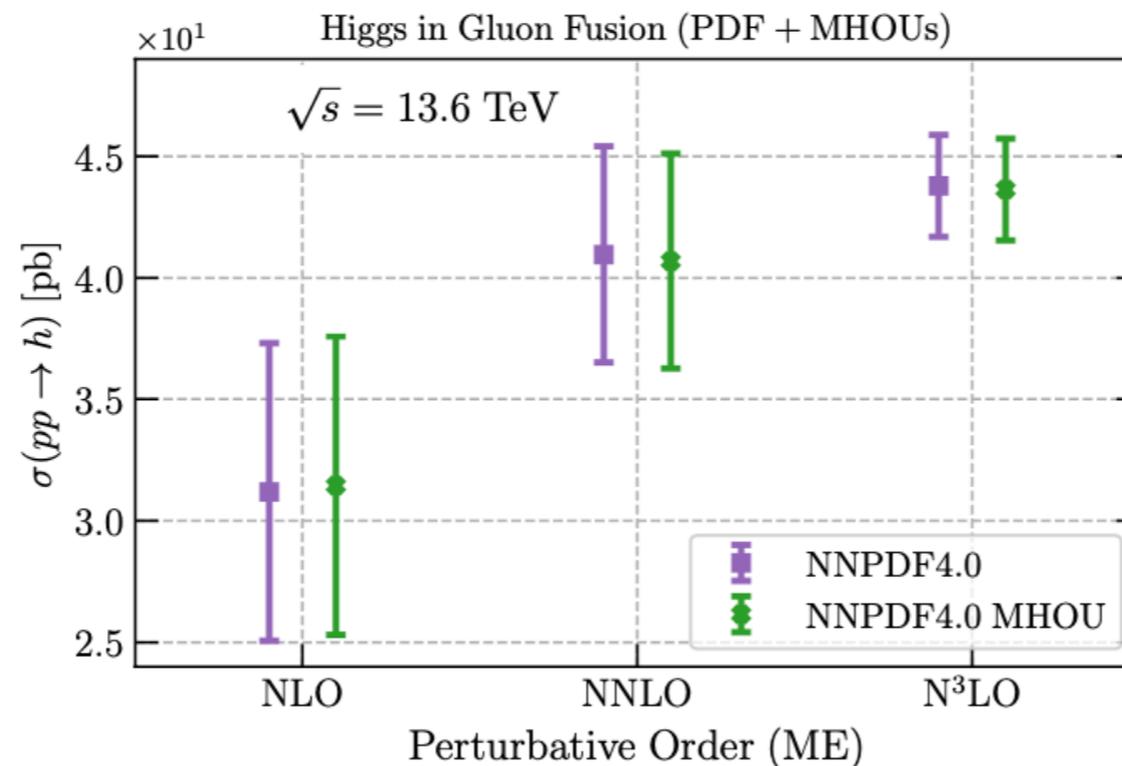


NNPDF progress and the path to N³LO PDFs

Juan Rojo, VU Amsterdam & Nikhef



Motivation I

Reducing PDF uncertainties entering LHC predictions requires an **in-depth understanding of the differences and similarities between PDF analysis**

ATLAS strong coupling extraction from Z p_T data at 8 TeV

PDF set	$\alpha_s(m_Z)$	PDF uncertainty	g [GeV ²]	q [GeV ⁴]
baseline MSHT20 [37]	0.11839	0.00040	0.44	-0.07
NNPDF4.0 [84]	0.11779	0.00024	0.50	-0.08
CT18A [29]	0.11982	0.00050	0.36	-0.03
HERAPDF2.0 [65]	0.11890	0.00027	0.40	-0.04

$$\Delta_{\text{PDF}} (\text{MSHT20 only}) = 0.34 \%$$

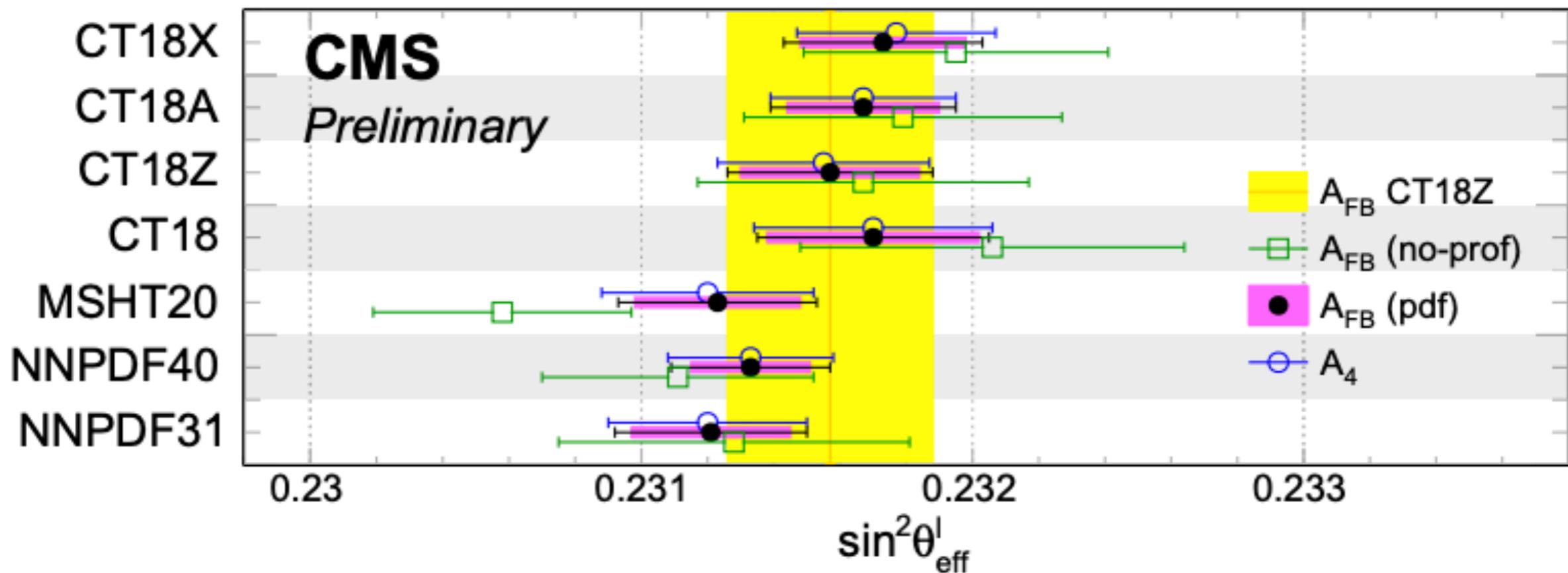
$$\Delta_{\text{PDF}} (\text{NNPDF4.0} - \text{CT18A}) = 1.6 \%$$

What is the “true PDF uncertainty” that should be associated to this measurement?

Motivation II

Reducing PDF uncertainties entering LHC predictions requires an **in-depth understanding of the differences and similarities between PDF analysis**

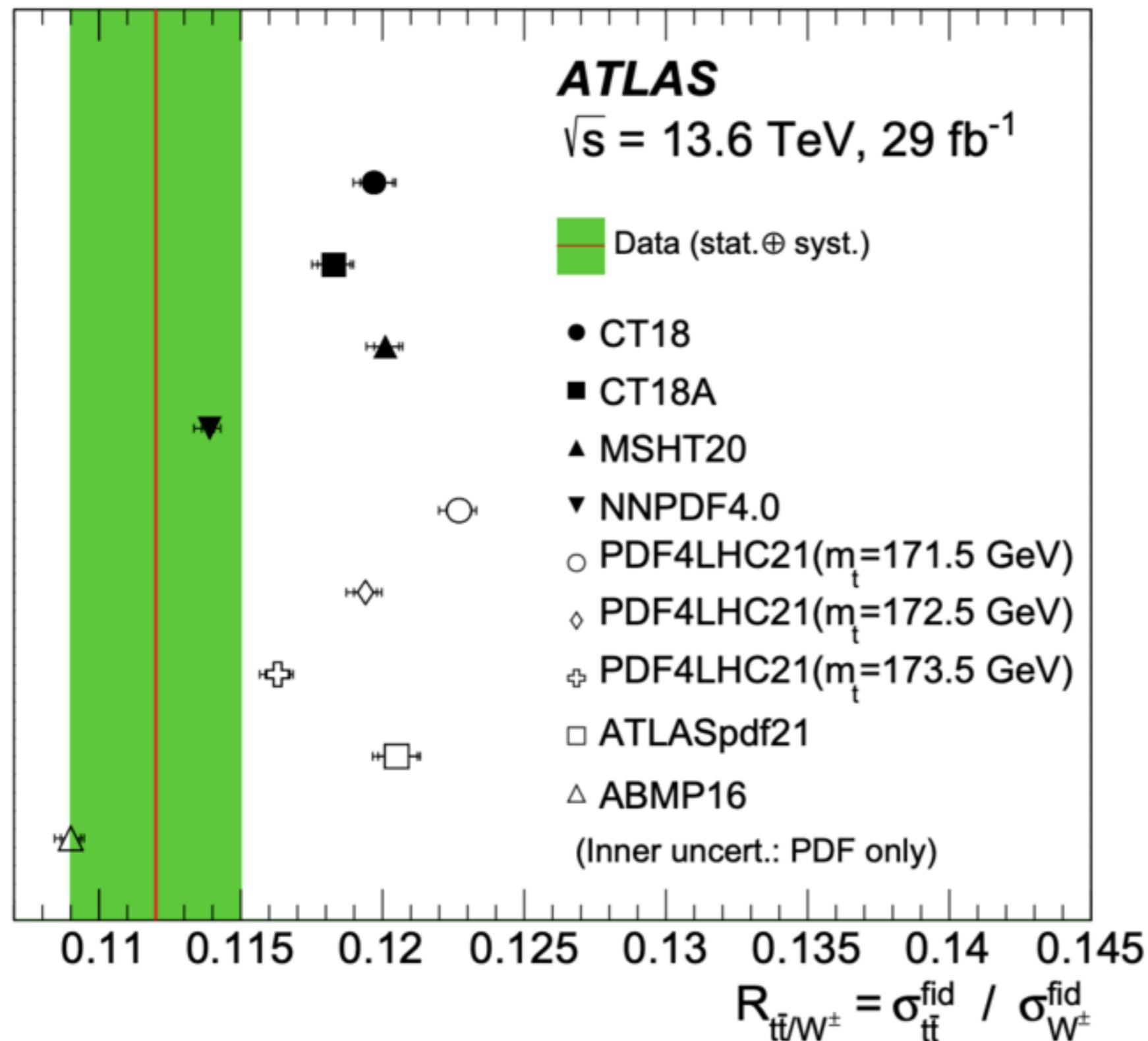
CMS determination of the weak mixing angle at 13 TeV



What is the “true PDF uncertainty” that should be associated to this measurement?

