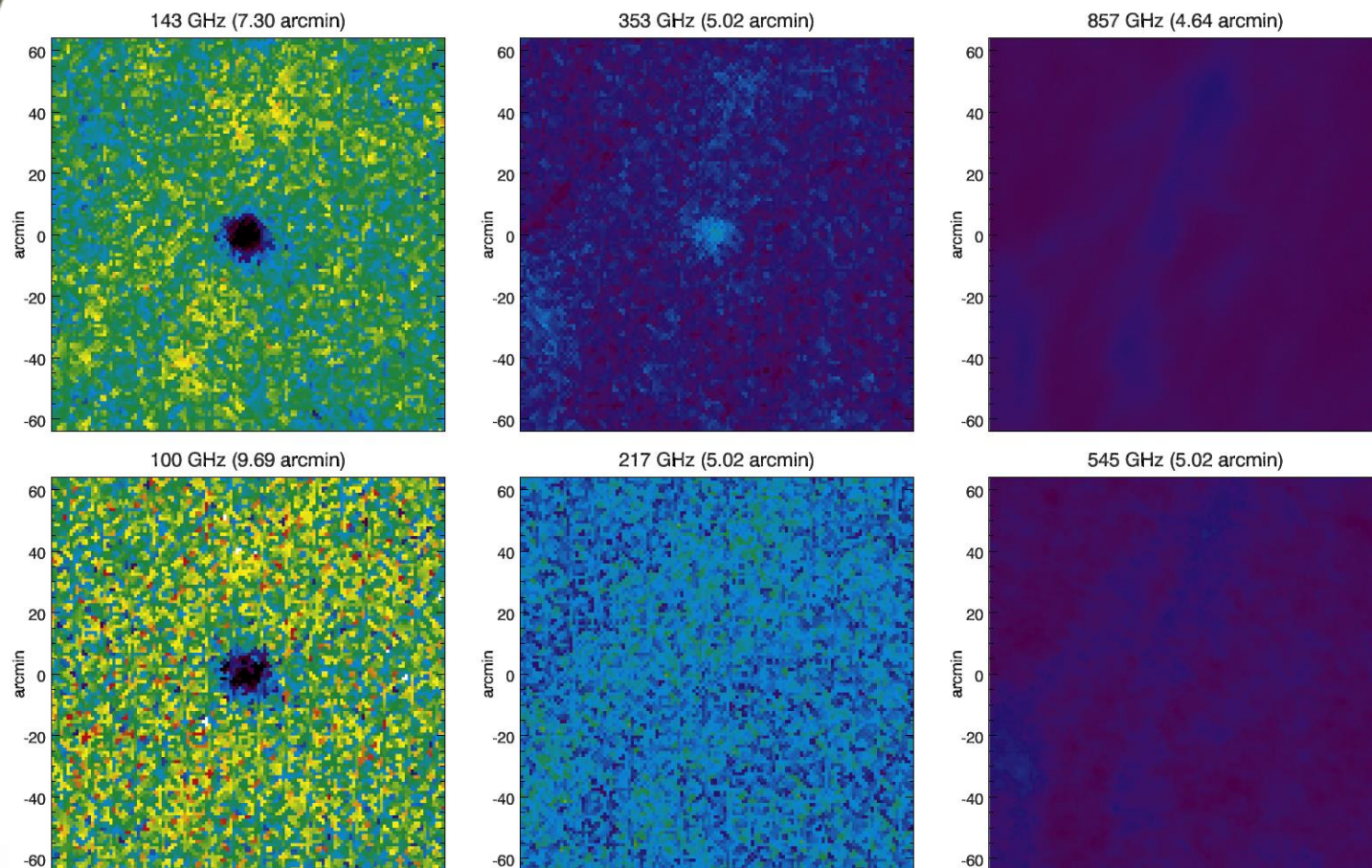
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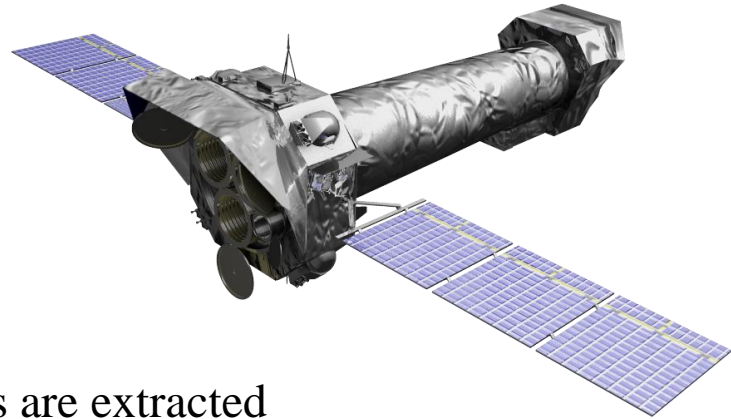
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Filtered *Planck*-HFI SZ frequency maps of A2163 from [Bourdin et al. \(2017\)](#).

