

# Partial N<sup>3</sup>LL + NNLO Resummed Predictions for the Drell-Yan Process in Rapidity Dependent Jet Veto Observables

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Based on work done in collaboration with Jonathan Gaunt (University of Manchester) and Shireen Gangal (University of Mumbai)

31<sup>st</sup> International Workshop on Deep Inelastic Scattering  
Grenoble, 10<sup>th</sup> April 2024



The University of Manchester

# Aims of Analysis

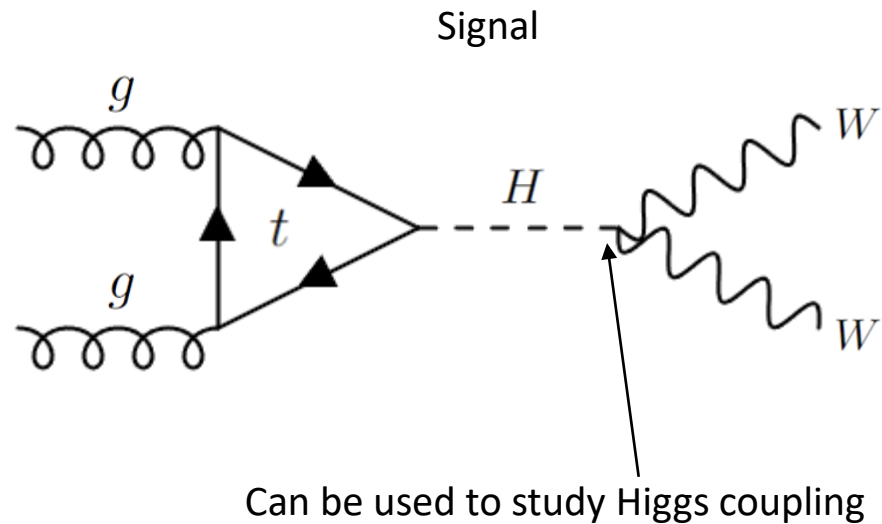
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- Produce partial N<sup>3</sup>LL + NNLO phenomenological predictions in the Drell-Yan process for two jet veto variables
- Demonstrate the benefit of resumming logarithms in these jet veto variables by comparing to fixed-order (FO) predictions

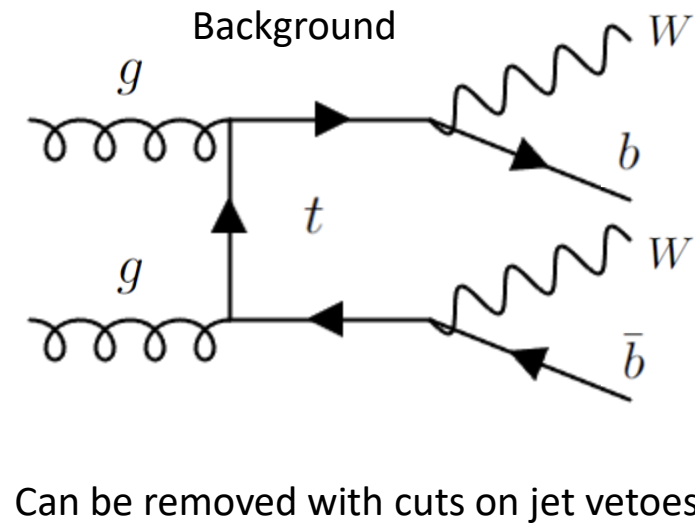
# Jet Vetoes

Class of observable used to separate final states by number of final state jets. A common jet veto is the leading jet transverse momentum  $P_{Tj}$ .

Can separate hard processes, cut out background events and study QCD radiation. For example:



Same initial states,  
final states differ  
by number of jets.

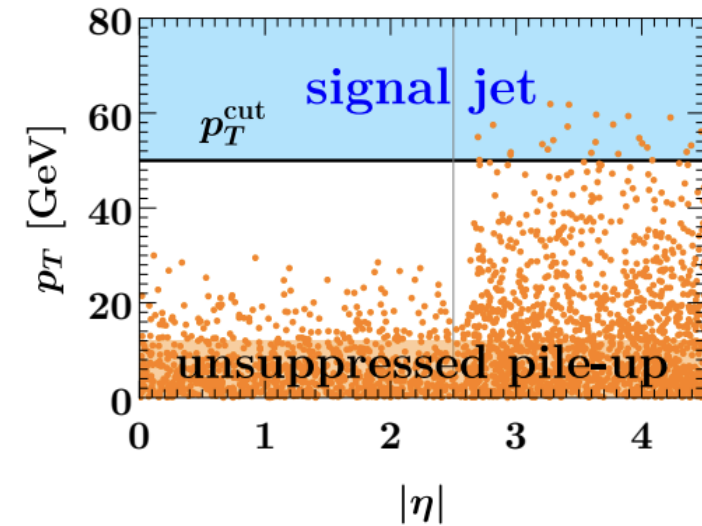


# Rapidity Dependent Jet Vetoes

Useful to control the tightness of the  $P_T$  cut depending on kinematics of jet.

Due to a lack of tracking information, high rapidity, low  $P_T$  jets are hard to resolve experimentally.

A rapidity dependent jet veto allows tighter  $P_T$  cuts in central rapidities and looser  $P_T$  cuts at forward rapidities to cut out these low  $P_T$  jets.



Michel, Pietrulewicz, Tackman, arXiv:1810.12911

$$\tau_f^{\text{jet}} = \text{Max}_{j \in J} | p_{Tj} | f(Y, y_j)$$

Rapidity of hard system

Rapidity of jet

# Rapidity Dependent Jet Vetoes

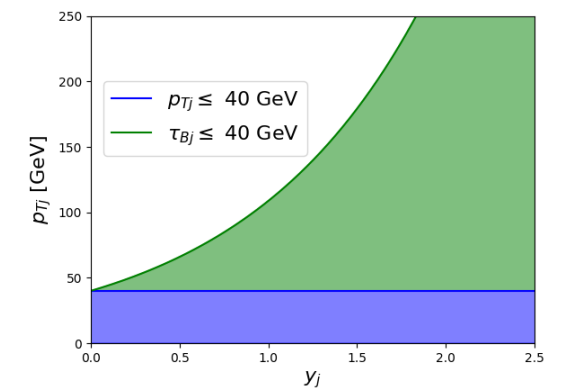
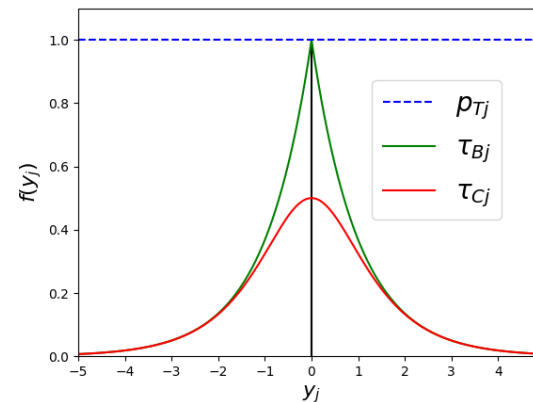
Study two of these based on the different weighing functions.

$\tau_B$  is tighter at central rapidities than  $\tau_C$  but they are equivalent at forward rapidities.

These jet vetoes are more inclusive of QCD radiation due to tight veto being over smaller range. Allows QCD radiation to be studied from a different point of view.

