



# The physics of Atom- Surface interactions and its applications

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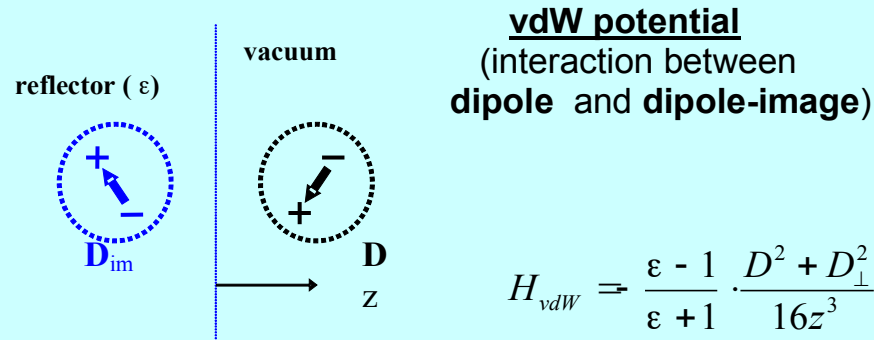
**EU FASTNet network, IFRAF**

Critical Stability, Erice, Oct. 2008

## ATOM-SURFACE VAN DER WAALS INTERACTION

### The model of electrostatic images

(perturbative regime, non resonant coupling)



non-retarded and  
near-field interaction:  $z^{-3}$

$D$ , atomic dipole operator

For a neutral atom,  $\langle e|D|e \rangle = 0$ , but  $\langle e|D^2|e \rangle \neq 0$   
(atomic dipole fluctuations)

$$\rightarrow \langle i|H|i \rangle = -C_3(i) / z^3$$

## *Long-range interactions between atomic systems and surfaces*

- Influence of the composite nature of the atomic system (internal energy level, ground/excited state, rotational symmetry, symmetry breaking...)
- “*real*” surfaces: dispersive materials, surface roughness
- Atom external dynamics: Quantum mechanical features of atomic motion (quantum reflection, bound states, interaction with “fast” (thermal) atoms...)

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### *Two experimental approaches*

- Laser spectroscopy at vapor-dielectric interfaces (surface potential)
- Atom beam passing at surfaces (momentum spectroscopy- surface forces)

# Long-range atom-surface interactions

## OUTLINE

- I. Introduction. Distance scaling
- II. The surface response: material dispersion, temperature excitations...
- III. Symmetry properties: symmetry break, inelastic vW reflection
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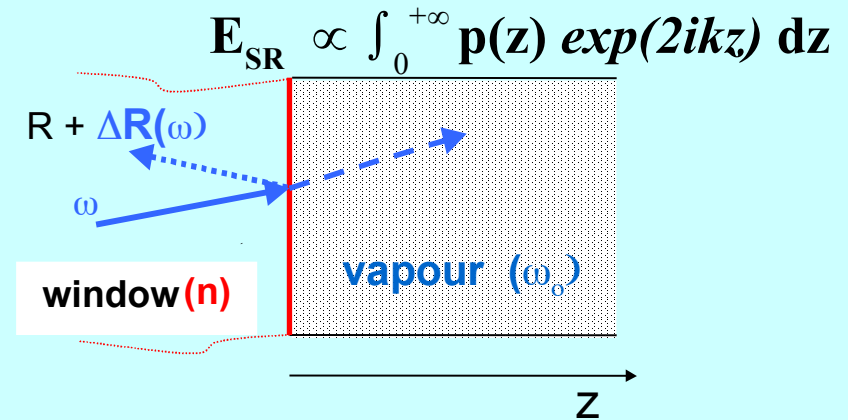
# Spectroscopic Measurements

Optical Spectroscopy: DIFFERENCE between potentials  $C_3(j) - C_3(i)$

**Thermal vapours** : spatial integration

Selective Reflection :

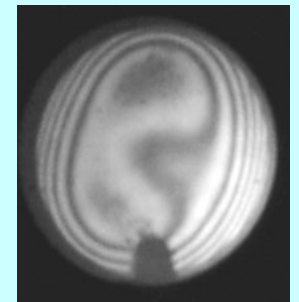
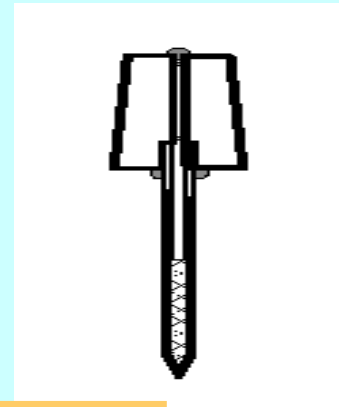
**Resolution**  $\sim \lambda/2\pi \sim 100 \text{ nm}$



Thin Cells :

**Mechanical confinement**

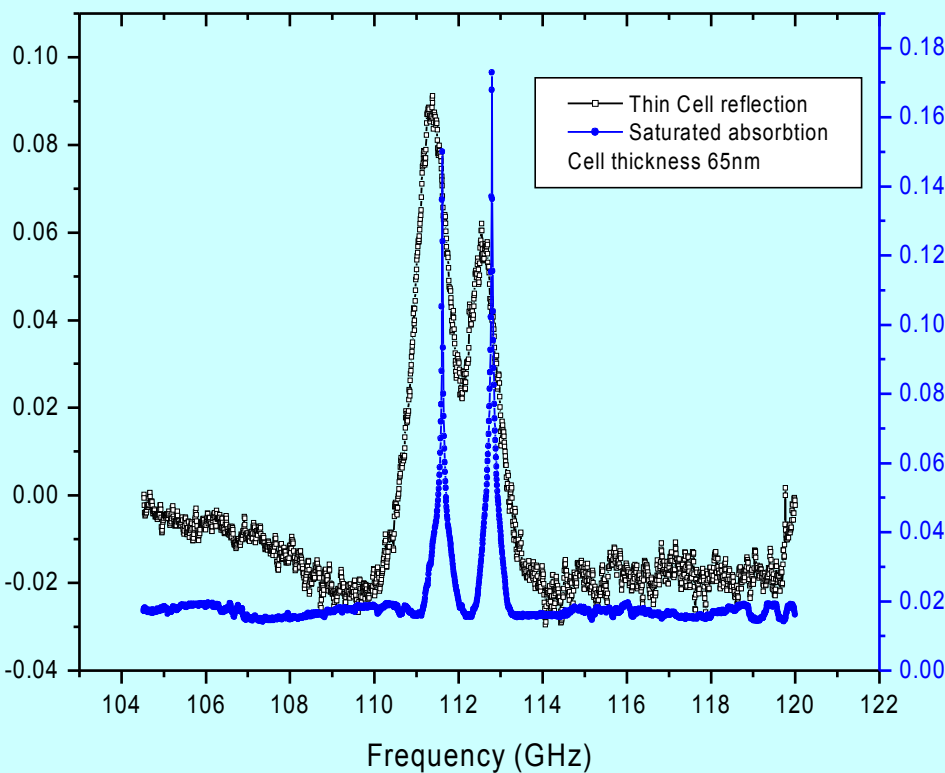
**thickness**  $\sim 20\text{-}1000 \text{ nm}$



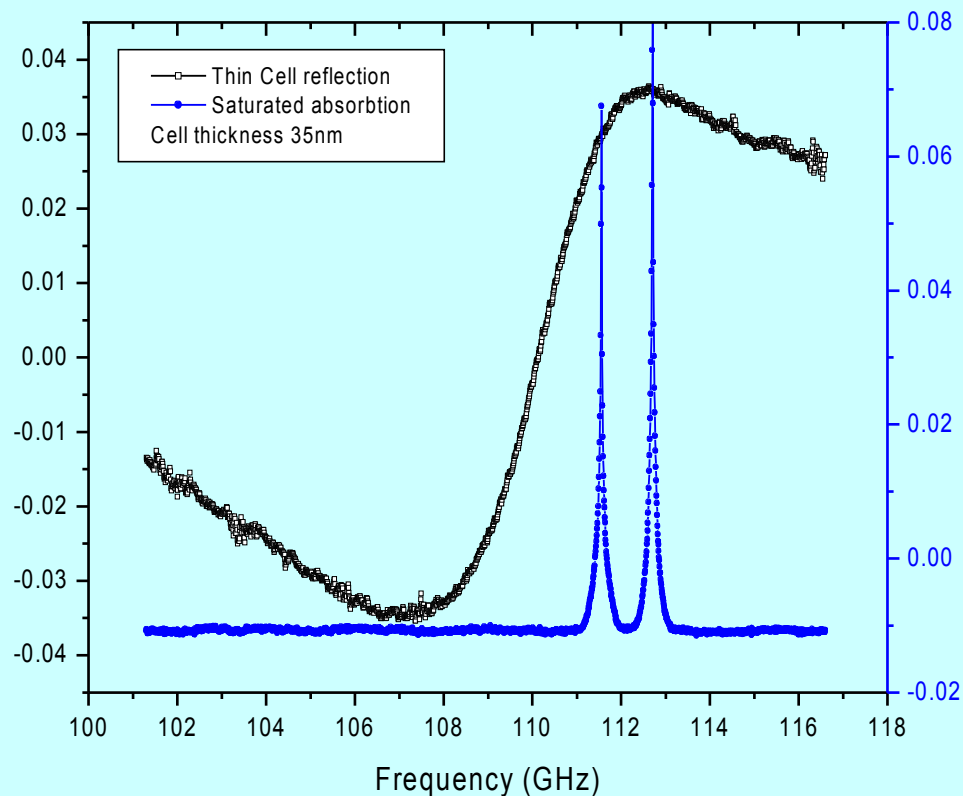
# Cesium D<sub>1</sub> transition (894nm)

*Reflection* spectra on vapor nano-cells (FM mode)

**65nm**



**35 nm**



# Modelling transmission spectra in nanocells

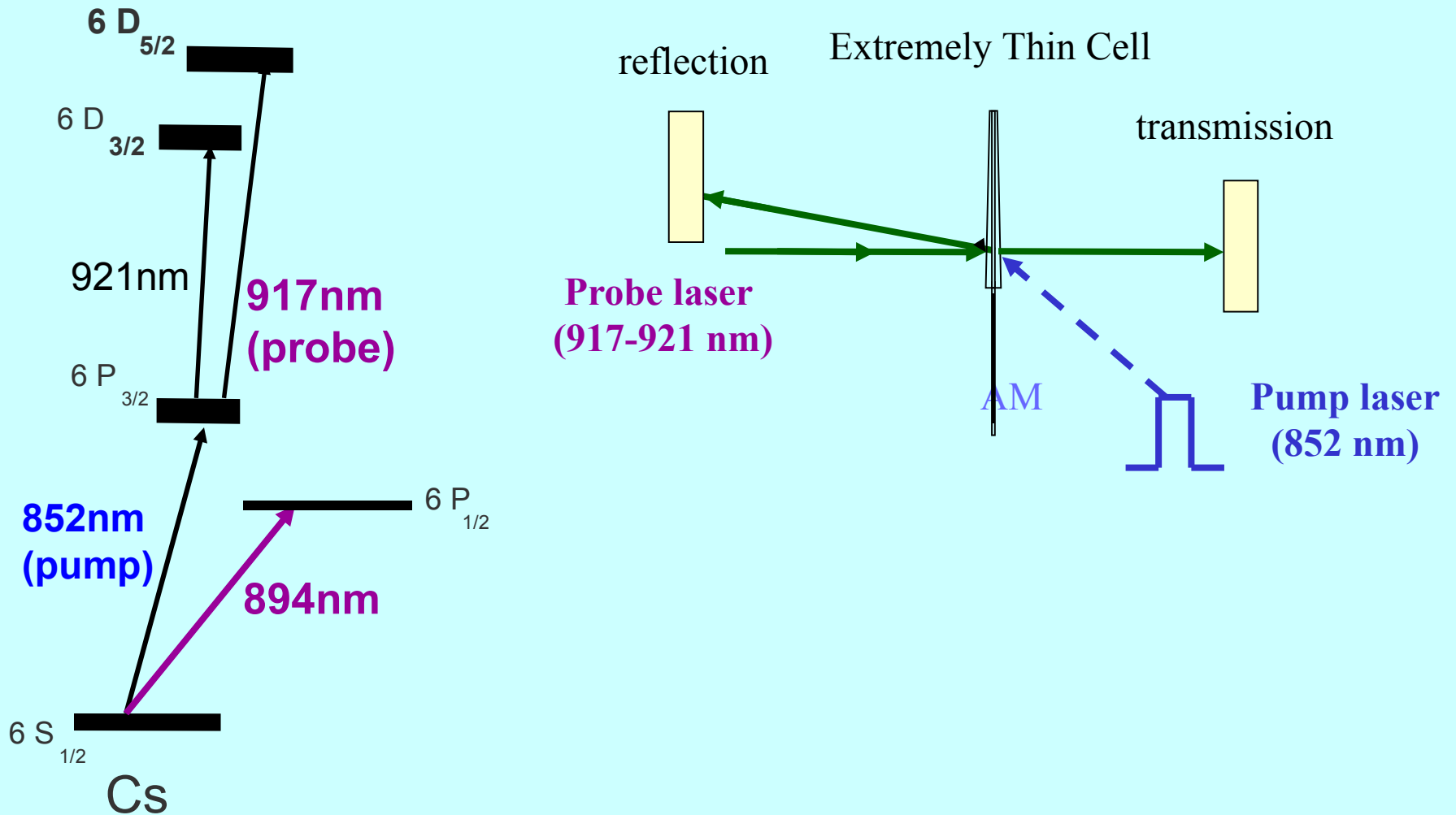
- **2-wall van der Waals potential** (adding 2 walls, or multiple image modeling)
- **Spatial integration** of transient interaction regimes in the nano-cell
- **Velocity distribution** *i.e.* distribution over atom-light interaction times
- **Pressure effects** (broadening, shift)