## Data analysis: X-ray signal

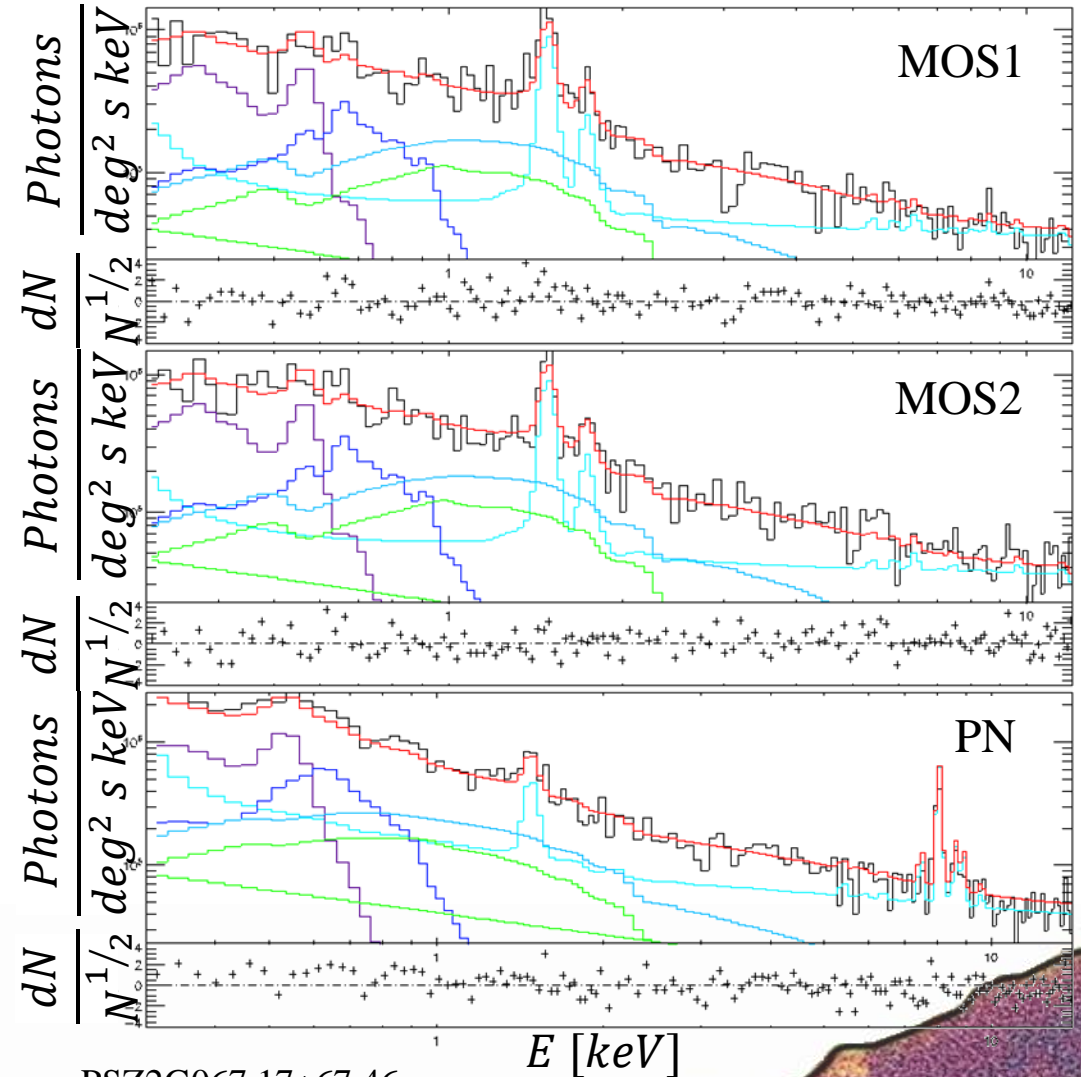


The SZ and X-ray signals are extracted with an optimised application of the [Bourdin<sup>2</sup> et al. \(2017\)](#) work.

- Instruments: XMM-Newton telescope EPIC cameras;
- Parametric spectral modelling of the astrophysical (CXB and Galactic emission) and instrumental components;
- Forward modelling of density and temperature [Vikhlinin et al. \(2006\)](#) profiles.

