



arXiv:[1206.2913](https://arxiv.org/abs/1206.2913)

[J. Phys. G 48 \(2021\) 11. 110501](https://arxiv.org/abs/1206.2913)

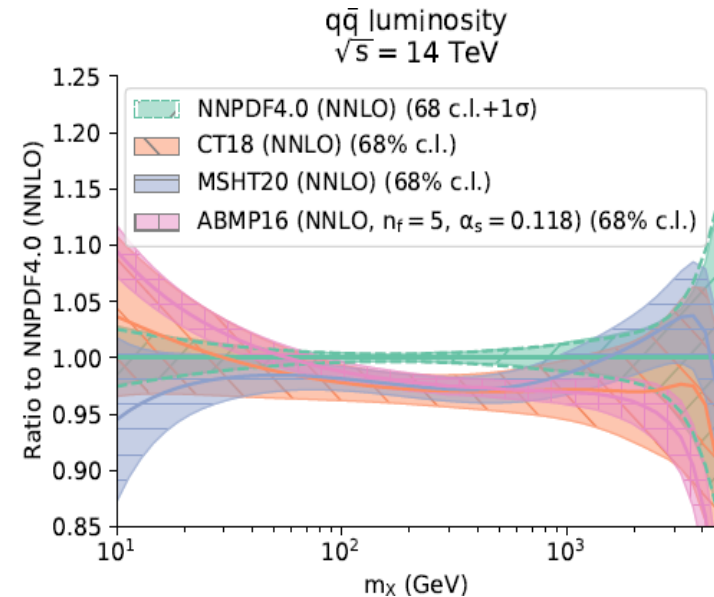
(arXiv:[2007.14491](https://arxiv.org/abs/2007.14491))



see also, [FCC CDR](#), vols 1 and 3:

physics, [EPJ C79 \(2019\). 6. 474](#)

FCC with eh integrated, [EPJ ST 228 \(2019\). 4. 755](#)



Why an LHeC? Many reasons

One of them is to improve precision of proton PDFs

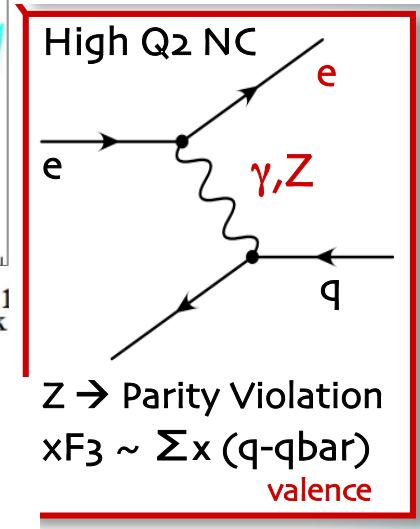
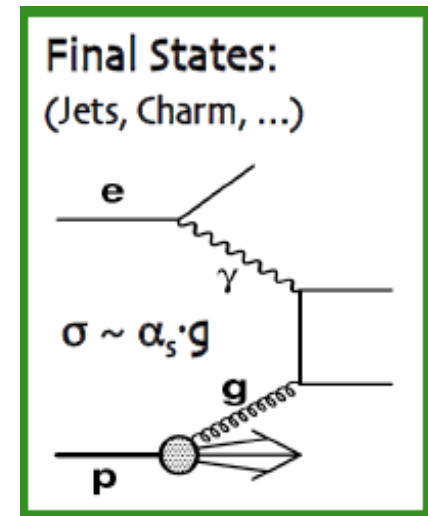
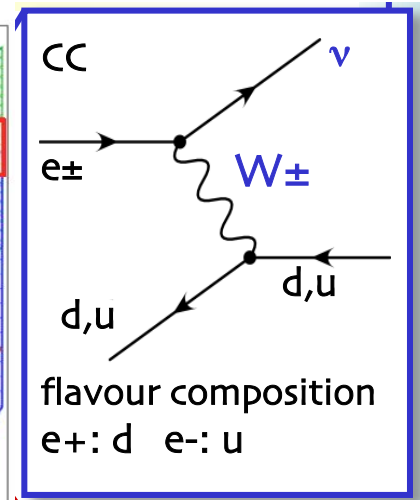
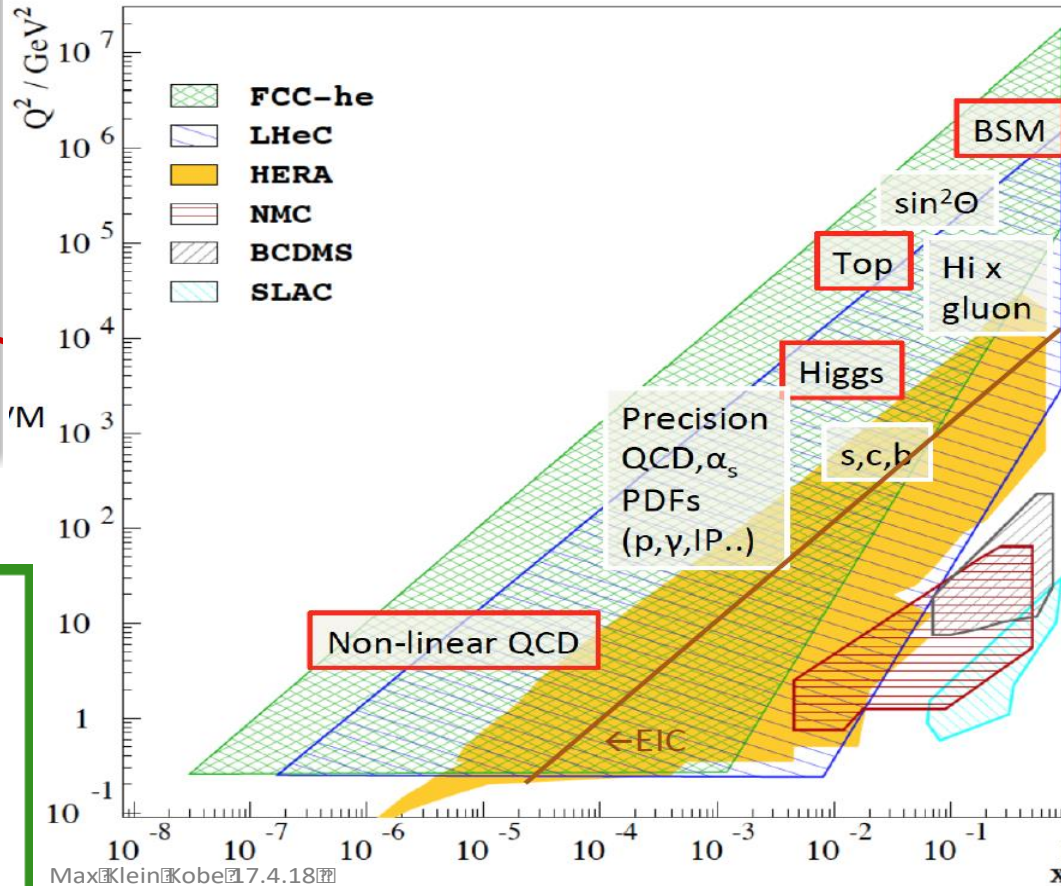
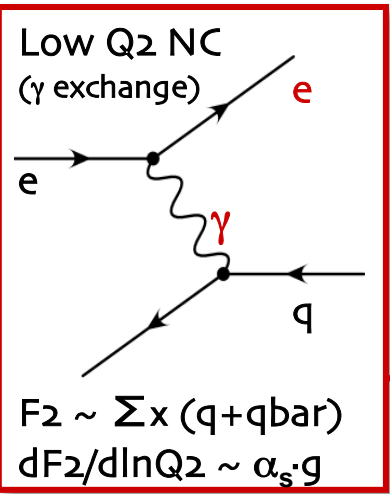
Today PDFs from each of the big groups CT, MSHT, NNPDF are each heading towards percent level precision BUT the differences between them are at the few percent level— even in the ‘well-known’ central x region

This is not good enough if we aim to find deviations from the SM in the deviations of the values of SM parameters M_W , $\text{Sin}^2\theta_W$

What could help?

A precise new data set over a very wide kinematic range with consistent correlated systematics--- that’s what the LHeC could provide

Where does the information come from?



