

Discovering (true) tauonium at colliders

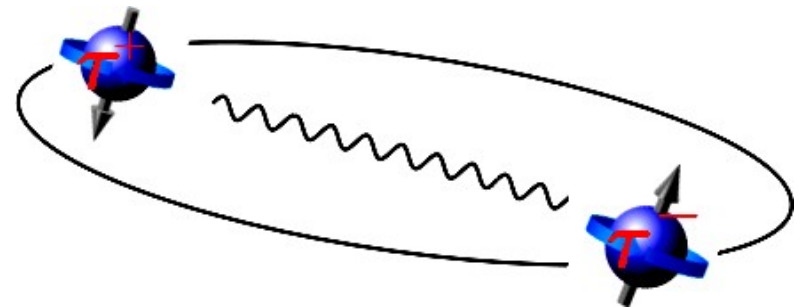


Details: [arXiv:2202.02316](https://arxiv.org/abs/2202.02316) [hep-ph], [2204.07269](https://arxiv.org/abs/2204.07269) [hep-ph], [arXiv:2302.07365](https://arxiv.org/abs/2302.07365) [hep-ph]

Exotic leptonium atoms

- Opposite-charge leptons ($\ell^\pm = e^\pm, \mu^\pm, \tau^\pm$) can form transient “onium” bound states under their QED interaction. Out of 6 possible exotic leptonic atoms (e^+e^-), ($\mu^\pm e^\mp$), ($\mu^+\mu^-$), ($\tau^\pm e^\mp$), ($\tau^\pm\mu^\mp$), ($\tau^+\tau^-$), only the two first (positronium in 1951) and (muonium in 1960) have been observed.

- Para- ($J^{PC} = 0^{-+}$) and ortho- ($J^{PC} = 1^{--}$) leptonium ground states form depending on relative spin orientation of leptons.



- Ditaonium $\tau \equiv (\tau^+\tau^-)$, barely studied, is **smallest & most-bound leptonium** state:

Mass: $m_\tau = 2m_\tau + E_{\text{bind}} = 3553.6962 \pm 0.2400 \text{ MeV}$, $E_{\text{bind}} = -\alpha^2 m_\tau / (4n^2) = -23.7 \text{ keV}$

Bohr radius: $a_0 = 2/(\alpha m_\tau) = 30.4 \text{ fm}$ ($\times 3500$ smaller than positronium)

Rydberg const (γ ionization): $R_\infty = m_\tau \alpha^2 / 4\pi = 3.76 \text{ keV}$ ($\times 3500$ larger than positronium)

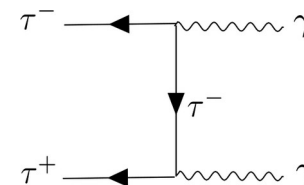
- Compared to other exotic atoms, ditaonium can provide:

- Precision SM: **Most competitive measurement of the tau mass** possible.
- **New tests of QED & CPT** symmetries at much **higher masses** (smaller distances).
- **Sensitivity to any BSM** enhanced by $(m_\ell / \Lambda_{\text{BSM}})^n$, unaffected by hadronic uncertainties.

Ditauonium partial widths & decays

- **Para- τ** decays mostly to $\gamma\gamma$ (BR $\approx 80\%$):

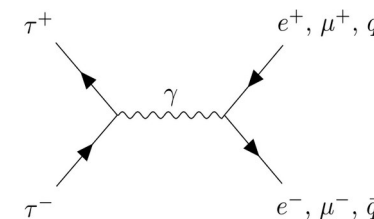
$$\Gamma^{(0)}(n^1S_0 \rightarrow \gamma\gamma) = \frac{\alpha^5 m_\tau}{2n^3} \Big|_{n=1} = 0.018384 \text{ eV}$$



- **Ortho- τ** has many open channels: e^+e^- , $\mu^+\mu^-$, $q\bar{q}$
BR $\approx 20\%$, 20% , 45%

$$\Gamma^{(0)}(n^3S_1 \rightarrow e^+e^-, \mu^+\mu^-) = \frac{\alpha^5 m_\tau}{6n^3}$$

$$\Gamma^{(0)}(n^3S_1 \rightarrow q\bar{q}) = \frac{\alpha^5 m_\tau}{6n^3} R_{\text{had}}(m_{\tau_0}^2) = 2.2 \frac{\alpha^5 m_\tau}{6n^3}$$



- **Weak decay of constituent τ^\pm** : $\Gamma_{(2)\tau \rightarrow X} = 2/\tau = 0.004535 \text{ eV}$ ($\tau \approx 290 \text{ fs}$)
BR_{eff} $\approx 19\%$, 14% for para-,ortho- τ

- **Ditauonium spectroscopy** (NNLO* non-relativ. QED):

→ **Lamb** shifts:

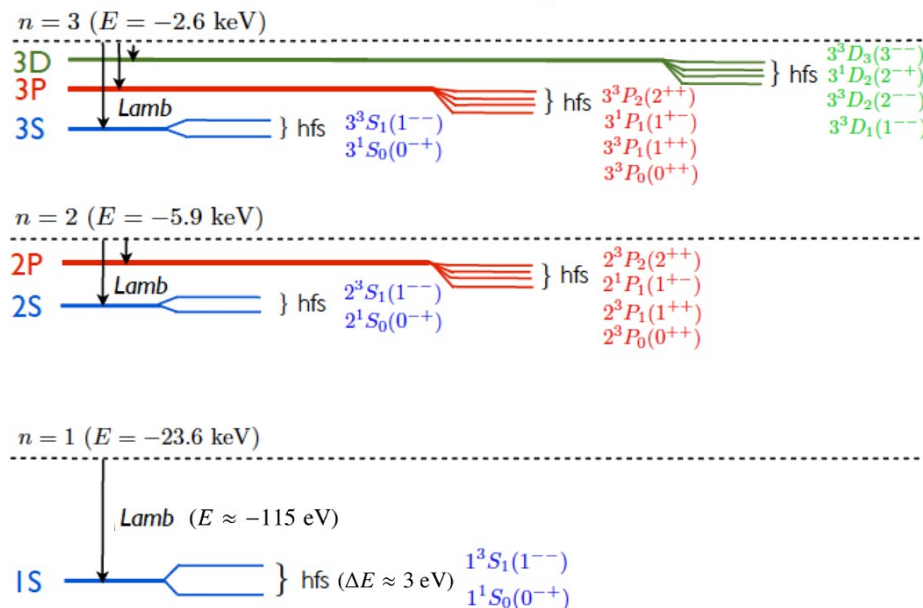
$$\Delta E^{1S,2S,\dots} = -115.4, -14.4, \dots \text{ eV}$$

→ **Hyperfine** splittings:

$$\Delta E_{\text{hfs}}(1^1S_0, 1^3S_1, \dots) = -1.65, +1.29, \dots \text{ eV}$$

[DdE, R.Perez-Ramos, H-S. Shao:
arXiv:2204.07269]

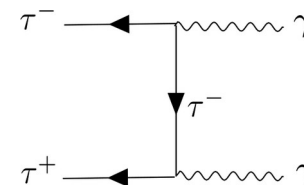
Ditauonium energy levels



Ditauonium partial widths & decays

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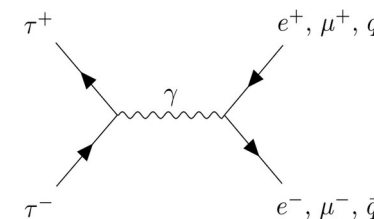
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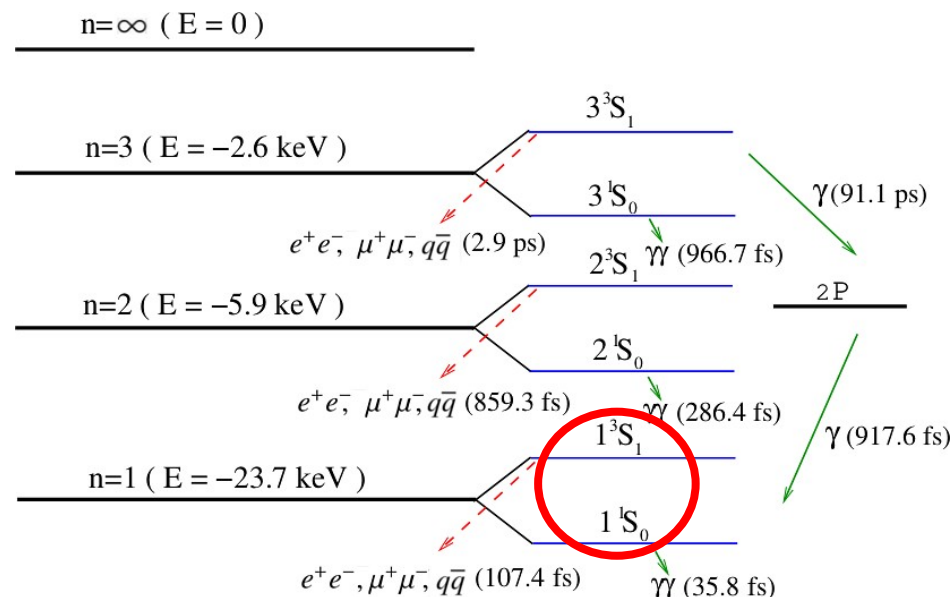
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- **Ditauonium spectroscopy** (NNLO* non-relativ. QED):