## Transmission and Reflection spectra:

2 linearly **independent combinations** of absorptive and dispersive properties



# Experimental Principle



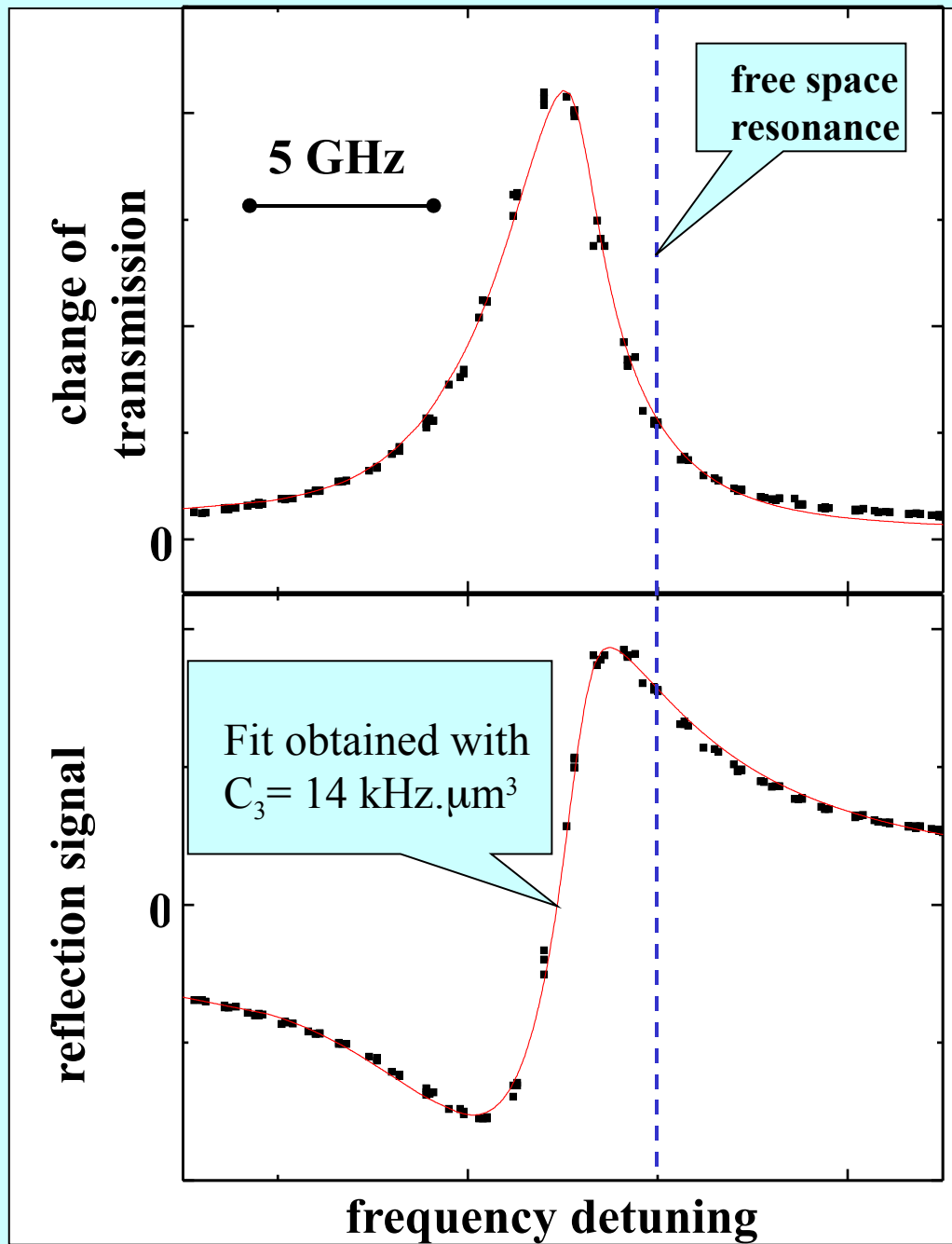
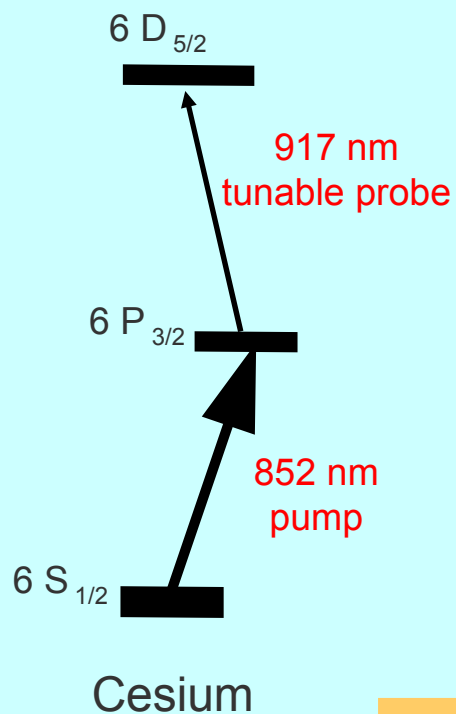
# YAG/Cs thin cell transmission and reflection

*strong red shift*

$L=50$  nm

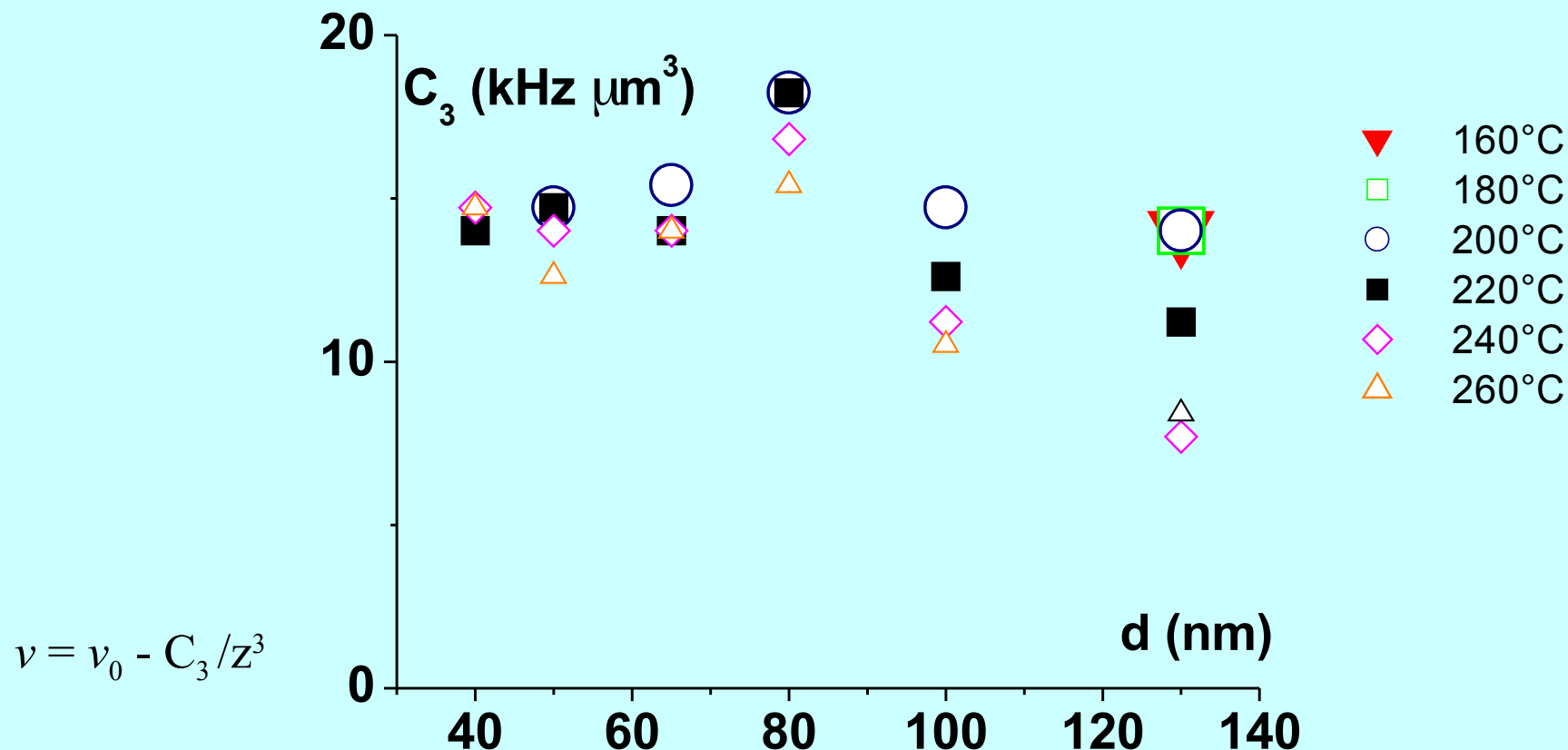
$\lambda=917$  nm

$T=220^\circ\text{C}$ ,



# YAG/Cs cell ; $6P_{3/2}-6D_{5/2}$ experiment

$\lambda = 917 \text{ nm}$



$$\nu = \nu_0 - C_3/z^3$$

$C_3$  is found to be independent of thickness

M. Fichet *et al*, Europhysics Letters **77**, 54001 (2007)

# Long-range atom-surface interactions

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III. Symmetry properties: symmetry break, inelastic vW reflection

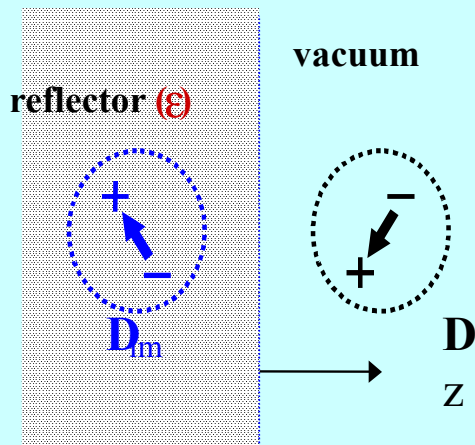
IV. Quantum mechanical features. Conclusion

# ATOM-SURFACE INTERACTION : *dielectric interface*

## The model of Electrostatic images

vW potential : an interaction between **dipole** *and* **dipole-image**

$$H_{vw} = - \frac{\epsilon - 1}{\epsilon + 1} \frac{D^2 + D_z^2}{16 z^3}$$



A summing over virtual dipole transitions  $\omega_{ij}$

$$\langle i | D^2 | i \rangle = \sum_j r(\omega_{ij}) \langle i | D | j \rangle \langle j | D | i \rangle$$

**For  $\epsilon(\omega_{ij})$  complex (i.e. dispersion)**

**How the image coefficient  $r$  behaves ?**

# IMAGE COEFFICIENT for DISPERSIVE DIELECTRICS

How  $(\epsilon-1)/(\epsilon+1)$  is transformed ?

## Virtual absorption

$$\omega_0 \geq 0$$

$|g\rangle$  Mac Lachlan or  
Mavroyanis 1963

$$r(\omega_0) = \frac{2}{\pi} \int_0^\infty \frac{\epsilon(iu) - 1}{\epsilon(iu) + 1} \frac{\omega_0}{\omega_0^2 + u^2} du$$

$$0 \leq r \leq 1$$

## Virtual emission

$$\omega_0 \leq 0$$

*(concerns only  
excited atom)*

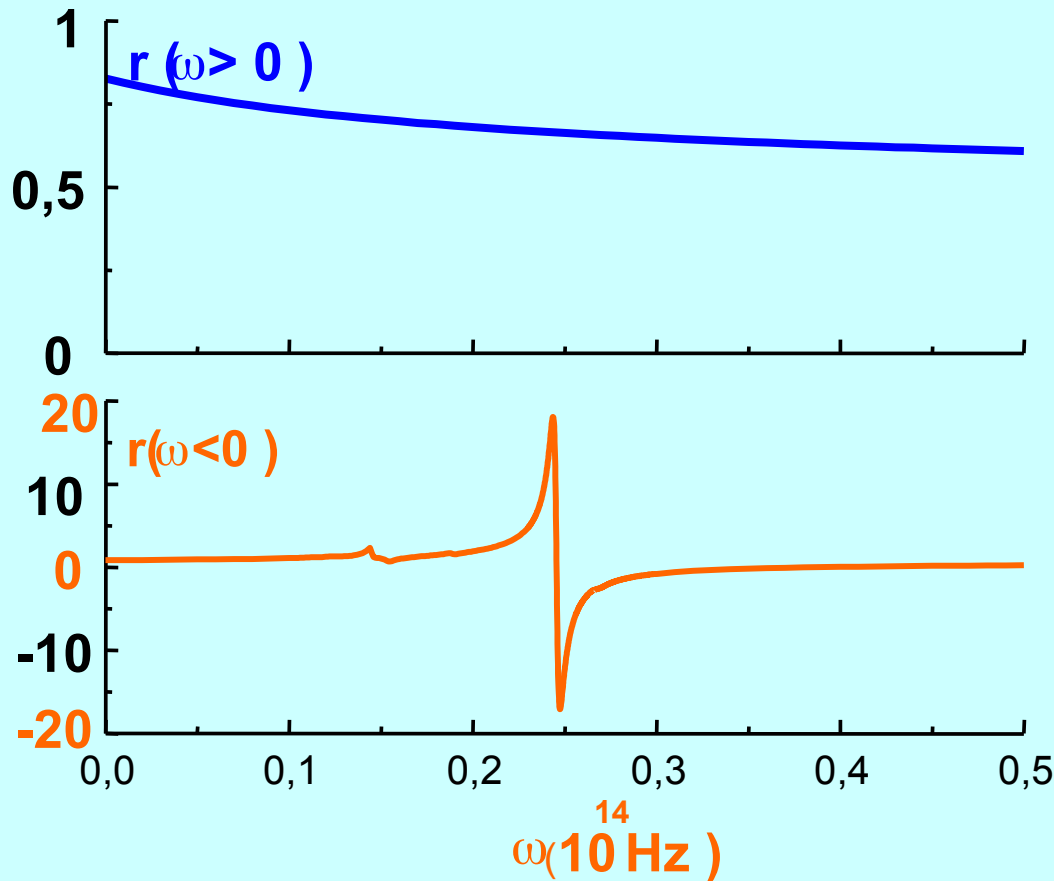
$$r(-|\omega_0|) = -\frac{2}{\pi} \int_0^\infty \frac{\epsilon(iu) - 1}{\epsilon(iu) + 1} \frac{|\omega_0|}{\omega_0^2 + u^2} du + 2 \operatorname{Re} \frac{\epsilon(|\omega_0|) - 1}{\epsilon(|\omega_0|) + 1},$$