A future DIS machine would be a vast improvement on HERA in both luminosity and kinematic reach

×15/120 extension in $Q^2, 1/x$ reach vs HERA

LHeC ep simulated data and QCD fits

NEW: LHeC simulations (e: 50 GeV*, p: 7 TeV†)

simulation: M. Klein

dataset	e charge	e pol.	lumi (fb ⁻¹)	
NC/CC	–	–0.8	5,500	luminosity
NC/CC	+	0	1,10	positron
NC/CC	–	0	50	polarisation (important for EW)
NC/CC	–	+0.8	10,50	
NC/CC	–	0	1	low-E (p: 1 TeV)

uncert. assumptions:
 elec. scale: 0.1%
 hadr. scale 0.5%
 radcor: 0.3%
 yp at high y: 1%
 uncorrelated uncert.: 0.5%
 CC syst.: 1.5%
 luminosity: 0.5%

*corresponds to possibility of smaller ERL cf. previous 60 GeV simulations

†except for low-E

various combinations studied;
 shown frequently in following slides:

LHeC 1st Run
 (50 fb⁻¹ e⁻ only; 3 yrs)

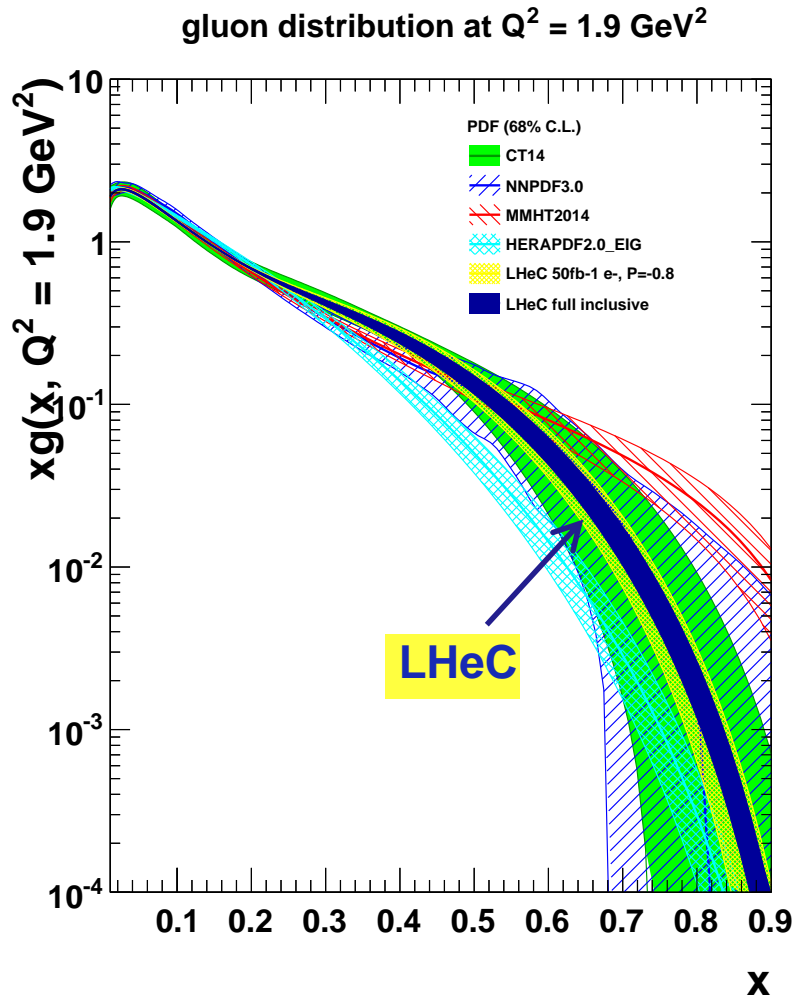
LHeC full inclusive

QCD analysis a la HERAPDF2.0, except **more flexible**, notably in **NO constraint** requiring dbar=ubar at small x;

4+1 xuv, xdv, xUbar, xDbar and **xg** (**14 free parameters**, cf. 10 by default in CDR)

5+1 xuv, xdv, xUbar, xdbar, xsbar and **xg** (if strange and HQ included; **17 free parameters**)

Gluon at large x



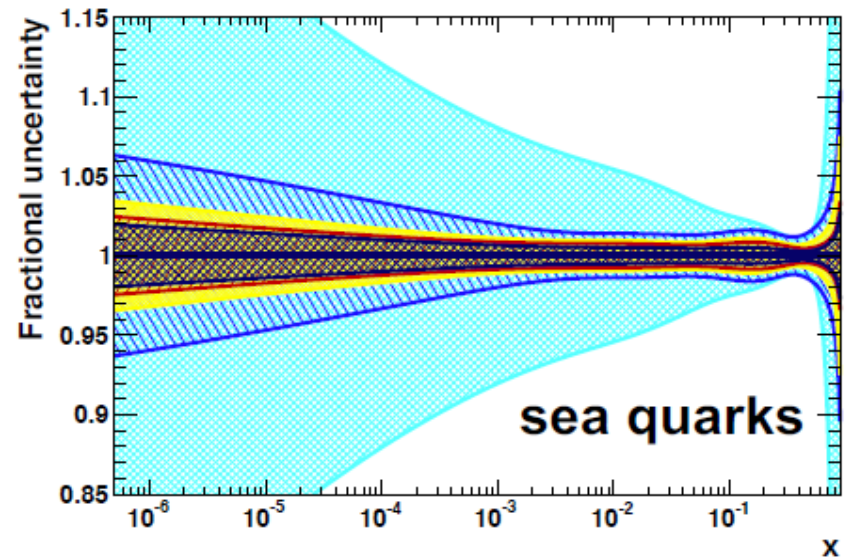
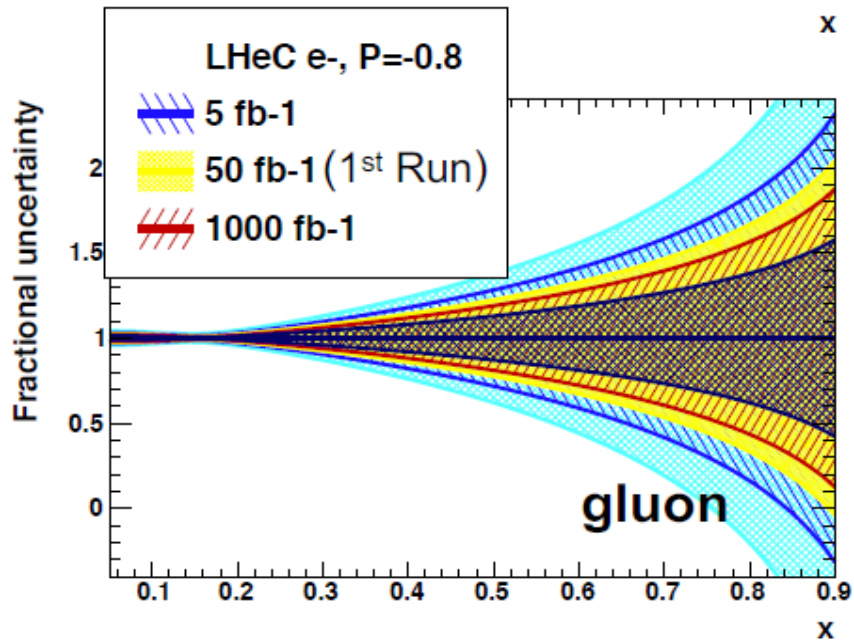
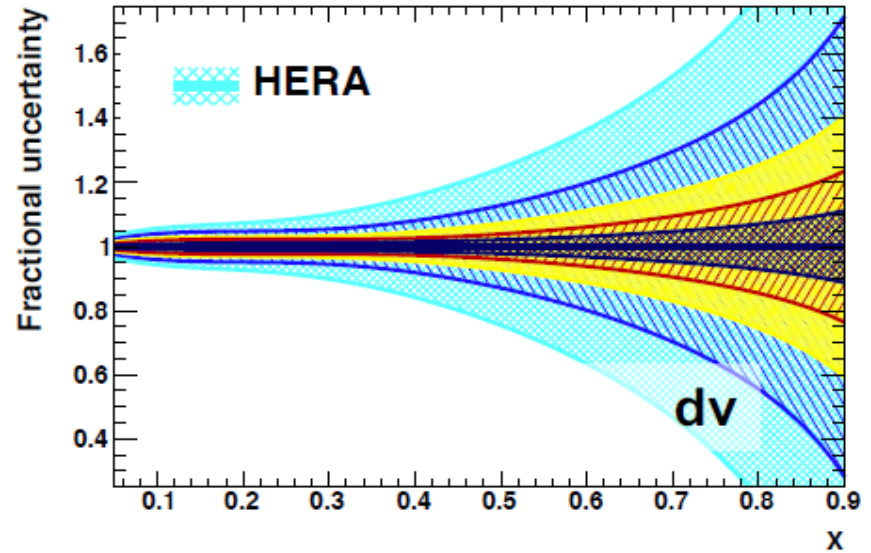
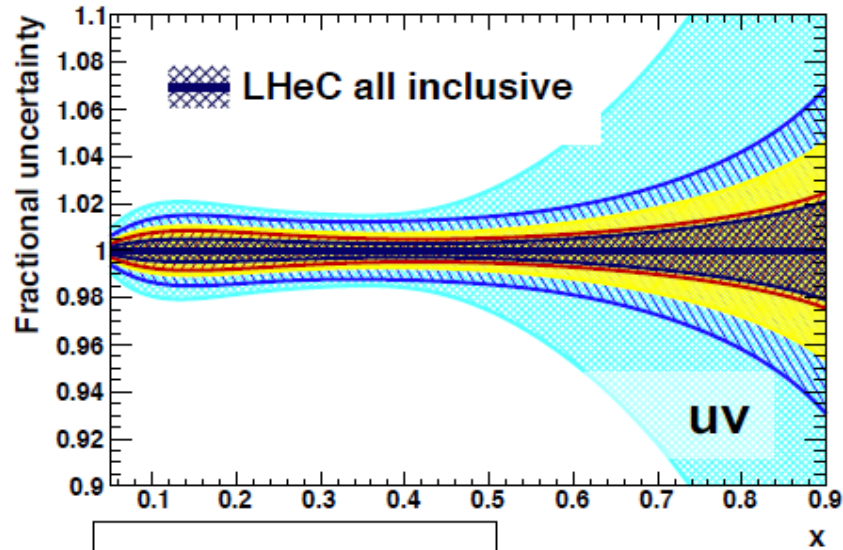
gluon at large x is small and currently
very poorly known;
crucial for new physics searches