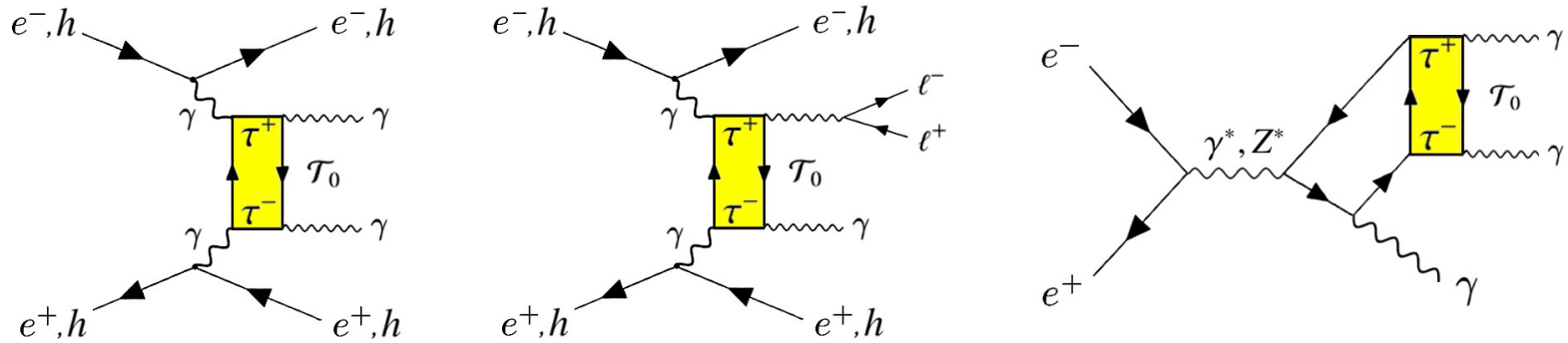
→ Only the **two lowest states** (1^1S_0 & 1^3S_1) have lifetimes shorter ($\tau \approx 27.6, 20.83 \text{ fs}$) than the weak decay of the constituents tau's.



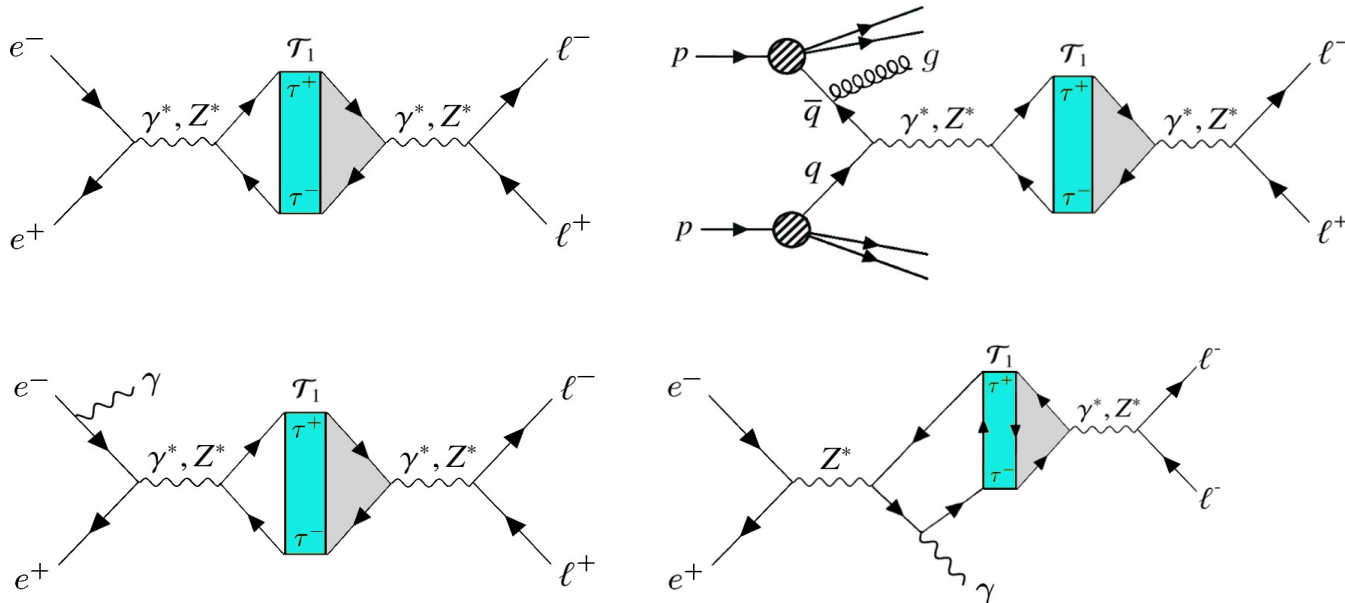
[DdE, R.Perez-Ramos, H-S. Shao: arXiv:2204.07269]

Ditauonium production at e^+e^- & hadron colliders

- 3 para-ditauonium prod./decay channels: photon-photon, s-channel+ γ

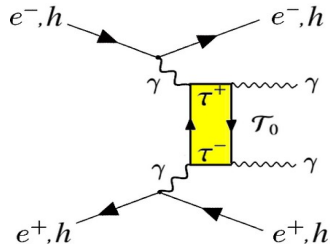


- 4 ortho-ditauonium prod./decay channels: s-channel fusion (w/ & w/o γ)



Para-ditauonium via $\gamma\gamma \rightarrow \tau_0 \rightarrow \gamma\gamma$

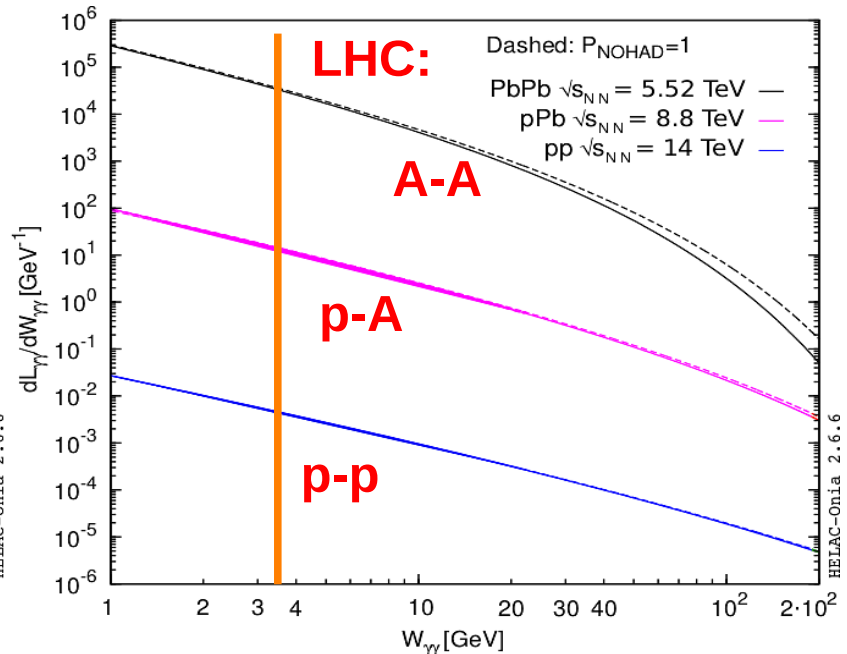
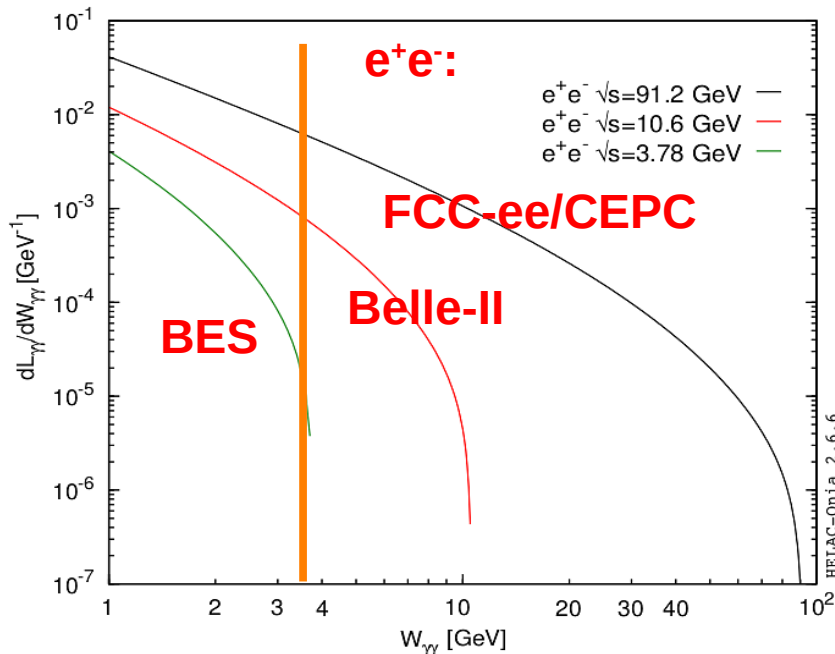
- Cross sections for signal & backgrounds computed in the Weizsäcker-Williams approximation (EPA) for $\gamma\gamma$ collisions via [gamma-UPC 2207.03012 \[hep-ph\]](#)



$$\sigma(ab \rightarrow ab + X) = 4\pi^2(2J + 1) \frac{\Gamma_{\gamma\gamma}(X)}{m_X^2} \left. \frac{d\mathcal{L}_{\gamma\gamma}^{(ab)}}{dW_{\gamma\gamma}} \right|_{W_{\gamma\gamma}=m_X}$$

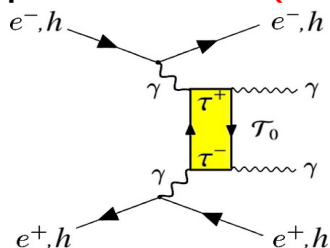
- Photon-photon luminosity for e^+e^- & ultraperipheral p-p, p-A & A-A collisions

$$\frac{d\mathcal{L}_{\gamma\gamma}^{(AB)}}{dW_{\gamma\gamma}} = \frac{2W_{\gamma\gamma}}{s_{NN}} \int \frac{dE_{\gamma_1}}{E_{\gamma_1}} \frac{dE_{\gamma_2}}{E_{\gamma_2}} \delta\left(\frac{W_{\gamma\gamma}^2}{s_{NN}} - \frac{4E_{\gamma_1}E_{\gamma_2}}{s_{NN}}\right) \frac{d^2N_{\gamma_1/Z_1, \gamma_2/Z_2}^{(AB)}}{dE_{\gamma_1}dE_{\gamma_2}}$$