Is **in-situ profiling of PDFs** always justified? Back-reaction in other experiments?

Motivation III



- LHC precision measurements provide **discrimination power** ...
- ... but only their **combination into a consistent global analysis** can provide a coherent picture of the overall data vs theory comparison
- The **interpretation of precision LHC measurements** is a challenging effort pushing the limits of both theory calculations and methodological approaches

demands strong cross-talk between theory and experiment & dedicated benchmark exercises

NNPDF Timeline

NNPDF timescale

Sep 2021: **NNPDF4.0**
(paper & code)

Sept 2022: **PDFs & BSM**
searches (A_{FB} high-mass)

Aug 2022:
Intrinsic charm



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asymmetry study

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aN3LO

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MHOUs & QED

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📌 **WIP:** Implications of
NNPDF4.0 for LHC processes

📌 **WIP:** NNPDF4.0 aN3LO
& QED & MHOU

📌 **WIP:** NNPDF4.0 for
MC event generators

📌 **WIP:** Towards NNPDF4.1

NNPDF timescale

- 📍 Beyond neural networks: PDFs from Bayesian inference
- 📍 Improved ML hyper-parameter optimisation from parallel replica training on GPUs
- 📍 Fixed functional forms for Hessian fits in NNPDF
- 📍 Determination of strong coupling at aN³LO
- 📍 Determination of higher twist corrections
- 📍 Updated NNPDF polarised fits and EIC projections
- 📍

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Many new results
presented here at DIS2024!

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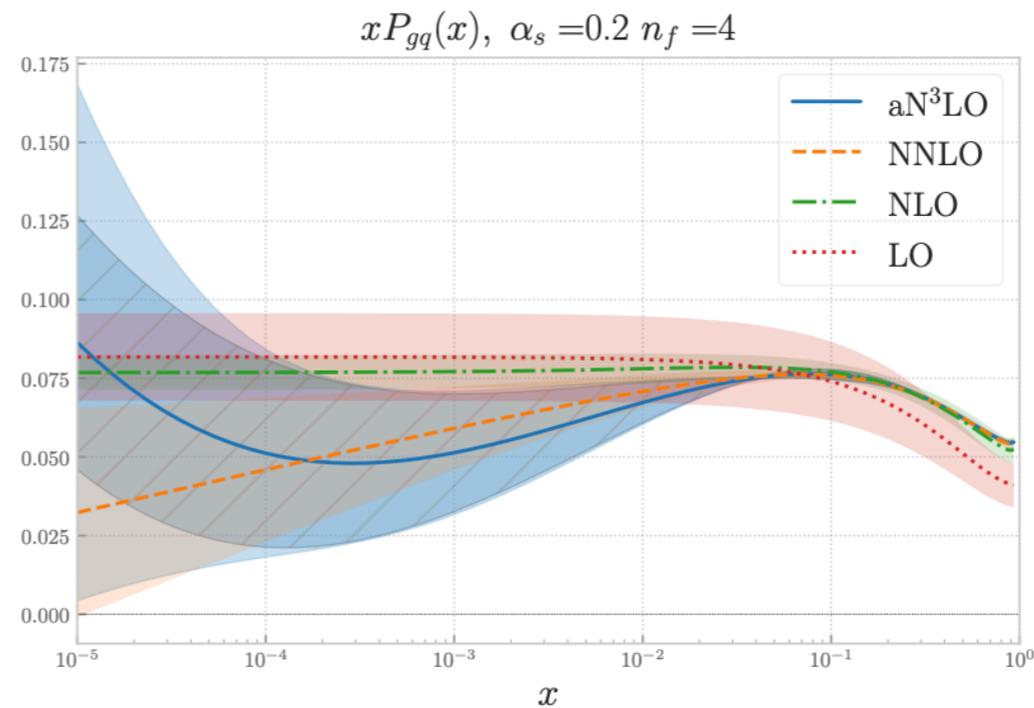
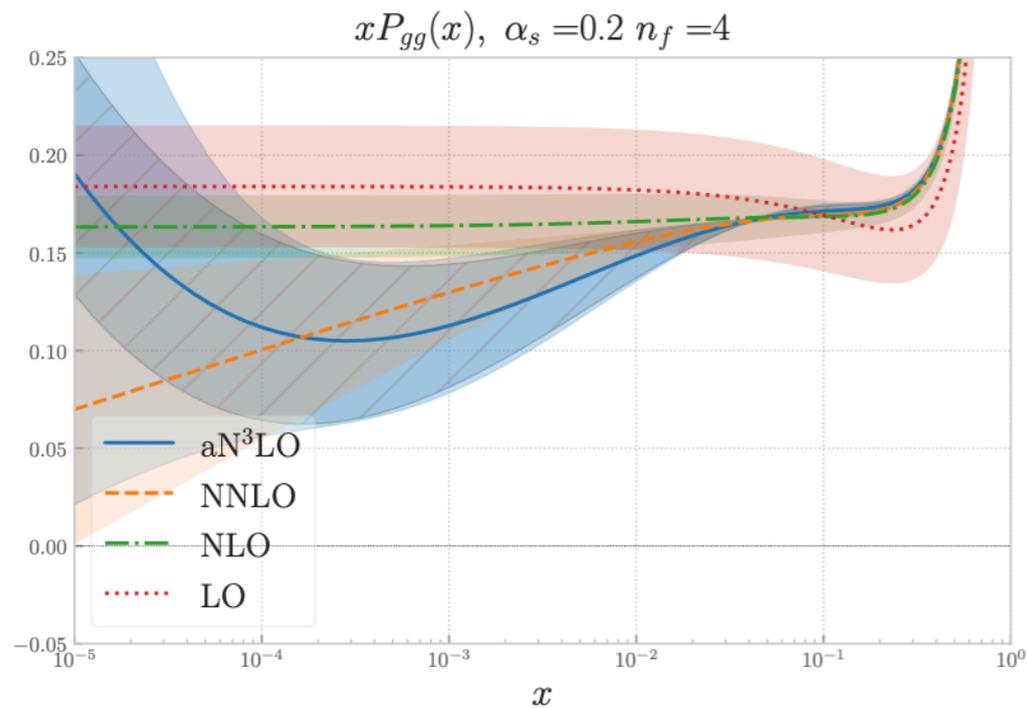
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The Path to PDFs at N³LO

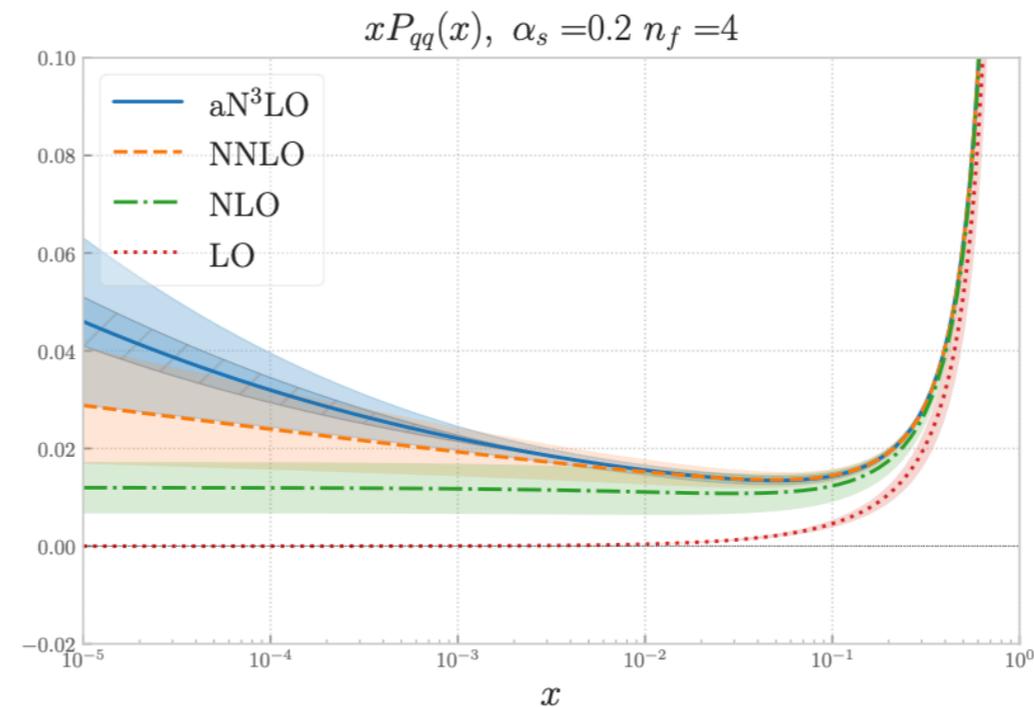
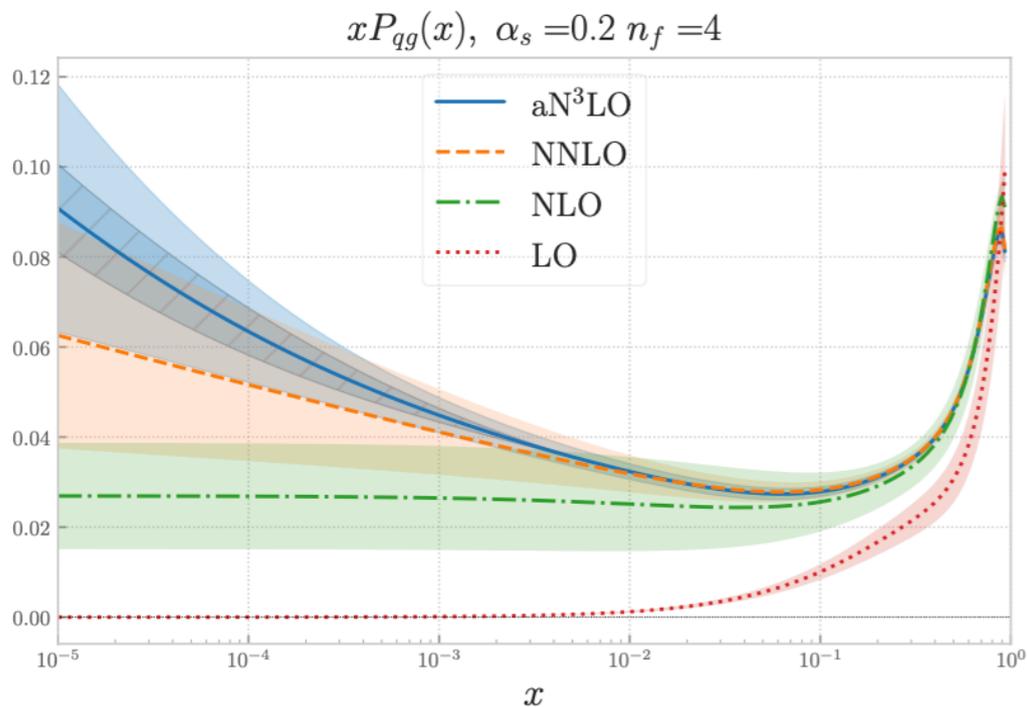
aN³LO splitting functions