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# METHOD



PSZ2G067.17+67.46  
Background spectral analysis

## The samples

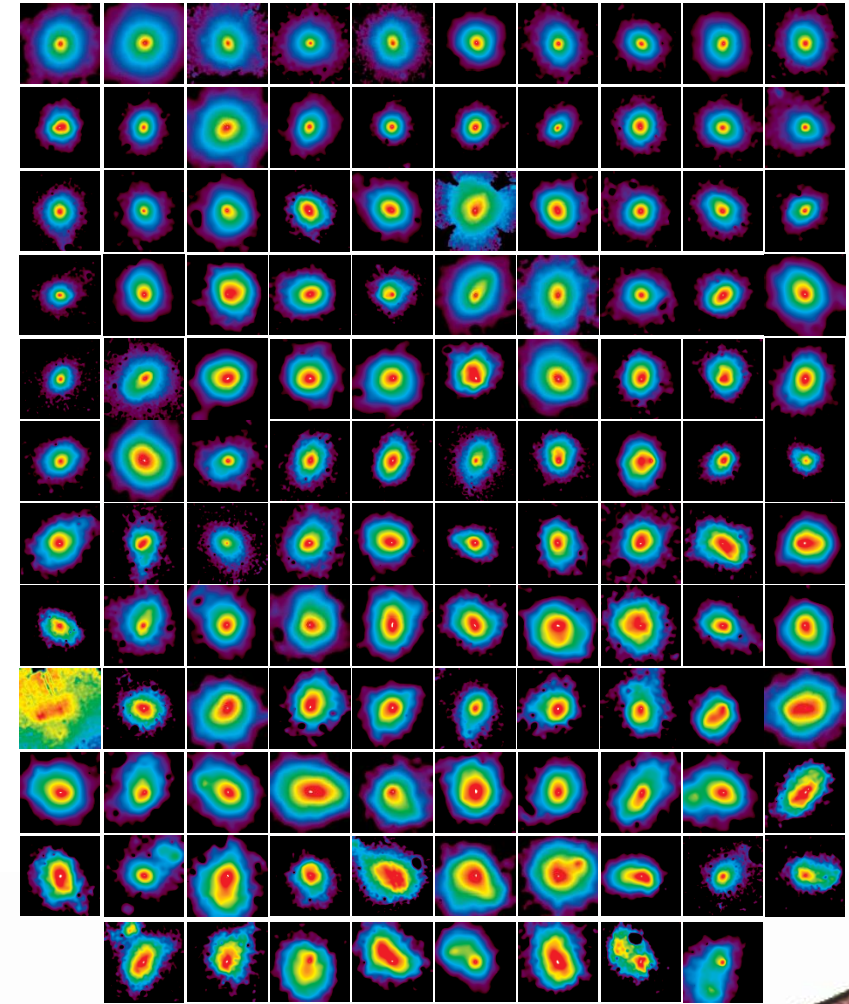
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Observed sample: the **CHEX-MATE**<sup>3</sup> project.

- 117 clusters (over 118) extracted from PSZ2 catalogue within the cosmological mask and with *Planck*  $S/N > 6.5$ ;
- Homogeneous and high-quality X-ray exposures:  $S/N=150$ ;
- Temperature measurements with statistical 15% of accuracy at  $R_{500}$ ;
- Temperature profiles with more than 8 radial bins.