Para-ditauonium via $\gamma\gamma \rightarrow \tau_0 \rightarrow \gamma\gamma$: Backgrounds

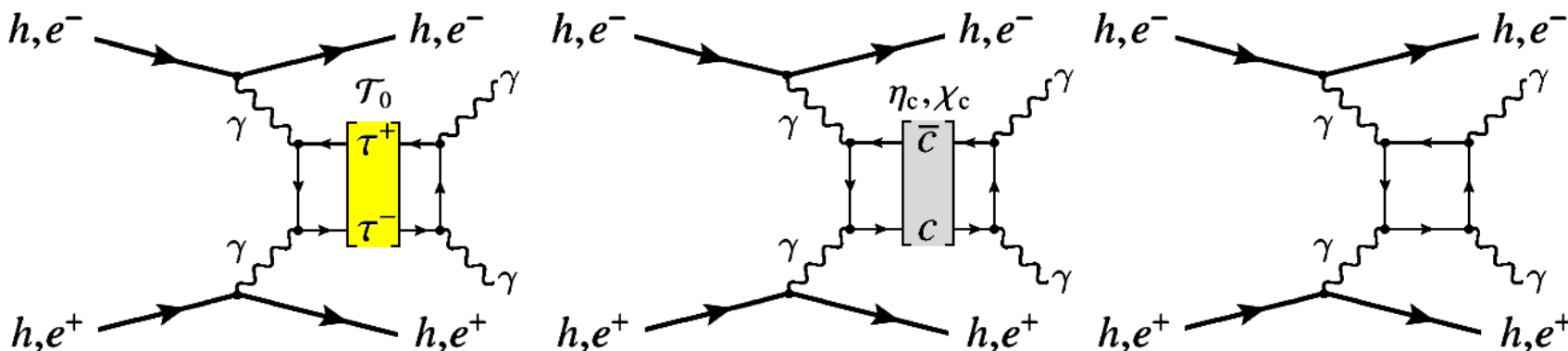
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$$\sigma(ab \rightarrow ab + X) = 4\pi^2(2J + 1) \frac{\Gamma_{\gamma\gamma}(X)}{m_X^2} \left. \frac{d\mathcal{L}_{\gamma\gamma}^{(ab)}}{dW_{\gamma\gamma}} \right|_{W_{\gamma\gamma}=m_X}$$

- **Backgrounds** within $m_{\gamma\gamma} \approx 2.9\text{--}3.7$ GeV:

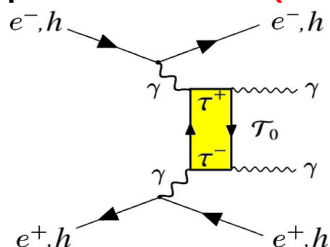
- **C-even charmonium**: 3 $c\bar{c}$: $\eta_c(2S)$, $\chi_{c1,2}$ resonances within ~ 100 MeV of τ_0
- **Light-by-light scattering** (LbL) continuum.



- **Charmonia** resonances have $\mathcal{O}(\text{keV})$ diphoton widths: $\mathcal{O}(10^5)$ larger than para- τ_0 .
But, **diphoton BR** is $\mathcal{O}(10^4)$ larger for para- τ_0 than for c-cbar states.

Para-ditauonium via $\gamma\gamma \rightarrow \tau_0 \rightarrow \gamma\gamma$: Yields

- Cross sections for signal & backgrounds computed in the Weizsäcker-Williams approximation (EPA) for $\gamma\gamma$ collisions via [gamma-UPC 2207.03012 \[hep-ph\]](#)



$$\sigma(ab \rightarrow ab + X) = 4\pi^2(2J + 1) \frac{\Gamma_{\gamma\gamma}(X)}{m_X^2} \left. \frac{d\mathcal{L}_{\gamma\gamma}^{(ab)}}{dW_{\gamma\gamma}} \right|_{W_{\gamma\gamma}=m_X}$$

- Results for e^+e^- and ultraperipheral p-p, p-A & A-A collisions:

Colliding system, c.m. energy, \mathcal{L}_{int} , exp.	$\sigma \times \mathcal{B}_{\gamma\gamma}$					$N \times \mathcal{B}_{\gamma\gamma}$		
	$\eta_c(1S)$	$\eta_c(2S)$	$\chi_{c,0}(1P)$	$\chi_{c,2}(1P)$	LbL	\mathcal{T}_0	\mathcal{T}_0	$\chi_{c,2}(1P)$
e^+e^- at 3.78 GeV, 20 fb ⁻¹ , BES III	120 fb	3.6 ab	15 ab	13 ab	30 ab	0.25 ab	–	–
e^+e^- at 10.6 GeV, 50 ab ⁻¹ , Belle II	1.7 fb	0.35 fb	0.52 fb	0.77 fb	1.7 fb	0.015 fb	750	38 500
e^+e^- at 91.2 GeV, 50 ab ⁻¹ , FCC-ee	11 fb	2.8 fb	3.9 fb	6.0 fb	12 fb	0.11 fb	5 600	$3 \cdot 10^5$
p-p at 14 TeV, 300 fb ⁻¹ , LHC	7.9 fb	2.0 fb	2.8 fb	4.3 fb	6.3 fb	0.08 fb	24	1290
p-Pb at 8.8 TeV, 0.6 pb ⁻¹ , LHC	25 pb	6.3 pb	8.7 pb	13 pb	21 pb	0.25 pb	0.15	8
Pb-Pb at 5.5 TeV, 2 nb ⁻¹ , LHC	61 nb	15 nb	21 nb	31 nb	62 nb	0.59 nb	1.2	62

→ Relative prod. x-sections: $\eta_c(1S):\chi_{c,2}(1P):\chi_{c,0}(1P):\eta_c(2S):\tau_0 \approx 100:50:30:25:1$

→ Para- τ_0 x-sections increase with \sqrt{s} and Z^4 :

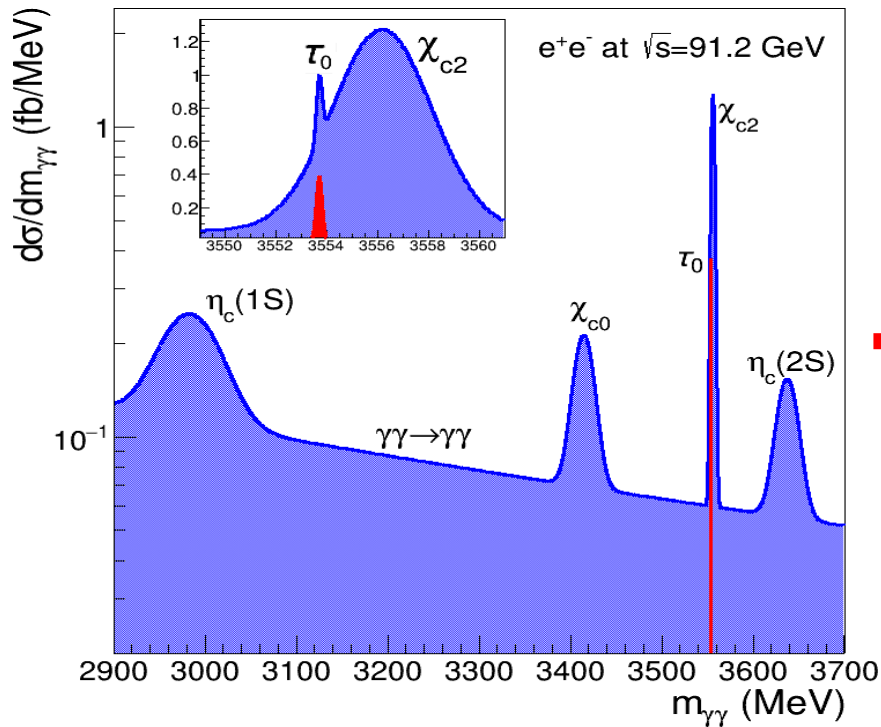
Largest x-sections (0.6 nb) in PbPb UPC (but handful of evts expected at LHC)

Largest yields: 750, 5600 counts at Belle-II, FCC-ee thanks to $\mathcal{L}_{\text{int}} = 50 \text{ ab}^{-1}$.