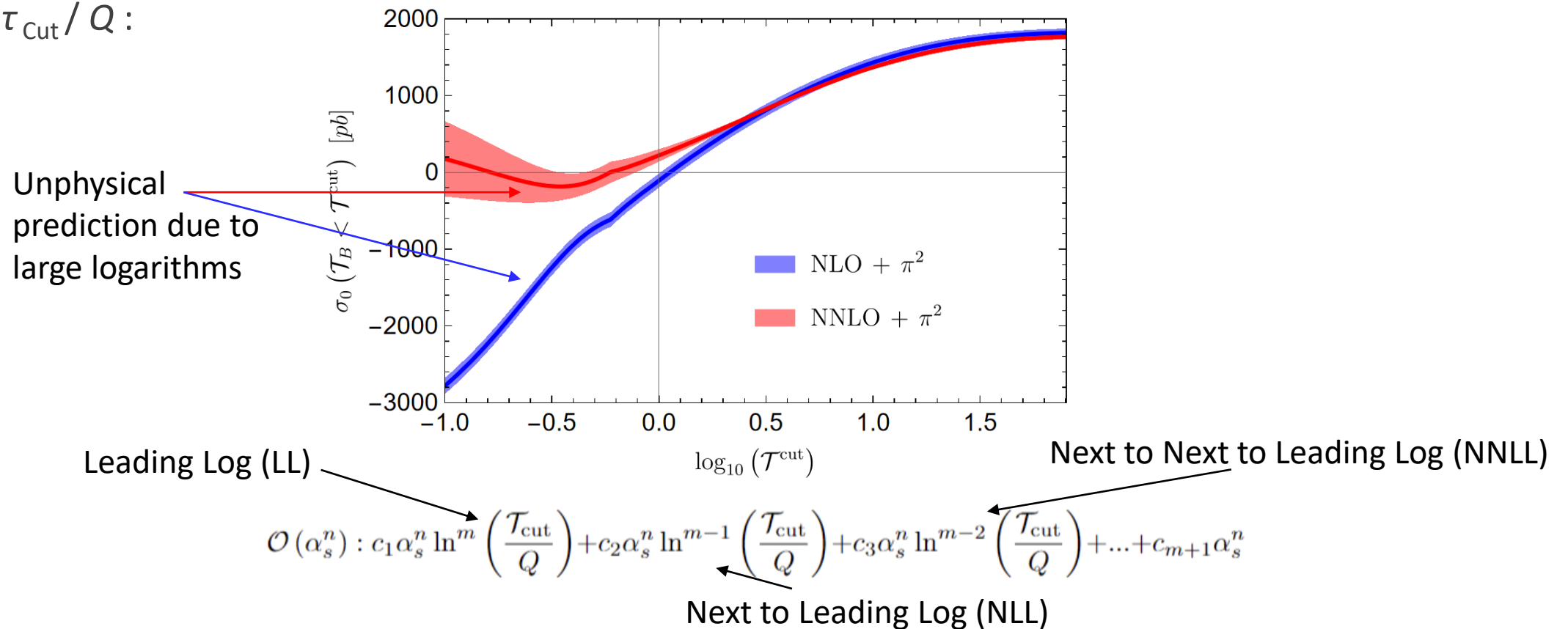
Tackmann, Walsh, Zuberi, arXiv:1206.4312  
Gangal, Stahlhofen, Tackmann, arXiv:1412.4792

$$\tau_B : f_B(Y, y_j) = e^{-|y_j - Y|}$$
$$\tau_C : f_C(Y, y_j) = \frac{1}{2 \cosh(y_j - Y)}$$



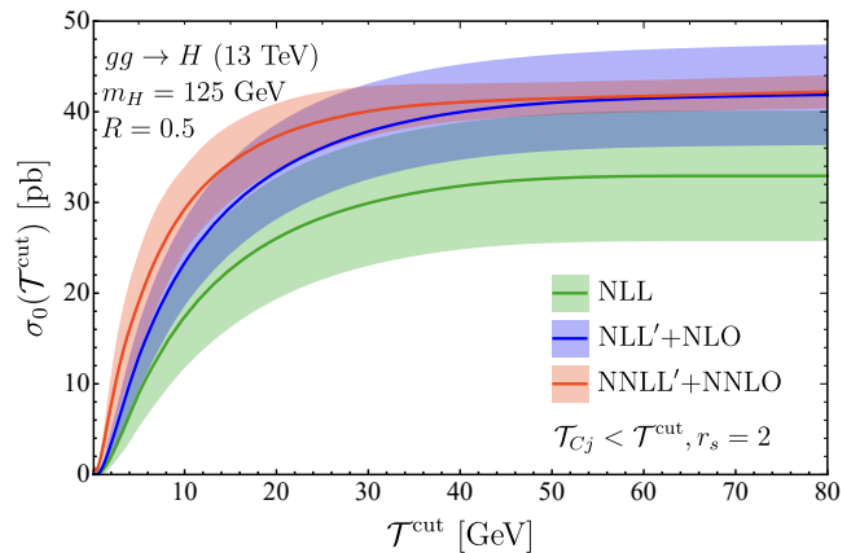
# Large Logarithms in Jet Vetoes

Often tight cuts on jet veto variables required. Leads to large logarithms in the FO predictions in  $\tau_{\text{cut}}/Q$ :

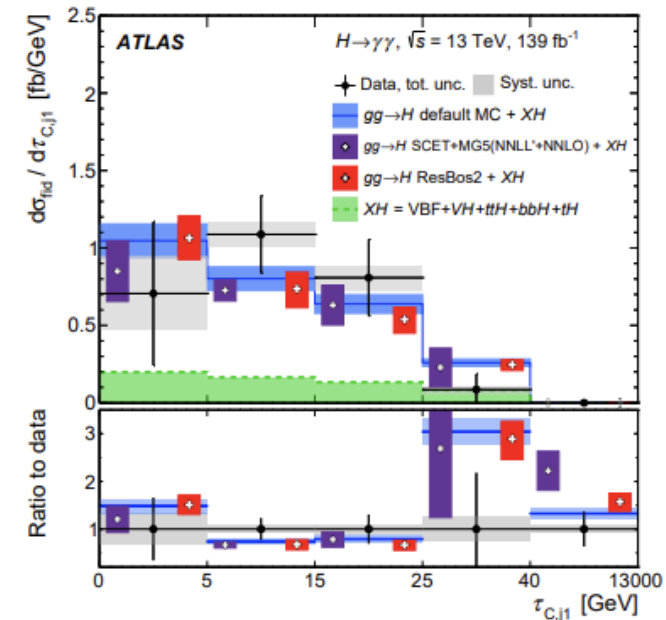


# Jet Veto Resummation Example: Higgs

Resummation of large logarithms in rapidity dependent jet vetoes for Higgs production has been produced and compared with experimental data.



Gangal, Gaunt, Tackmann, Vryonidou, arXiv:2003.04323



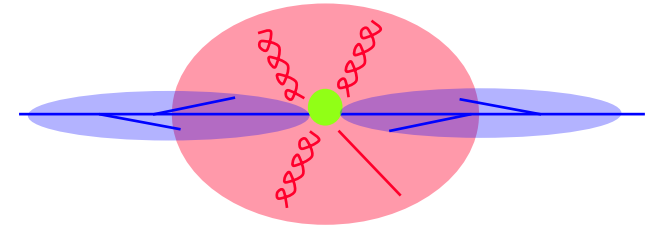
ATLAS collaboration, arXiv:2202.00487

N.B. see talk WG3 talk by Alessandra Cappati for CMS  $H \rightarrow ZZ$  results in  $\tau_B / \tau_C$

# Factorisation in Jet Vetoes

The below  $\tau_{\text{cut}}$  cross section can be factorised as follows for  $\tau_{\text{cut}} \ll Q$ :

$$H_{q\bar{q}}(Q, \mu) B_q(Q\mathcal{T}^{\text{cut}}, R, \mu) B_{\bar{q}}(Q\mathcal{T}^{\text{cut}}, R, \mu) S(\mathcal{T}^{\text{cut}}, R, \mu)$$



Tackmann, Walsh, Zuberi, arXiv:1206.4312

Gangal, Stahlhofen, Tackmann, arXiv:1412.4792

Gangal, Gaunt, Tackmann, Vryonidou, arXiv:2003.04323

Logarithms can be thought to come from each function in factorised cross section:

$$\ln^2\left(\frac{\mathcal{T}^{\text{cut}}}{Q}\right) = 2 \ln^2\left(\frac{Q}{\mu}\right) - \ln^2\left(\frac{Q\mathcal{T}^{\text{cut}}}{\mu^2}\right) + 2 \ln^2\left(\frac{\mathcal{T}^{\text{cut}}}{\mu}\right)$$