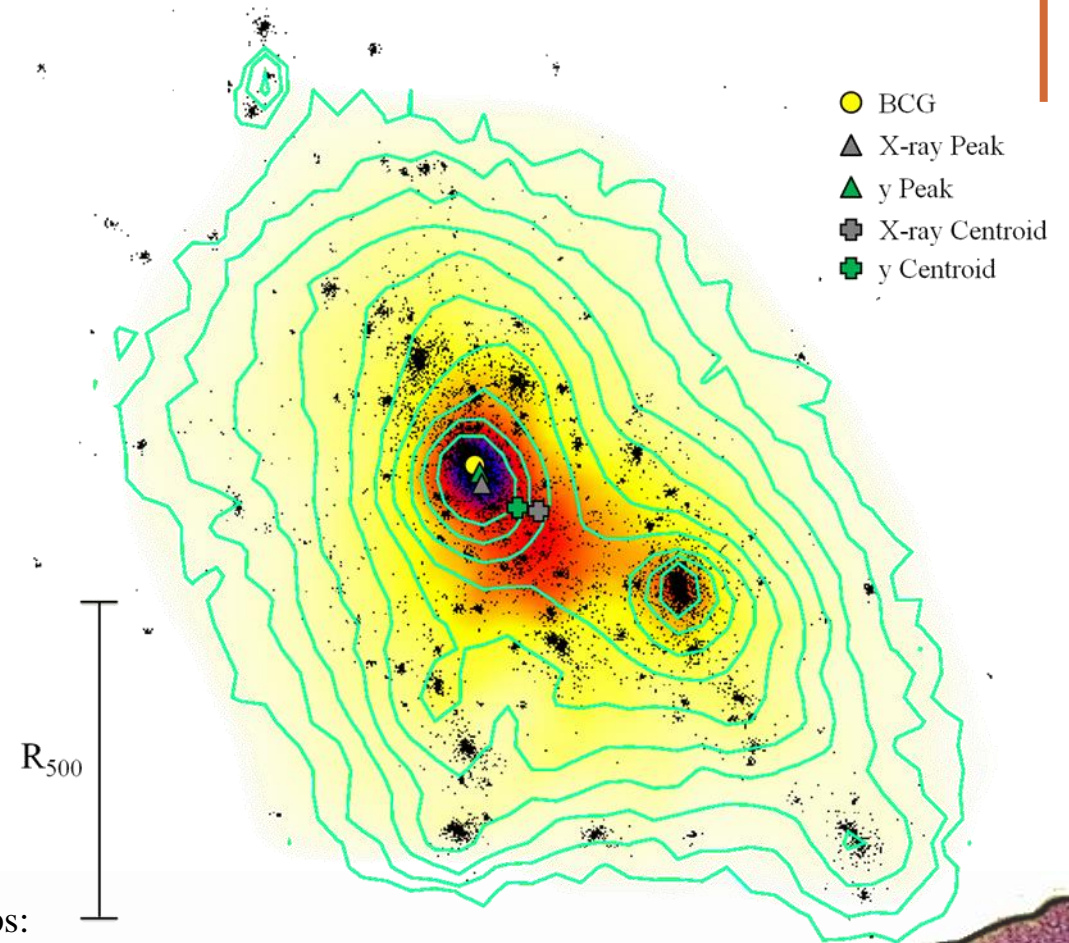
# METHOD

## The samples

For the Bayesian analysis, we need an observed and a simulated sample of clusters.

Synthetic sample - **THE THREE HUNDRED<sup>4</sup>** project

- Gadget-X run. Hydrodynamic simulation with a cosmology consistent with **Planck Collaboration et al. (2016)**;
- New  $\mathcal{B}$  bias applying the X-ray-SZ pipeline on a simulated sample of 975 clusters from the snapshot at  $z = 0$ .