📌 Approximate parametrisation for the N³LO splitting functions satisfying known **exact results and limits**



LO, NLO, NNLO:
MHOU (μ_F)

N³LO: **MHOU (μ_F)**
+ IHOU (dark)

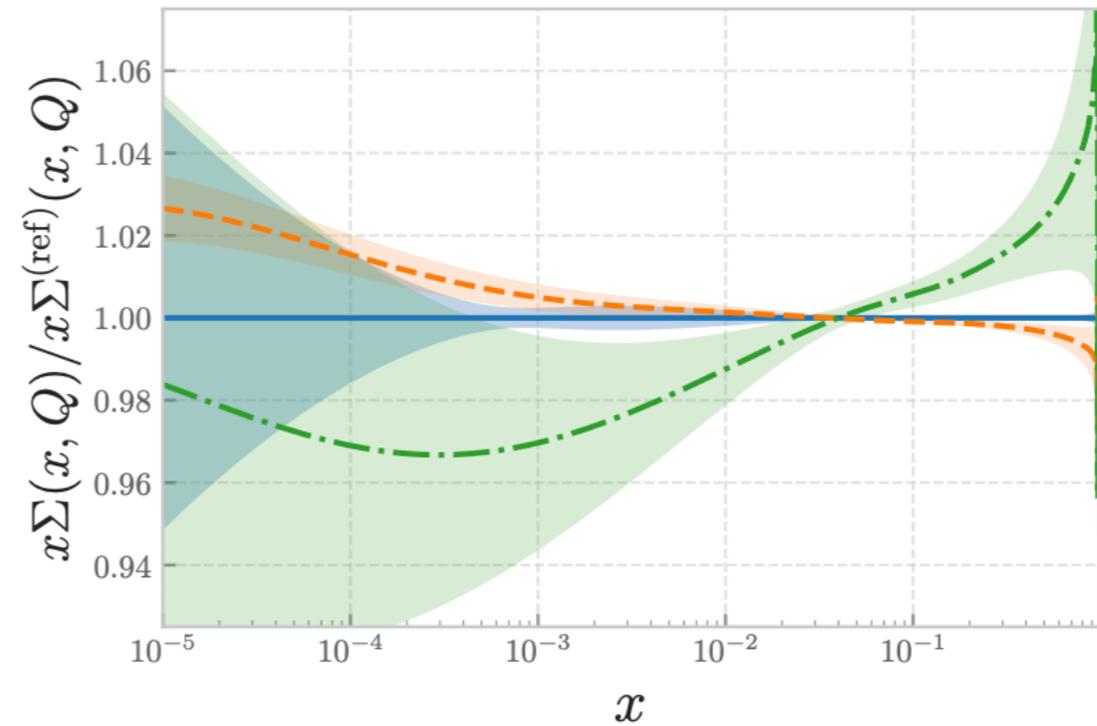
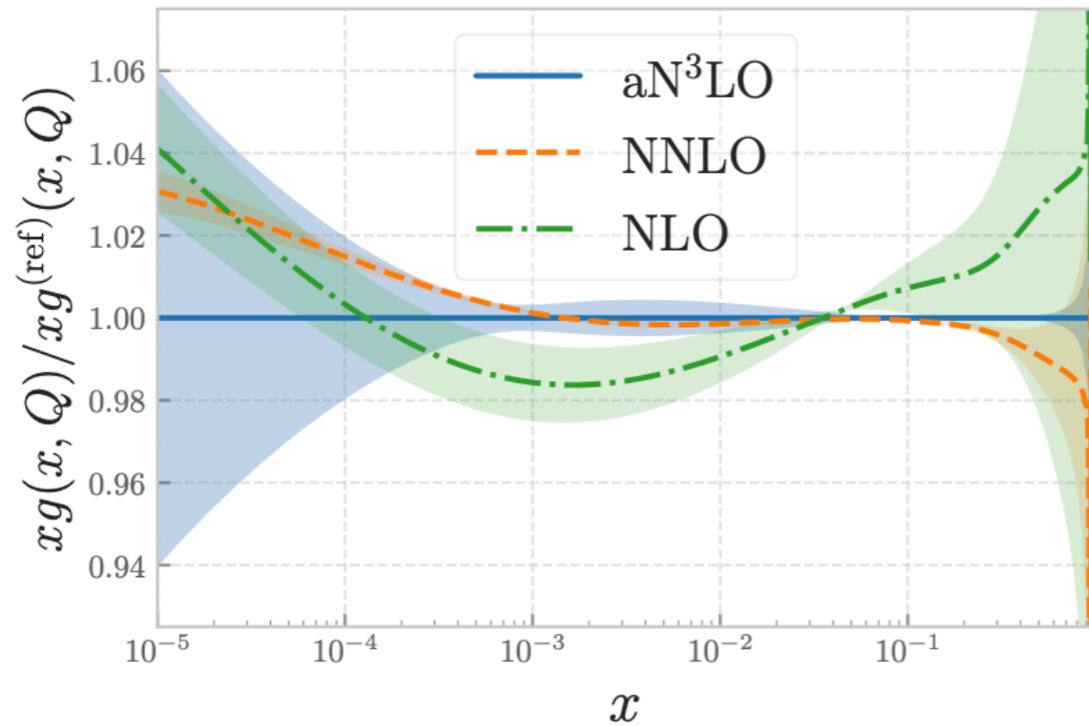


Estimate **Incomplete Higher Order Uncertainties (IHOU)** by varying interpolating functions connecting known limits

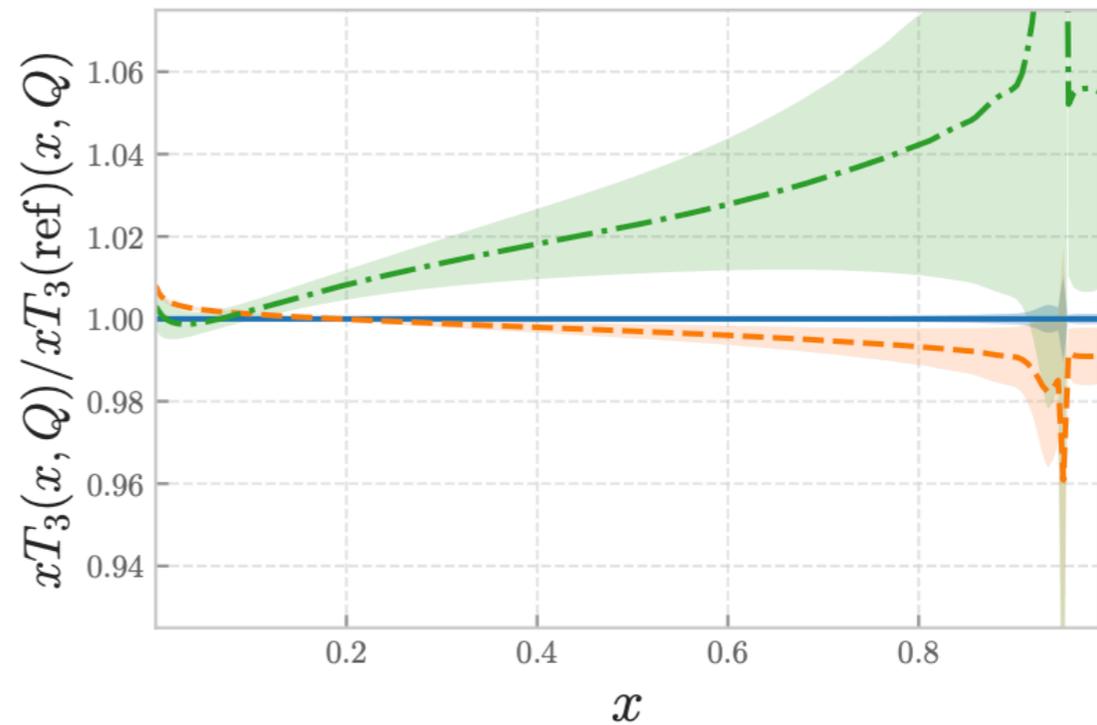
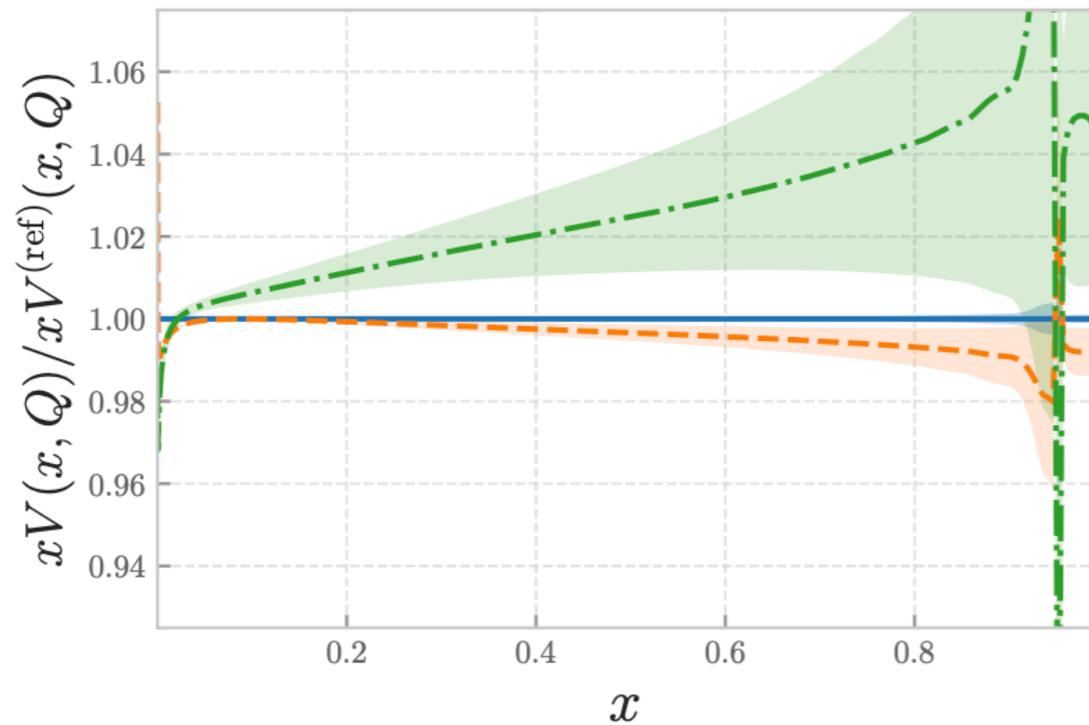
Good perturbative consistency within uncertainties