LHeC sensitivity at large x comes as
part of overall package

- high luminosity ($\times 50\text{--}1000$ HERA);
- fully constrained quark pdfs; small x;
- momentum sum rule

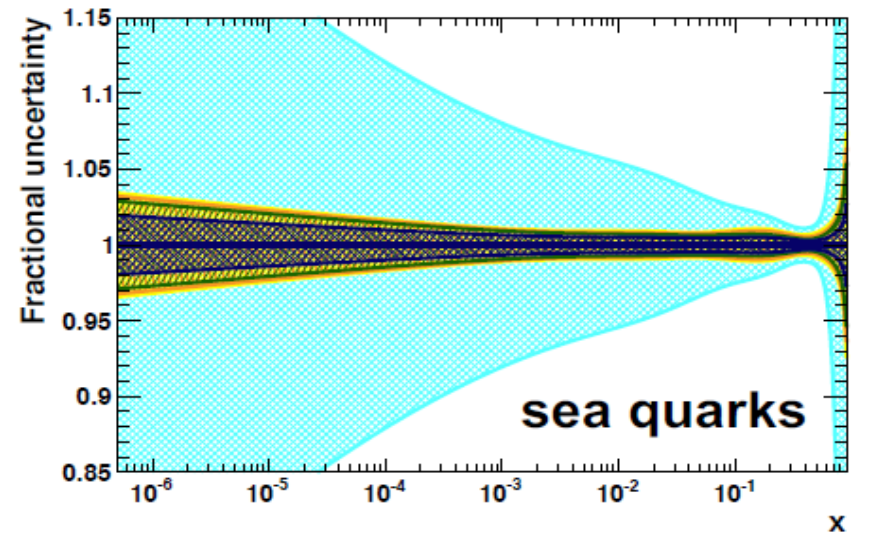
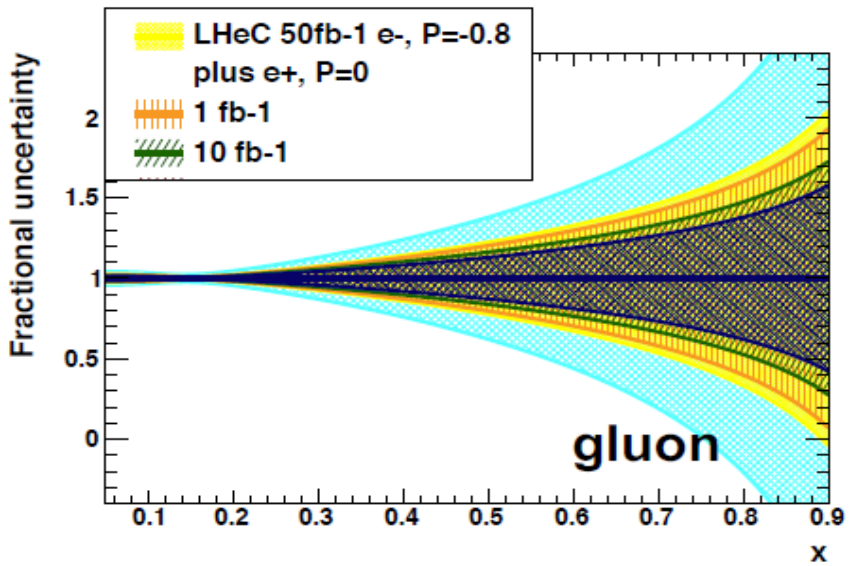
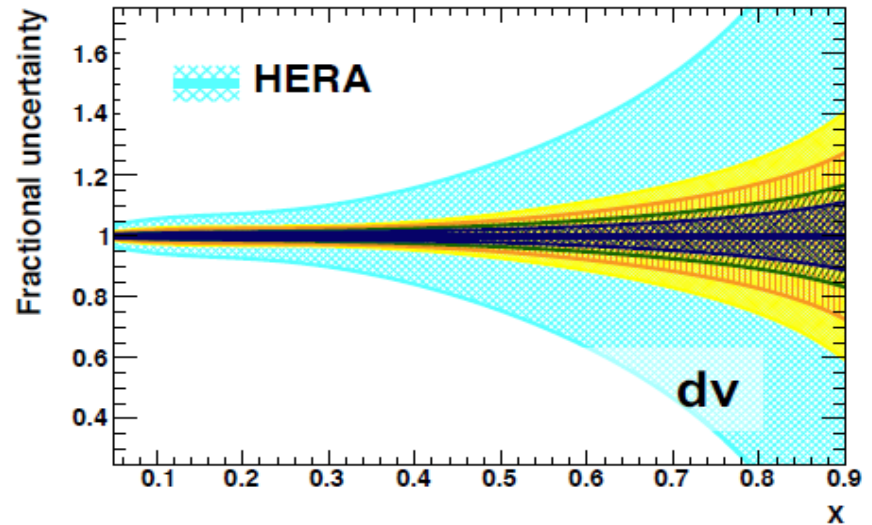
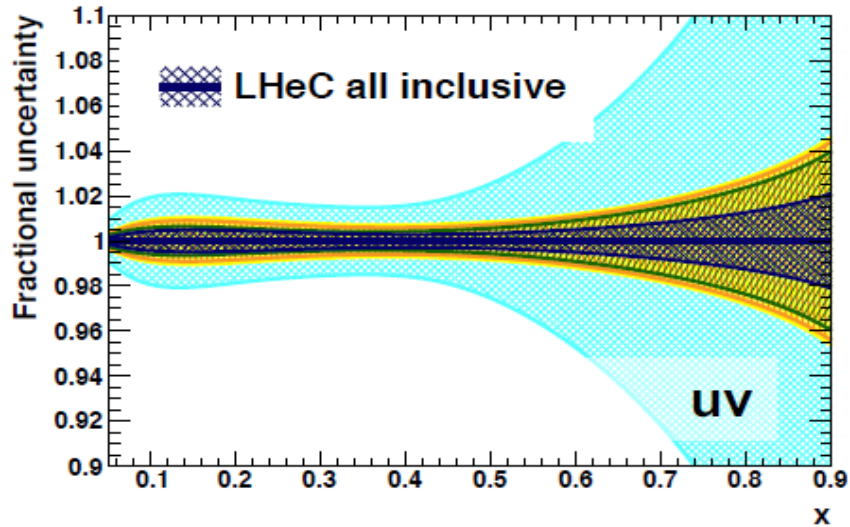
gluon and sea intimately related
LHeC can disentangle sea from
valence quarks at large x, with precision
measurements of **CC** and **NC** F_2^{YZ} , xF_3^{YZ}

Impact of luminosity on PDFs



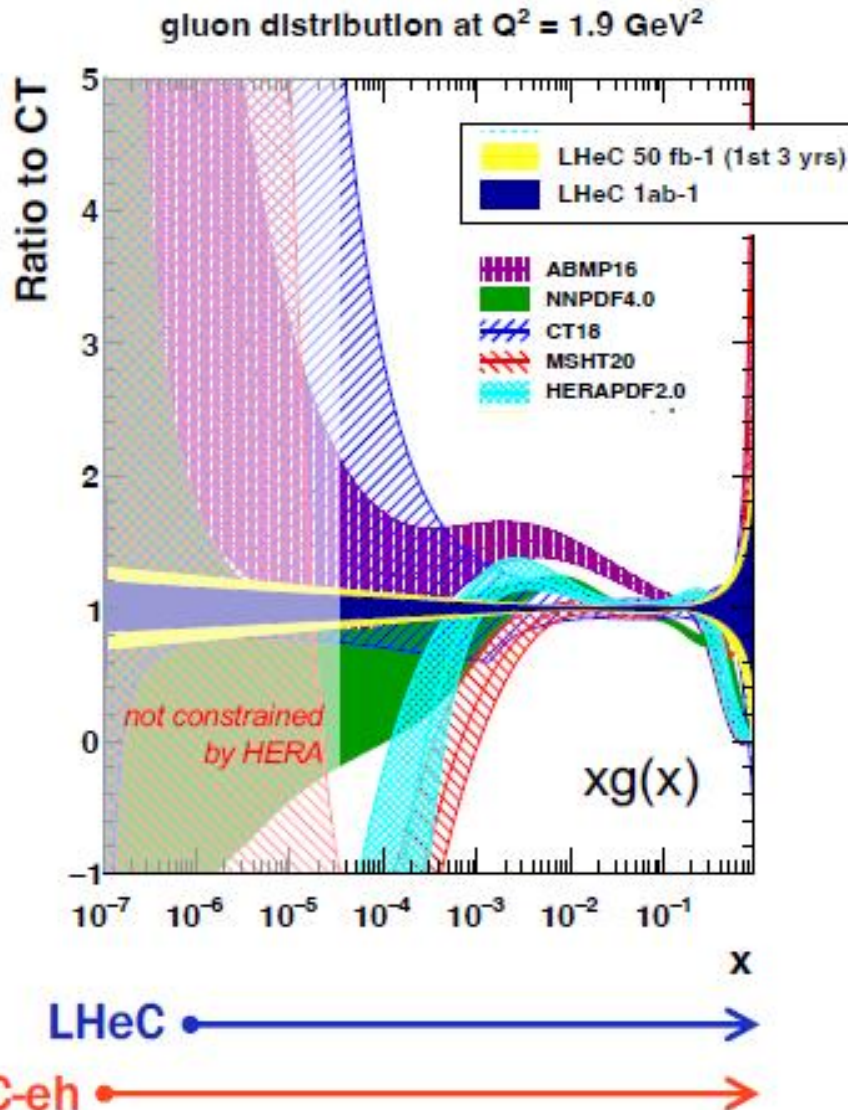
small and medium x quickly constrained (5 fb-1 \equiv $\times 5$ HERA \equiv 1 year LHeC)