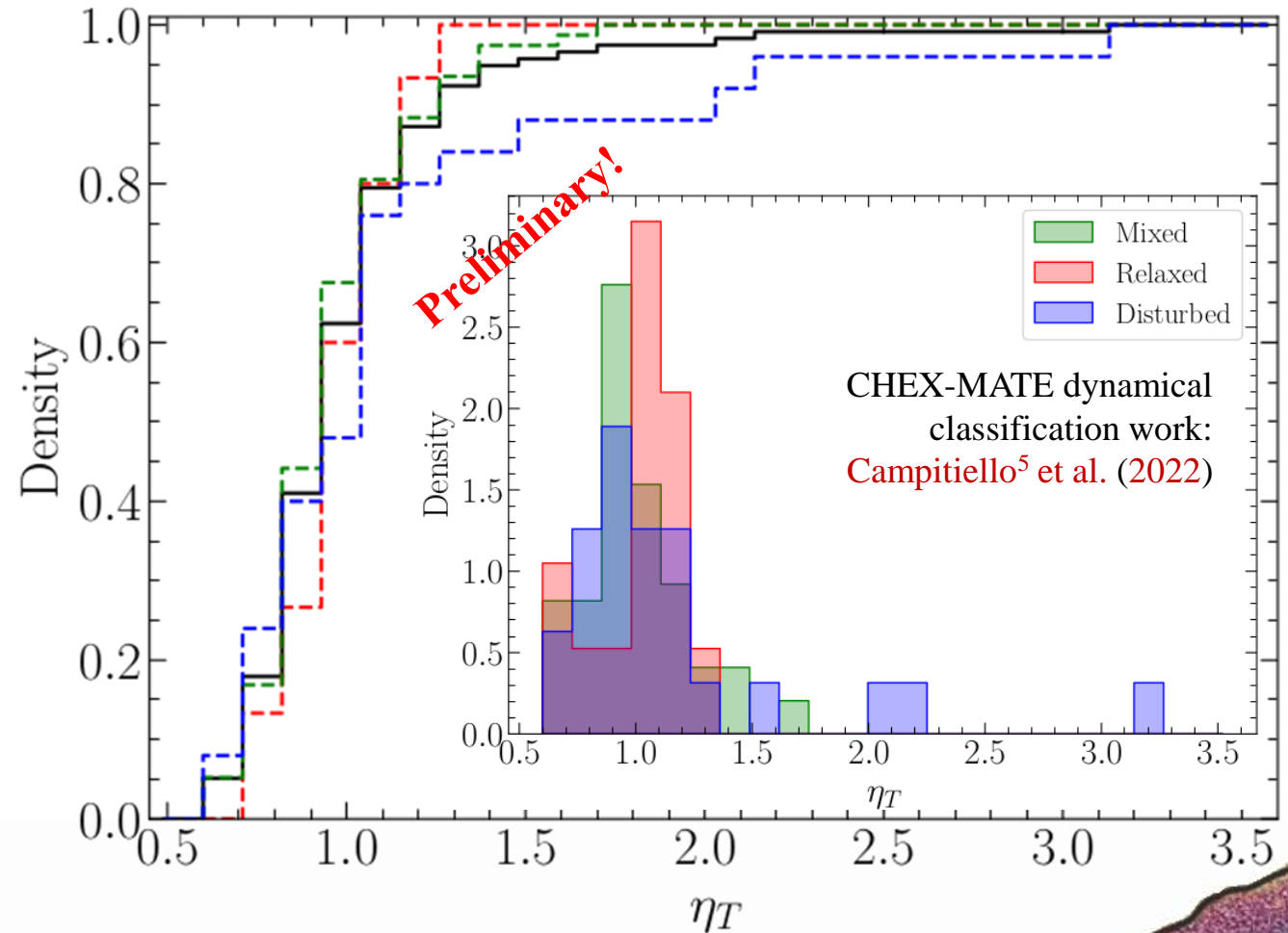


Mock maps:  
Contours: X-ray  
Colour map: tSZ  
Black dots: Optical SDSS

# RESULTS

## Observed sample: $\eta_T$ distribution

- Median:  $\eta_T = 0.98_{-0.19}^{+0.23}$   
( $\pm 16^{\text{th}}, 84^{\text{th}}$  percentiles);
- The distribution is compatible with the expected value ( $\eta_T \equiv 1$ );
- The analysis agree also with previous estimate available in the literature:
  - X-COP sample:  
 $\eta_T = 0.9624 \pm 0.0013$ ;
  - **Bourdin et al. (2017)** low-redshift sample:  $\eta_T = 1.01$  (median).



<sup>5</sup>DOI: [10.1051/0004-6361/202243470](https://doi.org/10.1051/0004-6361/202243470)

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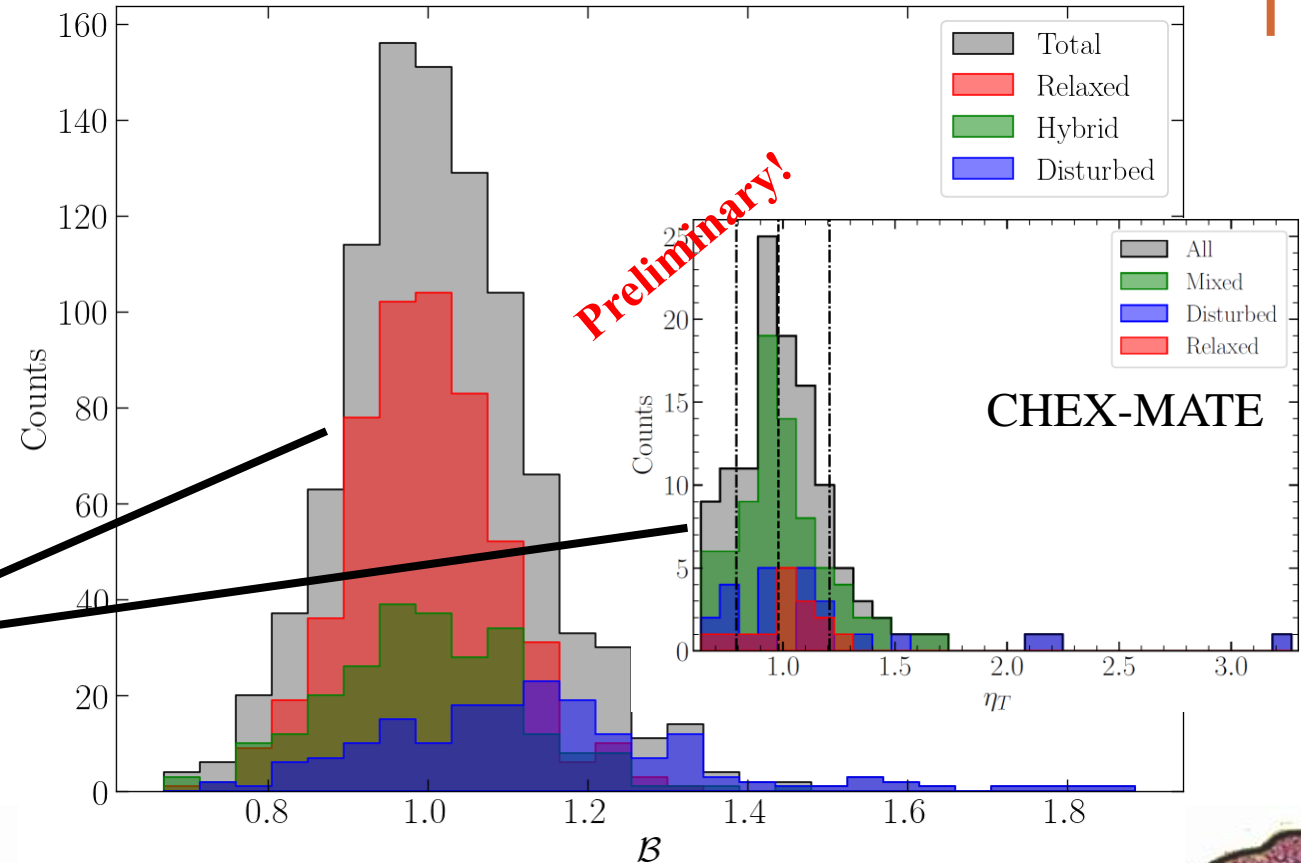
## Simulated sample: New $\mathcal{B}$ bias

With the simulated sample, we can:

- Derive a prior distribution  $\mathcal{B}$  for the cosmological inference;
- Study, with more clusters, the effect of the dynamical and morphological state in  $\eta_T$  distribution.