# Resummation in Jet Vetoes

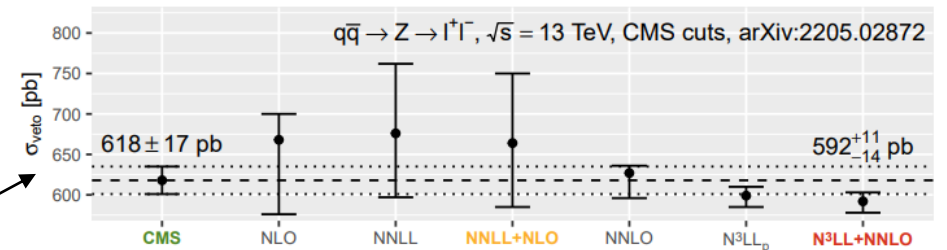
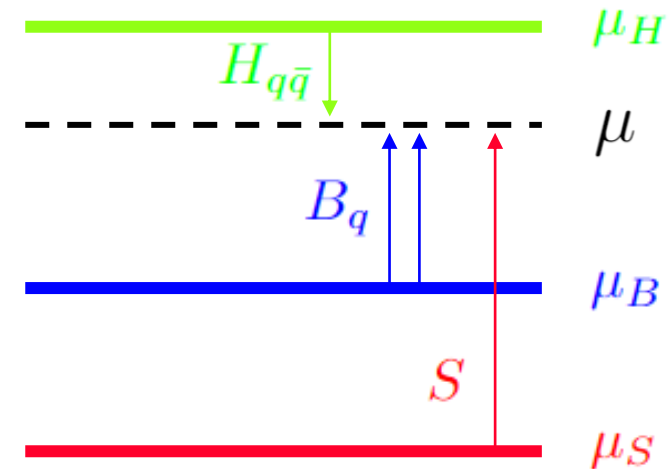
Can sum the logarithms by solving the RGE's of the functions in the factorisation formula.

Evolve all the scales to a common scale.

The goal precision is NNLL' +  $\pi^2$  (partial N<sup>3</sup>LL).

The results is matched to the FO +  $\pi^2$  cross section. The final precision is NNLL' + NNLO +  $\pi^2$  (n.b. State of the art for  $P_T$  veto is also partial N3LL).

Drell-Yan Ptj resummation at partial N3LL + NNLO compared with experimental data.



Campbell, Ellis, Neumann, Seth, arXiv:2301.11768

# Choice of Scales

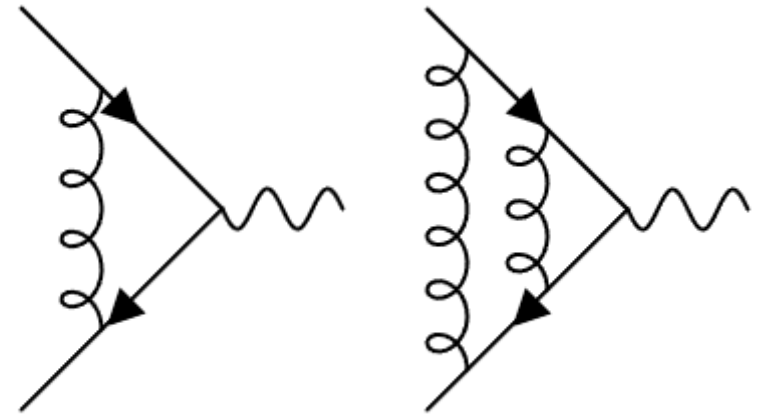
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For a particular value of  $\tau_{\text{cut}}$ , need to choose the beam, soft and hard scales.

Hard scale chosen to sum time-like logarithms ( $\pi^2$  resummation):

$$\mu_H = -i\mu_{FO}$$

Form of processes  
resummed by  $\pi^2$   
resummation  $\longrightarrow$



See e.g. Ahrens, Becher, Neubert, Yang, arXiv:0808.3008,0809.4283

The factorisation scale is generally taken to be equal to the beam scale.

# Choice of Scales

Non-perturbative region

$$\mathcal{T}_{\text{cut}} \sim \Lambda_{\text{QCD}}$$

'Freezing scale'  $\rightarrow \mu_0 > \Lambda_{\text{QCD}}$

$$\mu_S \sim \mu_0$$

$$\mu_B \sim \sqrt{\mu_S \mu_0}$$

Resummation region (Canonical scaling)

$$\mathcal{T}_{\text{cut}} \ll Q$$

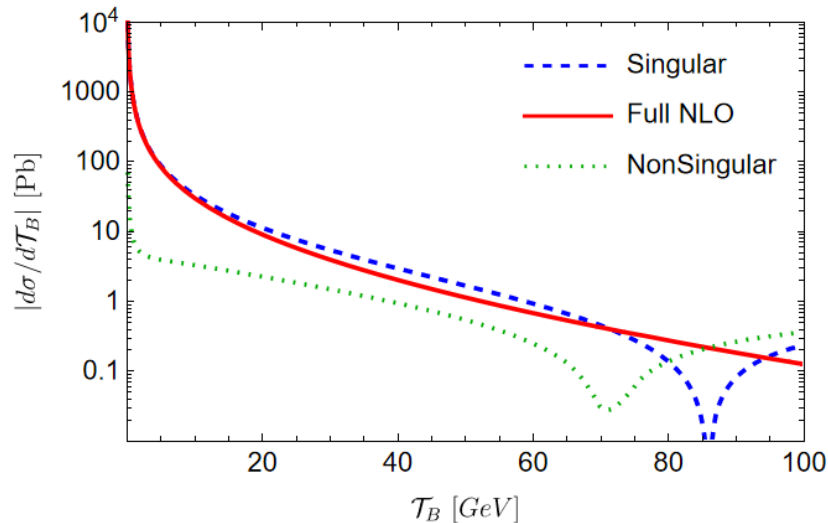
$$\mu_S \sim \mathcal{T}_{\text{cut}}$$

$$\mu_B \sim \sqrt{Q \mathcal{T}_{\text{cut}}}$$

Fixed-order region

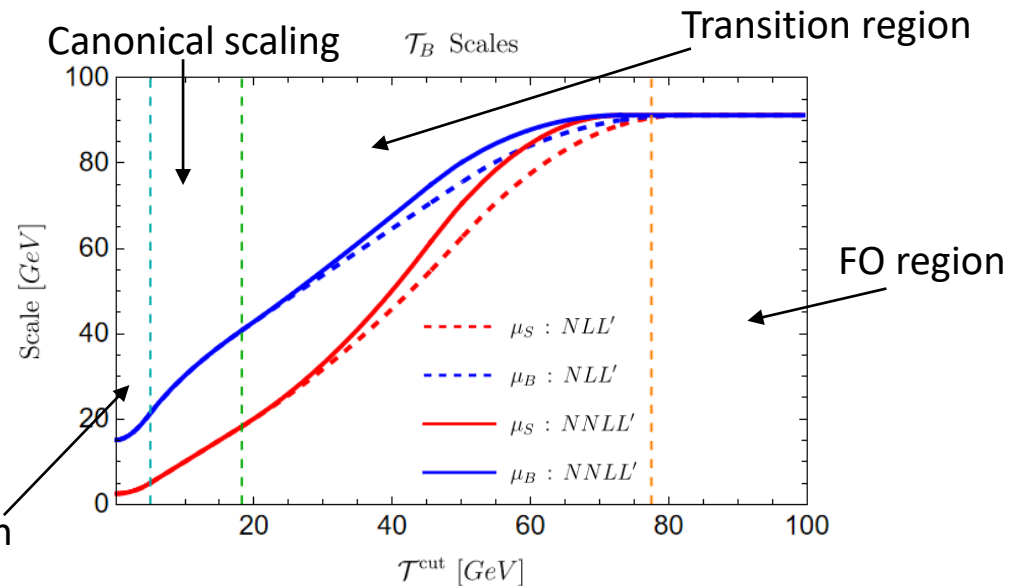
$$\mathcal{T}_{\text{cut}} \sim Q \sim \mu_{\text{FO}}$$