Impact of positrons on PDFs



CC: e^+ sensitive to d ; **NC:** e^\pm asymmetry gives $xF_3^{\nu Z}$, sensitive to valence

Gluon at small x



no current data much below $x=5 \times 10^{-5}$

LHeC provides single, precise and unambiguous dataset down to $x=10^{-6}$

FCC-eh probes to even smaller $x=10^{-7}$

explore low x QCD:

DGLAP vs BFKL; non-linear evolution;

gluon saturation; implications

for ultra high energy neutrino cross sections

Even if your specific interest is not in low-x physics

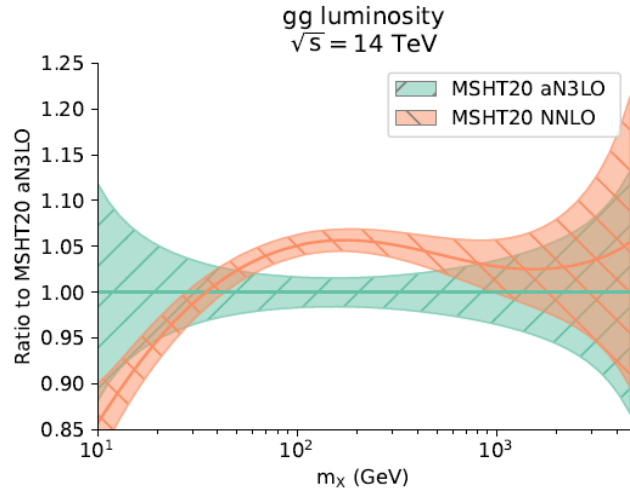
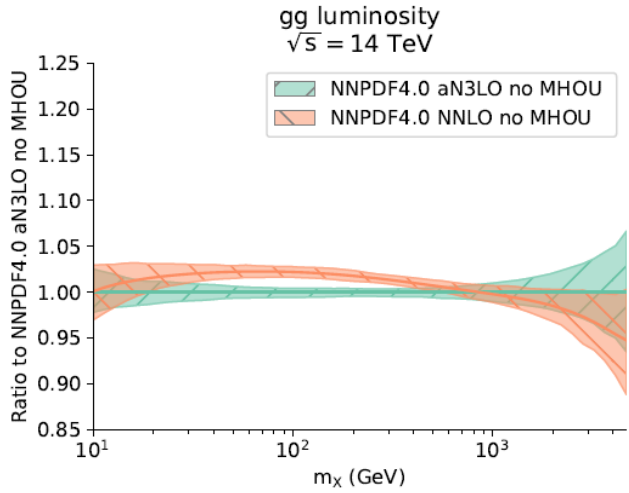
do not be complacent in thinking that this region does not affect you...

PDFs are going to N3LO – where the first of the BFKL ($\ln(1/x)$ resummation) terms matter..

We now have N3LO predictions..

-----Well at least approximately

This has a significant effect on the low-x gluon at low scales

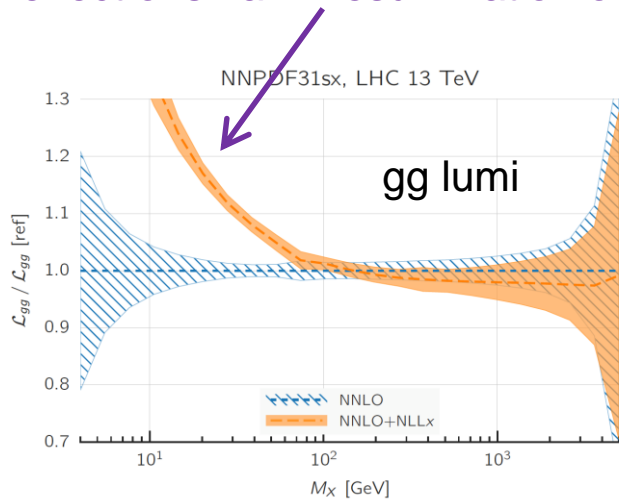


And that translates to an effect on the low M_x region for the gluon-gluon luminosity BUT this also has a ‘knock-on effect’ on the luminosity in the Higgs region $M_x = 125$ GeV

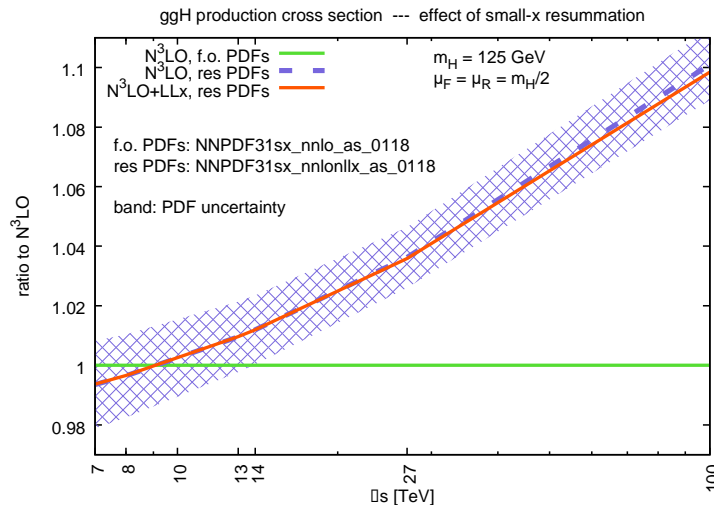
Differing groups have different ways of implementing the aN3LO For MSHT there is a 5% decrease in luminosity at the Higgs mass, for NNPDF this is more like 2%... BUT either way there is a significant difference BEWARE of low-x effects!!

Full $\ln(1/x)$ BFKL resummation

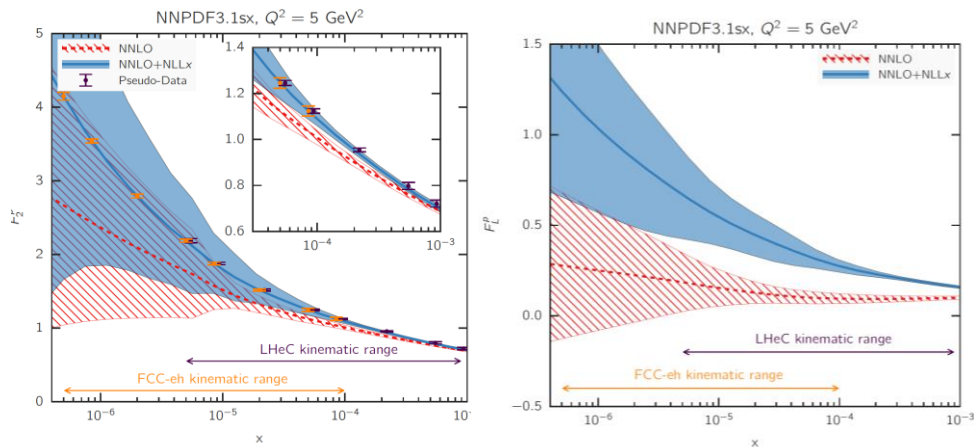
effect of small x resummation on LHC luminosity



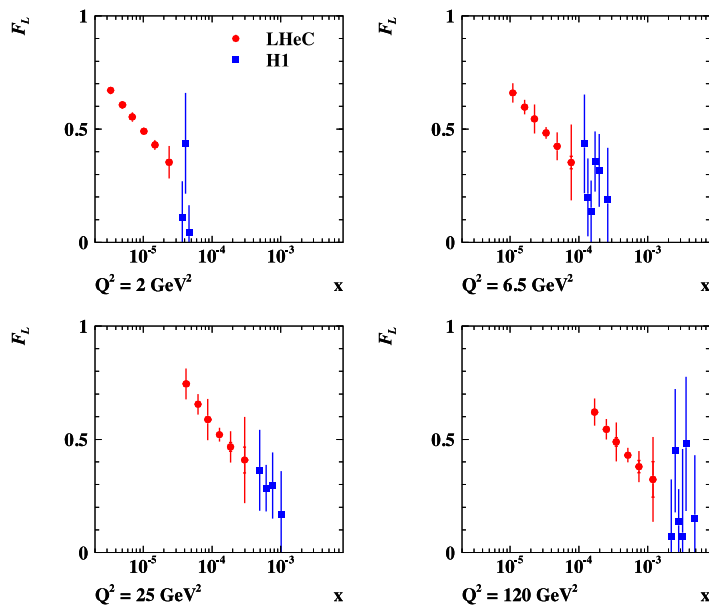
effect of small x resummation on ggH cross section for LHC, HE-LHC, FCC