Similar distribution of the observed CHEX-MATE sample!

THE THREE HUNDRED clusters



# RESULTS

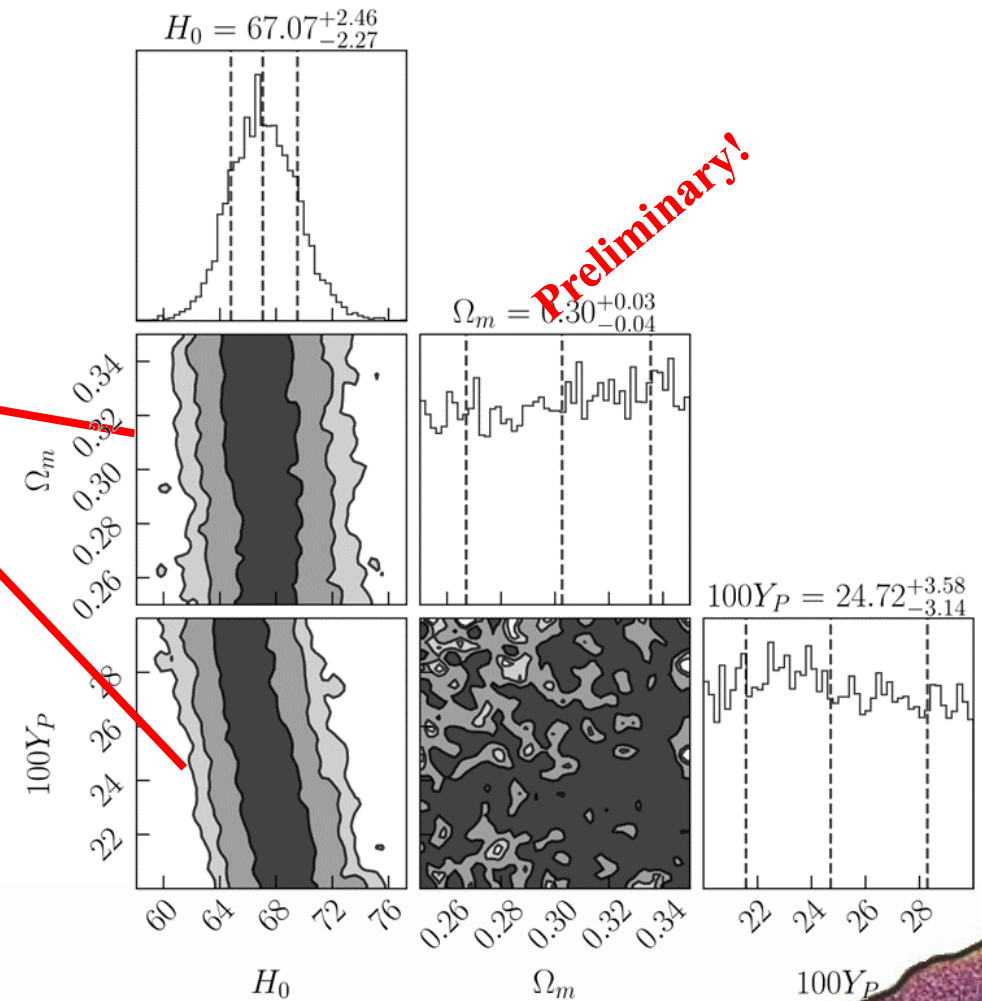
## Cosmological inference

Using the  $\mathcal{B}$  distribution from the synthetic sample, we can extract cosmological information from  $\eta_T$ .

The method is not sensitive enough to recover more than one free parameter ( $H_0$ ) at a time ( $\eta_T \propto D_A^{-1/2}$ ).

Bayesian prior setup of the MCMC runs

Parameter	Prior	Min	Max	$\mu$	$\sigma$
$H_0$	Uniform	50	100		
$\mathcal{B}_i$	Uniform	0	1		
$\Omega_m$	Uniform	0.25	0.35		
	Normal	0	1	0.3153	0.0073
$Y_P$	Uniform	0.20	0.30		
	Normal			0.243	0.024