$r$  not bounded,  $r \geq 0$  or  $r \leq 0$

pole of  $[\epsilon(\omega)+1]$  → resonant coupling w/ surface mode (polariton)

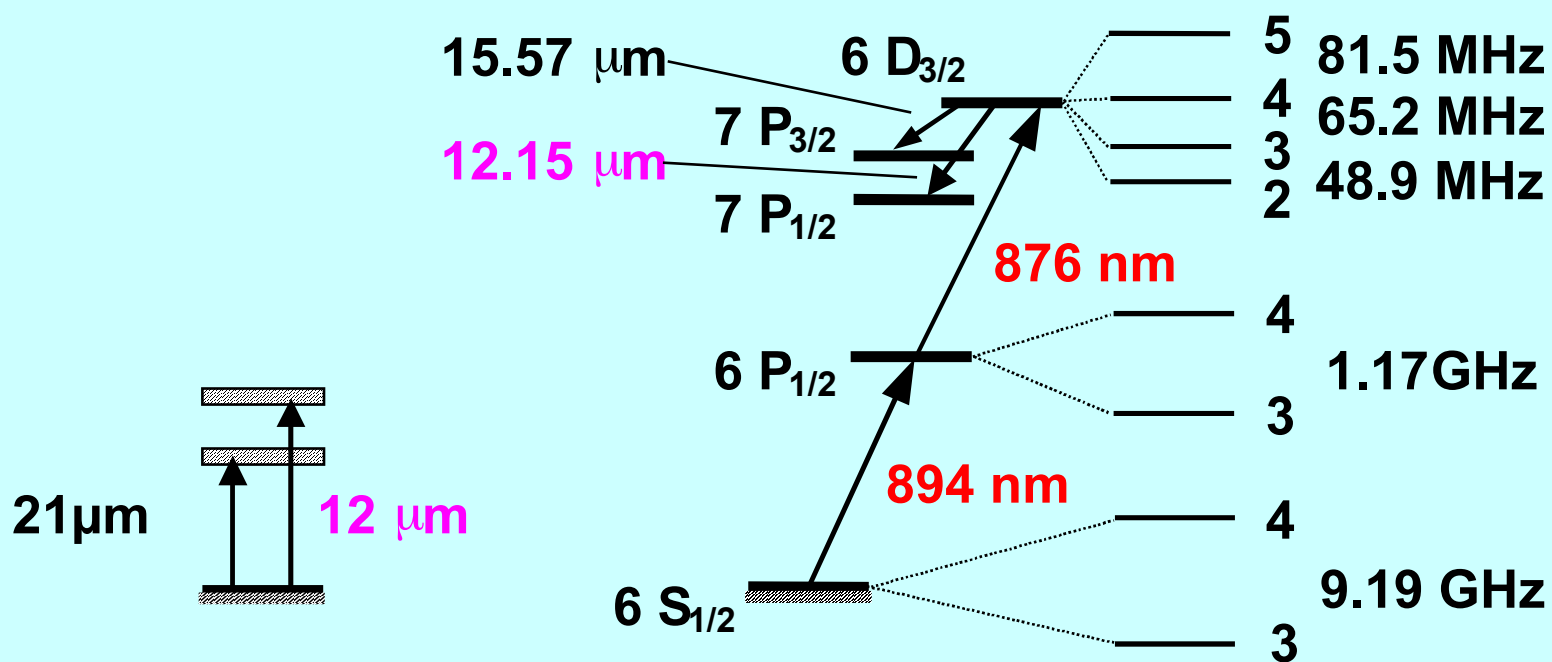
# THE DIELECTRIC IMAGE COEFFICIENT

## The case of **SAPPHIRE**



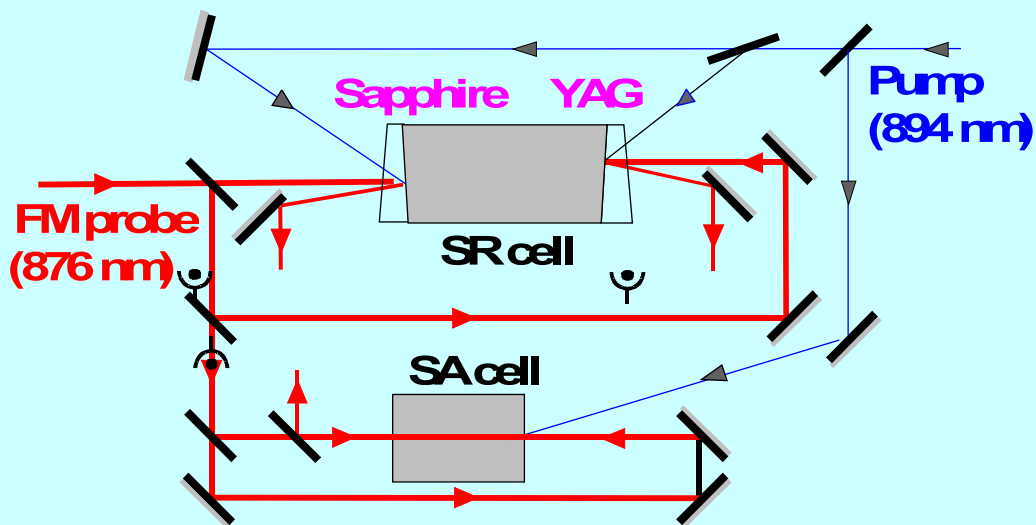
Virtual **ABSORPTION** of the atom (always non resonant)

Virtual **EMISSION** of the atom : resonant **COUPLING** to a **ABSORPTION** in a **SURFACE POLARITON MODE**: enhancement, van der Waals repulsion?

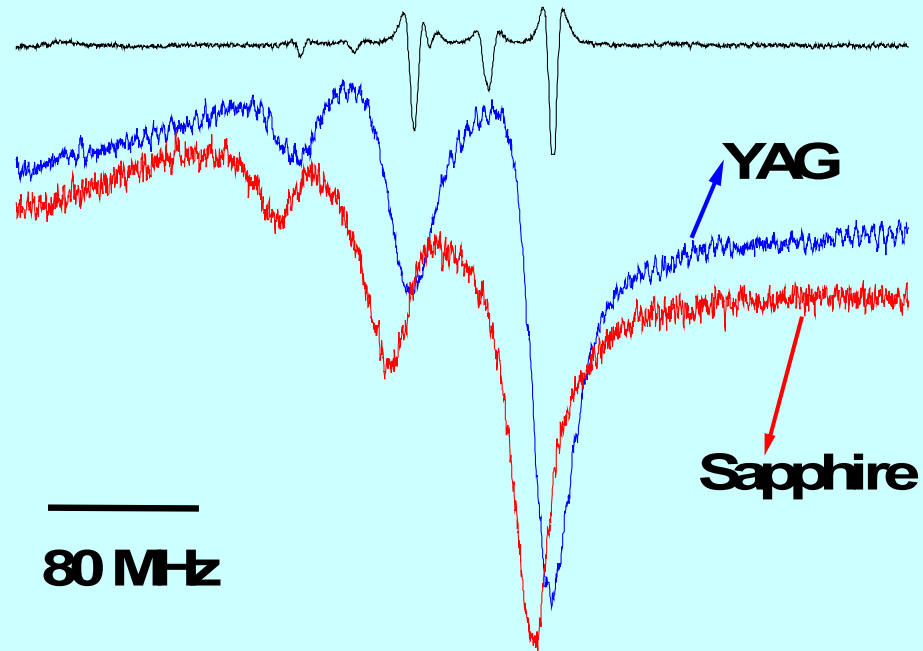


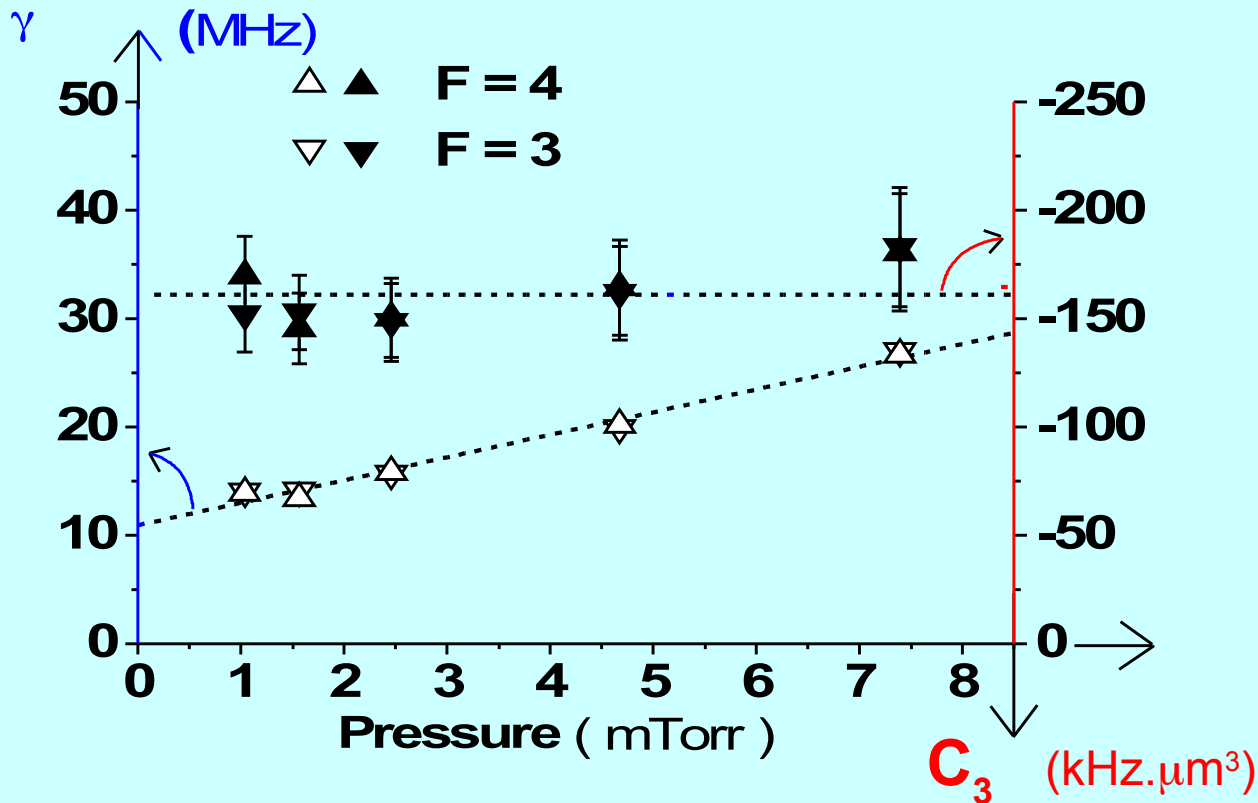
Sapphire surface polaritons

Cs









Cs ( $6D_{3/2}$ ) and sapphire interface

**Evidence of a vW surface repulsion ( $C_3 < 0$ ) consistent with pressure broadening in spite of phenomenological changes in the line-shapes**

Failache et al, PRL, **83**, 5467 (1999)

# van der Waals energy shift at non-zero temperature

$$\delta E_a = - \frac{1}{12Z^3} \sum_n |\langle a | D | n \rangle|^2 (\mathbf{r}_1^{\text{an}} + \mathbf{r}_2^{\text{an}} + \mathbf{r}_3^{\text{an}})$$

$$\mathbf{r}_1(\omega_{na}, T) = -2\text{Re} \frac{\epsilon(\omega_{na}) - 1}{\epsilon(\omega_{na}) + 1} \frac{e^{-\frac{\omega_{na}}{K_B T}}}{1 - e^{-\frac{\omega_{na}}{K_B T}}}$$