WIP: dedicated LH benchmark paper on N³LO splitting functions and PDFs (Robert's talk)

Impact on PDF evolution



evolution of fixed PDF boundary condition from $Q=1.65$ GeV to $Q=100$ GeV



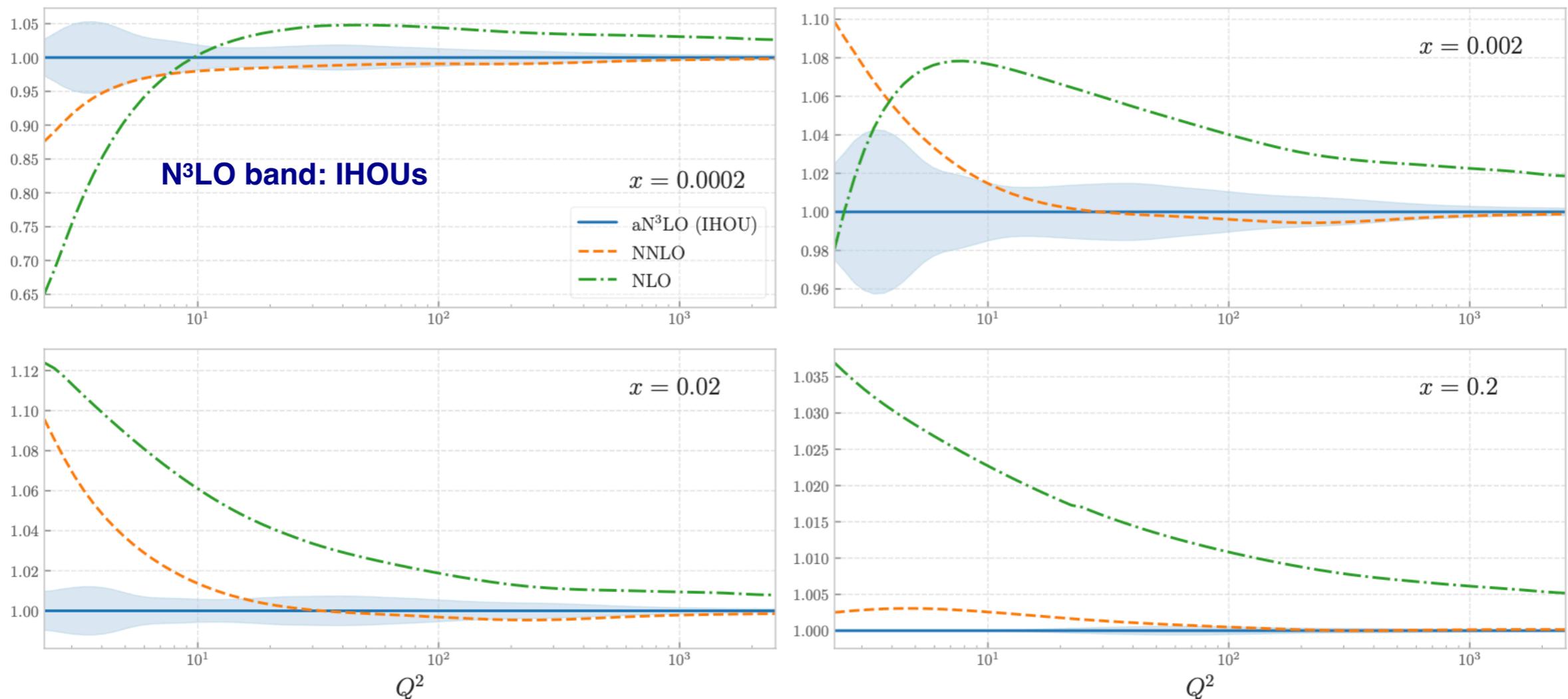
Effects of N³LO corrections to DGLAP evolution $< 1\%$ except at small- x and large- x

Excellent **perturbative convergence of PDF evolution**, may be improved with small- x or large- x resummations

Structure functions

- Exact (approximate) massless (massive) deep-inelastic coefficient functions at N³LO accuracy & extension of the **FONLL general -mass scheme at N³LO**
- Relies on parametrisation of massive DIS coefficients reproducing known results

$$F_2^{(\text{tot})}(x, Q^2), \text{ ratio to aN}^3\text{LO}$$



- N³LO corrections to DIS inclusive structure functions become significant at low- Q**
- IHOUs associated to **N³LO massive coefficient functions** deweight the impact of HERA low- Q data

Fit settings

- Same methodology, dataset, and **pipeline for theory calculations** as in NNPDF4.0 MHOU & QED sets
- Produce fit variants with and without theory uncertainties (using the theory covariance matrix)

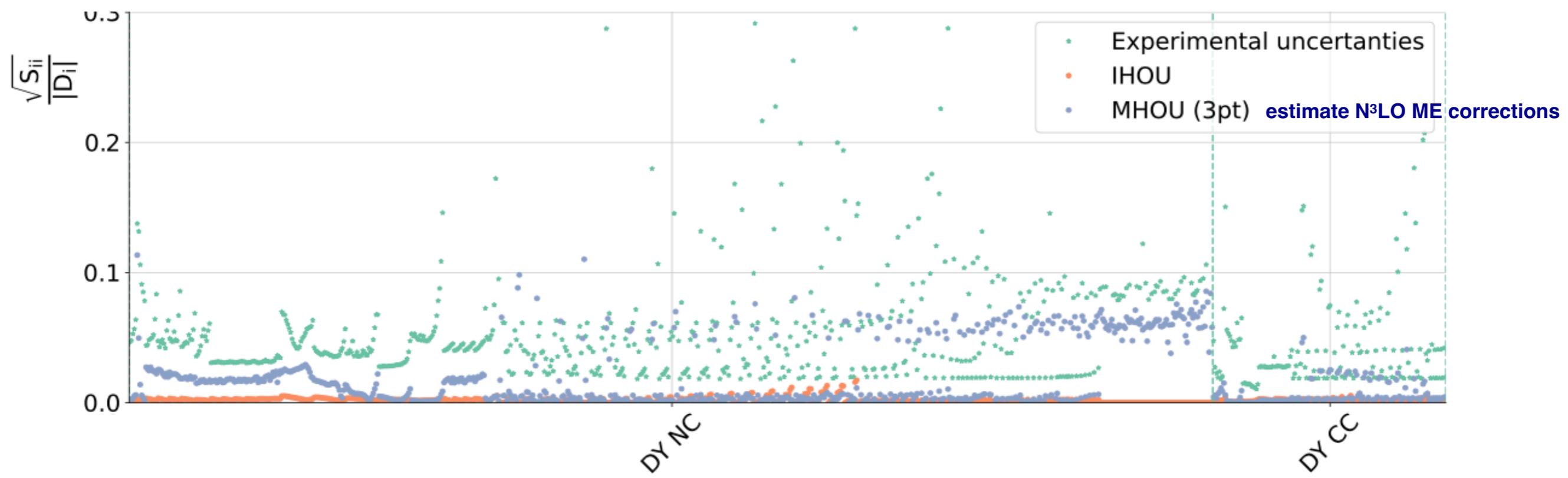
$$\Delta_i(\rho_f, \rho_r) \equiv T_i(\rho_f, \rho_r) - T_i(0, 0),$$

Shift wrt central theory on the physical observables due to theory variations (e.g. scales)

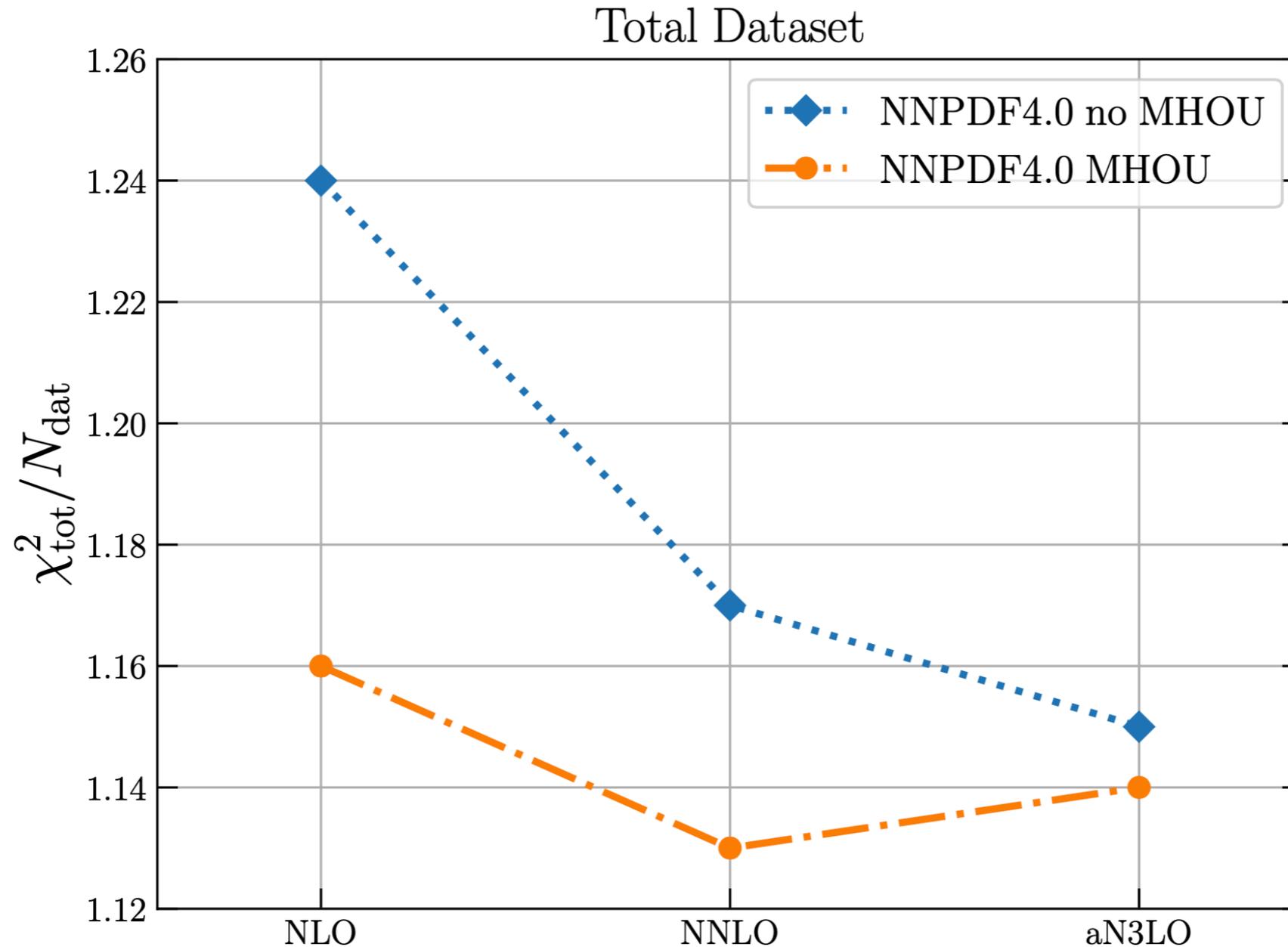
$$S_{ij} = n_m \sum_{V_m} \Delta_i(\rho_f, \rho_{r_i}) \Delta_j(\rho_f, \rho_{r_j}),$$