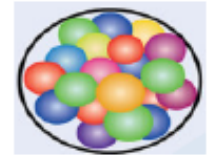
Effect of small x resummation on predictions for DIS F_2 and F_L



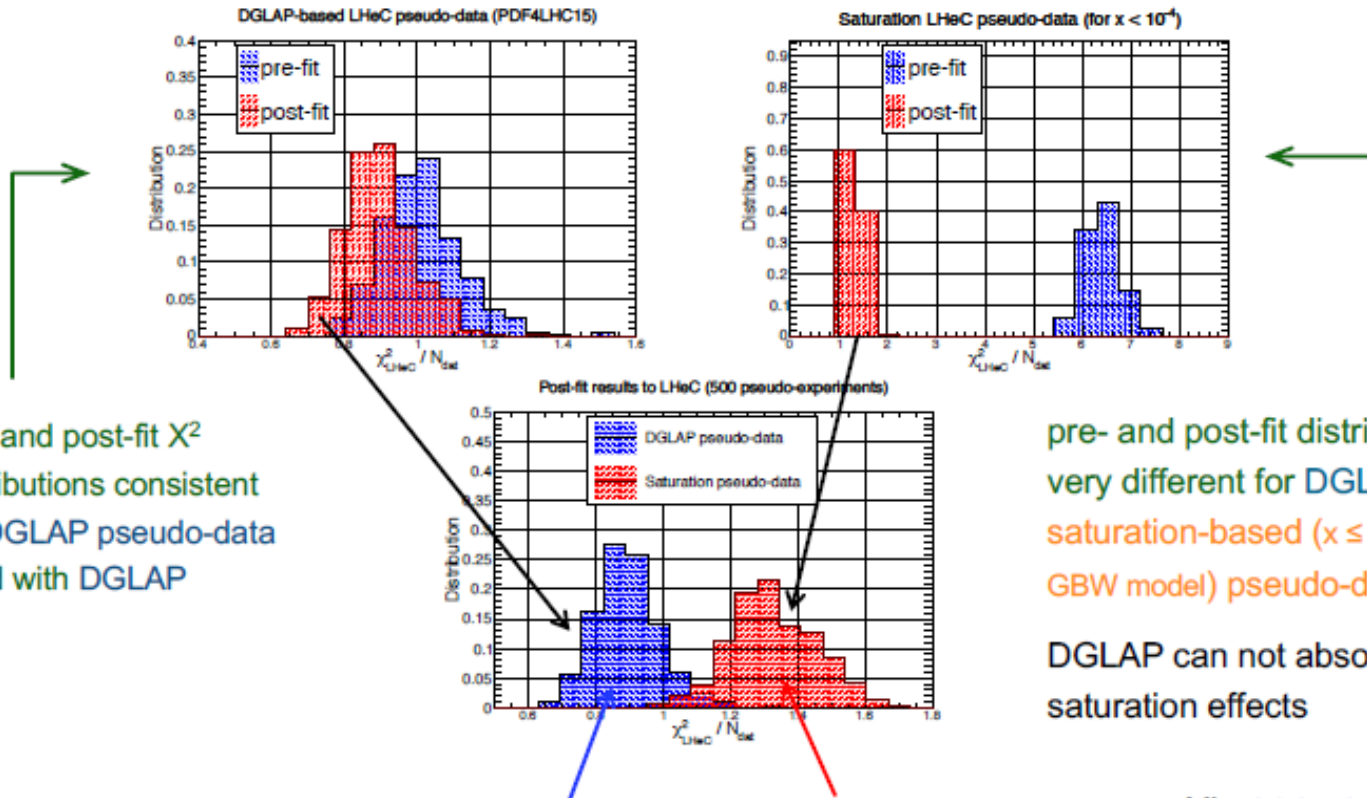
Prospects for FL measurement at LHeC



Novel dynamics at small x: saturation



- studies show linear evolution **cannot accommodate saturation**, even at NNLO or NNLO+NLLx
- EG, **DGLAP-** vs **saturation-** based simulated data fitted with NNLO DGLAP



pre- and post-fit χ^2 distributions consistent for DGLAP pseudo-data fitted with DGLAP

pre- and post-fit distributions very different for DGLAP fit to saturation-based ($x \leq 10^{-4}$, GBW model) pseudo-data

DGLAP can not absorb all saturation effects

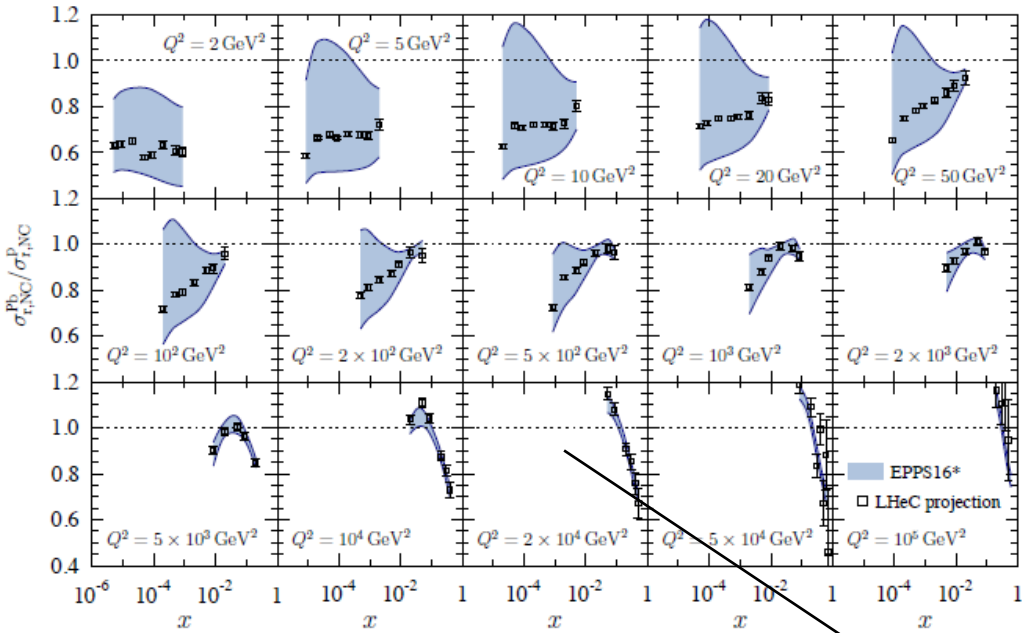
LHeC can distinguish between **DGLAP** and **saturation**

(NB, large lever arm in Q^2 crucial, see also arXiv:[1702.00839](https://arxiv.org/abs/1702.00839))

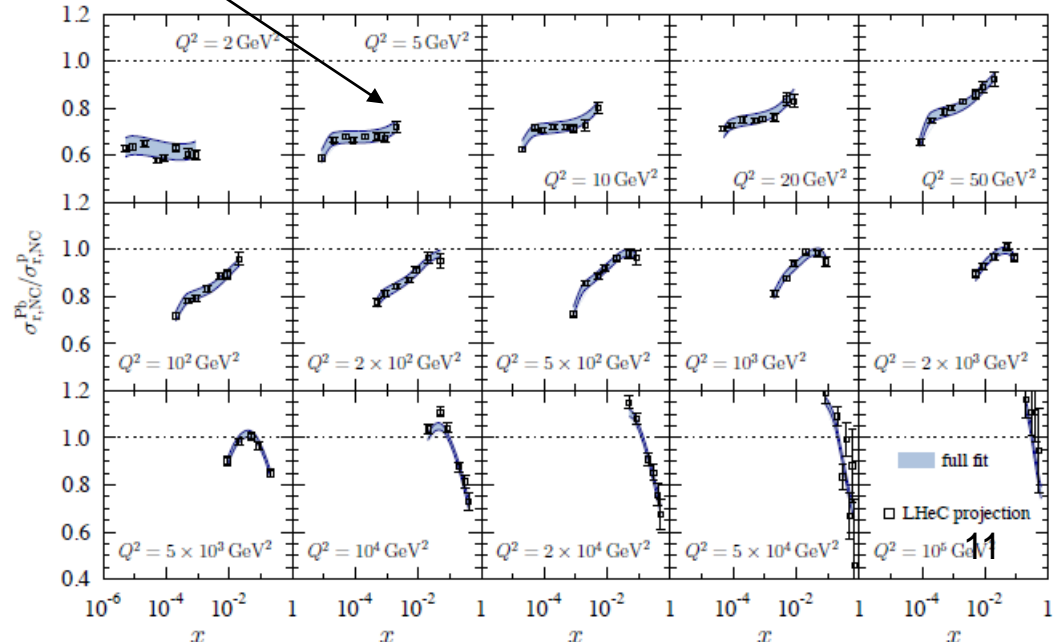
arXiv:[2007.14491](https://arxiv.org/abs/2007.14491)
(more detail in EXTRAS)