**virtual absorption** contribution

(null for **T=0**)

$$\mathbf{r}_2(\omega_{an}, T) = +2\text{Re} \frac{\epsilon(\omega_{an}) - 1}{\epsilon(\omega_{an}) + 1} \frac{1}{1 - e^{-\frac{\omega_{an}}{K_B T}}}$$

**virtual emission** contribution  
increases with T

[stimulated emission  $\sim \langle N \rangle$ ]

$$\mathbf{r}_3(\omega_{na}, T) = + \frac{4k_B T}{\omega_{na}^2} \sum_p \frac{\epsilon(i\xi_p) - 1}{\epsilon(i\xi_p) + 1} \frac{\omega_{na}}{\omega_{na}^2 + \xi_p^2}$$

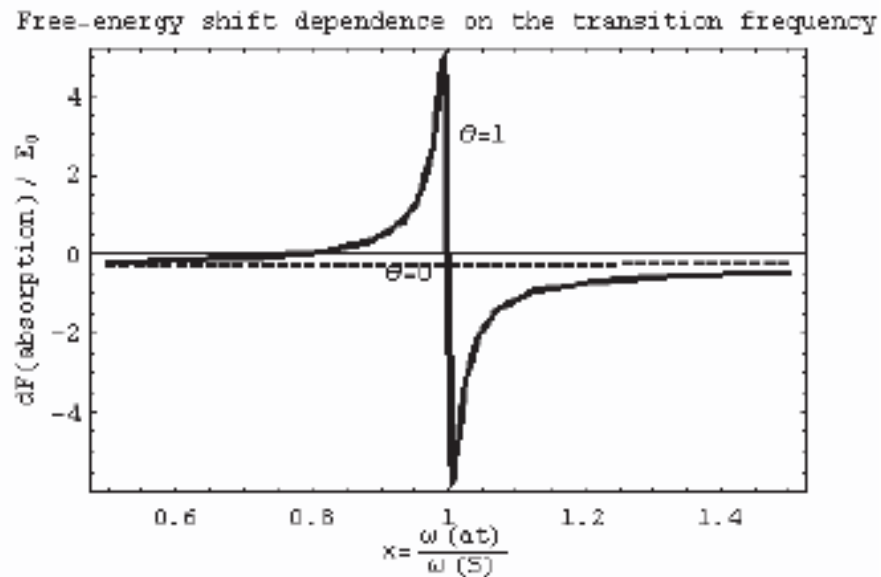
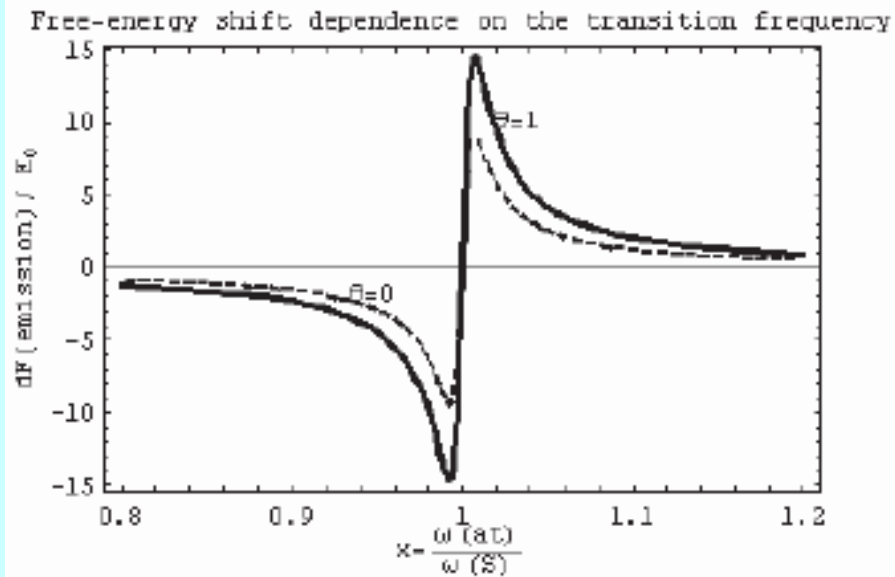
**non-resonant contribution**

(known since Mac Lachlan 1963)

with  $\xi_p = 2\pi k_B T / \hbar$

← **Matsubara frequency**

$$\theta = k_B T / \hbar \omega_S$$



*Influence of surface thermal excitations*

*M-P Gorza & M Ducloy, Eur. Phys. J. D 40, 343 (2006)*

# Long-range atom-surface interactions

## OUTLINE

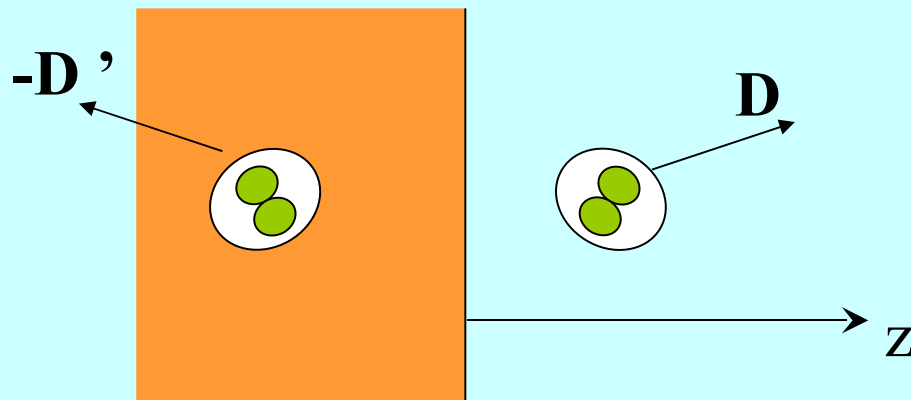
I. Introduction. Distance scaling

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# Non scalar van der Waals potential : a “prism” for atoms



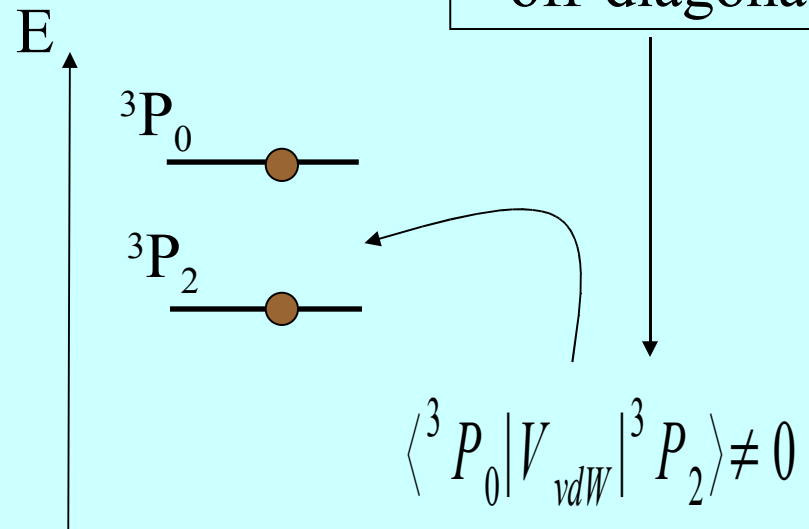
$$V_{vdW} = -\frac{1}{4\pi\epsilon_0} \left[ \frac{(4/3)D^2}{16z^3} + \frac{D_z^2 - D^2/3}{16z^3} \right]$$

Scalar  $T^0_0$

Anisotropic  $T^2_0$   
off-diagonal

Ar\*, Kr\*

2 metastable states,  $^3P_2$  and  $^3P_0$



Boustimi *et al.*, PRL, **86**, 2766 (2001)

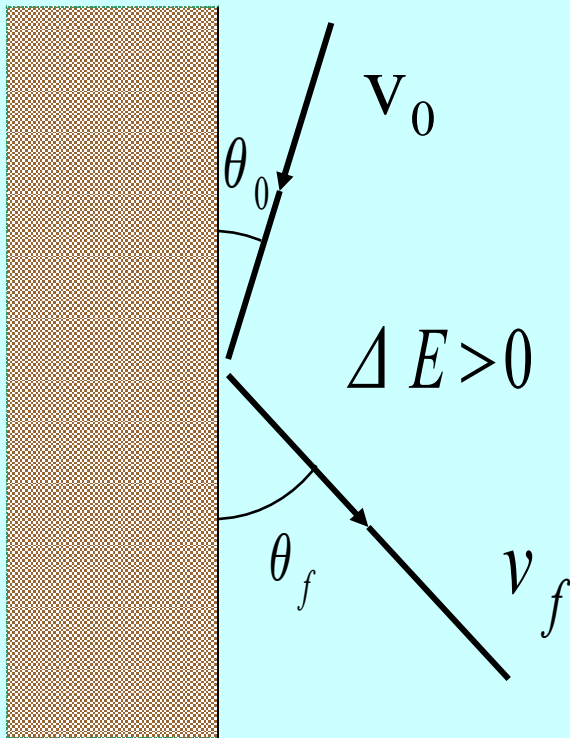
# Kinematics of inelastic transitions

Conservation of total Energy of the atom:

$$v_f = \left[ v_0^2 + \frac{2\Delta E}{m} \right]^{1/2}$$

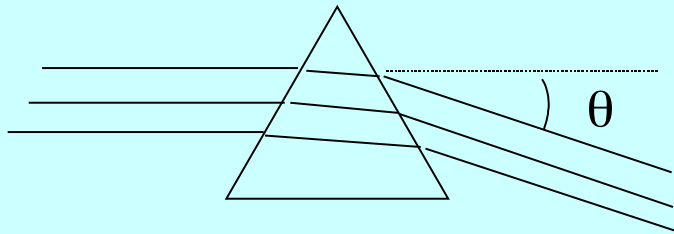
Conservation of the linear momentum  
in the plane // to the surface:

$$v_0 \cos \theta_0 = v_f \cos \theta_f$$

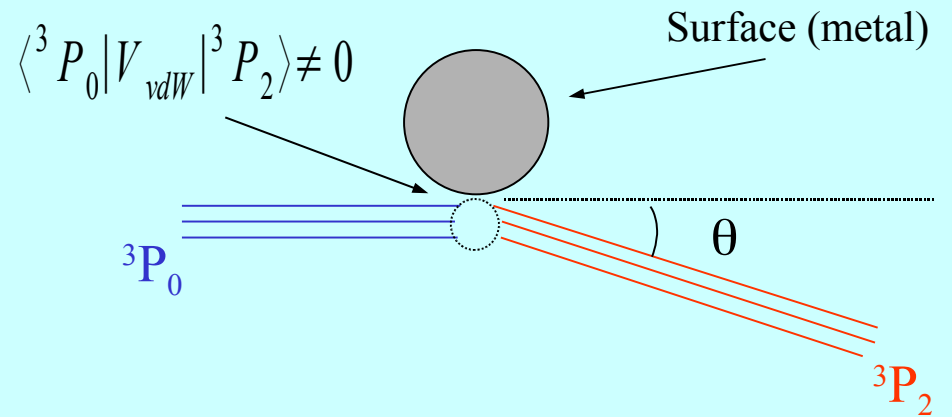


$$\cos \theta_f = \frac{\cos \theta_0}{\sqrt{1 + \frac{\Delta E}{E_0}}}$$

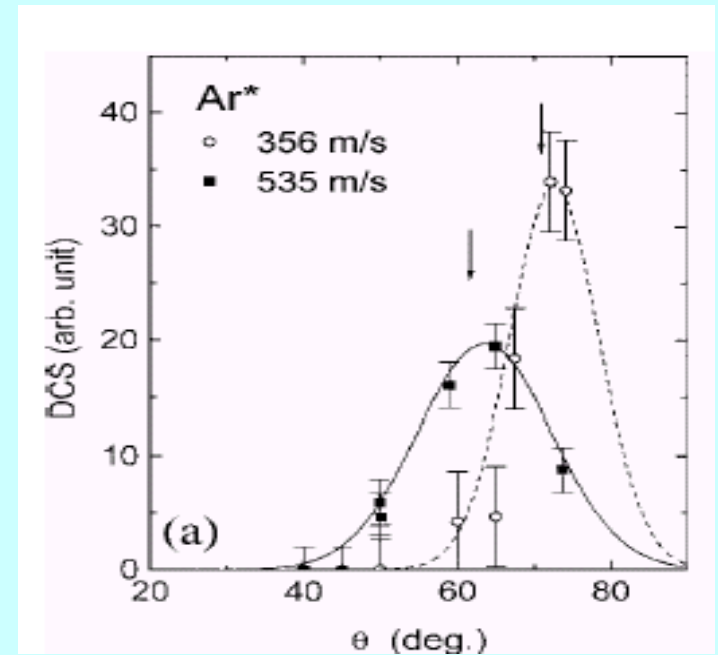
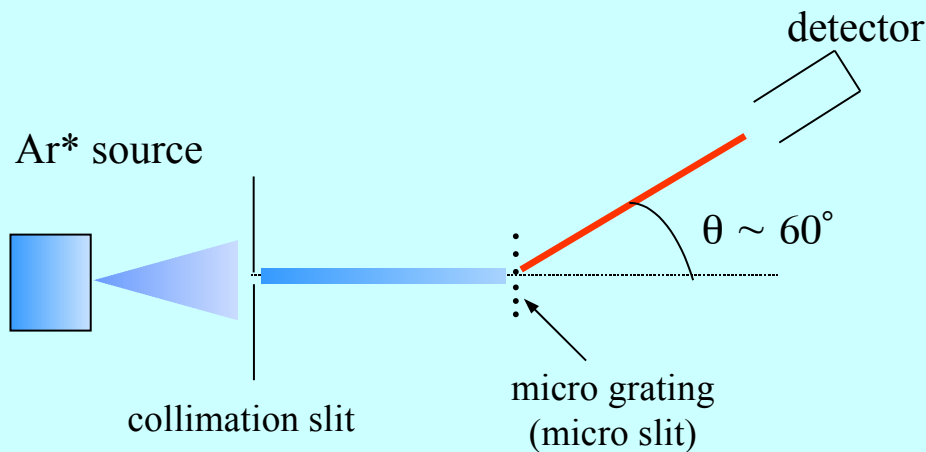
# Light Optics