Theory covariance matrix: combine all shifts, keeping into account their correlations

- The theory covariance matrix includes contributions from **MHOUs** (μ_F and μ_R variations) and **IHOUs**
- Hadronic data is fitted **using aN³LO evolution and NNLO matrix elements**, supplemented by MHOUs associated to μ_R variations to account for missing K-factors



Results: Fit quality

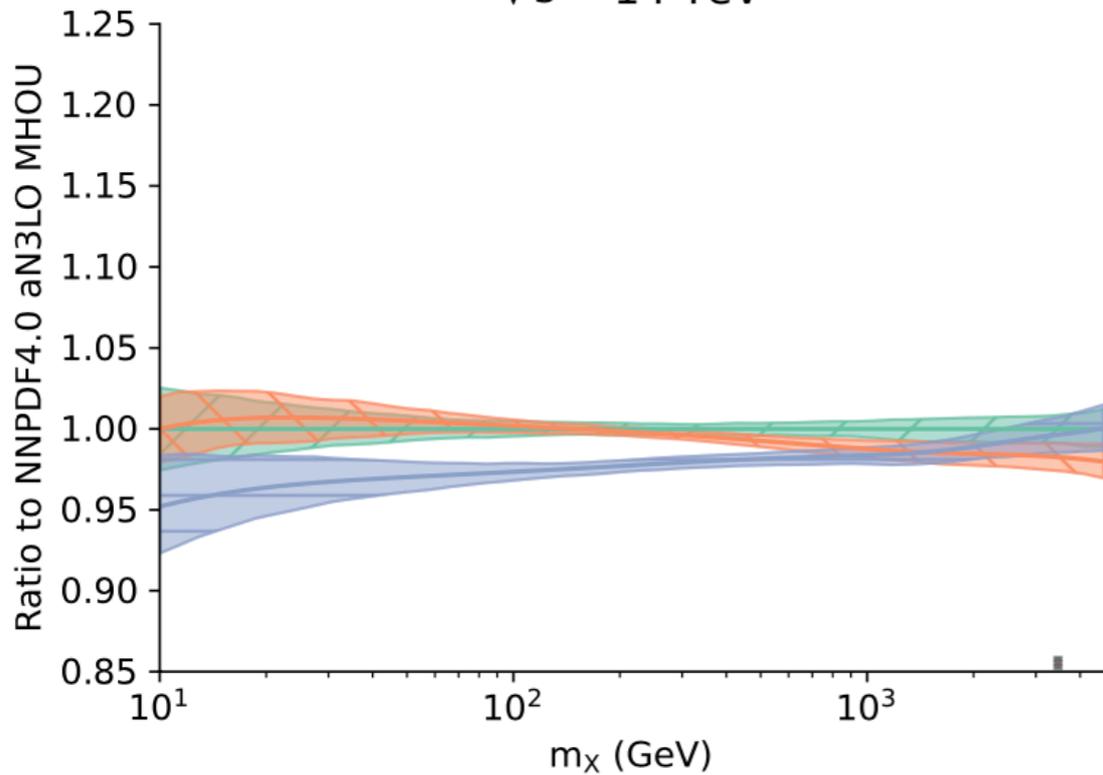


- Without MHOUs, the χ^2 improves with the perturbative accuracy of the PDF fit
- With MHOUs, the χ^2 becomes feebly dependent on the perturbative accuracy
- At aN³LO impact of MHOUs is small (also at PDF level) but non negligible

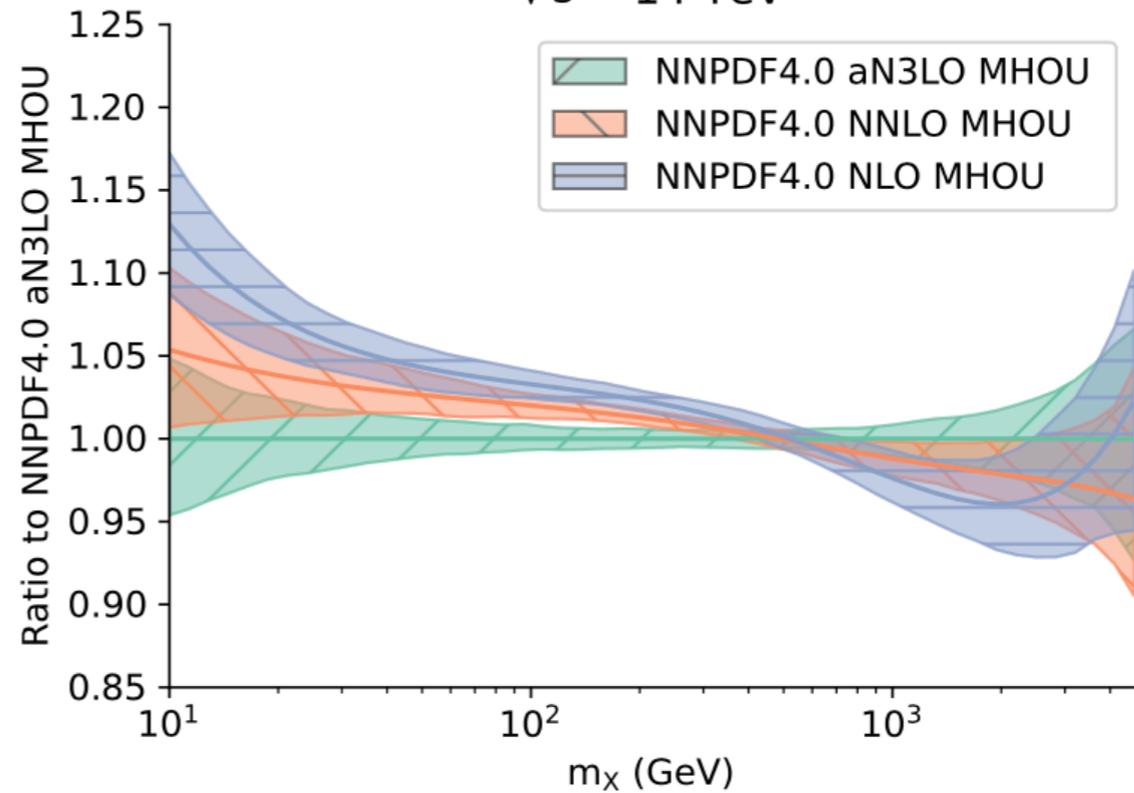
N³LO corrections required for perturbative convergence at the PDF fit level!