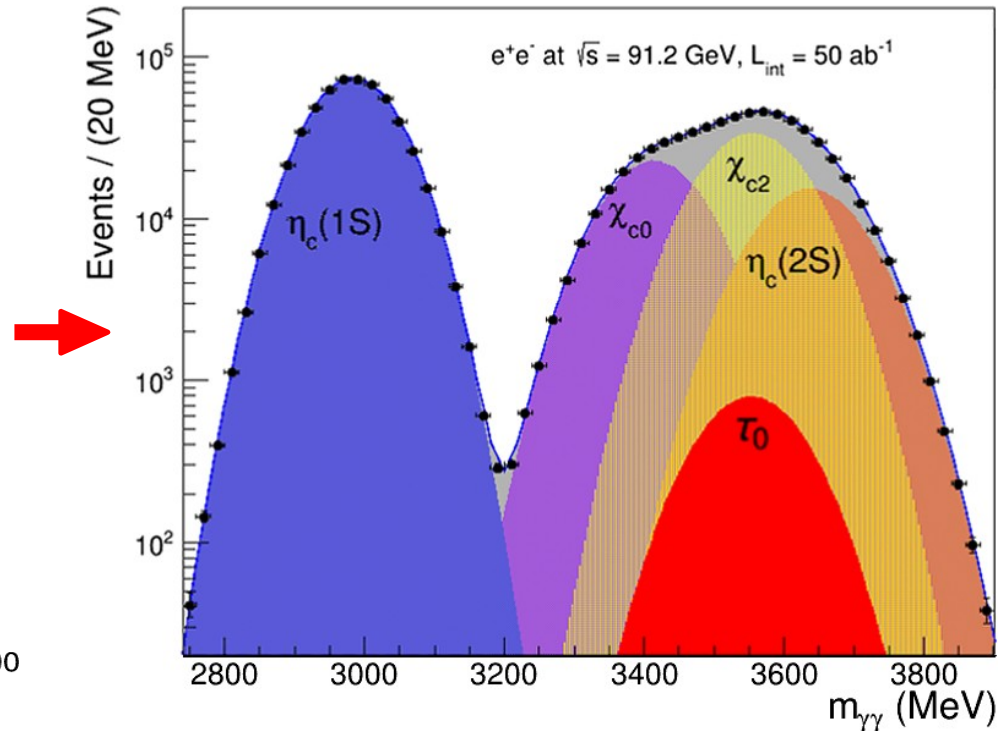
Para-ditauonium via $\gamma\gamma \rightarrow \tau_0 \rightarrow \gamma\gamma$ (Belle II/FCC-ee)

- Trigger: Require **two exclusive 1.5–2 GeV photons back-to-back** with $m_{\gamma\gamma} \approx m_{\tau_0}$
- Reco. performances (Belle-II type: high-reso low-energy crystal ECAL):
Acceptance: $10^\circ < \theta_\gamma < 170^\circ$. Mass resolution: $\sim 2\%$. Photon reco effic. $\sim 100\%$.
- All diphoton resonances **Gaussian-smeared with ~ 70 MeV widths**:

Generator-level x-sections (0.1-MeV τ_0 width)



Reconstructed yields (LbL subtracted)



- Ditauonium signal swamped by **overlapping $\chi_{c2}(1P)$ & neighboring $\chi_{c0}(1P)$, $\eta_c(2S)$**

Para-ditauonium via $\gamma\gamma \rightarrow \tau_0 \rightarrow \gamma\gamma$ (Belle II/FCC-ee)

- 1-million events generated for signal & backgrounds. Run **MVA (BDT) with 12 different single- γ and γ -pair kinematic variables** for signal/backgds separation:
 - (i) Strong **discrimination power (factor of ~ 20)** of LbL continuum from signal.
 - (ii) No discrimination achieved for overlapping charmonia (decay- γ **angular modulation of tensor χ_{c2} different than scalar τ_0 signal, but $\times 50$ suppressed yields**).

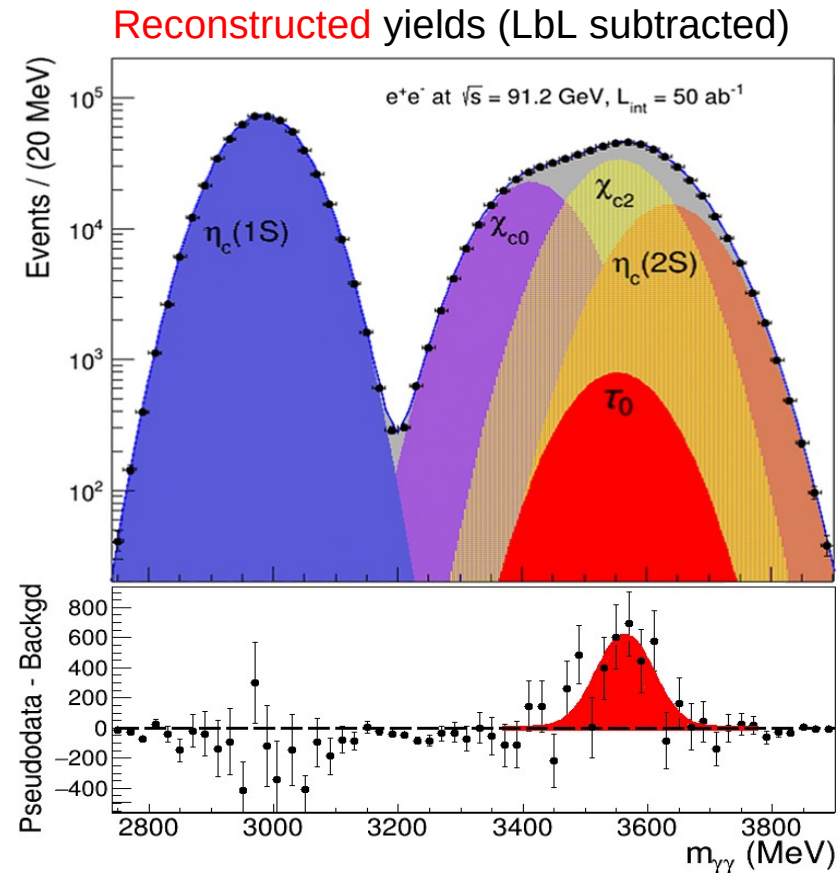
- Signal extracted through **multi-Gaussian $m_{\gamma\gamma}$ fit**.

- Statistical significance derived from **profile-likelihood of fits assuming signal presence or backgd-only**, with 0.3% background syst. uncertainty:

Significance (Belle-II) $\approx 3\sigma$

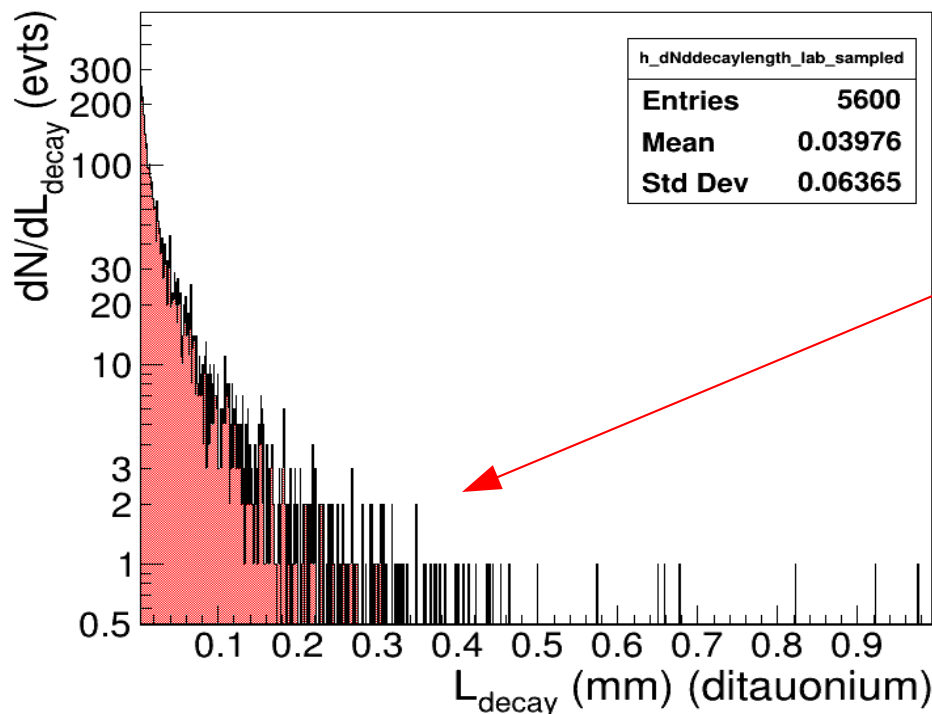
Significance (FCC-ee) $\approx 5\sigma$

- Pseudodata–null-hypothesis **fit residuals**:



Para-ditauonium via $\gamma\gamma \rightarrow \tau_0$ Dalitz decays?

- Whereas **background $c\bar{c}$ resonances decay directly from the IP**, the **para- τ_0** has a lifetime of $\tau \approx 28$ fs, i.e. a **decay-length $c\tau \approx 8$ μm** .



→ For $\beta\gamma \approx 3$: $\langle L_{\text{vtx}} \rangle \approx 25$ μm
 tail of events up to ~ 1 -mm.
 Any single event would be an **unambiguous τ_0 observation!**

→ However, diphoton **vertex pointing capabilities are much coarser**: 1-cm range for LHC-type EM calos.

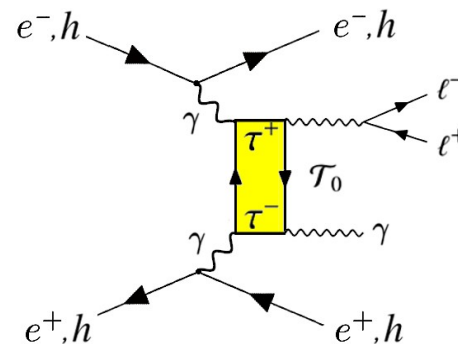
Pico-second(!) γ ToF needed to separate < 1 mm distances ☹

- Displaced charged lepton vertices from Dalitz decays**

$\tau_0 \rightarrow e^+e^-\gamma, \mu^+\mu^-\gamma$ with BR $\sim 2.3\%$?

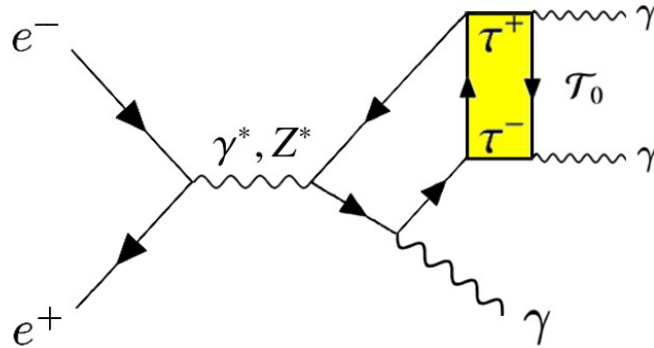
- $\mathcal{O}(150), \mathcal{O}(25)$ signal counts at FCC-ee/Belle-II...