$$\mu_S, \mu_B \sim Q \sim \mu_{\text{FO}}$$



Used to determine

Non-perturbative region



# Scale Variations

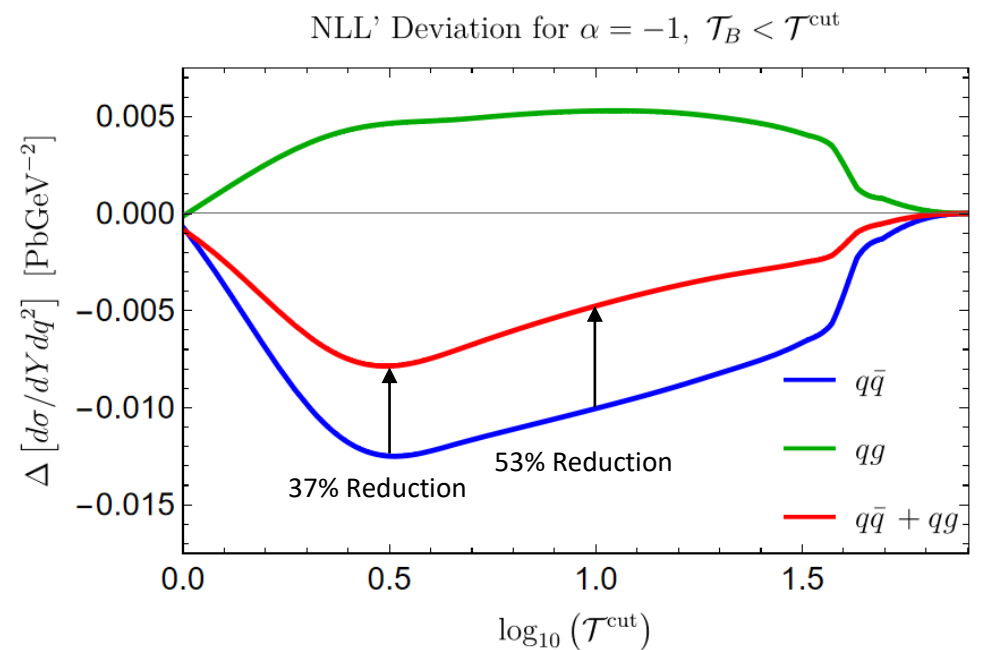
Standard FO variations are used:

$$\mu_{\text{FO}} = \left\{ \frac{1}{2}M_Z, M_Z, 2M_Z \right\}$$

Profile scales are varied using two parameters ( $\alpha, \beta$ ) that lead to  $\sim 2$  variation in the beam and soft scales and variation in the canonical beam scaling.

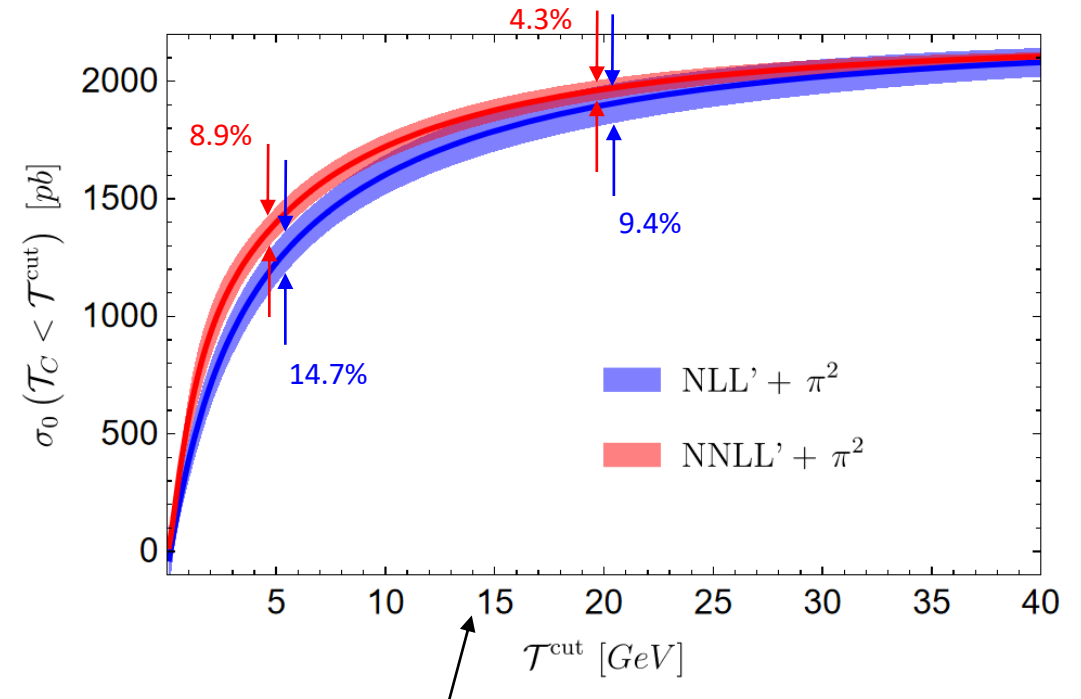
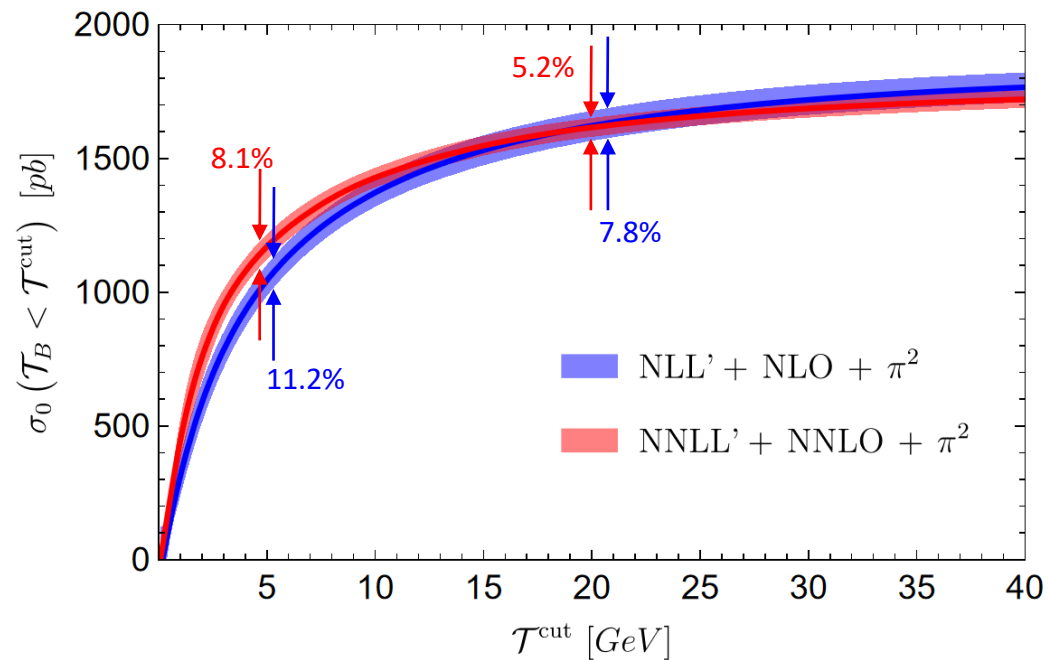
Cancellation between the  $q\bar{q}$  and  $qg$  channel variations led to only the  $q\bar{q}$  channel's beam scale being varied.

This cancellation was larger for NLL' than NNLL'.