# Atom Optics



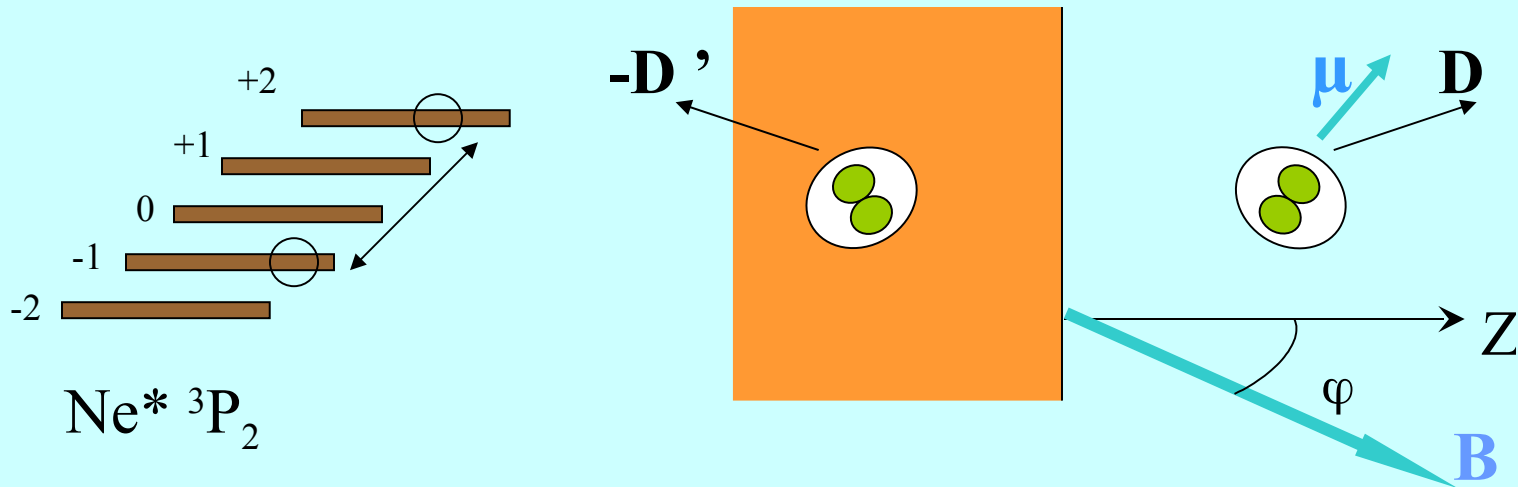
# Experiment



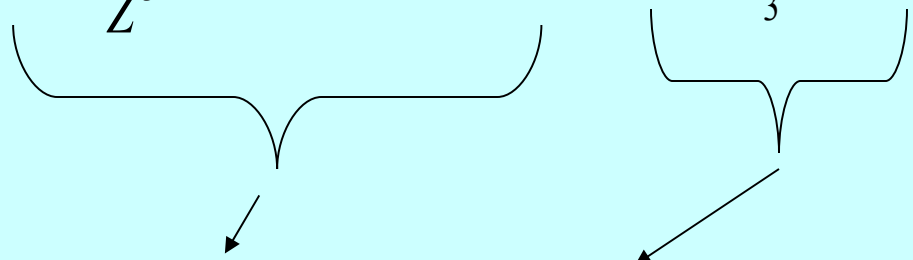
Boustimi *et al.*, PRL, **86**, 2766 (2001)



# van der Waals – Zeeman Transitions



$$V = -\frac{C_3}{Z^3} + g \mu_B B (J \cdot u_B) + \eta \left( J_Z^2 - \frac{1}{3} J^2 \right) / Z^3$$



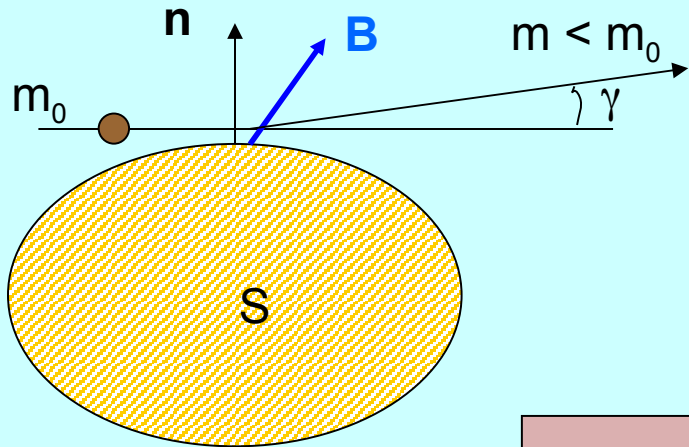
diagonal

quadrupolar

$$\langle ^3P_2, m_i | V | ^3P_2, m_j \rangle \neq 0$$

Karam *et al.*, Europhys. Lett., 74, 36 (2006)

# *van der Waals-Zeeman* transitions



Two quantisation axes :

- scalar + quadrupolar vW interaction (**n**)
- magnetic interaction (**B**)



Transitions among Zeeman sublevels  $m_0 \rightarrow m$

For  $m < m_0$ , repulsive deflection by an angle:

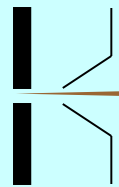
$\gamma \approx (\Delta E / E_0)^{1/2}$ , where  $\Delta E = g\mu_B B |\Delta m|$  (internal energy defect)

$\gamma E_0 =$  incident kinetic energy

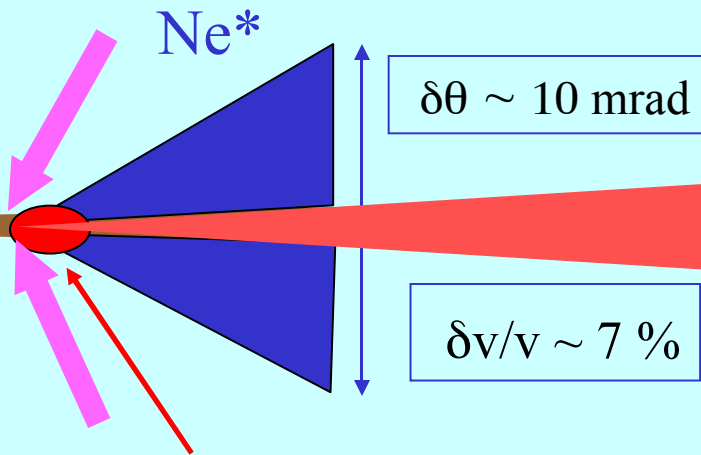
typically:  $\gamma \sim \text{mrad}$   $\longrightarrow$   $\delta\theta$  (beam)  $< \text{mrad}$

# Ultra narrow metastable Ne\* atoms Beam

Supersonic beam Ne  
ground state



*e- GUN*



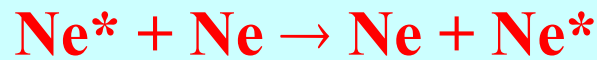
$\delta\theta \sim 10 \text{ mrad}$

$\delta v/v \sim 7 \%$

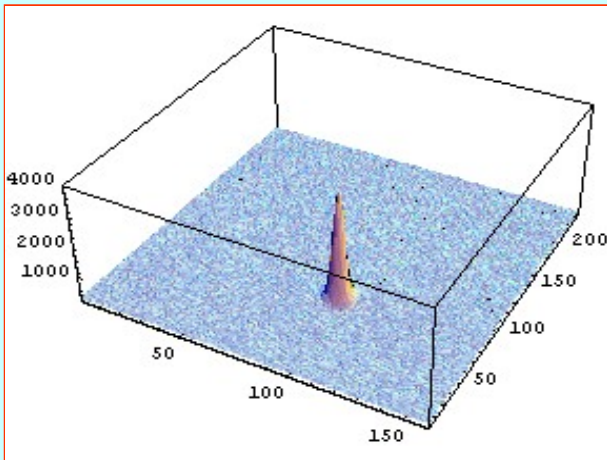
$\delta v/v \sim 1 \%$

$\delta\theta \sim 0.3 \text{ mrad}$

**Metastability Exchange**

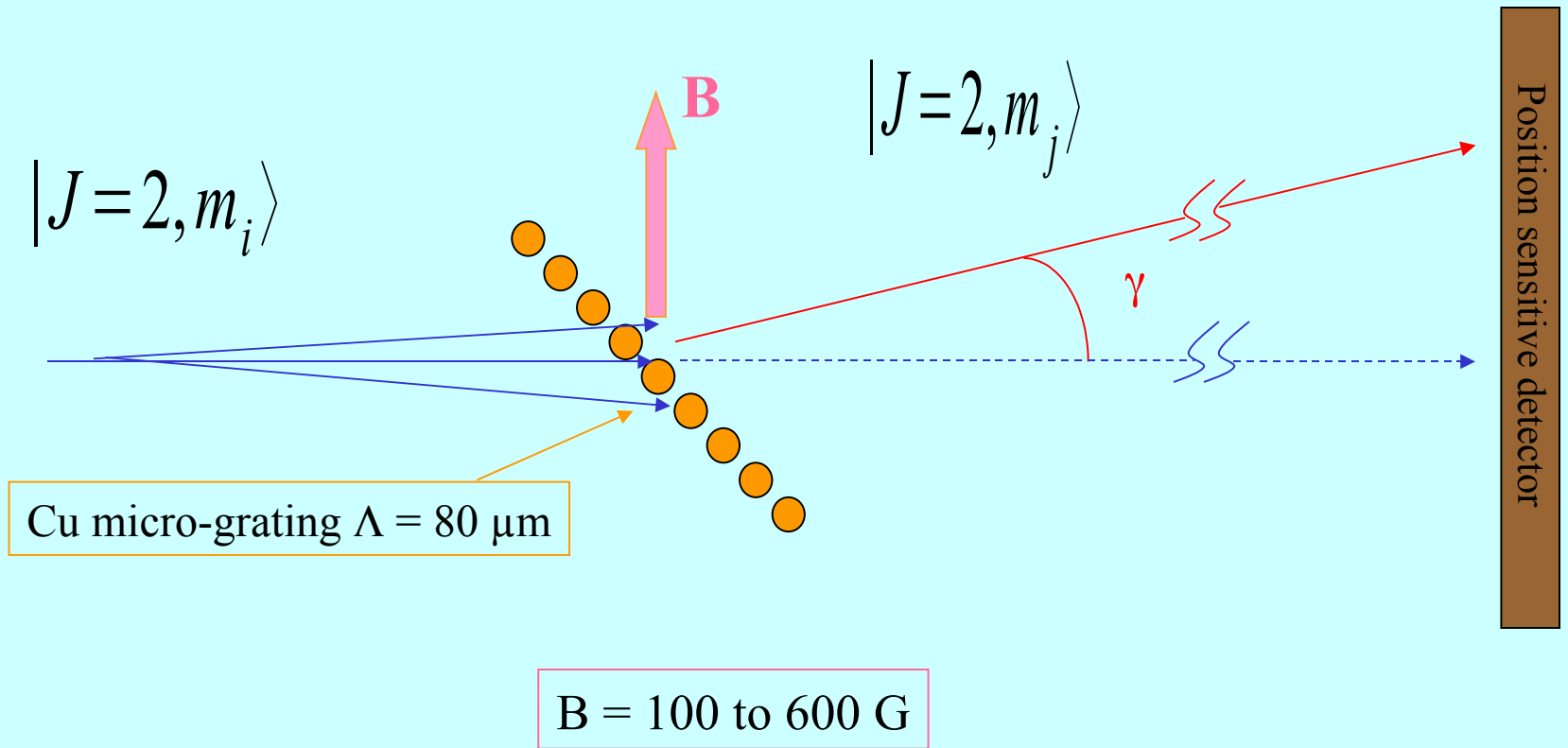


**Ne\***  
**Metastable**  
+  
**Initial beam**  
**qualities**



Karam *et al*, J. Phys. B, 2005

# Experiment



Grating → several slits covered : larger available surface

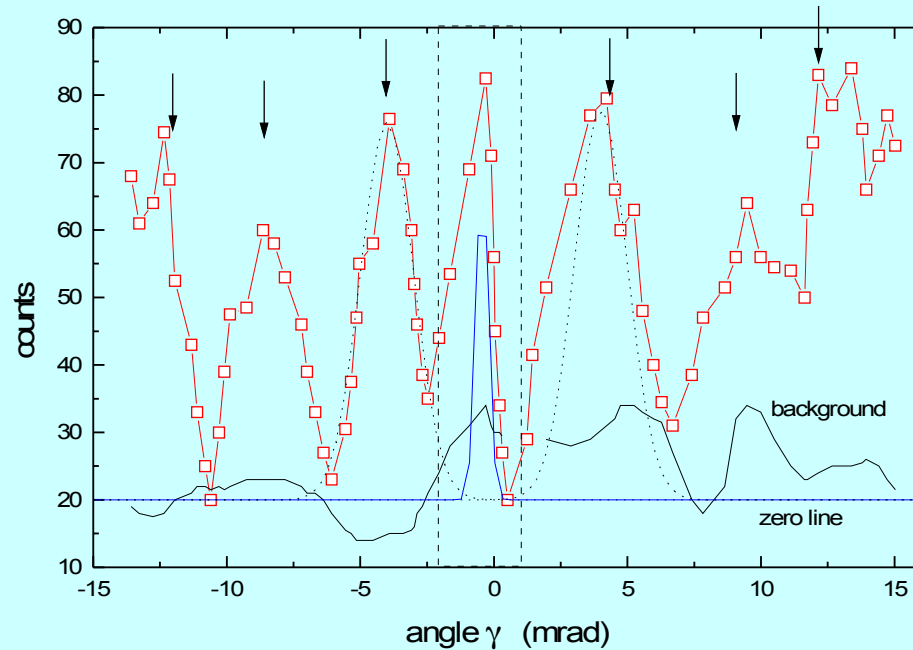
Tilted Grating → Better contrast of scattered signal