But **para- τ_0 produced almost at rest ($\beta\gamma \approx 0.06$)** ☹



Para-ditauonium via $e^+e^- \rightarrow \tau_0 + \gamma$?

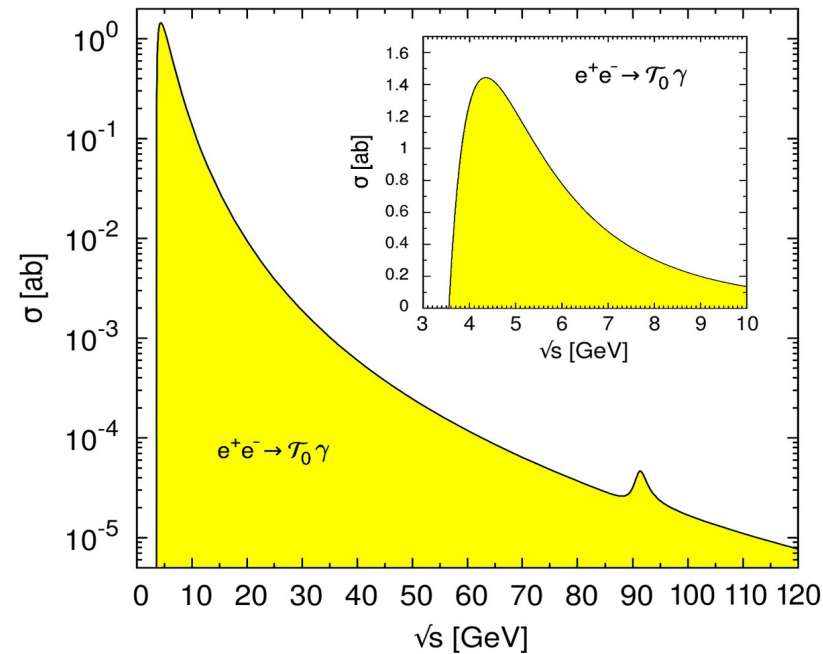
- s-channel production of **para-ditauonium plus FSR** in e^+e^- collisions:



$$\sigma(e^+e^- \rightarrow \tau_0 + \gamma) \approx \frac{2}{3} \frac{\pi \alpha^6}{n^3} \frac{m_{\mathcal{T}}^2}{s^2} \left(1 - \frac{m_{\mathcal{T}}^2}{s}\right)$$

- Tiny cross sections, in the **(sub)attobarn** range:

Colliding system, \sqrt{s} , \mathcal{L}_{int} , detector	$\sigma(\mathcal{T}_0 + \gamma) \times \mathcal{B}_{\gamma\gamma}$	$N(\mathcal{T}_0(\gamma\gamma) + \gamma)$
e^+e^- at 4.3 GeV, 1 ab^{-1} , STCF	1.1 ab	1
e^+e^- at 7 GeV, 1 ab^{-1} , STCF	0.37 ab	0.37
e^+e^- at 3.78 GeV, 20 fb^{-1} , BES III	0.69 ab	0.014
e^+e^- at 10.6 GeV, 50 ab^{-1} , Belle II	0.085 ab	4
e^+e^- at 91.2 GeV, 50 ab^{-1} , FCC-ee	$3.6 \cdot 10^{-5} \text{ ab}$	-

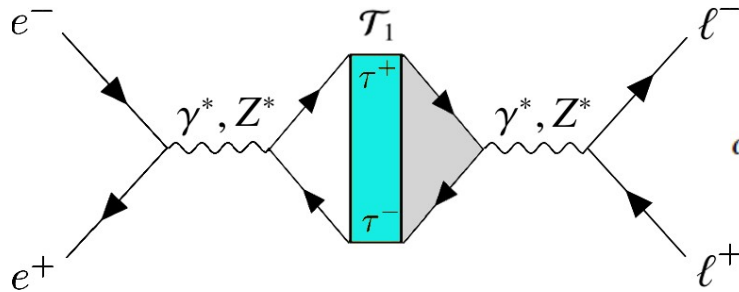


Negligible events expected, swamped by **huge backgrounds**:

$$\sigma(e^+e^- \rightarrow \gamma\gamma\gamma) \times \mathcal{L}_{\text{int}} = 15 \text{ pb} \times 50 \text{ ab}^{-1} = 7.5 \cdot 10^8 \text{ events at Belle II} \quad \text{☹}$$

Ortho-ditauonium via $e^+e^- \rightarrow \tau_1$ fusion

- **Resonant s-channel** production of ortho-ditauonium in e^+e^- collisions:



$$\sigma^{\text{ideal}}(e^+e^- \rightarrow \mathcal{T}_1) = \frac{12\pi\Gamma_{\text{tot}}(\mathcal{T}_1)\Gamma_{e^+e^-}(\mathcal{T}_1)}{(s - m_{\mathcal{T}}^2)^2 + \Gamma_{\text{tot}}^2(\mathcal{T}_1)m_{\mathcal{T}}^2} \stackrel{\sqrt{s}=m_{\mathcal{T}}}{=} 236.6 \mu\text{b}$$

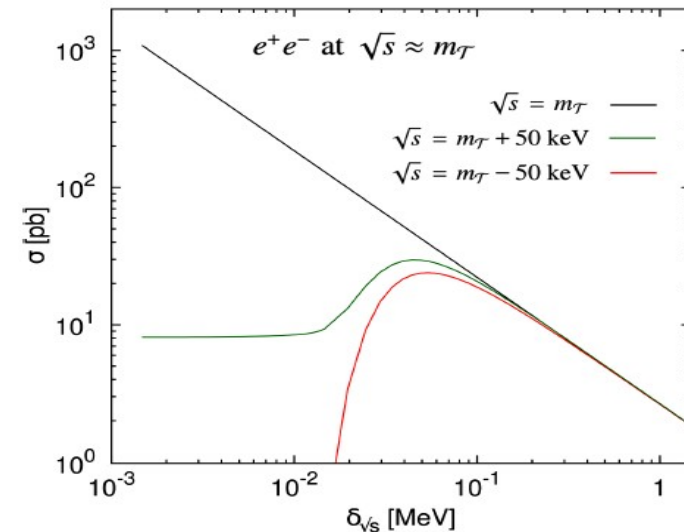
- Actual Breit-Wigner x-section **reduced by $>10^7$** , down to 2–20 pb, due to:

- **ISR & beam-energy spread $\delta_{\sqrt{s}}$** (reduceable via monochromatization)
- **Accurate knowledge of m_{τ} peak** position required for \sqrt{s} .

$$\sigma^{\text{actual}}(e^+e^- \rightarrow \mathcal{T}_1) = \frac{12\pi^2\Gamma_{e^+e^-}(\mathcal{T}_1)}{m_{\mathcal{T}}} \int_0^1 dx_1 \int_0^1 dx_2 f_{e^-/e^-}(x_1, s) f_{e^+/e^+}(x_2, s) V_2(\sqrt{x_1 x_2 s}; m_{\mathcal{T}}, \Gamma_{\text{tot}}(\mathcal{T}_1), \sqrt{x_1 x_2} \delta_{\sqrt{s}})$$

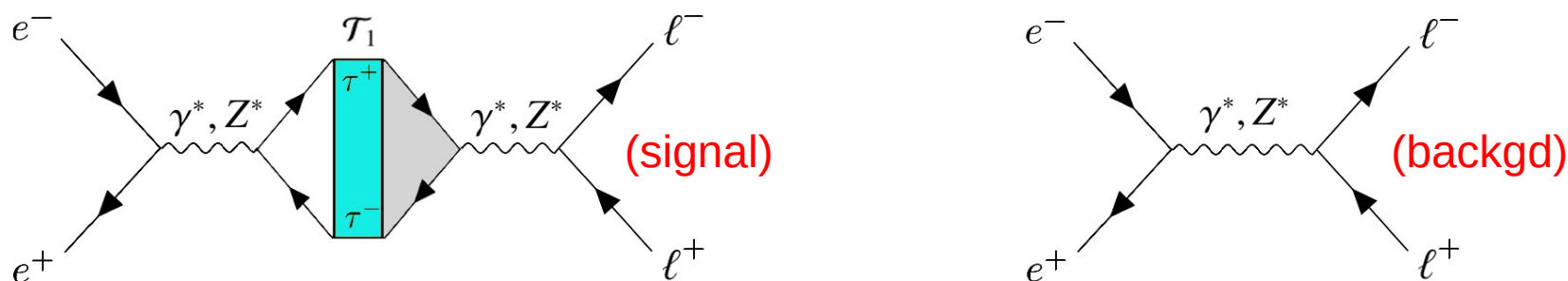
- **Threshold-scan** around $\sqrt{s} = 2m_{\tau}$:

Colliding system, \sqrt{s} ($\delta_{\sqrt{s}}$ spread), \mathcal{L}_{int} , experiment	σ	N
e^+e^- at 3.5538 GeV (1.47 MeV), 5.57 pb^{-1} , BES III	1.9 pb	10.4
e^+e^- at $\sqrt{s} \approx m_{\tau}$ (1.24 MeV), 140 pb^{-1} , BES III	2.2 pb	310
e^+e^- at $\sqrt{s} \approx m_{\tau}$ (1 MeV), 1 ab^{-1} , STCF	2.6 pb	$2.6 \cdot 10^6$
e^+e^- at $\sqrt{s} \approx m_{\tau}$ (100 keV), 0.1 ab^{-1} , STCF	22 pb	$2.2 \cdot 10^6$



Ortho-ditauonium observation via $e^+e^- \rightarrow \tau_1$ fusion

- Resonant s-channel production of ortho-ditauonium in e^+e^- collisions:



- Actual Breit-Wigner x-section reduced by $>10^7$, down to 2–20 pb, due to:

- ISR & beam-energy spread $\delta_{\sqrt{s}}$ (reduceable via monochromatization)
- Accurate knowledge of m_{τ} peak position required for \sqrt{s} .