# Jet Veto Predictions for Drell-Yan

$R = 0.5$      $80\text{GeV} \leq Q \leq 100\text{GeV}$



PRELIMINARY

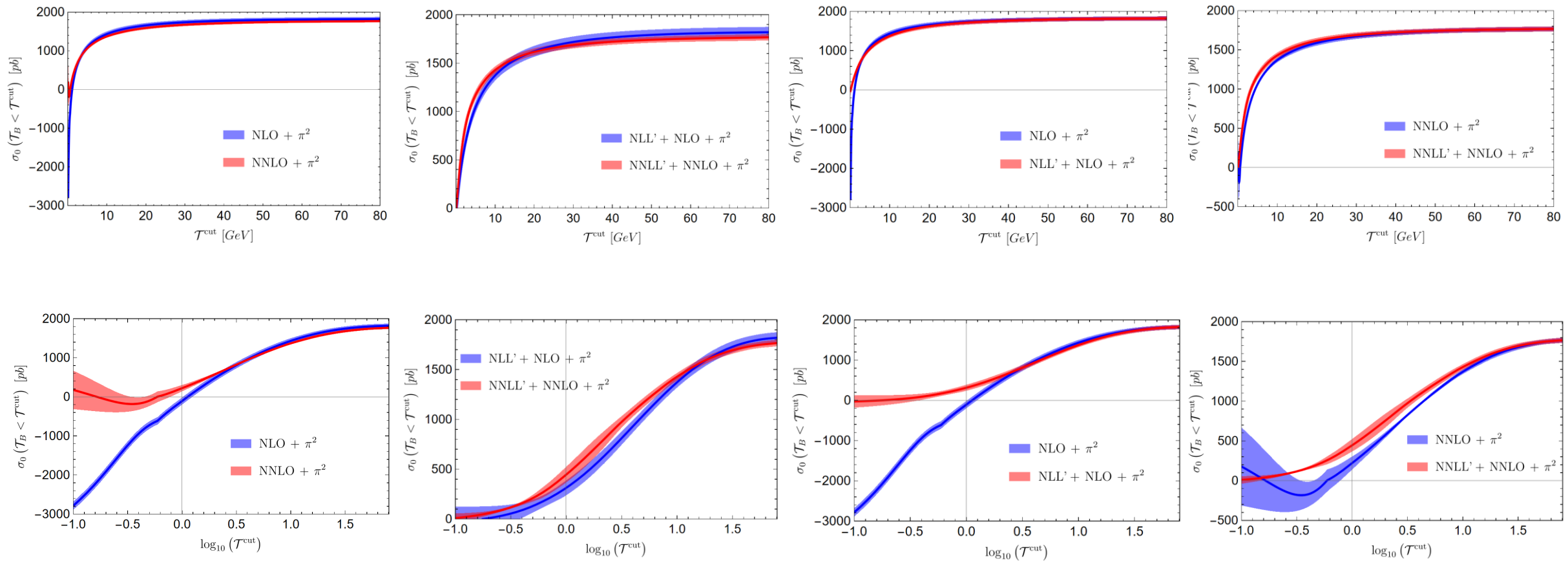
Needs to be matched to FO, to come very soon!

# Summary

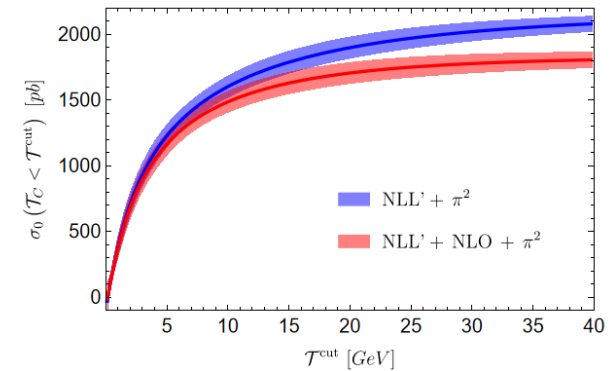
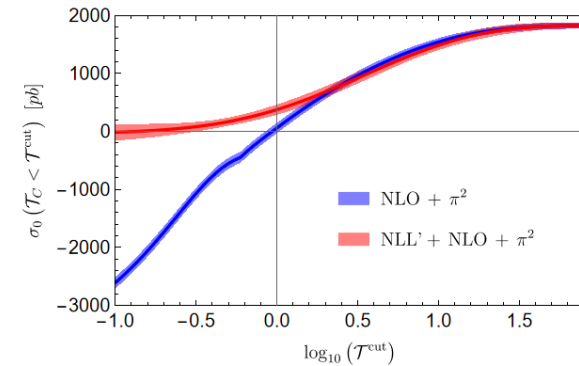
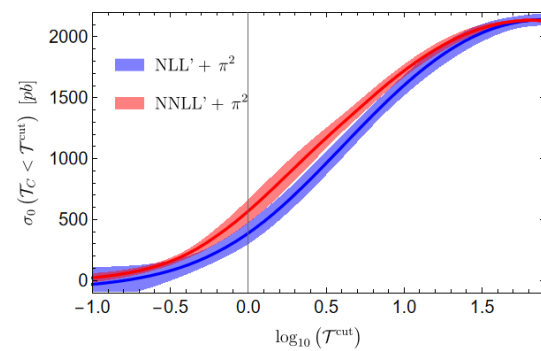
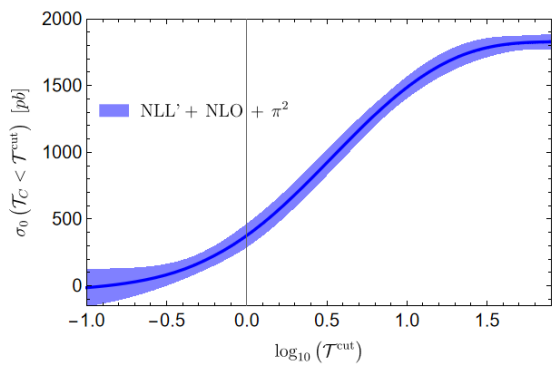
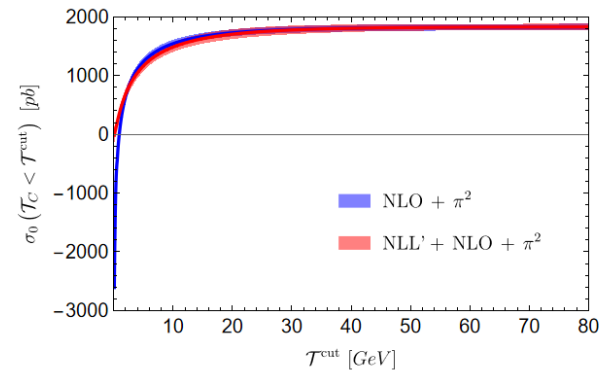
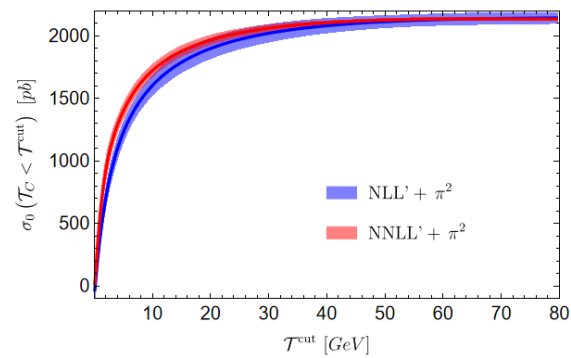
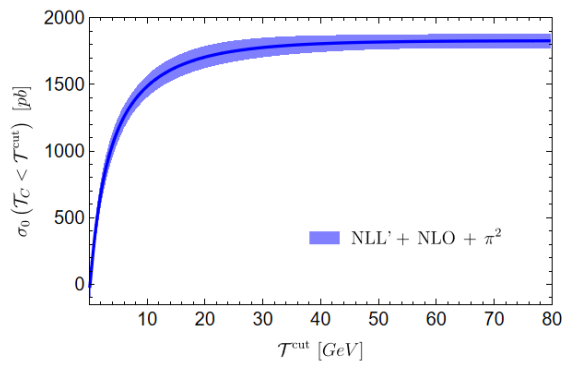
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- Produced cutting edge  $\text{NLL}' + \text{NLO} + \pi^2$  and  $\text{NNLL}' + \text{NNLO} + \pi^2$  predictions for  $\tau_B$
- Produced cutting edge  $\text{NLL}' + \pi^2$  and  $\text{NNLL}' + \pi^2$  predictions for  $\tau_c$ , in the process of matching to FO
- Demonstrated the need to perform resummation when tight cuts on  $\tau_B$  produce unphysical FO predictions
- The next key step is to compare these high precision results against experimental data