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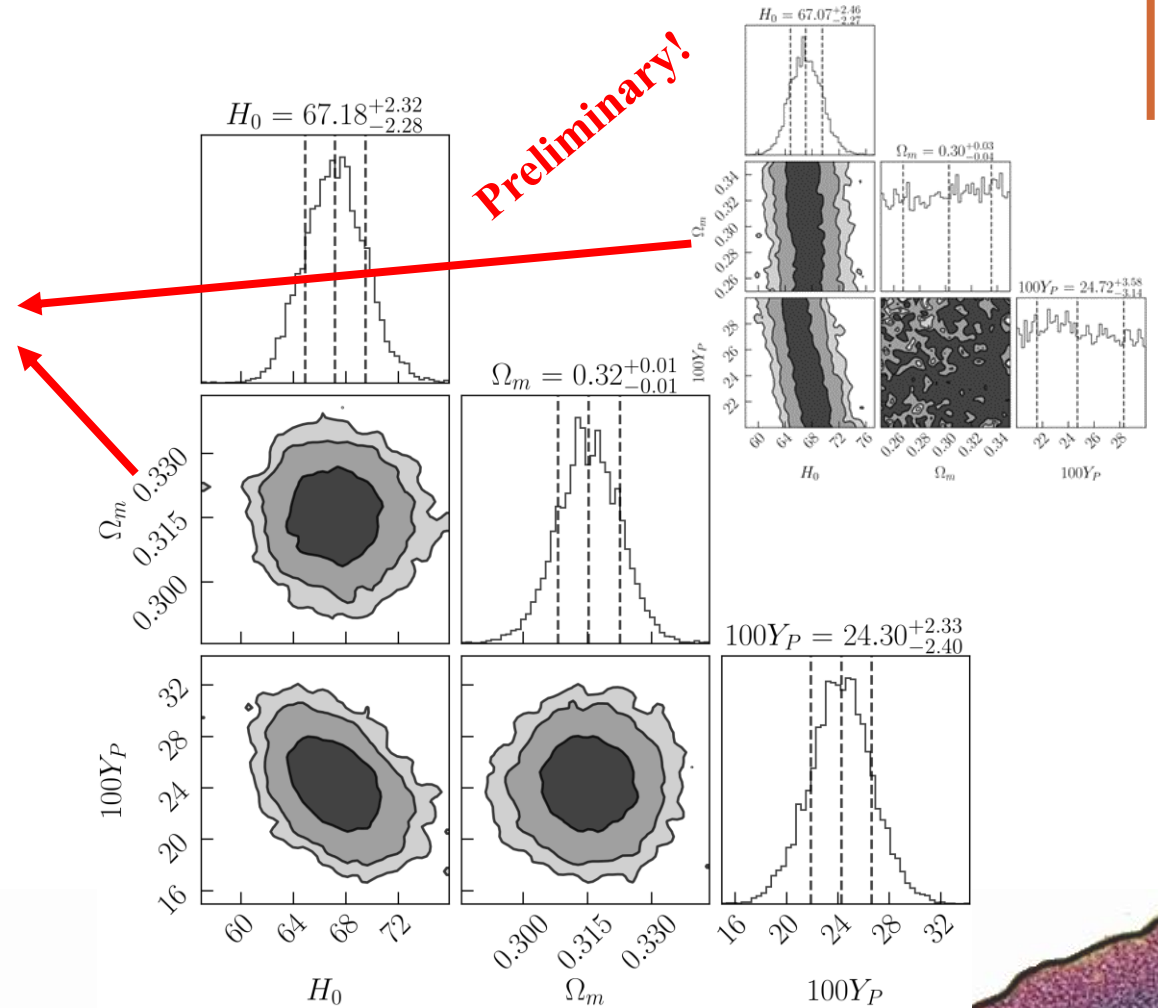
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# Cosmological inference: $H_0$ posterior