But saturation effects will show up most strongly in heavy nuclei

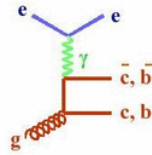
And LHeC can also measure ePb



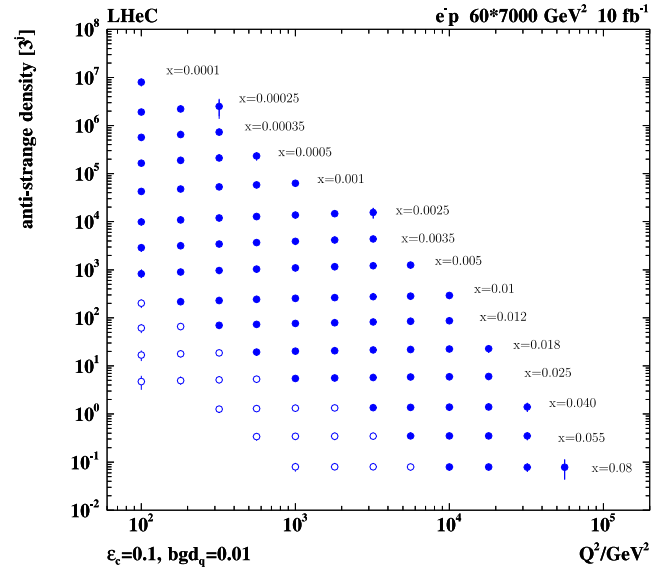
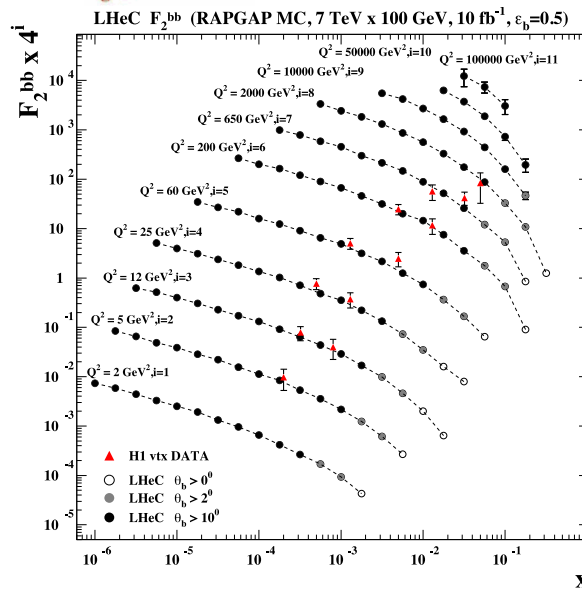
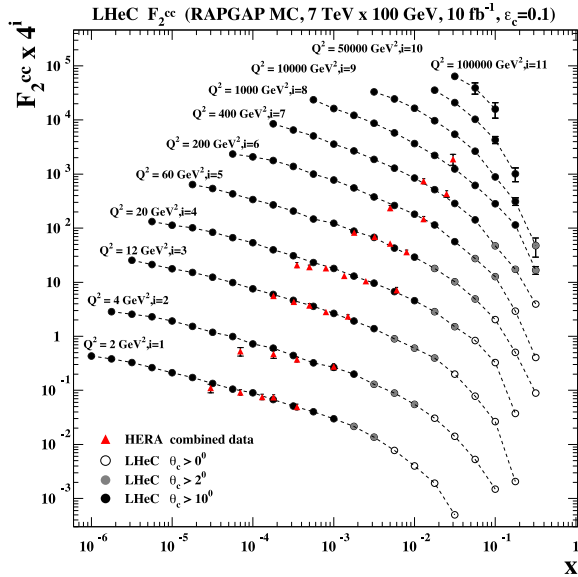
Pseudo data based on EPPS16 eA analysis bring vast improvement in previously unmeasured kinematic ranges



c, b quarks



strange



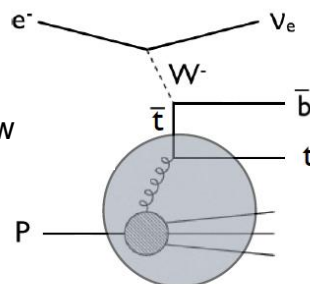
LHeC: enormously extended range and much improved precision c.f. HERA

strange pdf poorly known; how suppressed cf. other light quarks? $s \neq sbar$?

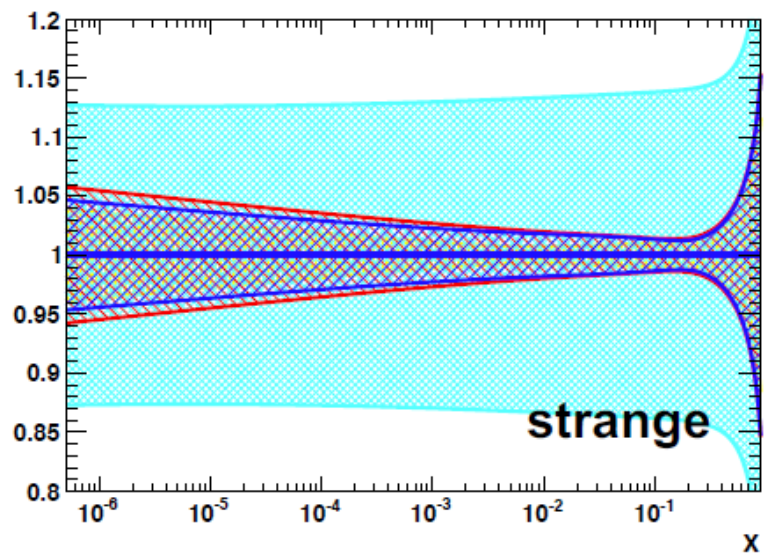
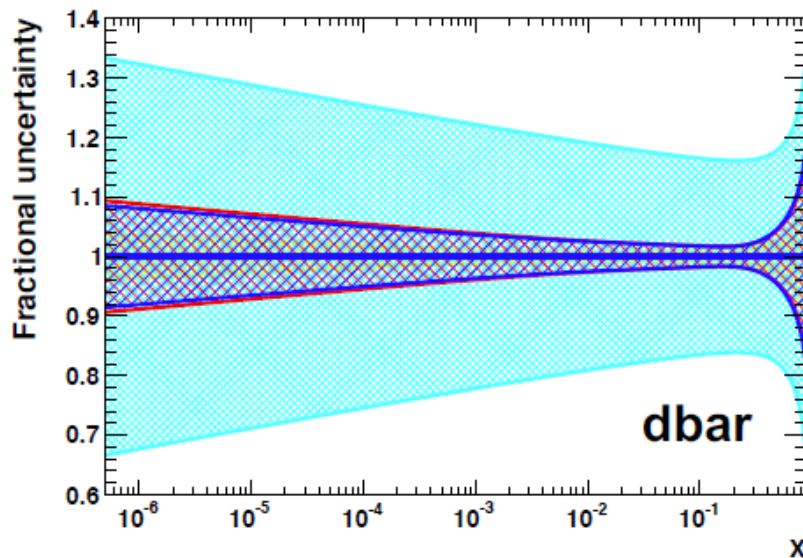
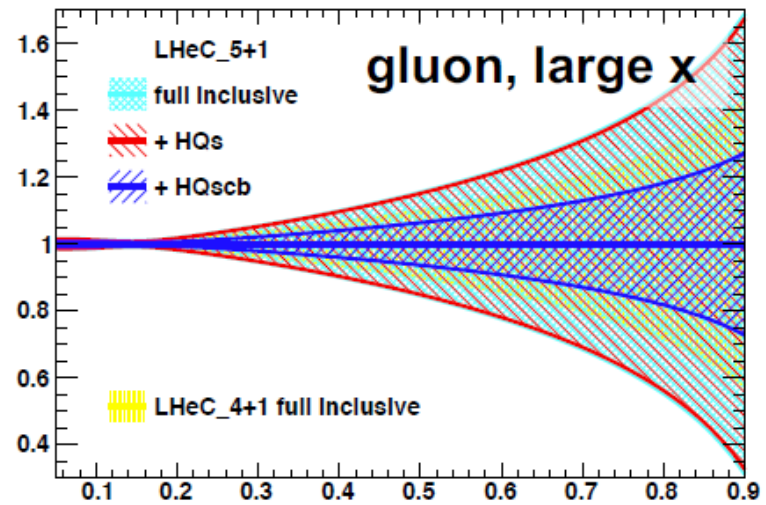
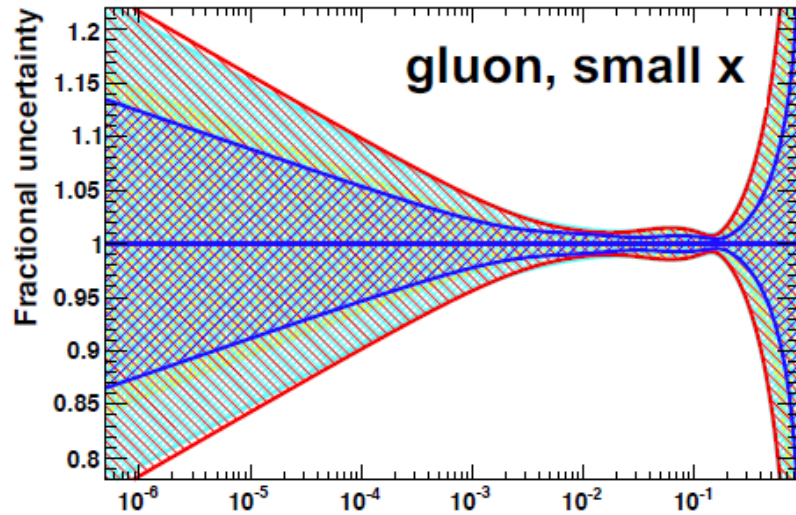
LHeC: direct sensitivity to strange via $W+s \rightarrow c$ (x, Q^2) mapping of (anti) strange for first time

also top PDF

top quark becomes light at large Q^2 : new field of research opens for top PDFs!