# ANGULAR SPECTRA

$B = 289$  Gauss

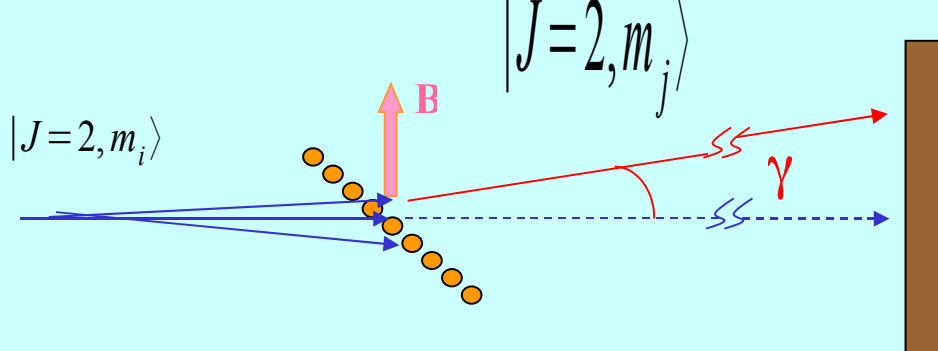
In blue: incident beam profile ( $\delta\theta = 0.35$  mrad)

Peaks are widened by diffraction (dotted line)



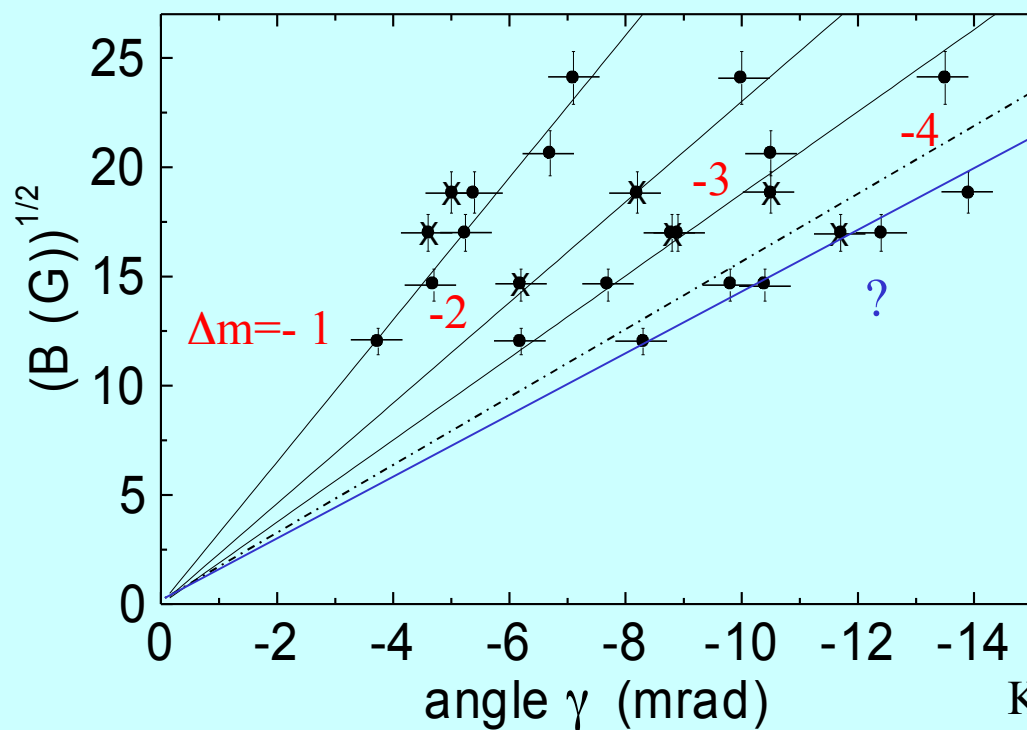
Metastable  $\text{Ne}^*(^3\text{P}_2)$  atoms traverse a micrometric copper grating submitted to a static magnetic field  $B$ . Exo-energetic transitions ( $\Delta m = -1, -2, -3, -4$ ) are identified by the deflection angles  $\gamma$

*This is a multiple & tunable beam splitter*



$$\gamma \approx \sqrt{\frac{\Delta E}{E_0}} = \sqrt{\frac{g\mu_B}{E_0}} \sqrt{B} \sqrt{|\Delta m|} \quad \longrightarrow \quad \sqrt{B} \propto \frac{1}{\sqrt{|\Delta m|}} \gamma$$

**No** adjustable parameter



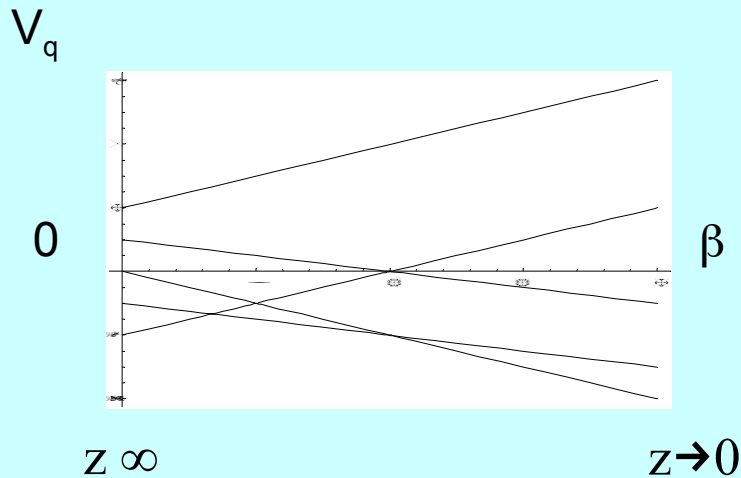
Evidence  
for vdW – Zeeman  
transitions

# Avoided crossings between Zeeman sublevels of Ar (J=2)

$$V = -\frac{C_3}{z^3} + g \mu_B B (J \cdot u_B) + \eta (J_Z^2 - \frac{1}{3} J^2) / z^3$$

**B** strictly normal to the surface ( $\theta=0$ )

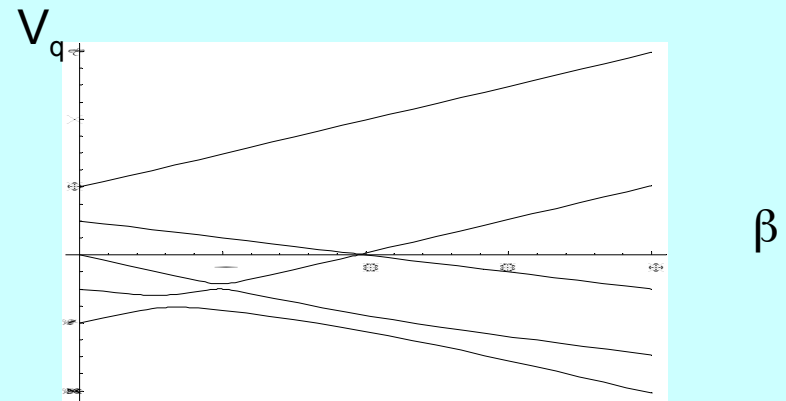
Level crossings for  $\beta=1/3, 1/2, 1$



For  $B=1G$ , the first level crossing appears at  $z \sim 20$  nm

**B** off-normal

Avoided crossings  
 $\theta = (\mathbf{u}_B, \mathbf{u}_S) = 17^\circ$



$$\beta = \frac{-\eta}{g \mu_B B z^3}$$

# Theoretical description of vW-Z transitions

- Large velocity: short interaction time ( $< 0.1$  ns), sudden approximation for the vW potential
- Small velocity: potential energy surfaces with anticrossings explored in the adiabatic regime

Karam *et al.*, Europhysics Letters, **74**, 36 (2006)