- Threshold-scan around $\sqrt{s} = 2m_{\tau}$: $\sigma^{\text{actual}}(e^+e^- \rightarrow \tau_1) = \frac{12\pi^2\Gamma_{e^+e^-}(\mathcal{T}_1)}{m_{\tau}} \int_0^1 dx_1 \int_0^1 dx_2 f_{e^-/e^-}(x_1, s) f_{e^+/e^+}(x_2, s) V_2(\sqrt{x_1 x_2 s}, m_{\tau}, \Gamma_{\text{tot}}(\mathcal{T}_1), \sqrt{x_1 x_2} \delta_{\sqrt{s}})$

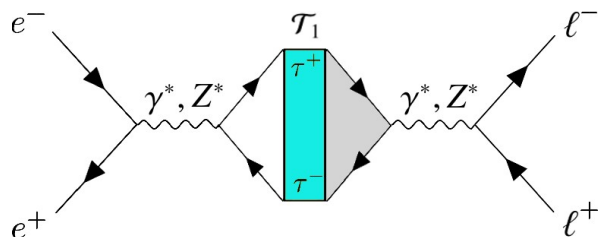
Colliding system, \sqrt{s} ($\delta_{\sqrt{s}}$ spread), \mathcal{L}_{int} , experiment	σ			N			S/\sqrt{B}
	\mathcal{T}_1	$\tau^+\tau^-$	$\mu^+\mu^-$	\mathcal{T}_1	$\mathcal{T}_1 \rightarrow \mu^+\mu^-$	$\mu^+\mu^-$	
e^+e^- at 3.5538 GeV (1.47 MeV), 5.57 pb $^{-1}$, BES III	1.9 pb	117 pb	6.88 nb	10.4	2.1	38 300	0.01 σ
e^+e^- at $\sqrt{s} \approx m_{\tau}$ (1.24 MeV), 140 pb $^{-1}$, BES III	2.2 pb	103 pb	6.88 nb	310	63	$9.63 \cdot 10^5$	0.06 σ
e^+e^- at $\sqrt{s} \approx m_{\tau}$ (1 MeV), 1 ab $^{-1}$, STCF	2.6 pb	95 pb	6.88 nb	$2.6 \cdot 10^6$	$5.3 \cdot 10^5$	$6.88 \cdot 10^9$	6.4 σ
e^+e^- at $\sqrt{s} \approx m_{\tau}$ (100 keV), 0.1 ab $^{-1}$, STCF	22 pb	46 pb	6.88 nb	$2.2 \cdot 10^6$	$4.5 \cdot 10^5$	$6.88 \cdot 10^8$	17 σ

- Ortho- τ_1 observable at STCF (6.4 σ) on top of $\mu^+\mu^-$ continuum in default run (1 ab $^{-1}$)

- Note: Ditauonium contributes 2% of the di-tau x-section at $\sqrt{s} = 2m_{\tau}$ at STCF

Ultraprecise tau mass via $e^+e^- \rightarrow \tau_1 \rightarrow \mu^+\mu^-$

- STCF with 0.1-MeV monochromatization & 4 mass points runs (0.1 ab^{-1} each) can determine very accurately **peak excess of $\mu^+\mu^-$ events** corresponding to the **ortho- τ_1 resonant mass point** (provided true m_τ is known to within $\pm 50 \text{ keV}$):



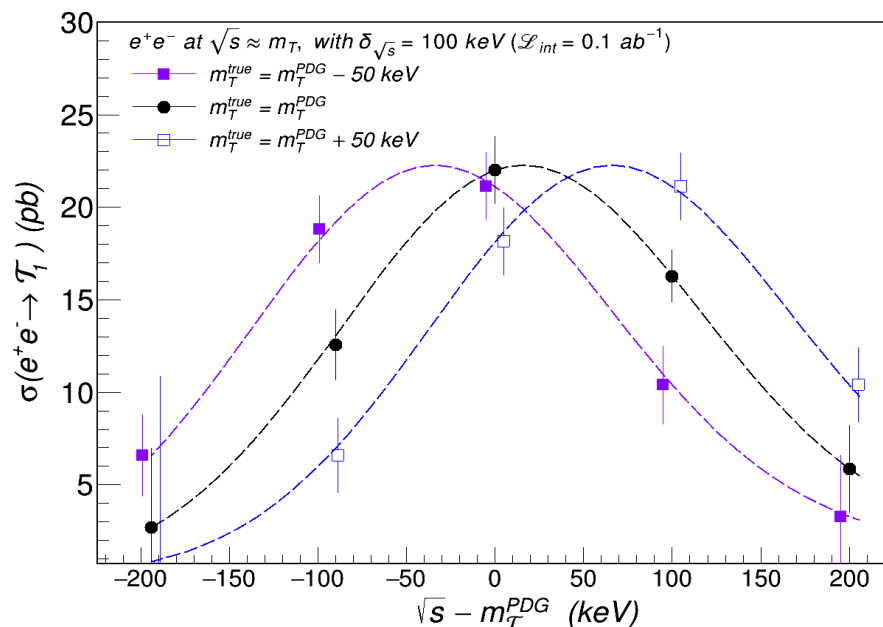
Colliding system, \sqrt{s} ($\delta\sqrt{s}$ spread), \mathcal{L}_{int} , experiment	σ			N		S/\sqrt{B}
	τ_1	$\tau^+\tau^-$	$\mu^+\mu^-$	$\tau_1 \rightarrow \mu^+\mu^-$	$\mu^+\mu^-$	
e^+e^- at $\sqrt{s} \approx m_\tau$ (1 MeV), 1 ab^{-1} , STCF	2.6 pb	95 pb	6.88 nb	$5.3 \cdot 10^5$	$6.88 \cdot 10^9$	6.4σ
e^+e^- at $\sqrt{s} \approx m_\tau$ (100 keV), 0.1 ab^{-1} , STCF	22 pb	46 pb	6.88 nb	$4.5 \cdot 10^5$	$6.88 \cdot 10^8$	17σ

- The **accuracy of the $m(\tau_1)$ position** depends only on the accuracy of the **beam energy calibration**:

With BES-III (BEMS method): $\Delta_{\sqrt{s}} = 10^{-5}$
 $\Rightarrow \mathcal{O}(25 \text{ keV})$ tau mass precision

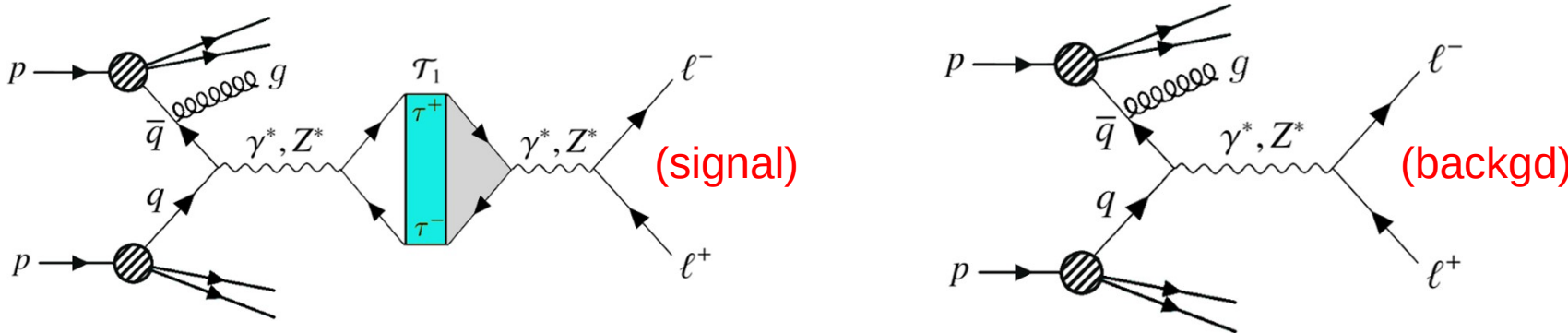
- Impact of ultraprecise m_τ :

- Improved LFU tests ($\propto m_{e,\mu}^5/m_\tau^5$)
- CKM $|V_{ij}|$ elements from τ decays
- Any other **SM checks** that parametrically depend on ratios of **e, μ , τ masses**



Ortho-ditauonium via DY+j production at the LHC

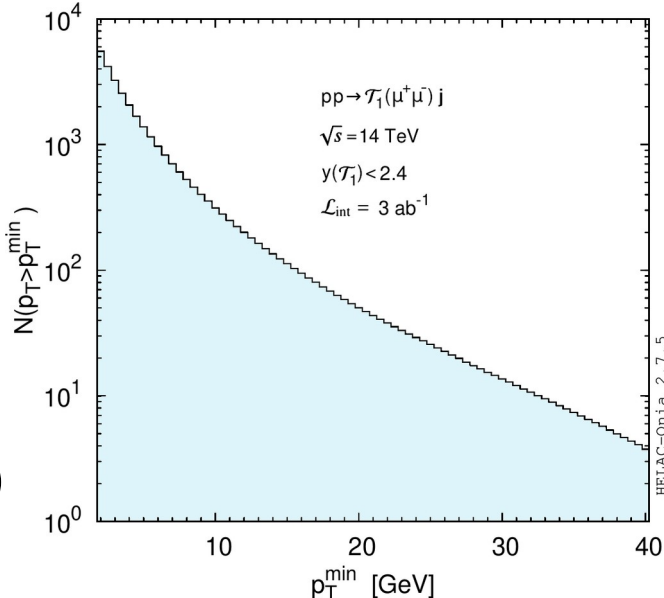
■ Drell-Yan production of **ortho-ditauonium + jet** in pp colls. at 14 TeV:



Back-to-back jet required to **boost ortho- τ_1** decay (**displaced secondary dimuon vertex**) & eliminate DY backgds. Only combinatorial heavy-Q dimuon sources left.