Results: perturbative convergence

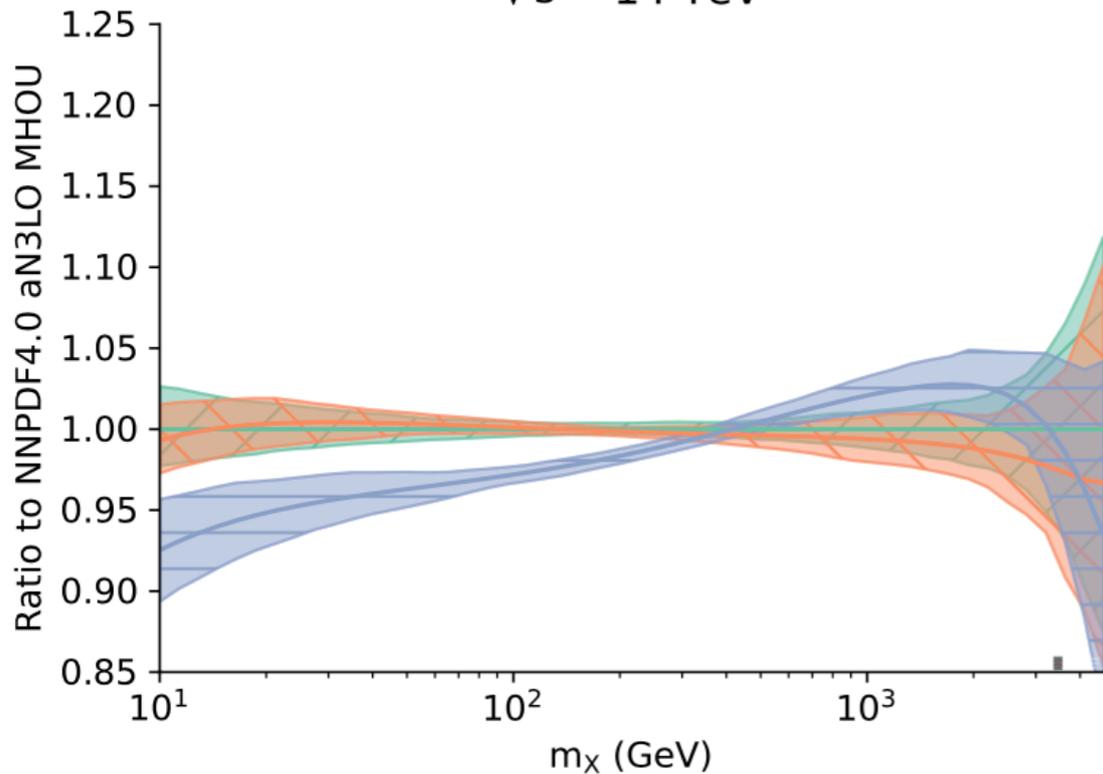
qq luminosity
 $\sqrt{s} = 14$ TeV



gg luminosity
 $\sqrt{s} = 14$ TeV



q \bar{q} luminosity
 $\sqrt{s} = 14$ TeV

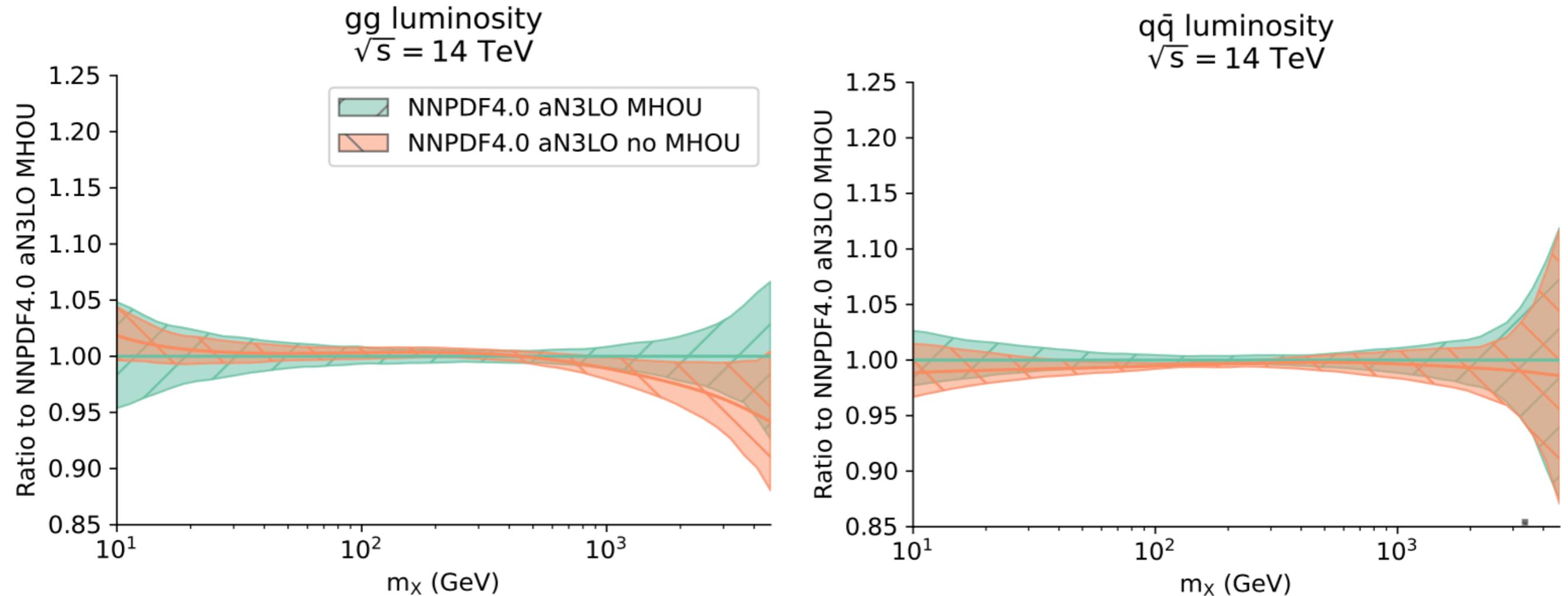


● **Good perturbative convergence**

● Impact of N³LO corrections moderate, specially for the quark luminosities

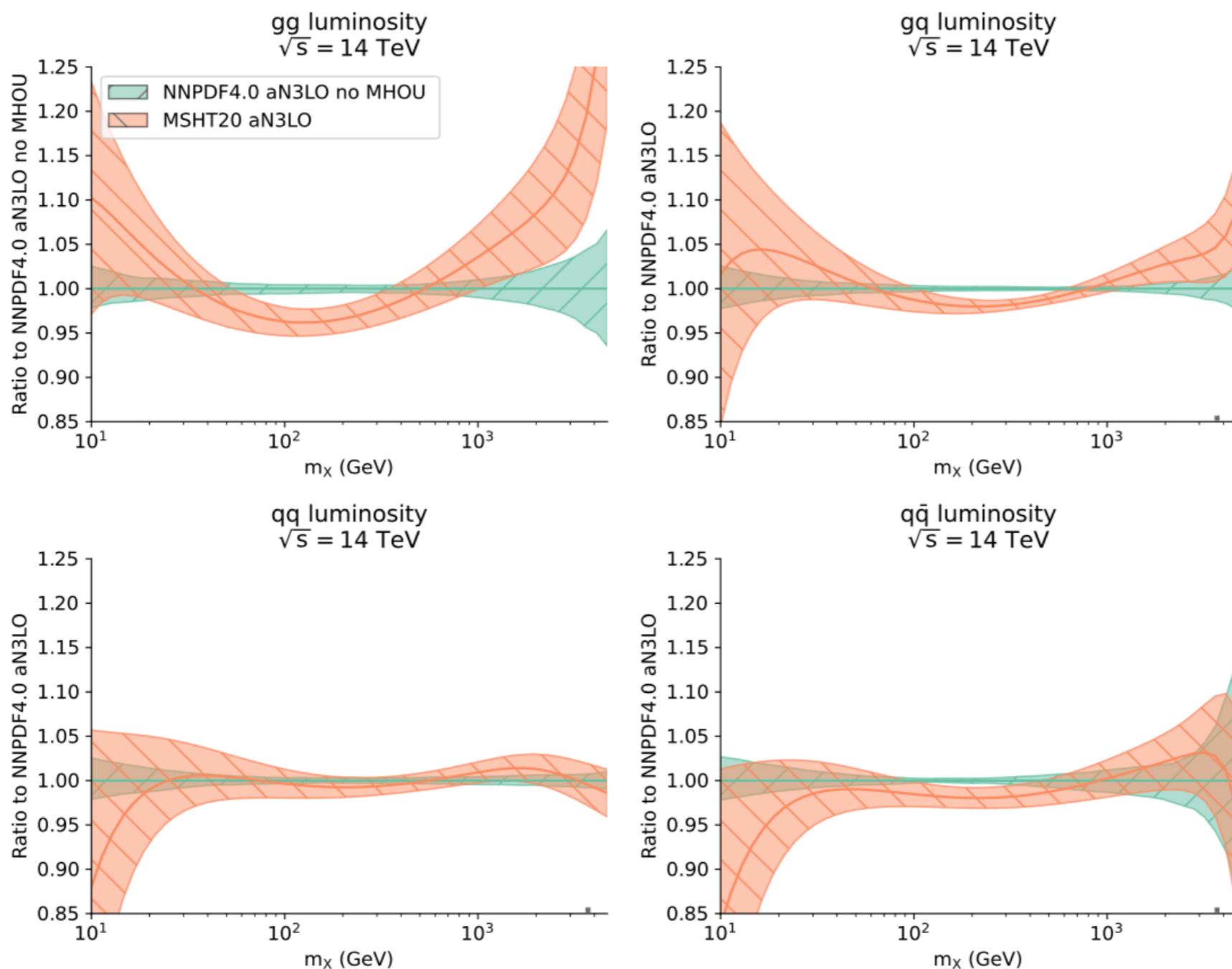
● For the gluon-gluon luminosity, NNPDF4.0 finds a **small suppression** around Higgs mass (2% effect)