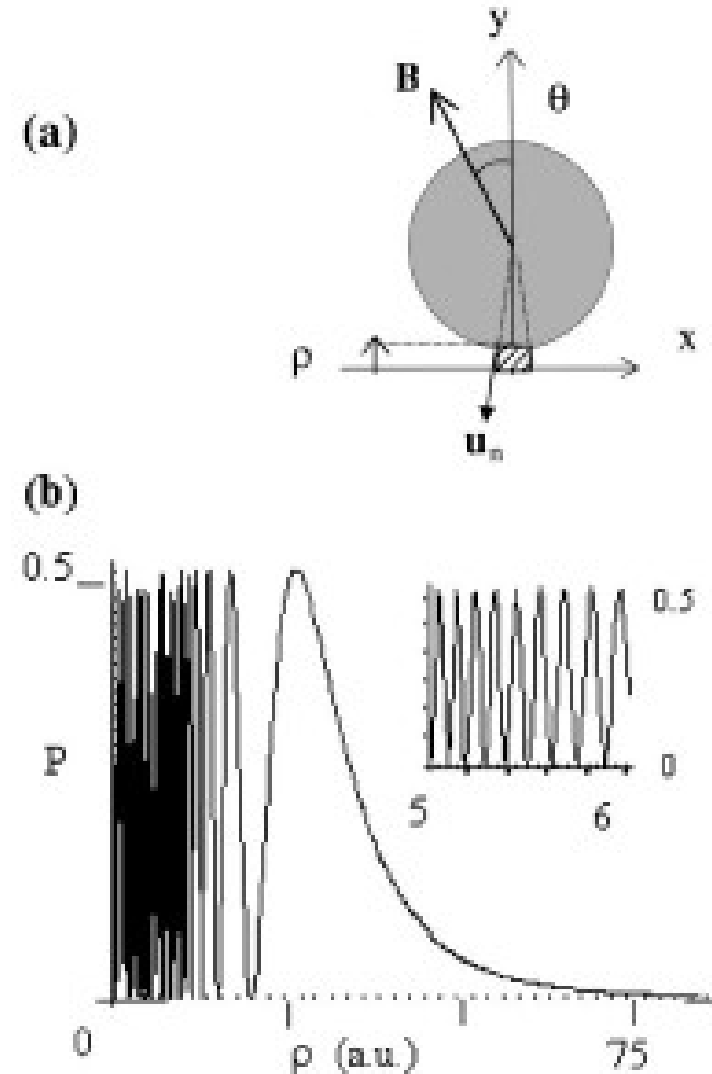


Fig. 4



# Long-range atom-surface interactions

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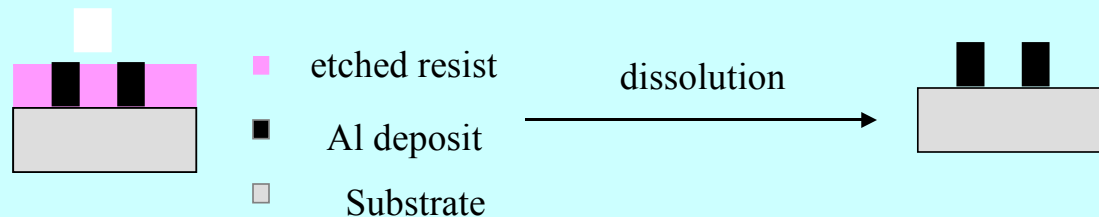
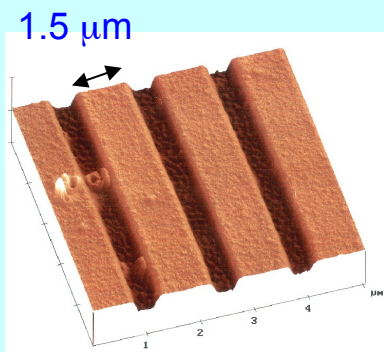
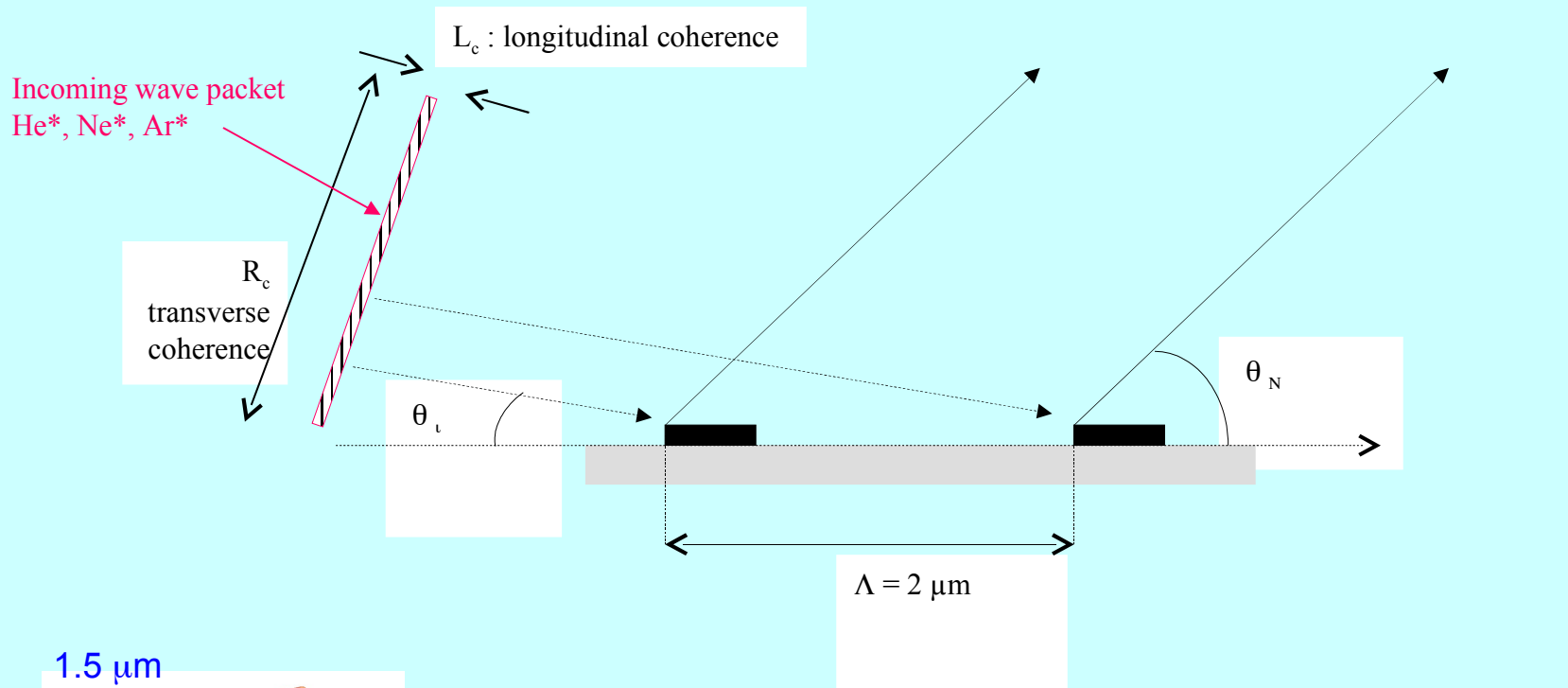
III. Symmetry properties: symmetry break, inelastic vW reflection

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# Diffraction experiment with 1D *reflection* grating

Fast metastable atoms:  $v \sim 1000\text{m/s}$

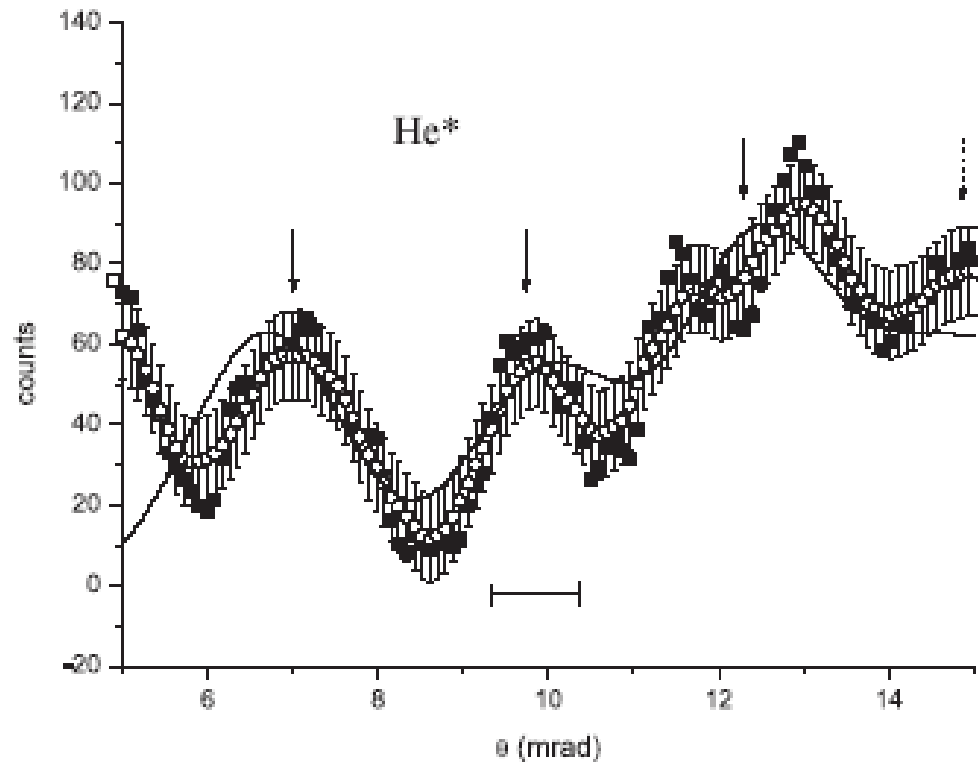
Elastic scattering



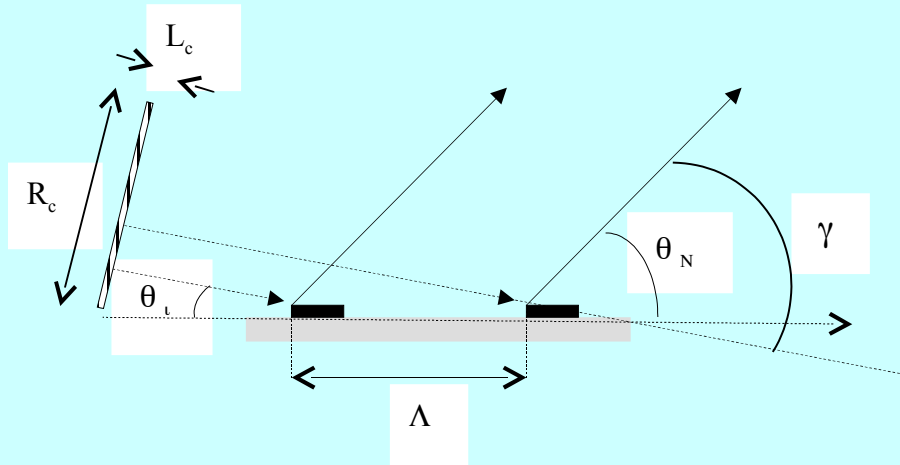
# Difficulties

- High Quenching factor ( $\text{He}^* \rightarrow \text{He}$ )  $\Rightarrow$   $10^{-4}$  of metastable atoms survive
- $\lambda_{\parallel} \sim 10^{-2}$  nm compared to  $\Lambda = 2000$  nm  $\Rightarrow$  Grazing incidence
- Small angles between diffracted peaks,  $\theta_N \sim 10$  mrad  $\Rightarrow$  Good angular definition

J. Grucker et al.: Diffraction of fast metastable atoms by micrometric reflection gratings

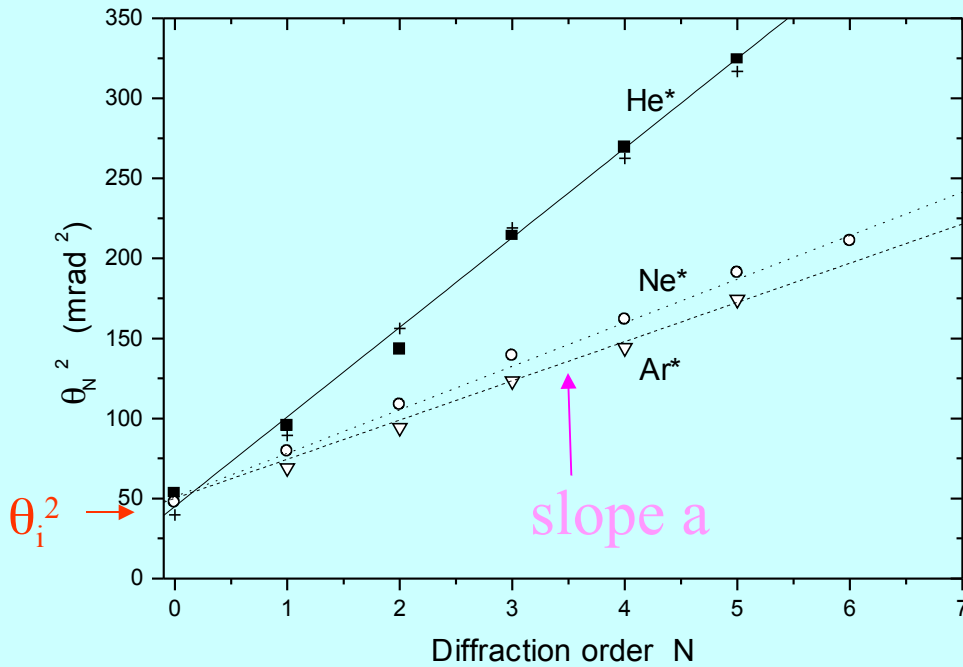


Grucker *et al*, Eur. Phys. J. D, **41**, 467 (2007)



$$\cos \theta_N = \cos \theta_i - N \frac{\lambda_{\parallel}}{\Lambda}$$

$$\theta_N^2 \approx \theta_i^2 + 2 N \frac{\lambda_{\parallel}}{\Lambda}$$



$$\frac{a_{He^{*i}}}{a_{Ne^{*i}}} \approx 2.05 \quad (+/- 0.5)$$

$$\frac{\lambda_{\parallel He^{*i}}}{\lambda_{\parallel Ne^{*i}}} \approx 2.3$$

$$\frac{a_{He^{*i}}}{a_{Ar^{*i}}} \approx 2.5 \quad (+/- 0.5)$$

$$\frac{\lambda_{\parallel He^{*i}}}{\lambda_{\parallel Ar^{*i}}} \approx 3.1$$

# Conclusion

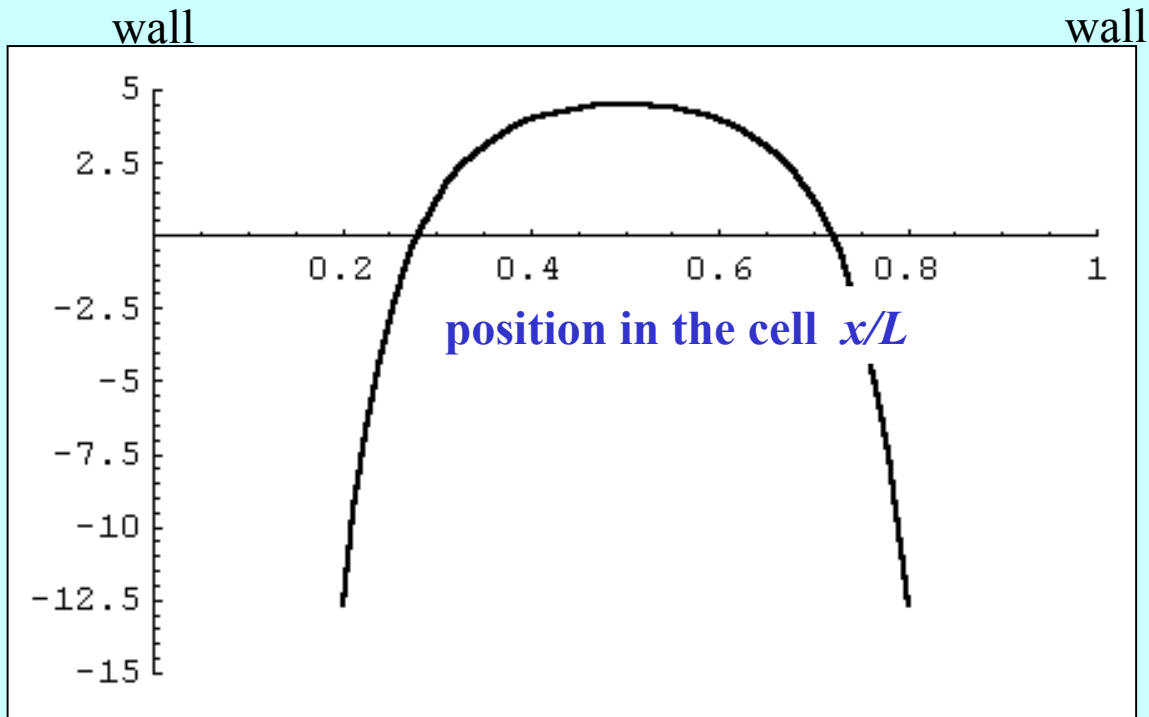
\* New experimental approaches allow one to study the non-retarded long-range ( $\sim 1-100$  nm) interactions between atoms in selected internal state, and dielectric or metallic surfaces, with observations of :

- *resonant atom-surface coupling*
- *atom symmetry break and transitions between internal energy levels*
- *atom diffraction via quantum reflection*

\* Most of the work performed up-to-date is about free atoms interacting with surfaces (continuum states). Observation of long-range atom-surface bound states ( $\neq$  adsorbed atoms) is hindered by overall attractive character of forces, short-range atom perturbations, surface irregularities...