■ Cross sections at ATLAS/CMS, ALICE/LHCb:

Colliding system, \sqrt{s} , \mathcal{L}_{int} , detector	σ_{NLO}		$N(\mathcal{T}_1 + j)$		with $L_{xy} > 30 (100) \mu\text{m}$	
	$\mathcal{T}_1 + X$	$\mathcal{T}_1 + j$	$\mathcal{T}_1 \rightarrow e^+e^-$	$\mathcal{T}_1 \rightarrow \mu^+\mu^-$	$\mathcal{T}_1 \rightarrow \ell^+\ell^-$	$\mathcal{T}_1 \rightarrow \mu^+\mu^-$
p-p at 14 TeV, 3 ab^{-1} , ATLAS/CMS	42_{-19}^{+11} fb	18 ± 9 fb	1100	1100	130 (10)	130 (10)
p-p at 14 TeV, 300 fb^{-1} , LHCb	42_{-19}^{+11} fb	18 ± 9 fb	110	110	5 (-)	5 (-)
p-p at 114.6 GeV, 10 fb^{-1} , ALICE/LHCb	$2.2_{-0.4}^{+0.3}$ fb	1 ± 0.5 fb	<10	<10	-	-

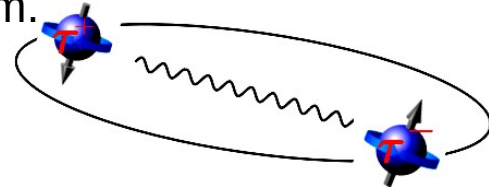


■ About **130 (10) displaced dimuon events** with $L_{xy} > 30 (100) \mu\text{m}$ expected in ATLAS/CMS (3 ab^{-1})
 Observation feasible (even with less int. lumi)!

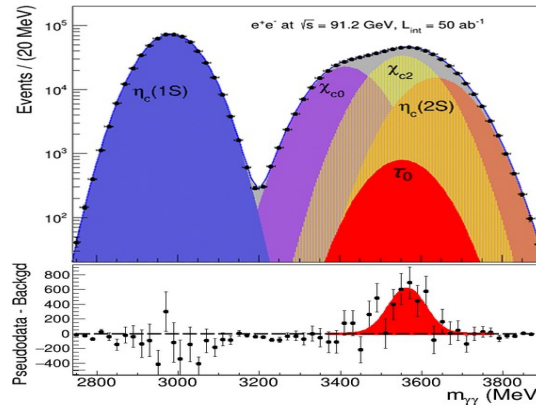
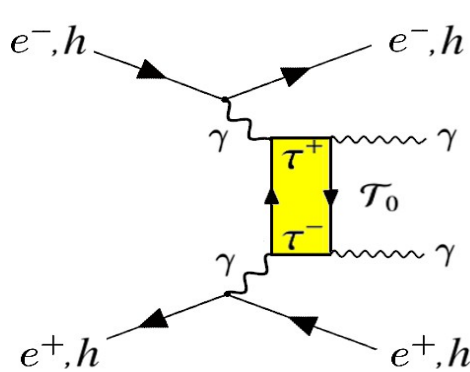
Summary (I)

■ First-ever comprehensive study of ditauonium production/detection in the lab:

- Unobserved. Heaviest & most compact leptonic “atomic” system.
- Tests of bound QED & CPT symmetries at high-mass (BSM?).
- Ultraprecise τ mass extraction possible via $e^+e^- \rightarrow \tau_1 \rightarrow \mu^+\mu^-$

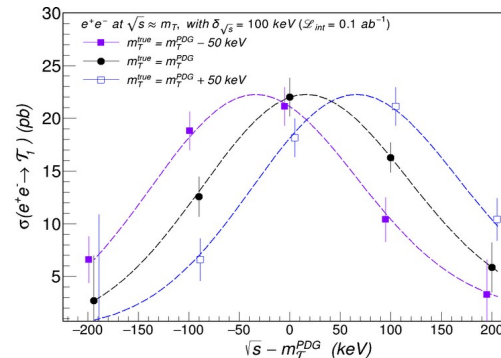
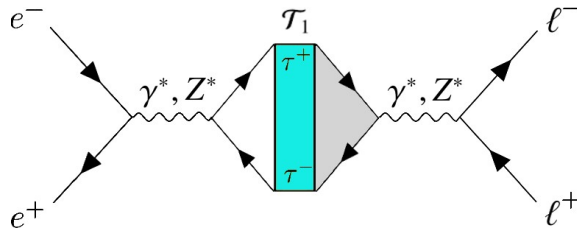


■ Para-ditauonium: Observable via $\gamma\gamma$ fusion at high-lumi e^+e^- colliders:



- Requires accurate in-situ measure of overlapping $c\bar{c}$ resonances.
- Stat. significance (multi-Gaussian $m_{\gamma\gamma}$ fit): $S(\text{Belle-II/FCC-ee}) \approx 3\sigma, 5\sigma$

■ Ortho-ditauonium: Observable as s-channel resonance at STCF e^+e^- at $\sqrt{s} = 2m_\tau$:

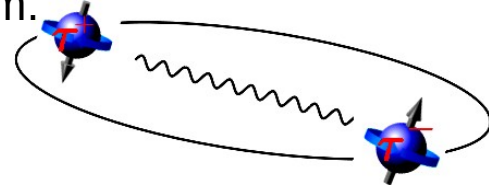


- Dimuon excess ($>6\sigma$) in a nominal STCF year (1 ab^{-1})
- With 0.1-MeV beam monochrom. tau mass with 25-keV (or better) precision (beam calibration).

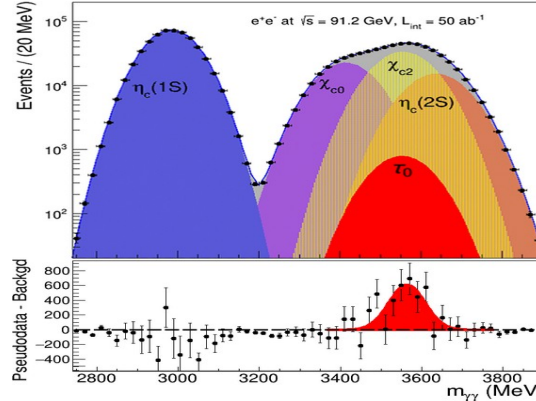
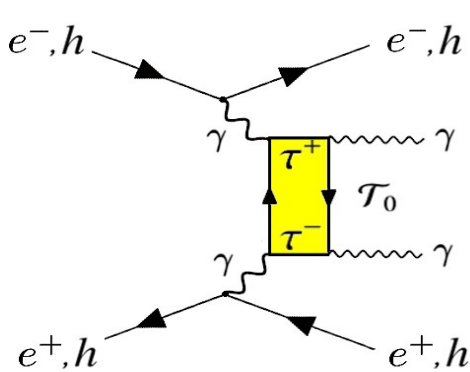
Summary (II)

■ First-ever comprehensive study of ditauonium production/detection in the lab:

- Unobserved. Heaviest & most compact leptonic “atomic” system.
- Tests of bound QED & CPT symmetries at high-mass (BSM?).
- Ultraprecise τ mass extraction possible via $e^+e^- \rightarrow \tau_1 \rightarrow \mu^+\mu^-$

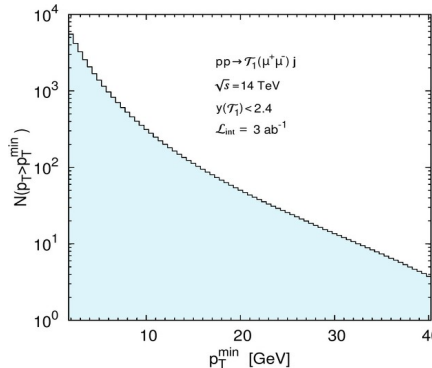
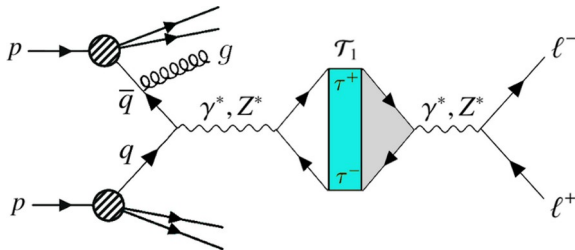


■ Para-ditauonium: Observable via $\gamma\gamma$ fusion at high-lumi e^+e^- colliders:



- Requires accurate in-situ measure of overlapping $c\bar{c}$ resonances.
- Stat. significance (multi-Gaussian $m_{\gamma\gamma}$ fit): $S(\text{Belle-II/FCC-ee}) \approx 3\sigma, 5\sigma$

■ Ortho-ditauonium+jet: Observable in DY production in p-p collisions at the LHC:



- $N_{\text{evts}} = 130$ (10) displaced dimuon with $L_{xy} > 30$ (100) μm at ATLAS/CMS (3 ab^{-1}).
- Observation feasible (even with less int. lumi)!