Results: impact of MHOUs at N³LO



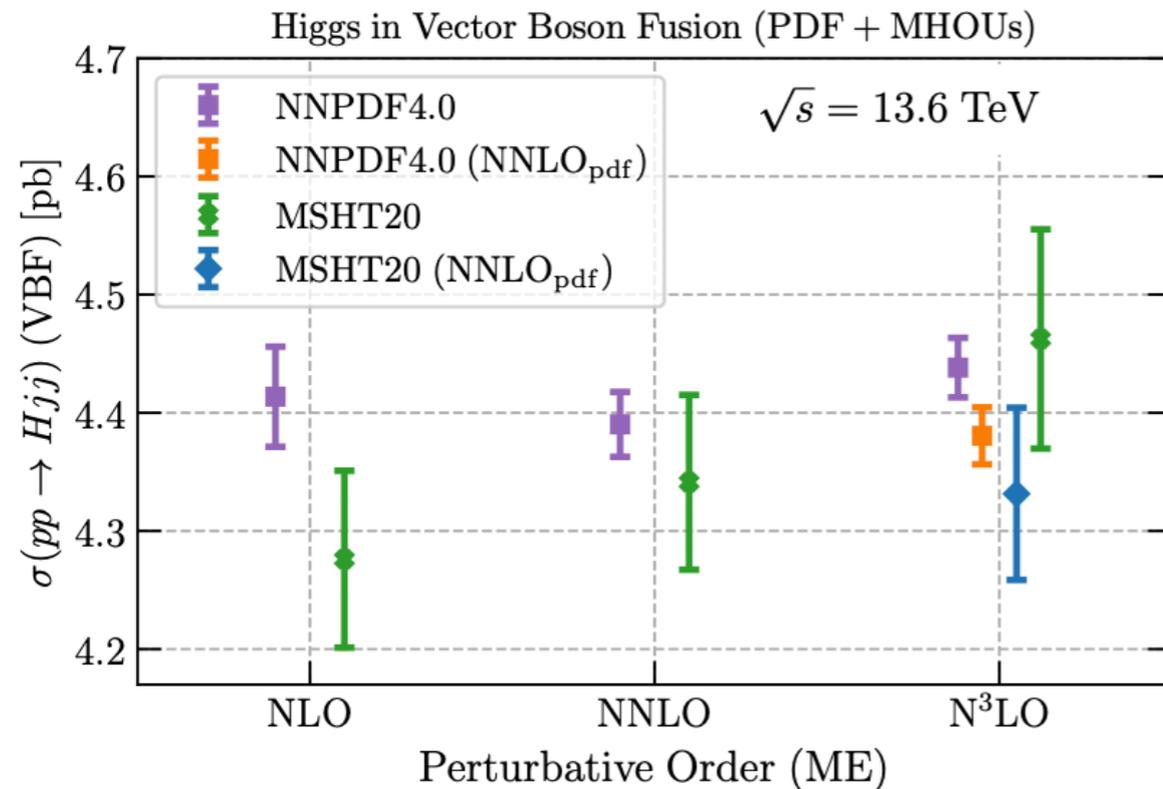
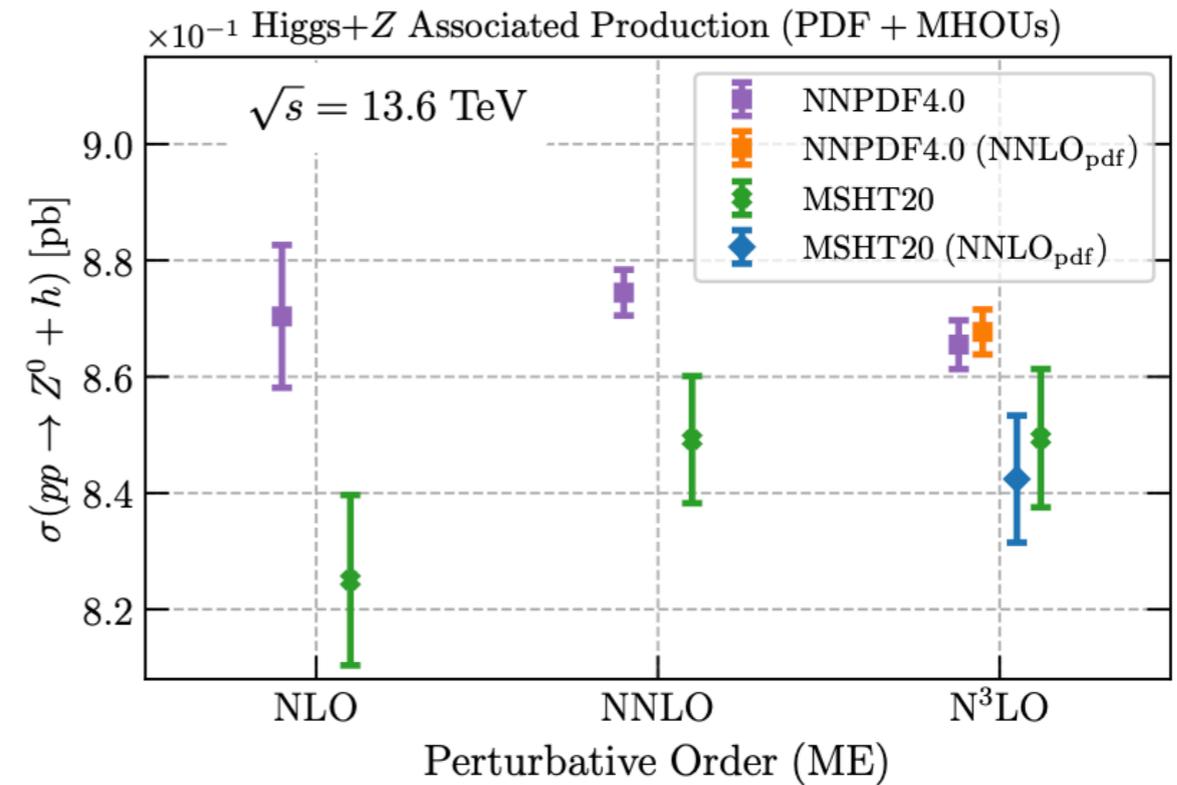
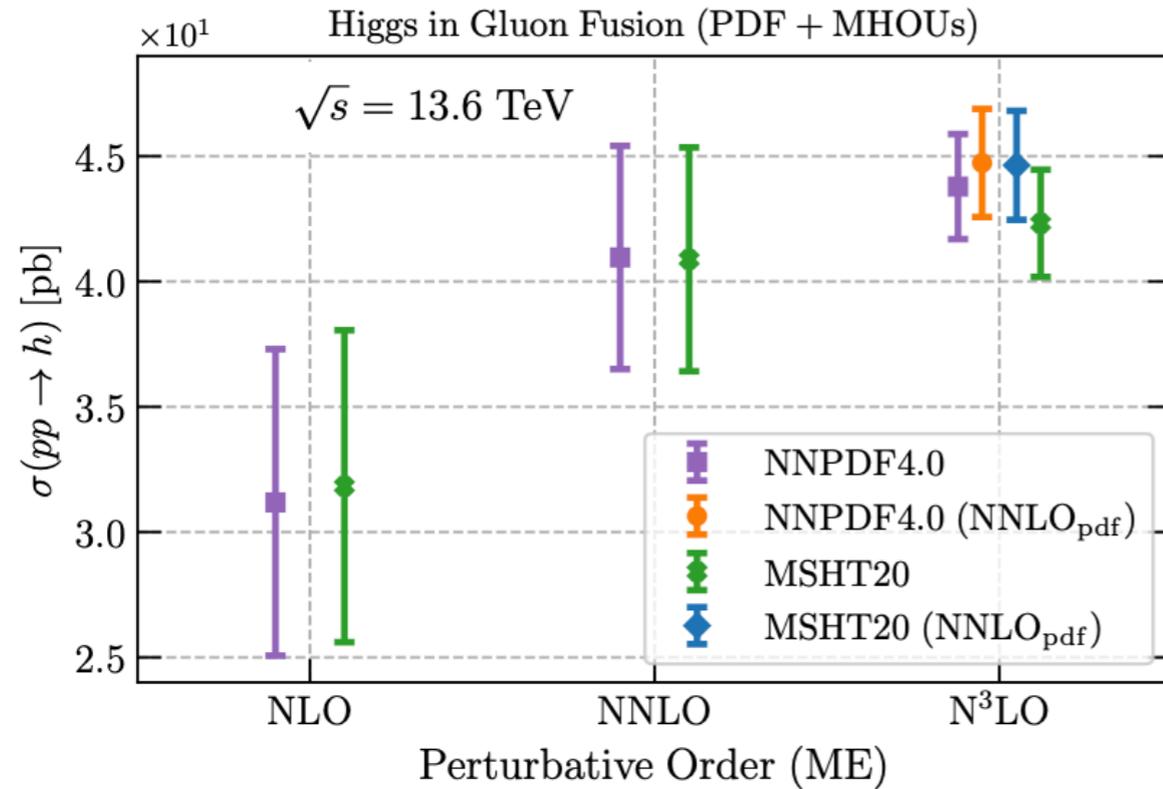
- 🔊 Impact of **MHOUs is not negligible** even at N³LO, both in terms of central values and uncertainties
- 🔊 Motivates inclusion of **exact N³LO calculations** for hadronic processes in the global PDF fit (*e.g.* Drell-Yan production, which is already available)
- 🔊 Further highlights the relevance of MHOUs also for NNLO and NLO fits

