### Phenomenology of TMD distributions in Drell-Yan and Z<sub>0</sub> boson production with the Hadron Structure Oriented approach

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#### Based on

#### Phenomenology of TMD parton distributions in Drell-Yan and Z<sup>0</sup> boson production in a hadron structure oriented approach

#### (ArXiv:2401.14266)

• (F. Aslan, M. Boglione, J. O. Gonzalez-Hernandez, T. Rainaldi, T. C. Rogers, A. Simonelli)

- The resolution to the problem of consistent large transverse momentum in TMDs (PhysRevD.107.094029)

- (J. O. Gonzalez-Hernandez, T. Rainaldi, T. C. Rogers)
- Combining nonperturbative transverse momentum dependence with TMD evolution (PhysRevD.106.034002)
  - (J. O. Gonzalez-Hernandez, T. C. Rogers, N. Sato)





## Studying the role of intrinsic or **nonperturbative effects** in hadrons

## **Predicting** transverse momentum distributions in **cross sections** after evolution to **high energies**

Factorization theorems

**Evolution equations** 

**SIDIS** 

#### What we know



At small  $q_T \ll Q$  the cross section is determined solely by TMD factorization (TMD pdfs and/or TMD FFs)

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\boldsymbol{q}_T\dots} \stackrel{\boldsymbol{q}_T \ll Q}{\sim} \sum_j H_{j\bar{j}} \int \mathrm{d}^2 \boldsymbol{k}_{T,1} \mathrm{d}^2 \boldsymbol{k}_{T,2} f_j(\boldsymbol{x}, \boldsymbol{k}_{T,1}; \boldsymbol{\mu}, \boldsymbol{\zeta}) f_{\bar{j}}(\boldsymbol{x}, \boldsymbol{k}_{T,1}; \boldsymbol{\mu}, \boldsymbol{\zeta}) \delta^{(2)}(\boldsymbol{q}_T - \boldsymbol{k}_{T,1} - \boldsymbol{k}_{T,2})$$

At large  $q_T \sim Q$  the cross section is determined solely by fixed order collinear factorization (SIDIS, Drell-Yan, e<sup>+</sup>e<sup>-</sup> --> back-to-back hadrons,...)

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\boldsymbol{q}_T \dots} \stackrel{q_T \sim Q}{\sim} H(q_T) \otimes f \otimes f.$$
 Collinear PDFs

#### What we know

Similarly, at large TM ( $k_T$ )/ small  $b_T$  the TMDs are **uniquely** determined by an OPE expansion in terms of collinear PDFs/FFs

 $f_{i/H}(x, b_T; \mu, \zeta) = \widetilde{C}_{ij}(x, b_T; \mu, \zeta) \otimes f_{j/H}(x; \mu) + \mathcal{O}(mb_T)$ Perturbatively calculable **Usual PDFs** 



Most of these integrals are divergent. A more careful treatment is necessary

> <u>Credits: Lorcé, Pasquini and</u> <u>Vanderhaeghen</u>

## Conventional approach

### Final parametrization of a TMD

#### (Some) Issues with conventional approach





### (Some) Questions

- What do we mean by **perturbative and nonperturbative** contributions?
- How much **sensitivity to collinear functions** do the TMDs have?
- Can we test different models and our assumptions in a manageable manner?
- Can we maximize the predictive power?



## Hadron Structure Oriented approach

#### TMD PDF HSO parametrization at input scale





#### Choose "core" models (examples)

$$f_{\text{core},i/p}^{\text{Gauss}}(x, \mathbf{k}_{\text{T}}; Q_0^2) = \frac{e^{-k_{\text{T}}^2/M_F^2}}{\pi M_F^2}$$