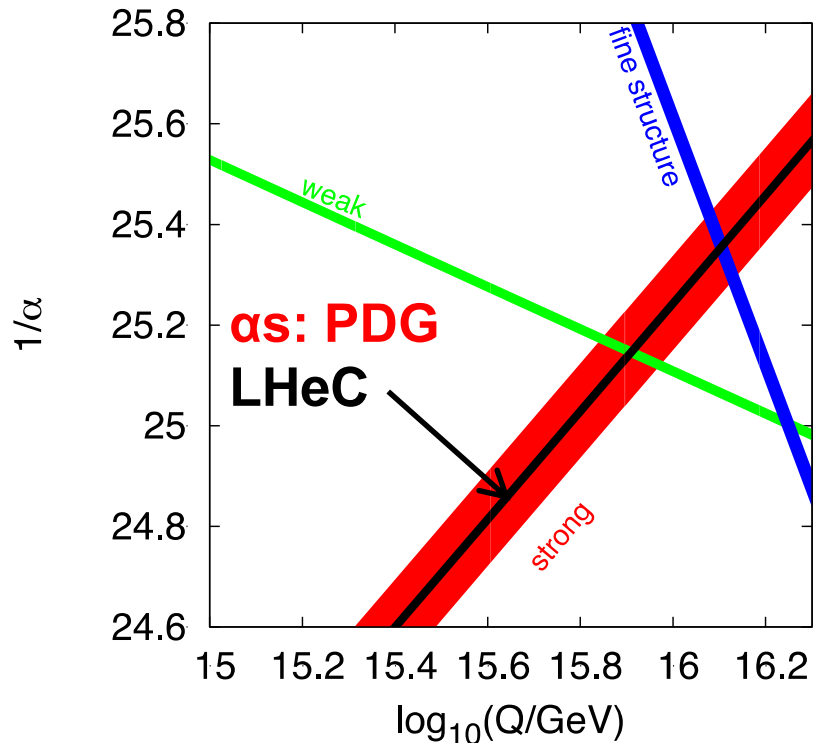


impact of HQ data on LHeC pdfs



more flexible parameterisation (5+1): $xu\bar{v}$, $x\bar{d}v$, $x\bar{u}$, $x\bar{d}$, $x\bar{s}$ and xg

And there will be further information from jet production at the LHeC..... which will mostly contribute to the precision of the gluon PDF and thus to the determinations of strong coupling, α_S (M_Z)



precise α_s needed:

to constrain GUT scenarios; for cross section predictions, including Higgs; ...

LHeC: permille precision possible in **combined QCD fit for pdfs+ α_s**

$\alpha_S(M_Z)$

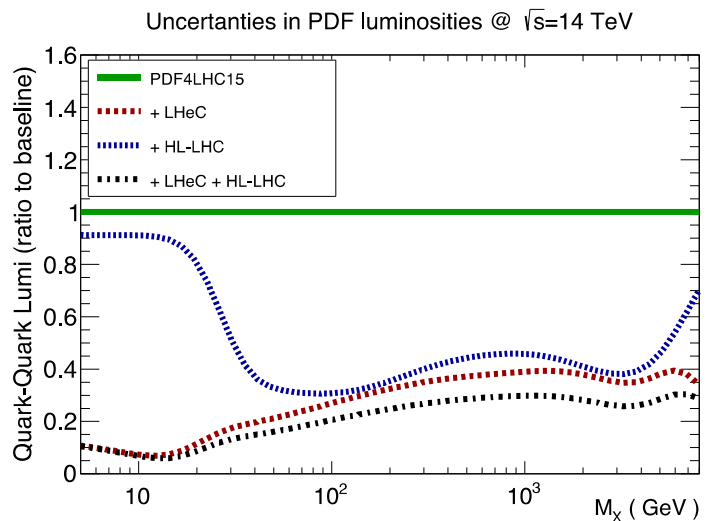
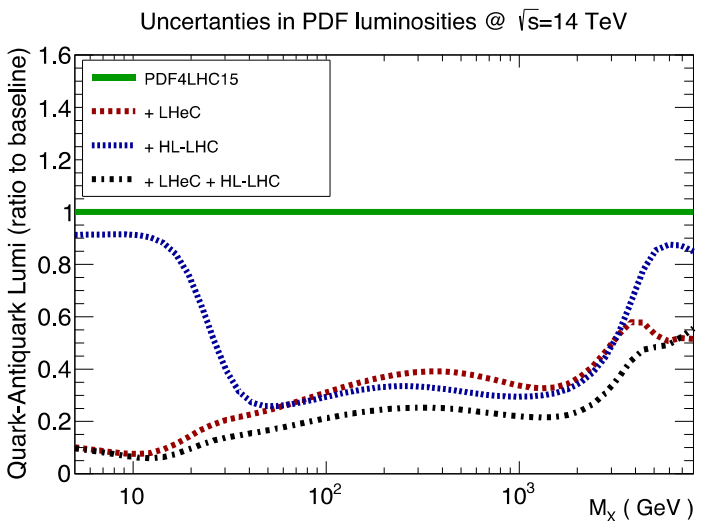
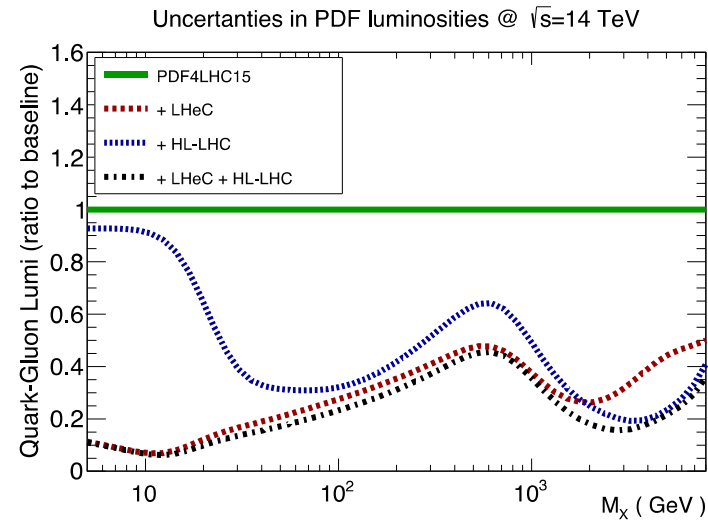
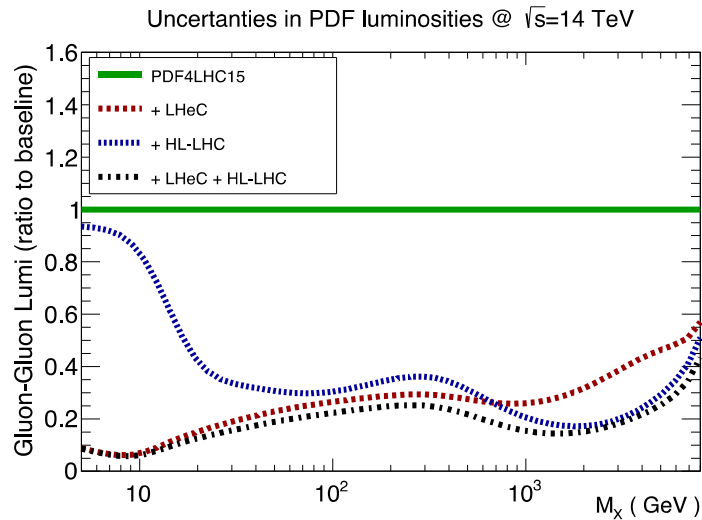
- LHeC simultaneous PDF+ α_s fit:
 - $\Delta\alpha_S(m_Z) = \pm 0.00022_{(\text{exp.}+\text{PDF})}$
 - $\Delta\alpha_S(m_Z) = \pm 0.00018$ (with ep jets)
- Achievable precision: **$\mathcal{O}(0.1\%)$** - x5-10 better than today

Summary

- PDF improvement is not just a matter of more data, consistency of data matters, consistency across a broad kinematic range is what LHeC/FEEeh offers
- A single team would analyse the whole kinematic region producing a consistent set of correlated systematic uncertainties----we have learnt our lessons at HERA
- This is also theoretically cleaner + less subject to new physics contamination at high scale
- Improvement in PDFs at high-x important for direct discoveries, improvement in high-x gluon also brings improvement in $\alpha_s(M_Z)$
- Improvement at middling x important for SM precision measurements like M_W and $\sin^2\theta_W$ which may reveal BSM physics
- Improvement at low-x is necessary to be sure of this, but is interesting in its own right for studying QCD beyond DGLAP: BFKL resummation and saturation
- Saturation is stronger at eA
- The LHeC offers dramatic improvement for all of this (and more) and is complementary to the EIC