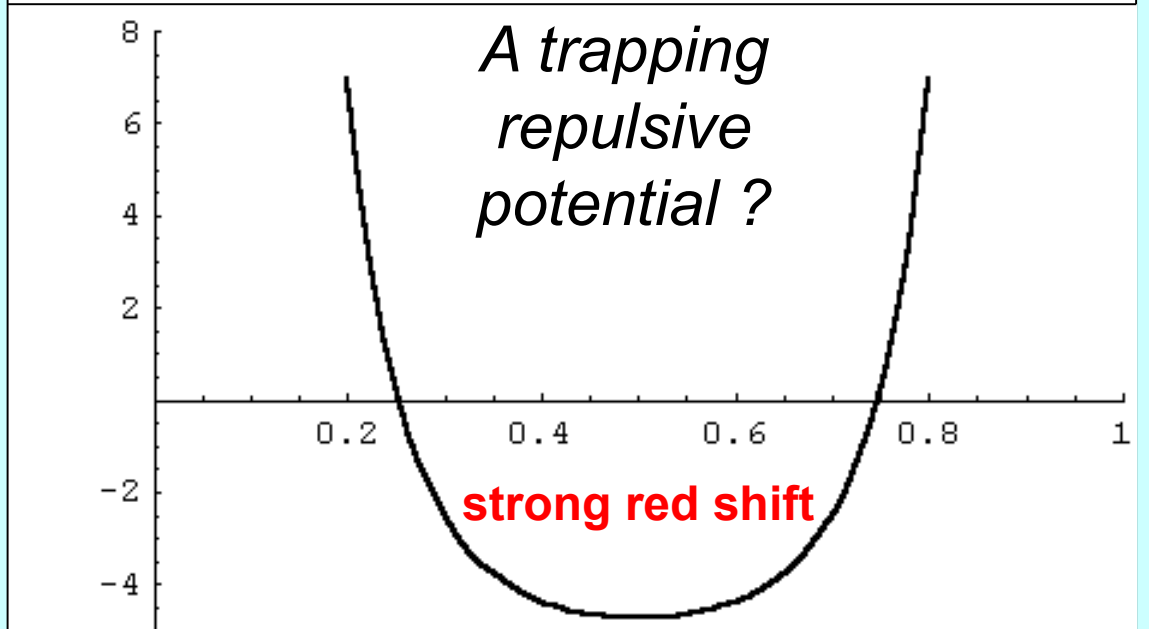
- *Necessity of one additional potential imposed by an applied field (one wall)*
- *Possibility of atom bound state in a thin cell with (resonant) repulsive walls*

**vW shift for**  
 $\omega/\omega_S = 0.999$  for  $\mu_i$



**vW shift for**  
 $\omega/\omega_S = 1.001$  for  $\mu_{||}$

Ultra-thin cells with  
repulsive walls, close to  
resonant coupling



(M.P. Gorza, Laser Physics 2005,  
and unpublished)

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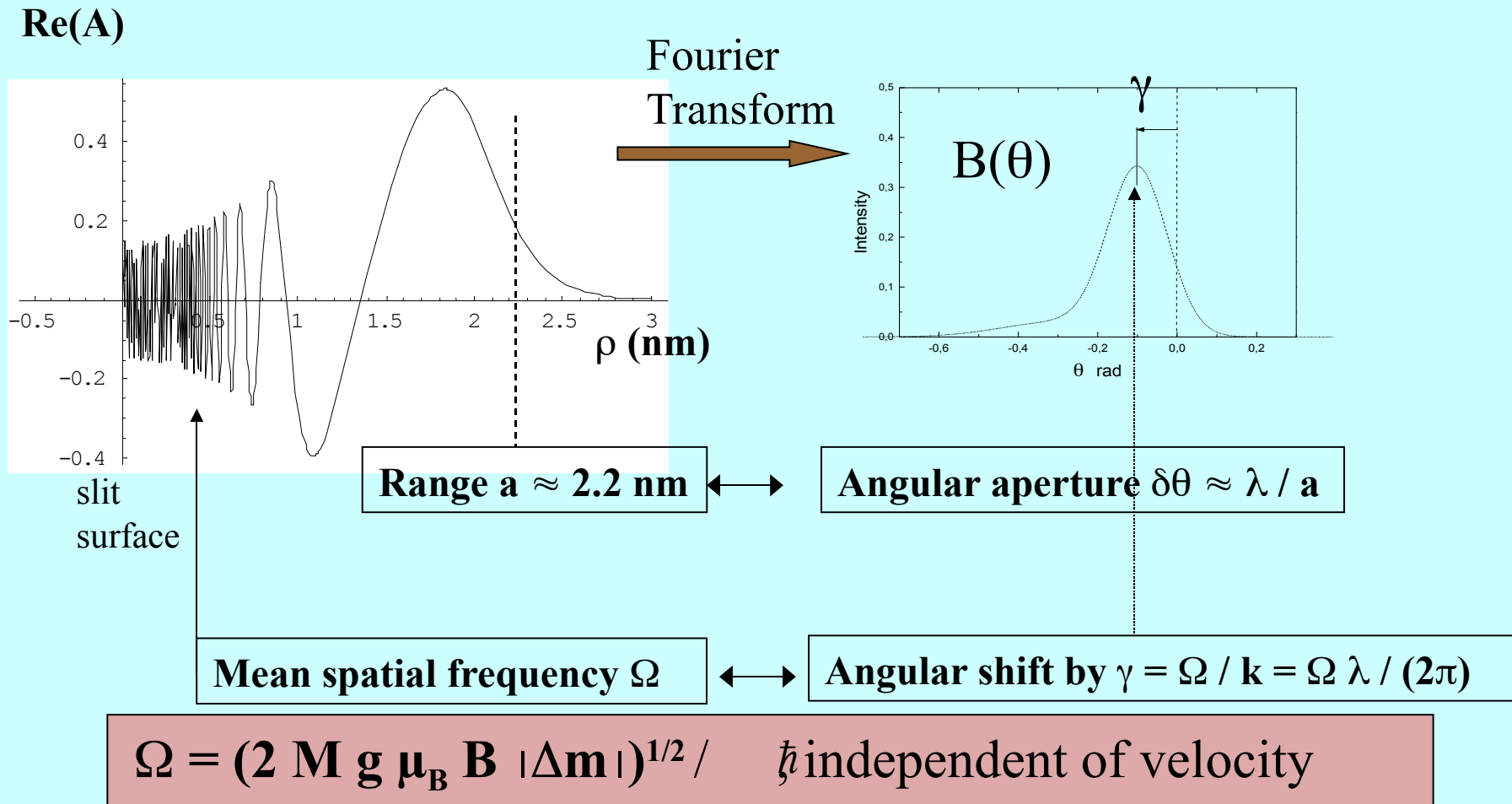
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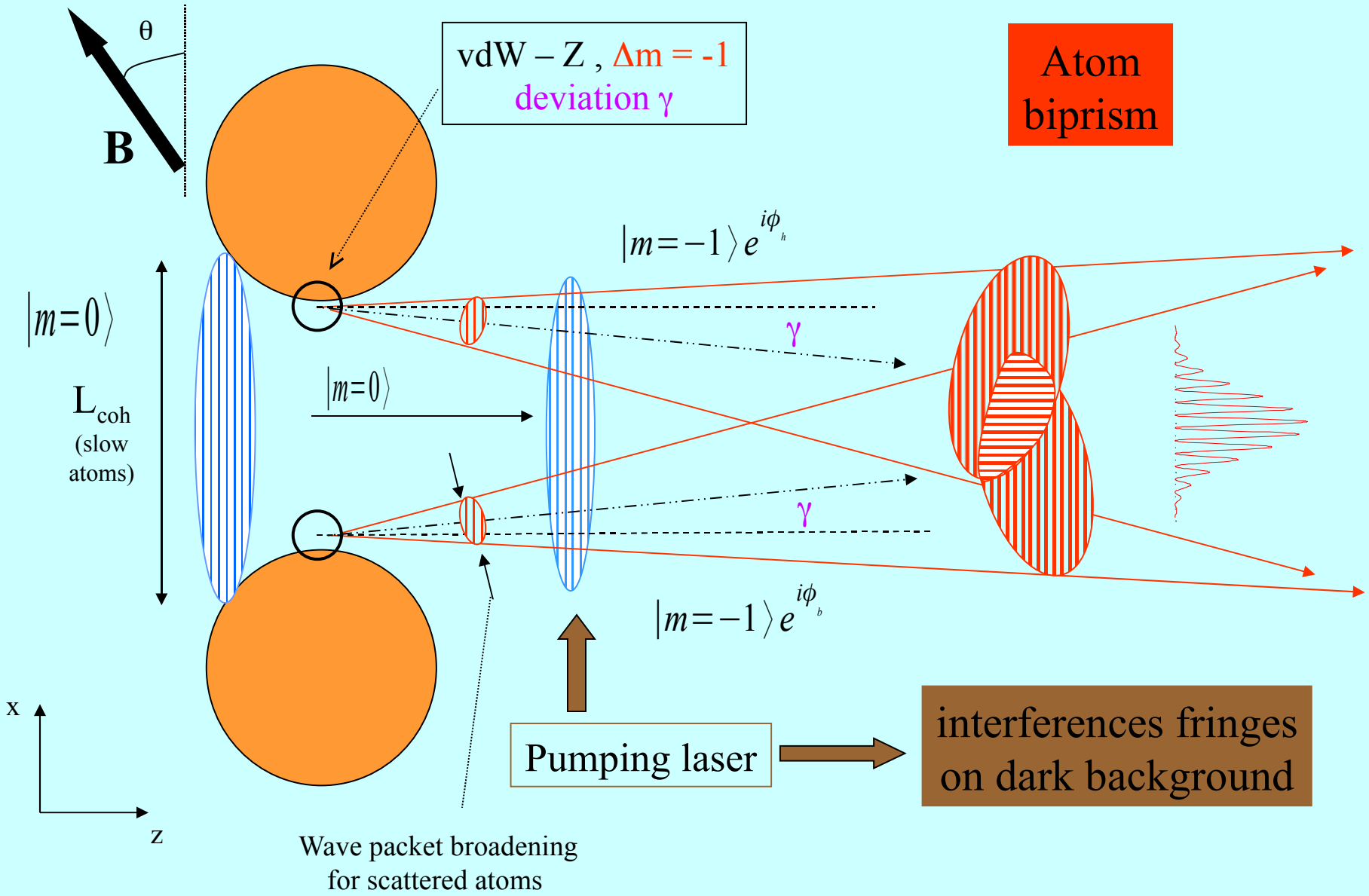


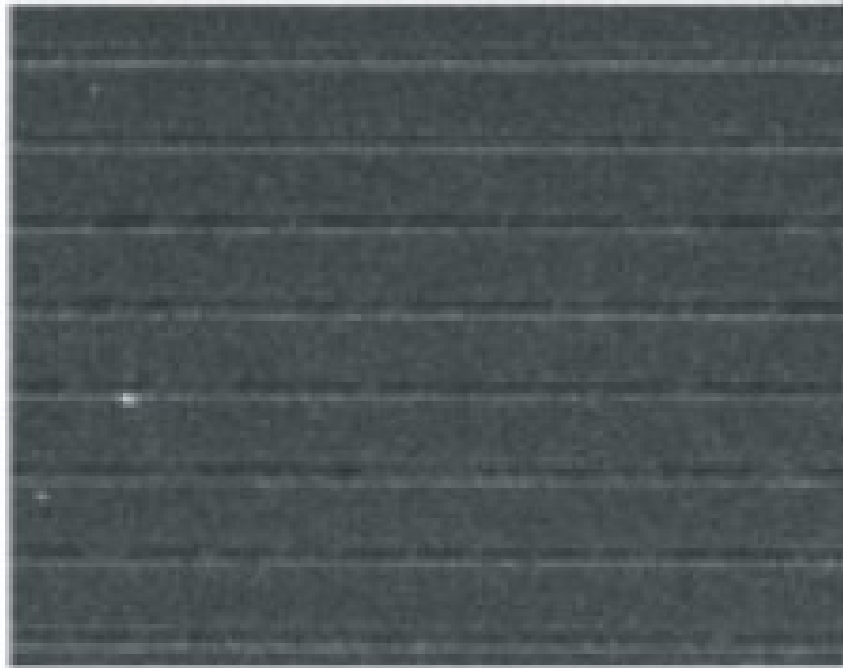
# Fraunhofer diffraction from one inelastic (vdW-Z) complex *transition* amplitude $A(\rho)$



# Principle of Fresnel atomic bi-prism

Grucker *et al*, Eur. Phys. J. D **47**, 427 (2008)





**Fig. 3.** Scanning Electron Micrograph of the magnetic grating G2 (see text) of period  $\Lambda = 1.8 \mu\text{m}$  and width  $w = 1.5 \mu\text{m}$ .

Grucker *et al*, Eur. Phys. J. D, **41**, 467 (2007)