# Additional: All final plots $\tau_B$



# Additional: All final plots $\tau_C$





# Additional: Parameter Values

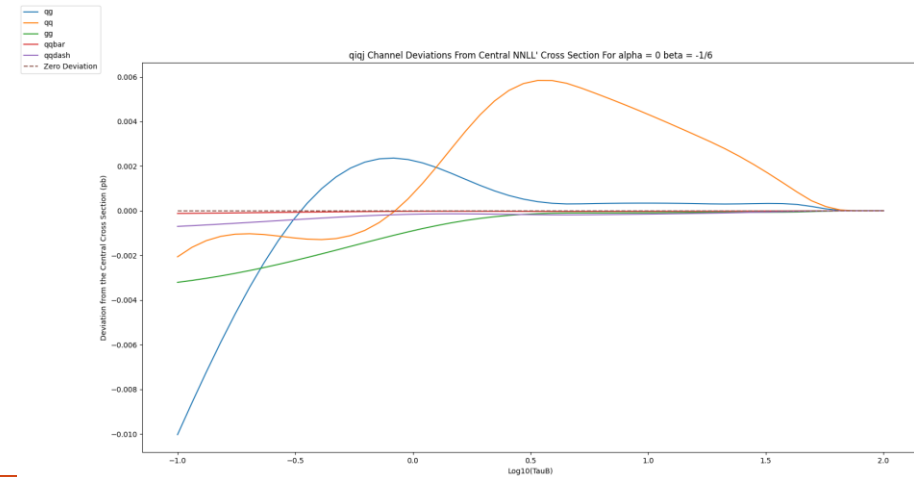
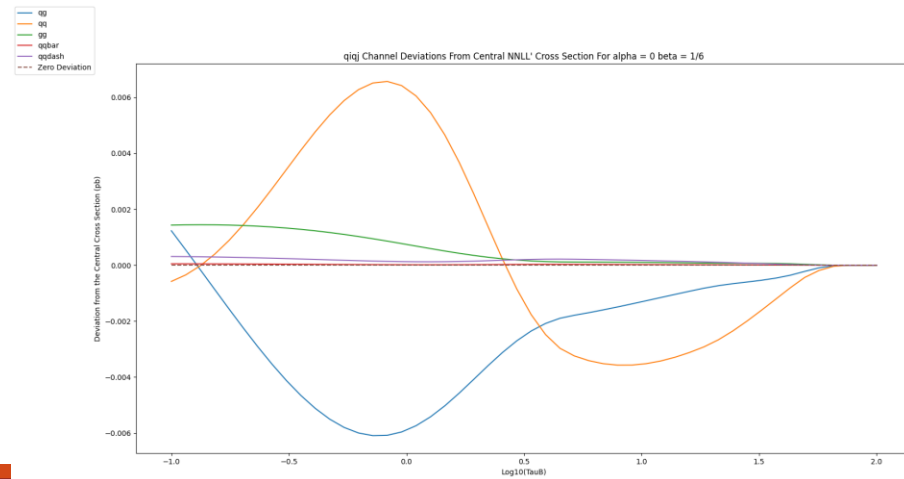
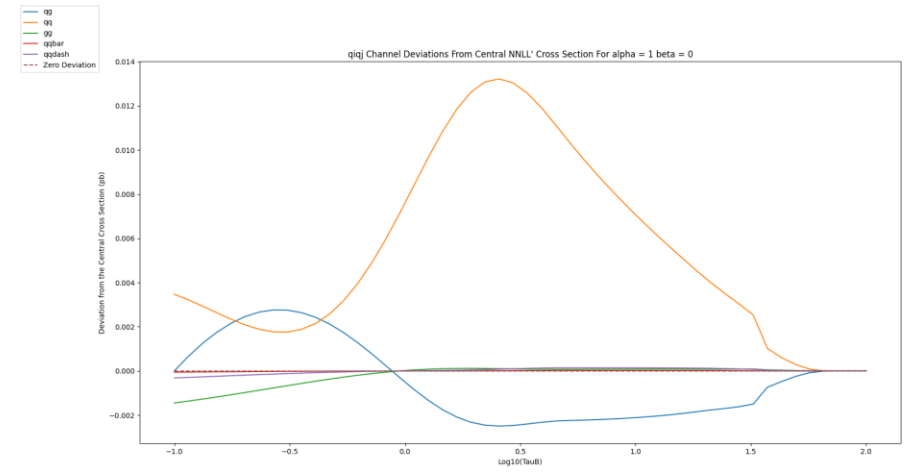
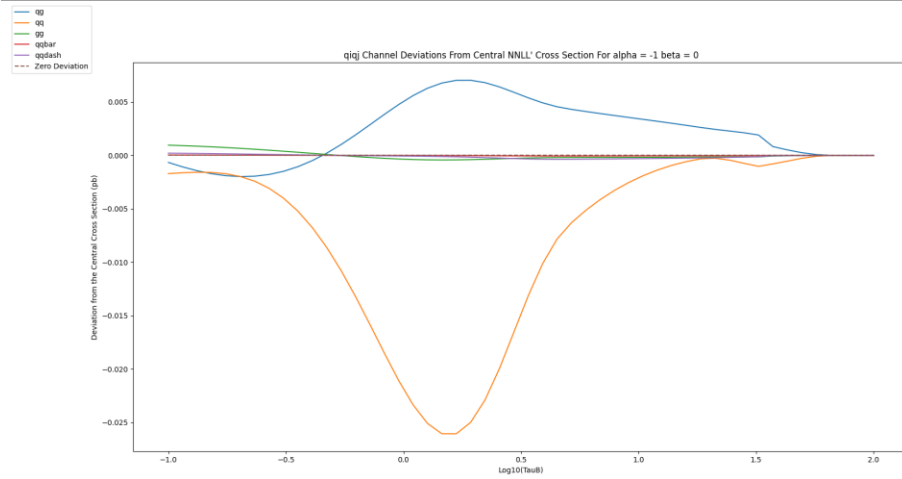
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Description	Parameter	Value	Unit
Z boson mass	$M_Z$	91.1876	GeV
Z boson width	$\Gamma_Z$	2.4952	GeV
Centre of mass energy	$E_{\text{COM}}$	13	TeV
Jet Radius	$R$	0.5	N/A
Sin squared of weak mixing angle	$\sin^2(\theta_W)$	0.22301383694753507	N/A
Fine structure constant	$\alpha_{\text{EM}}$	0.0075652121285480845	N/A
NLO strong coupling at $M_Z$	$\alpha_s^{\text{NLO}}(M_Z)$	0.120	N/A
NNLO strong coupling at $M_Z$	$\alpha_s^{\text{NNLO}}(M_Z)$	0.118	N/A