Results: comparison with MSHT20



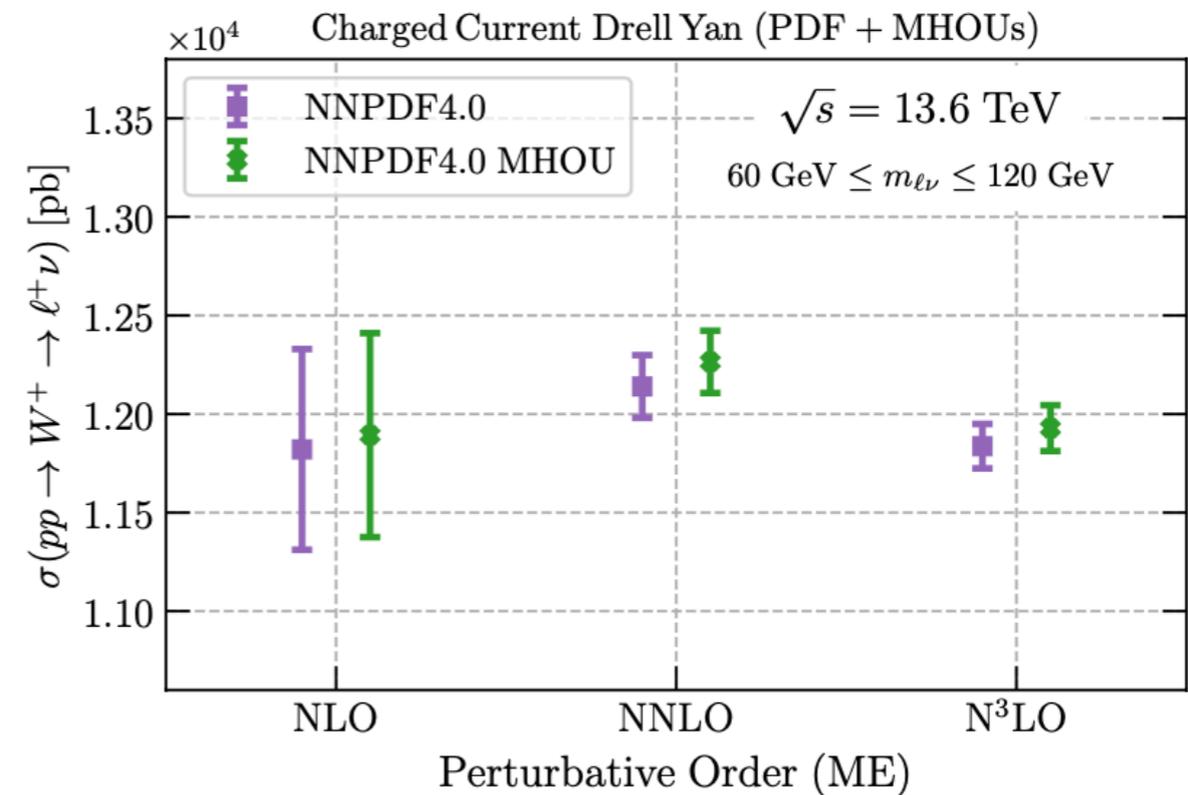
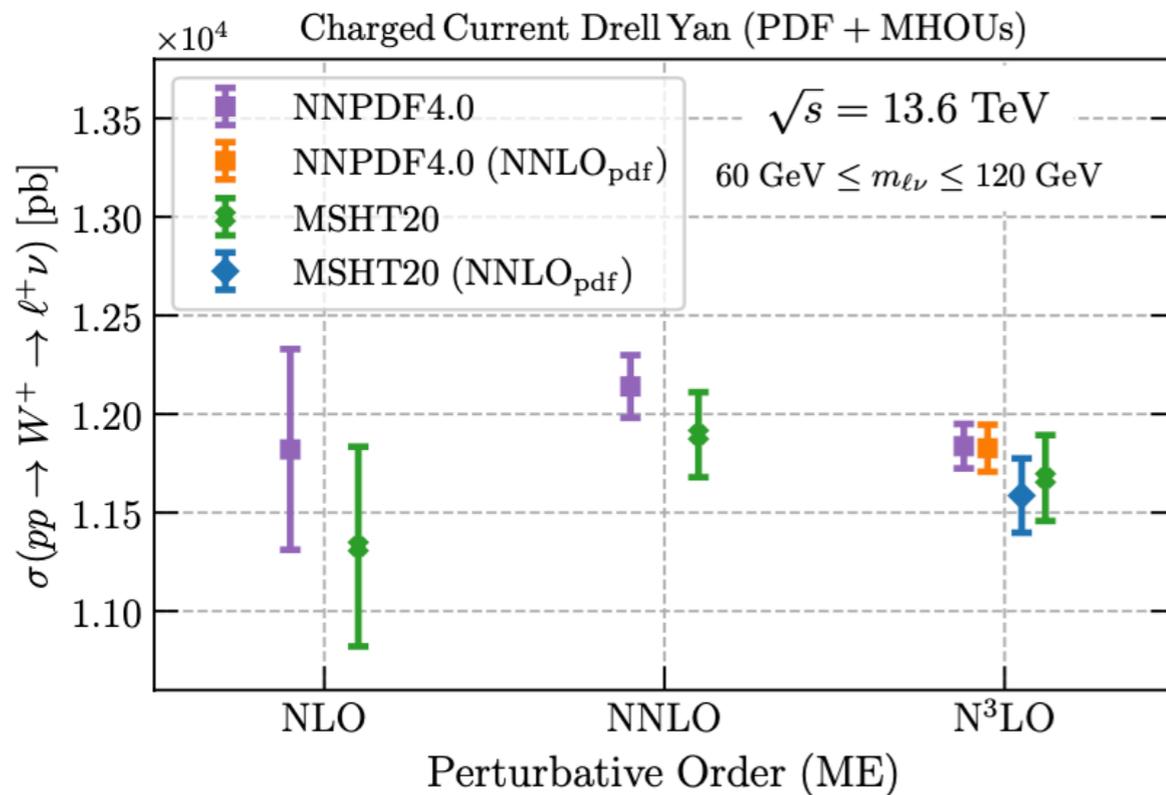
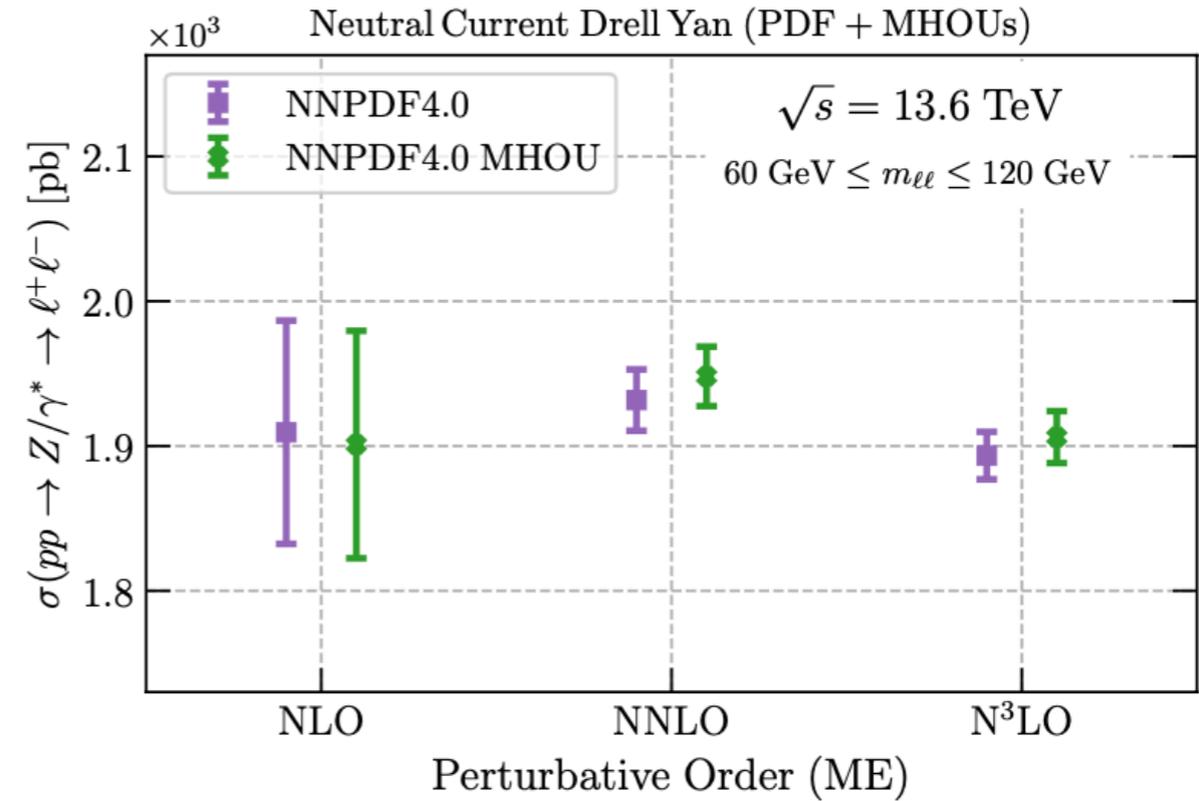
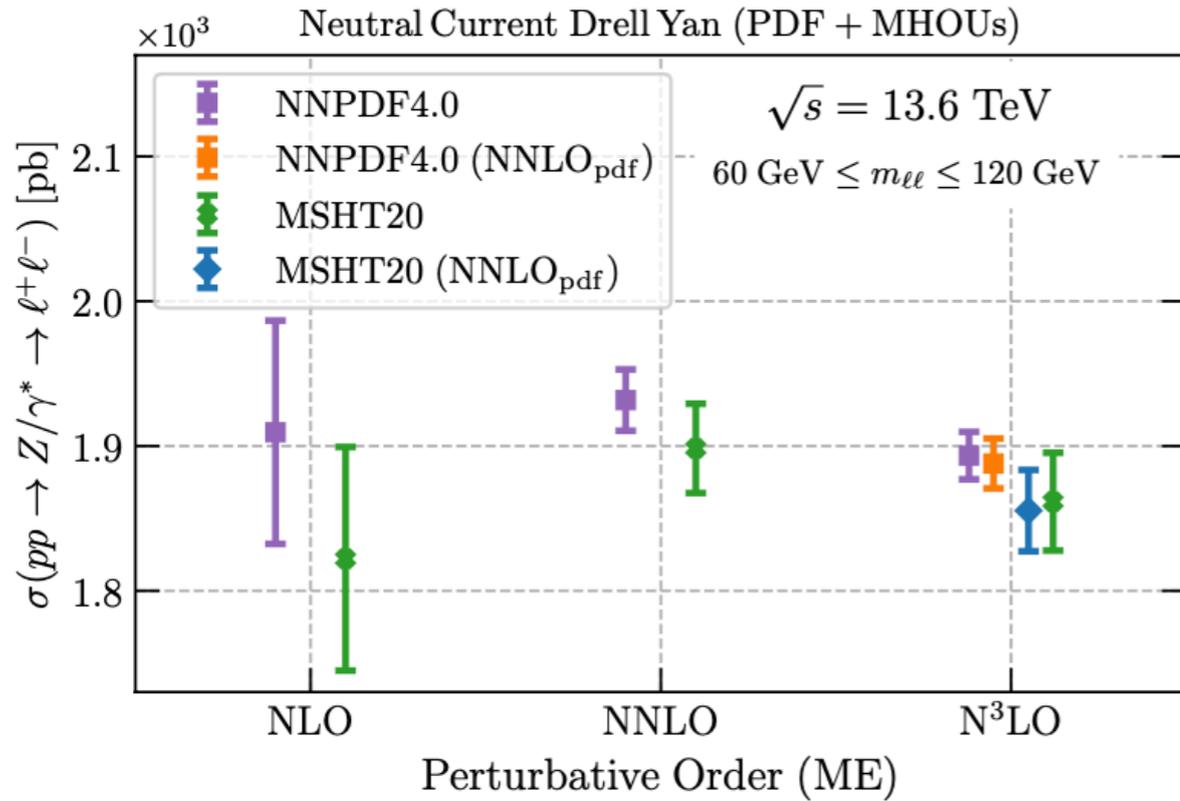
- **Good agreement** with MSHT20 for the quark luminosities
- Likewise for the gluon luminosities, except **around the Higgs mass** and for **$m_\chi > 3$ TeV**
- Ongoing benchmark exercise to understand the differences
- In general, agreement between NNPDF4.0 and MSHT20 tends to **improve in the N³LO fits**

LHC phenomenology: Higgs production



- N³LO PDF corrections to **Higgs in gluon fusion** **small**, with a 1.5% suppression wrt NNLO PDFs
- N³LO corrections improve agreement between NNPDF4.0 and MSHT20 for **hZ**
- **Higgs VBF** perturbatively stable

LHC phenomenology: Drell-Yan



Good perturbative convergence at N³LO also for **quark-initiated processes**

Summary and outlook

- ☑ A key ingredient to **LHC phenomenology at 1% precision** are $N^3\text{LO}$ PDFs which account for all sources of theory uncertainties
- ☑ The new NNPDF4.0 $aN^3\text{LO}$ determination enables **consistent $N^3\text{LO}$ calculations** of LHC cross-sections. An initial study suggests good perturbative convergence for inclusive **Higgs** and **Drell-Yan production**
- ☑ Work in progress aims to **combine $aN^3\text{LO}$ PDFs with QED and MHOU** effects, study the phenomenological implications of the NNPDF4.0 family, and **determine precision SM parameters** such as the strong coupling constant
- ☑ Also steady progress in the implementation of new datasets and updated theory calculations (based on NNLO grid technology) **aiming to NNPDF4.1**
- ☑ Lots of progress in related projects, such as NNPDF4.0 for MC event generators and methodological studies. Stay tuned!

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Thanks for your attention