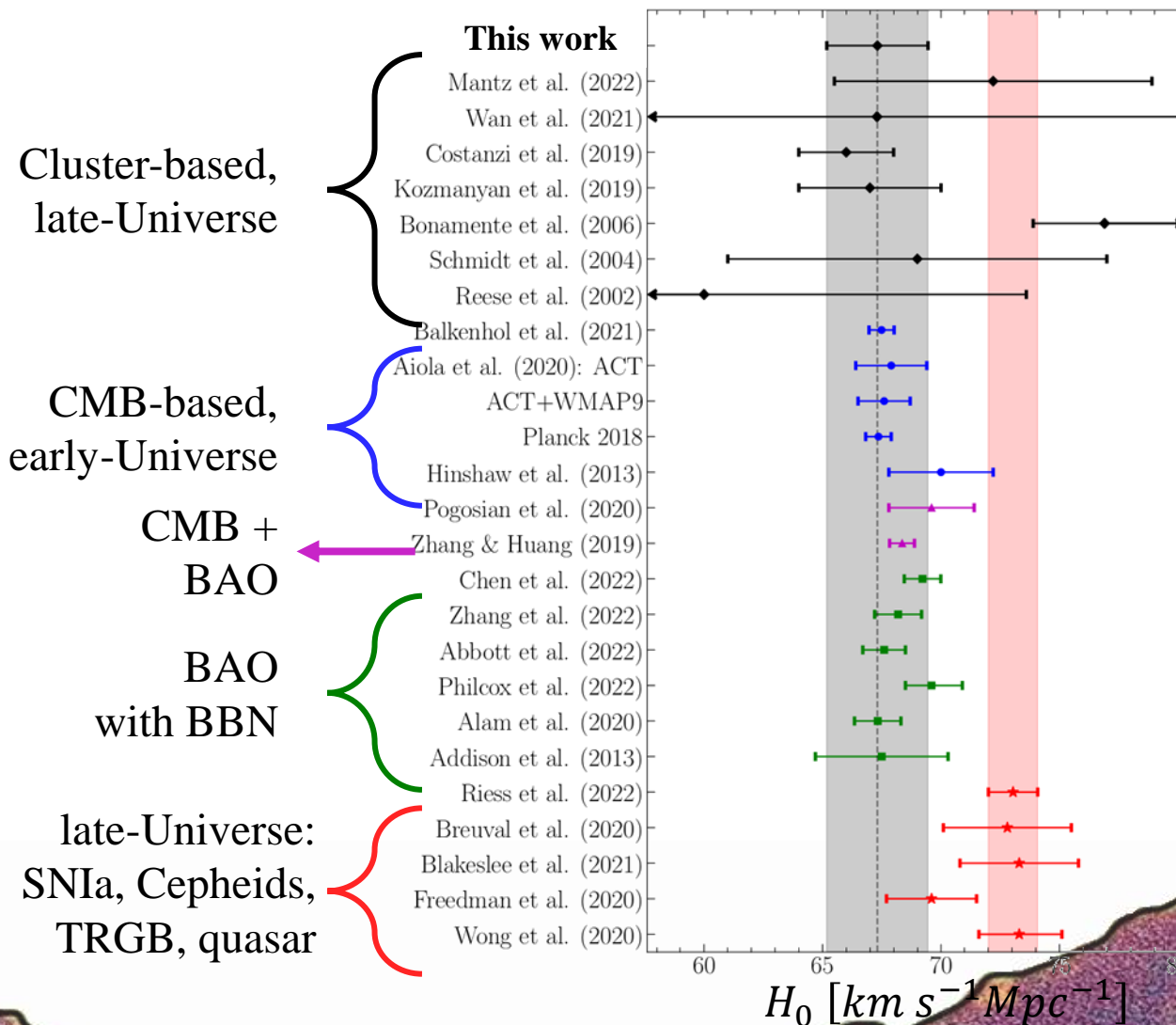
With the [Kozmany et al. \(2019\)](#) method, we have a [preliminary](#) measure for the CHEX-MATE clusters:

$$H_0 \sim 67.2 \pm 2.3 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Compatibly with the precedent estimates based on multiwavelength cluster studies or with early-Universe and LSS estimates.

More in tension with late-Universe SNIa, Cepheids, TRGB, quasars.

# RESULTS



## Potential systematics

- Astrophysical uncertainties: ( $N_H$ , X-ray/millimetre contaminants, relativistic SZ effect, etc.);
- X-ray temperature cross-calibration (see [Wan et al. 2021](#)):
  - Cross-calibration depends on the cluster temperature (higher at higher temperatures);
  - Temperatures from *Chandra* and XMM are known to disagree;
  - XMM EPIC cameras give different results if not jointly used;
- Hydrodynamical simulations:
  - Are we sure that our synthetic samples are accurate representations of real clusters?

## DISCUSSION & CONCLUSION

- ✓ Our results on  $\eta_T$  or  $H_0$  are compatible with precedent estimates from *Planck* and XMM and with [Wan et al. \(2021\)](#);
- ✓ Our method for  $H_0$  is mainly driven by the thermodynamical state at intermediate-large scales, where the temperature is lower;
- ✓ Different hydrodynamical simulations ([Rasia et al. 2015](#) and THE THREE HUNDRED Gadget-X run) give compatible estimates for  $H_0$ ;
- ✓ More tests can be done for new runs (as Gadget-Simba) or using new hydrodynamical simulations with different physics.

# DISCUSSION & CONCLUSION

- ✓ The CHEX-MATE Project allows accurate characterisation of the thermodynamical state of galaxy clusters with its sample definition and observational strategy;
- ✓ Accurate mass selection function with 117 clusters in total, double compared to [Kozmany et al. \(2019\)](#) and a factor of 10 more than [Wan et al. \(2021\)](#) or the X-COP sample;
- ✓ Need hydrodynamical simulation priors, but it is not restricted to only relaxed sample;
- ✓ Our local estimate for  $H_0$  agrees with the precedent constraints based on XMM, *Chandra*, and *Planck*;
- ✓ The uncertainty on  $H_0$  is continually decreasing with the cluster size;

## Future prospective:

- Possibility to extend the analysis to larger samples (e.g. early-SZ+CHEX-MATE ~ 160 objects).
- For 200 clusters: 2% uncertainty level;
- Combination with other X-ray or millimetre instruments (e.g. SPT, Chandra);
- Inclusion of more systematics in the model, such as the relativistic SZ effect or temperature cross calibration;
- Possible combination with other cluster probes, such as the  $f_{gas}$  (e.g.  $f_{gas} \propto D_A^{3/2}$ )



**THANKS FOR THE  
ATTENTION!**