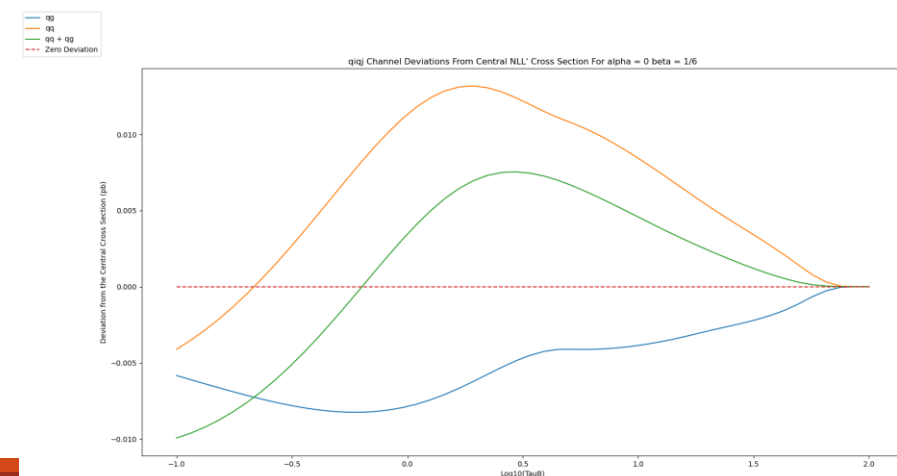
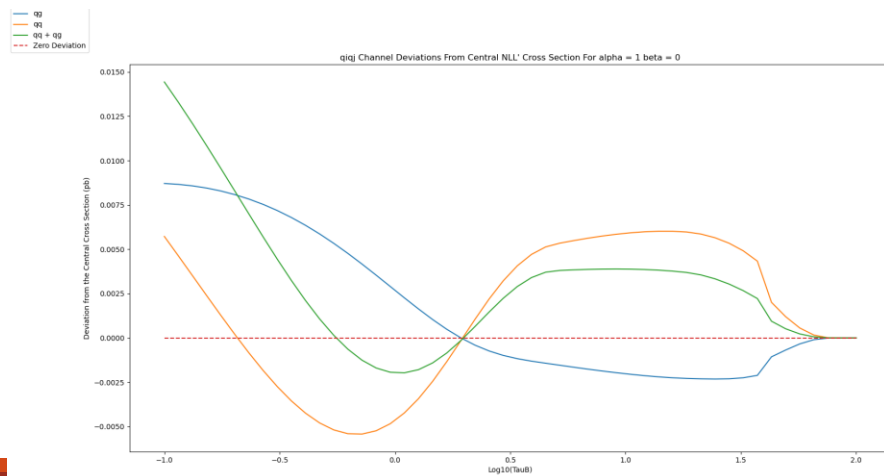
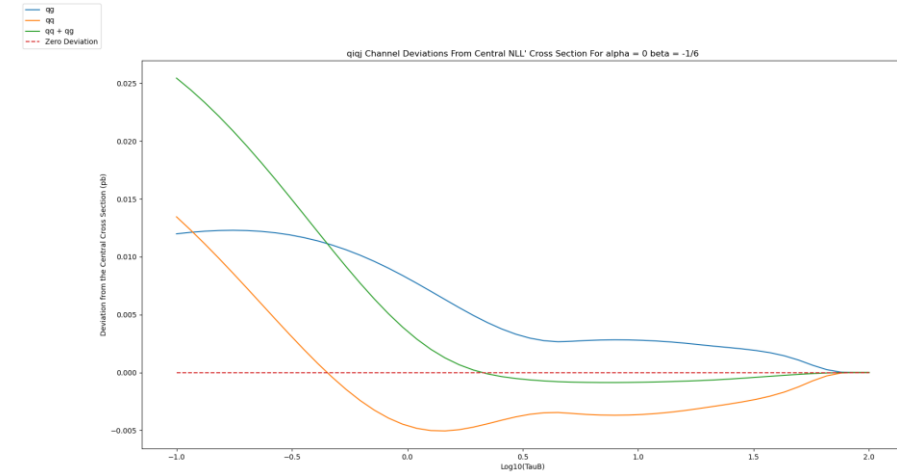
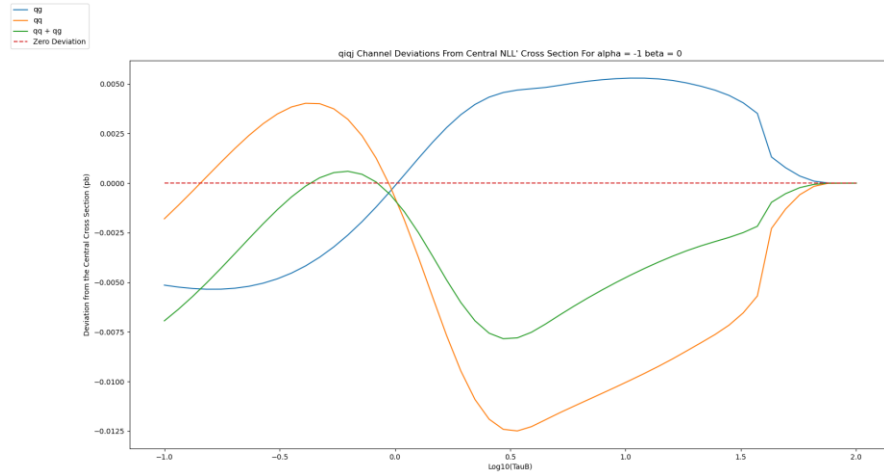
PDF Set for NLL' + NLO: MSHT20nlo\_as120

PDF Set for NNLL' + NNLO: MSHT20nnlo\_as118

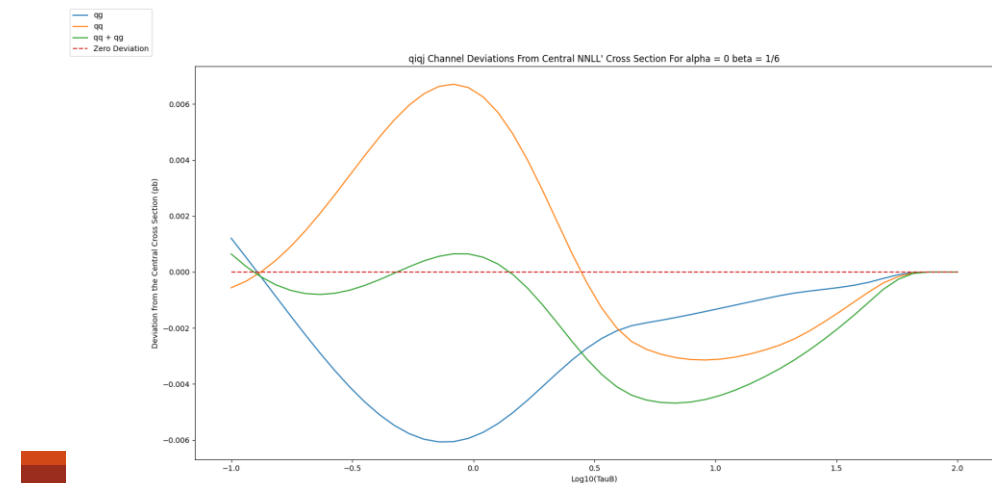
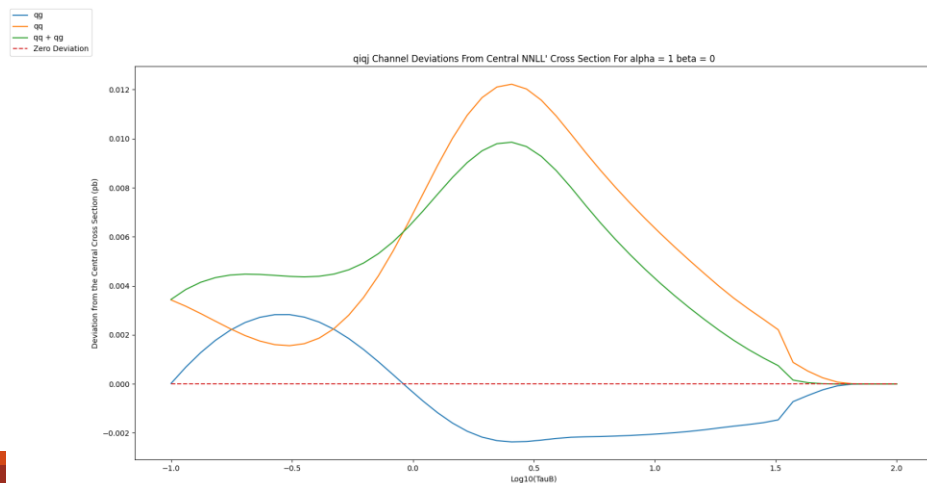
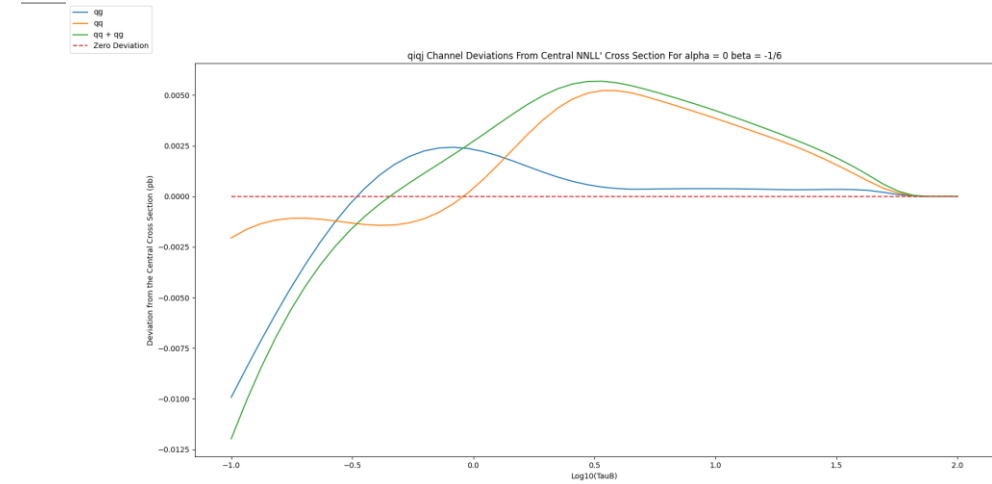
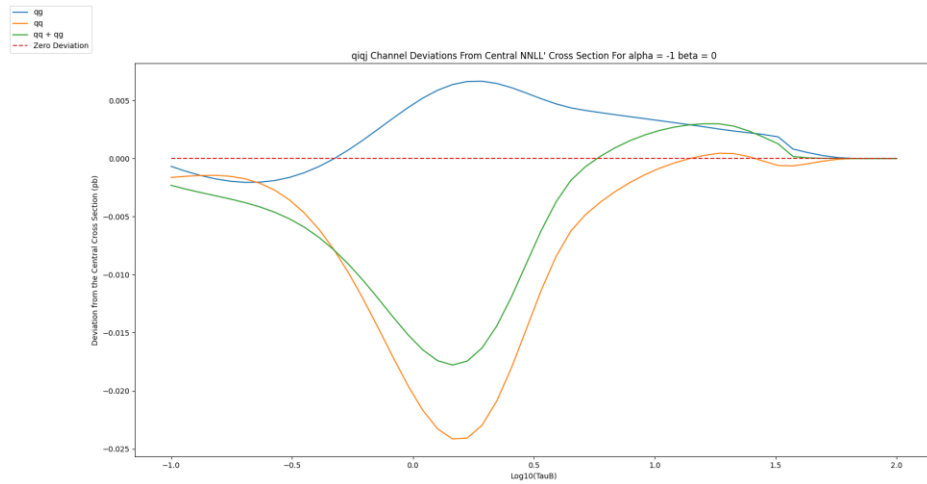
# Additional: qiqj Channel Breakdown