Gaussian "core" models

Spectator-like "core" models

$$f_{\text{core},j/p}^{\text{Spect}}\left(x, \boldsymbol{k}_{\text{T}}; Q_{0}^{2}\right) = \frac{6M_{0F}^{6}}{\pi\left(2M_{F}^{2} + M_{0F}^{2}\right)} \frac{M_{F}^{2} + k_{\text{T}}^{2}}{\left(M_{0F}^{2} + k_{\text{T}}^{2}\right)^{4}}$$

#### Pheno strategy:

#### Data at different Q not on the same footing





#### Comparison with MAP22





### Higher Q postdictions: test different fits on the same experiment



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# Higher Q postdictions: test different models on the same experiment

#### A postdiction of CDFII with E288 GAUSSIAN fit

A postdiction of CDFII with E288 SPECTATOR fit



#### TMDs are affected by collinear distributions



**Example**: take two pdfs associated with the same flavor (s here) and compute the input TMD

Maybe unexpected different small  $k_T$  behavior because of integral relation

• Expected different tails because of the OPE expansion

<u>Changing the integral **necessarily**</u> <u>changes the integrand</u>

### Why is this important?

• We can **quantitatively** and **conclusively** answer the question:

How much collinear dependence do my TMD extractions carry?



#### The NP Collins-Soper kernel





### Summary

We have a framework that

- 1. Is consistent with the large  $k_T$  tail from theory (where it should)
- 2. Satisfies an integral relation: pseudo probabilistic interpretation
- 3. No  $b_{max}$  or  $b_{min}$  dependance: all errors are under control
- 4. NP (core) models are very easily swappable and testable

Pheno methodology: Fit low Q, test against higher Q (not mandatory)

#### NEXT/SOON:

SIDIS large  $q_T$  issue, more refined models, input from Lattice?, higher orders...

Thank you

# Backup slides

#### RG improvements for CS-kernel (LO example)



#### HSO coefficients

$$\begin{split} A_{i/p}(x;\mu_{Q_0}) &\equiv \sum_{i'} \delta_{i'i} \frac{\alpha_s(\mu_{Q_0})}{\pi} \left\{ \left[ (P_{ii'} \otimes f_{i'/p})(x;\mu_{Q_0}) \right] - \frac{3C_F}{2} f_{i'/p}(x;\mu_{Q_0}) \right\} ,\\ B_{i/p}(x;\mu_{Q_0}) &\equiv \sum_{i'} \delta_{i'i} \frac{\alpha_s(\mu_{Q_0})C_F}{\pi} f_{i'/p}(x;\mu_{Q_0}) ,\\ A_{i/p}^g(x;\mu_{Q_0}) &\equiv \frac{\alpha_s(\mu_{Q_0})}{\pi} \left[ (P_{ig} \otimes f_{g/p})(x;\mu_{Q_0}) \right] ,\\ C_{i/p} &\equiv \frac{1}{N_{i/p}} \left[ f_{i/p}(x;\mu_{Q_0}) - A_{i/p}(x;\mu_{Q_0}) \ln \left(\frac{\mu_{Q_0}}{m_{i,p}}\right) - B_{i/p}(x;\mu_{Q_0}) \ln \left(\frac{\mu_{Q_0}}{m_{i,p}}\right) \ln \left(\frac{Q_0^2}{\mu_{Q_0}m_{i,p}}\right) - A_{i'/p}^g(x;\mu_{Q_0}) \ln \left(\frac{\mu_{Q_0}}{m_{g,p}}\right) + \frac{\alpha_s(\mu_{Q_0})}{2\pi} \left\{ \sum_{i'} \delta_{i'i} [\mathcal{C}_{\Delta}^{i/i'} \otimes f_{i'/p}](x;\mu_{Q_0}) + [\mathcal{C}_{\Delta}^{i/g} \otimes f_{g/p}](x;\mu_{Q_0}) \right\} \right] \end{split}$$

#### Pseudo-probability distribution property saved





# Summary slide WG5





1.2

0.8

0.0

0.4

k<sub>T</sub>/Q

No b<sub>max</sub> or b<sub>min</sub> Smooth interpolation P to NP