Backup slides

Ditauonium partial widths & decays

\mathcal{T} state	m_X (MeV)	J^{PC}	Γ_{tot} (eV)	Lifetime (fs)	Decay mode	Γ_X (eV)	\mathcal{B}_X
1^1S_0	3553.696 ± 0.240	0^{-+}	0.02384	27.60	$\gamma\gamma$	0.018533	77.72%
					$\gamma e^+ e^-$	$4.28 \cdot 10^{-4}$	1.79%
					$\gamma \mu^+ \mu^-$	$1.24 \cdot 10^{-4}$	0.52%
					$\gamma q\bar{q}$	$2.20 \cdot 10^{-4}$	0.92%
					$e^+ e^- e^+ e^-$	$2.32 \cdot 10^{-6}$	0.0094%
					$e^+ e^- \mu^+ \mu^-$	$1.38 \cdot 10^{-6}$	0.0058%
					$e^+ e^- q\bar{q}$	$1.20 \cdot 10^{-6}$	0.0050%
					$\mu^+ \mu^- \mu^+ \mu^-$	$1.65 \cdot 10^{-7}$	0.00069%
					$\mu^+ \mu^- q\bar{q}$	$2.72 \cdot 10^{-7}$	0.0011%
					$q\bar{q}q'\bar{q}'$	$8.23 \cdot 10^{-8}$	0.00035%
$(2)\tau \rightarrow X$	0.004535	19.02%					
\mathcal{T} state	m_X (MeV)	J^{PC}	Γ_{tot} (eV)	Lifetime (fs)	Decay mode	Γ_X (eV)	\mathcal{B}_X
1^3S_1	3553.696 ± 0.240	1^{--}	0.03159	20.83	$e^+ e^- (\gamma)$	0.006436	20.37%
					◦ $e^+ e^-$	$2.95 \cdot 10^{-3}$	9.33%
					◦ $e^+ e^- \gamma$	$3.49 \cdot 10^{-3}$	11.04%
					$\mu^+ \mu^- (\gamma)$	0.006436	20.37%
					◦ $\mu^+ \mu^-$	$6.10 \cdot 10^{-3}$	19.30%
					◦ $\mu^+ \mu^- \gamma$	$3.38 \cdot 10^{-4}$	1.07%
					$q\bar{q} (\gamma)$	0.01416	44.82%
					$\gamma\gamma\gamma$	$1.62 \cdot 10^{-5}$	0.051%
					$e^+ e^- e^+ e^-$	$5.55 \cdot 10^{-6}$	0.0176%
					$e^+ e^- \mu^+ \mu^-$	$4.21 \cdot 10^{-6}$	0.0133%
					$e^+ e^- q\bar{q}$	$1.85 \cdot 10^{-6}$	0.0058%
					$\mu^+ \mu^- \mu^+ \mu^-$	$1.23 \cdot 10^{-7}$	$\mathcal{O}(10^{-6})$
					$\mu^+ \mu^- q\bar{q}$	$7.36 \cdot 10^{-8}$	$\mathcal{O}(10^{-6})$
					$q\bar{q}q'\bar{q}'$	$9.73 \cdot 10^{-9}$	$\mathcal{O}(10^{-7})$
					$\nu_\tau \bar{\nu}_\tau$	$1.32 \cdot 10^{-8}$	$\mathcal{O}(10^{-7})$
					$\nu_e \bar{\nu}_e$	$4.30 \cdot 10^{-11}$	$\mathcal{O}(10^{-9})$
					$\nu_\mu \bar{\nu}_\mu$	$4.30 \cdot 10^{-11}$	$\mathcal{O}(10^{-9})$
					$(2)\tau \rightarrow X$	0.004535	14.35%

Para-ditauonium production via $\gamma\gamma$ collisions

- Cross sections for signal & backgrounds computed in the Weizsäcker-Williams approx. (EPA) for $\gamma\gamma$ collisions (implemented in HelacOnia2.6/gamma-UPC):

$$\sigma(ab \rightarrow ab + X) = 4\pi^2(2J + 1) \frac{\Gamma_{\gamma\gamma}(X)}{m_X^2} \frac{d\mathcal{L}_{\gamma\gamma}^{(ab)}}{dW_{\gamma\gamma}} \Big|_{W_{\gamma\gamma}=m_X}$$

- Diphoton charmonium resonances within $m_{\gamma\gamma} \approx 2.9\text{--}3.7$ GeV:

Resonance	J^{PC}	m_X (MeV)	Γ_{tot} (MeV)	$\Gamma_{\gamma\gamma}$ (MeV)	$\mathcal{B}_{\gamma\gamma}$
\mathcal{T}_0	0^{-+}	3553.696 ± 0.240	$2.28 \cdot 10^{-8}$	$1.83 \cdot 10^{-8}$	$\sim 80\%$
$\eta_c(1S)$	0^{-+}	2983.9 ± 0.5	32.0 ± 0.7	$(5.06 \pm 0.34) \cdot 10^{-3}$	$(0.0158 \pm 0.0011)\%$
$\eta_c(2S)$	0^{-+}	3637.5 ± 1.1	11.3 ± 3.1	$(2.15 \pm 1.47) \cdot 10^{-3}$	$(0.019 \pm 0.013)\%$
χ_{c0}	0^{++}	3414.71 ± 0.30	10.8 ± 0.6	$(2.203 \pm 0.097) \cdot 10^{-3}$	$(0.0204 \pm 0.0009)\%$
χ_{c2}	2^{++}	3556.17 ± 0.07	1.97 ± 0.09	$(5.614 \pm 0.197) \cdot 10^{-4}$	$(0.0285 \pm 0.0010)\%$

- Charmonia resonances have $\mathcal{O}(\text{keV})$ diphoton widths: $\mathcal{O}(10^5)$ larger than para- τ_0 .
But, the diphoton BR is $\mathcal{O}(10^4)$ larger for para- τ_0 than for c-cbar states.

$\gamma\gamma$ collision x-sections (signal & backgds)

- Cross sections for signal & backgrounds computed in the Weizsäcker-Williams approximation (EPA) for $\gamma\gamma$ collisions via gamma-UPC: 2207.03012 [hep-ph].
- $\sigma(\text{LbL})$ computed with MG5@NLO (virtual box) with same photon fluxes.
- Results for e^+e^- and ultraperipheral p-p, p-A & A-A collisions:

Colliding system, c.m. energy, \mathcal{L}_{int} , exp.	$\sigma \times \mathcal{B}_{\gamma\gamma}$						$N \times \mathcal{B}_{\gamma\gamma}$	
	$\eta_c(1S)$	$\eta_c(2S)$	$\chi_{c,0}(1P)$	$\chi_{c,2}(1P)$	LbL	\mathcal{T}_0	\mathcal{T}_0	$\chi_{c,2}(1P)$
e^+e^- at 3.78 GeV, 20 fb $^{-1}$, BES III	120 fb	3.6 ab	15 ab	13 ab	30 ab	0.25 ab	–	–
e^+e^- at 10.6 GeV, 50 ab $^{-1}$, Belle II	1.7 fb	0.35 fb	0.52 fb	0.77 fb	1.7 fb	0.015 fb	750	38 500
e^+e^- at 91.2 GeV, 50 ab $^{-1}$, FCC-ee	11 fb	2.8 fb	3.9 fb	6.0 fb	12 fb	0.11 fb	5 600	$3 \cdot 10^5$
p-p at 14 TeV, 300 fb $^{-1}$, LHC	7.9 fb	2.0 fb	2.8 fb	4.3 fb	6.3 fb	0.08 fb	24	1290
p-Pb at 8.8 TeV, 0.6 pb $^{-1}$, LHC	25 pb	6.3 pb	8.7 pb	13 pb	21 pb	0.25 pb	0.15	8
Pb-Pb at 5.5 TeV, 2 nb $^{-1}$, LHC	61 nb	15 nb	21 nb	31 nb	62 nb	0.59 nb	1.2	62

(~10% uncertainties, today)

- Relative production x-sections: $\eta_c(1S):\chi_{c,2}(1P):\chi_{c,0}(1P):\eta_c(2S):\tau_0 \approx 100:50:30:25:1$
driven by their different $\Gamma^2(\gamma\gamma)/(\Gamma(\text{tot}) \cdot m_x^2)$ ratios.
- Cross sections increase with \sqrt{s} and Z^4 :
Largest x-sections (0.6 nb) in PbPb UPC (but handful of evts expected at LHCb)
Largest yields: 750, 5600 counts at Belle-II, FCC-ee thanks to $\mathcal{L}_{\text{int}} = 50 \text{ ab}^{-1}$.

Para-ditauonium signal extraction

- 1-million events generated for signal & backgrounds. Run **MVA (BDT) with 12 different single- γ and γ -pair kinematic variables** for signal/backgds separation:
 - (i) Strong **discrimination power (factor of ~ 20)** of LbL continuum from signal.
 - (ii) No discrimination achieved for overlapping charmonia (decay **γ angular modulation of tensor χ_{c2} different than scalar τ_0 signal, but $\times 50$ suppressed yields**)

- Signal extracted through **multi-Gaussian $m_{\gamma\gamma}$ fit**, by considering:

- $\eta_c(1S)$: No overlap w/ signal (“std.candle”): 0.5M clean evts to fully **control E_γ scale&res. plus exp. & theory uncertainties.**
- $\chi_{c0}, \eta_c(2S)$: Partial overlap with signal. Exploit **$\sim 100M \gamma\gamma \rightarrow \chi_{c0}, \eta_c \rightarrow X$ decays** with $\times 50$ larger BRs (e.g. $X=3-$ and 4-mesons) **to fully remove their contamination.**
- χ_{c2} : **Full overlap** with signal! Exploit **alternative $\gamma\gamma \rightarrow \chi_{c2} \rightarrow X$ decays** (e.g. 11M evts. for $X=4\pi$) to determine its **lineshape to within $\mathcal{O}(0.2\%)$.**