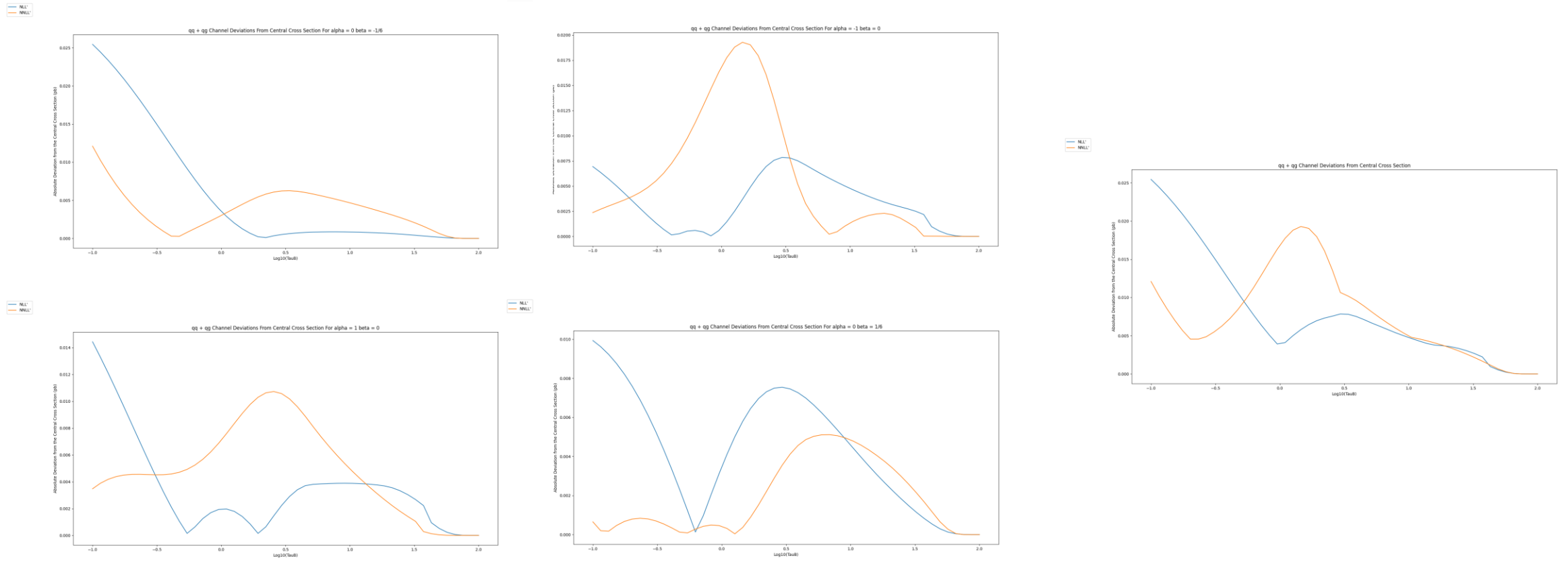
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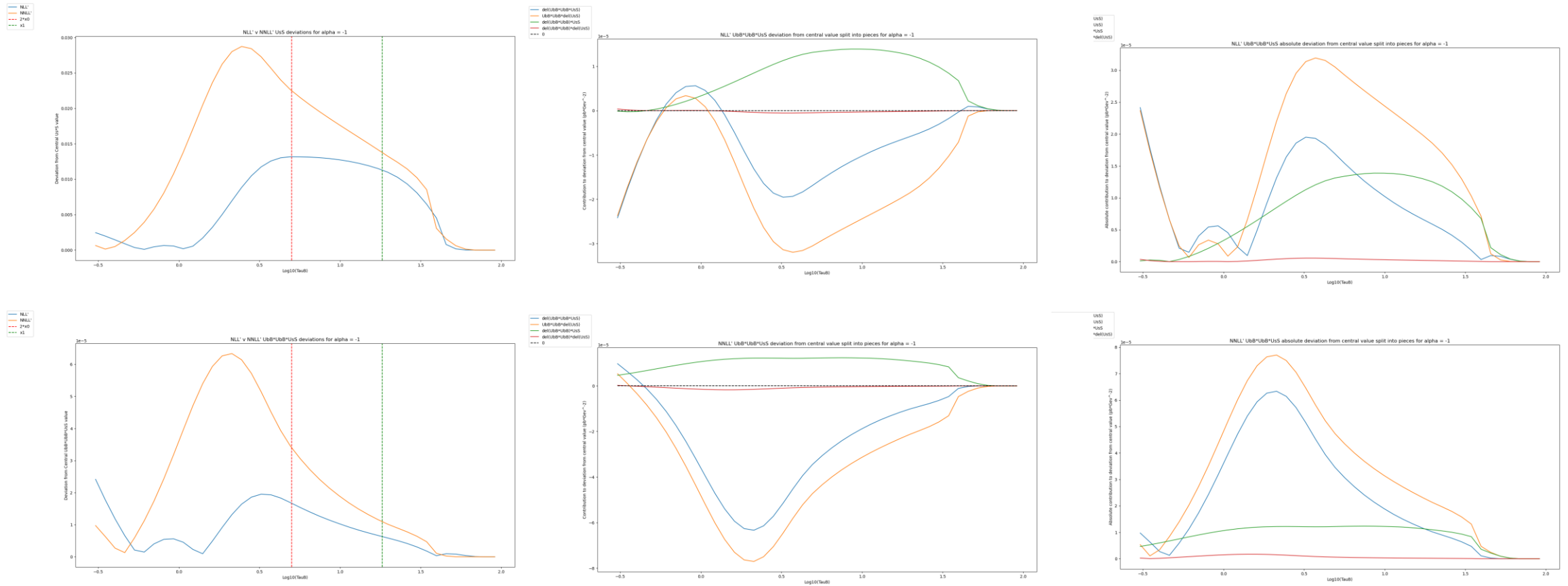
# Additional: qiqj Channel Breakdown



# Additional: qiqj Channel Breakdown



# Additional: Factorisation Formula Error Breakdown $\alpha = -1$



# Additional: Factorisation Formula Error Breakdown alpha = 1