Backup

Just in case you worry that a study of LHeC improvements based on a simple HERAPDF procedure may be optimistic. A study was done comparing future improvements from the HL-LHC to those from the LHeC in an ‘apples to apples’ manner. Profiling the PDF4LHC15 with HL-LHC pseudo-data or LHeC pseudo-data
 With consistent tolerance $T=3$



Abdul Khalek et al
 arXiv:1810.03639
 + 1906.10127

QCD fit parameterisation

QCD fit ansatz based on HERAPDF2.0, with following differences

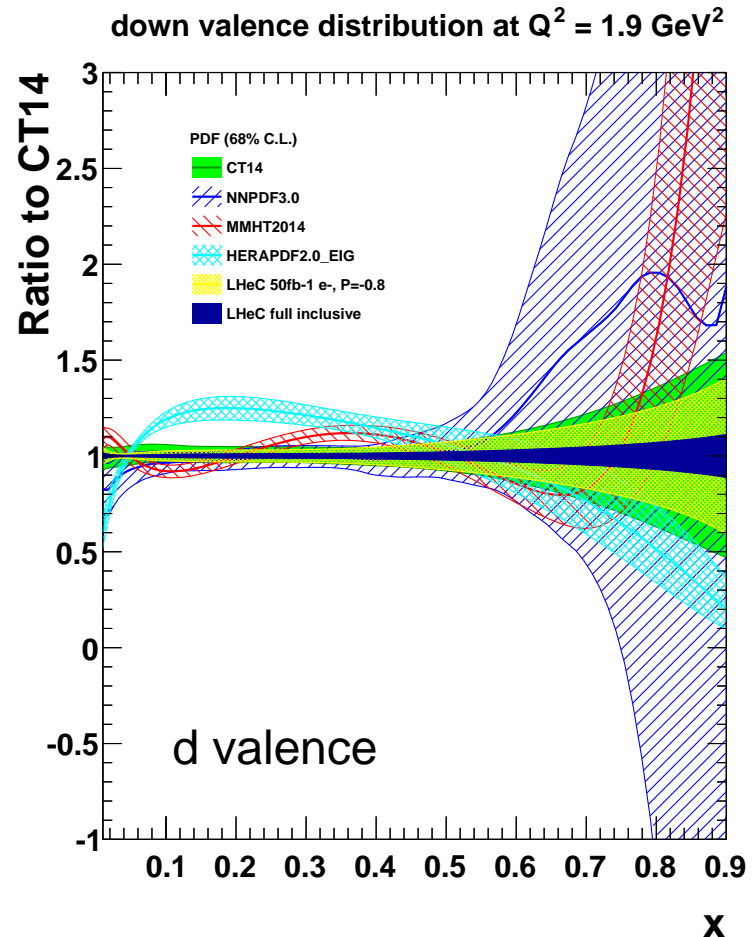
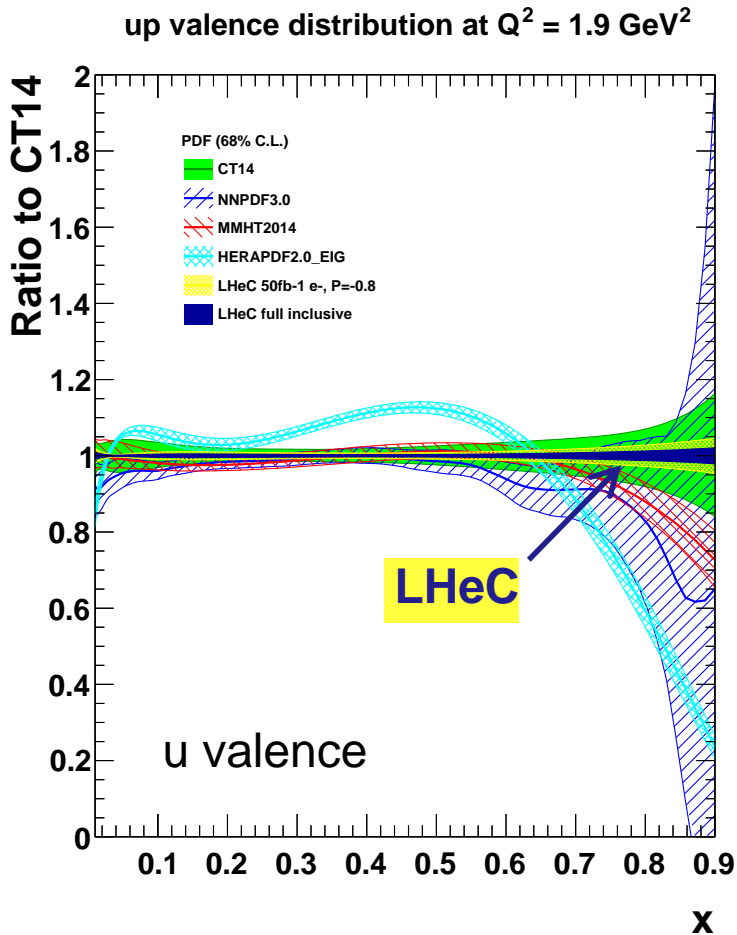
much more relaxed sea ie. no requirement that $\bar{u}=\bar{d}$ at small x
no negative gluon term (simply for the aesthetics of ratio plots – it has been checked that this does not impact size of projected uncertainties)

$$\begin{aligned}xg(x) &= A_g x^{B_g} (1-x)^{C_g} (1 + D_g x) \\xu_v(x) &= A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1 + E_{u_v} x^2) \\xd_v(x) &= A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}} \\x\bar{U}(x) &= A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} \\x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}\end{aligned}$$

4+1 pdf fit (above) has 14 free parameters

5+1 pdf fit for HQ studies parameterises \bar{d} and \bar{s} separately, and has 17 free parameters

valence quarks from LHeC

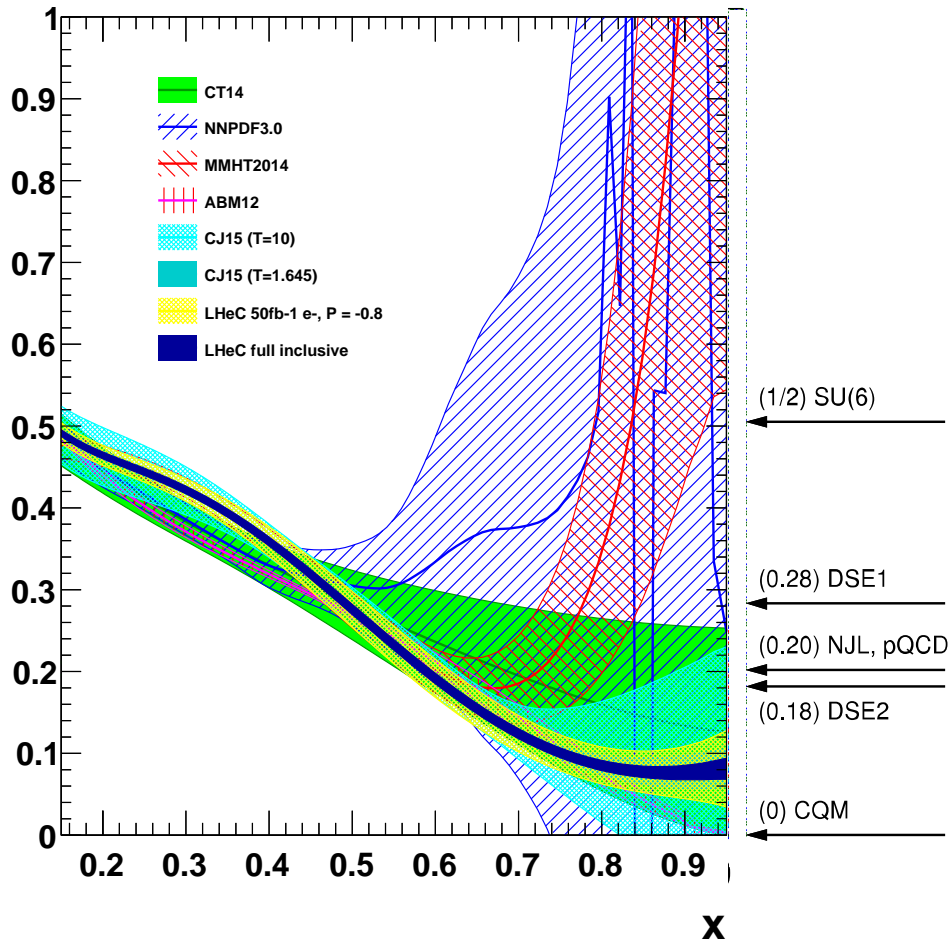


precision determination, free from higher twist corrections and nuclear uncertainties

large x crucial for HL/HE-LHC and FCC searches; also relevant for DY, MW etc.

d/u at large x

dv/uv distribution at $Q^2 = 10 \text{ GeV}^2$

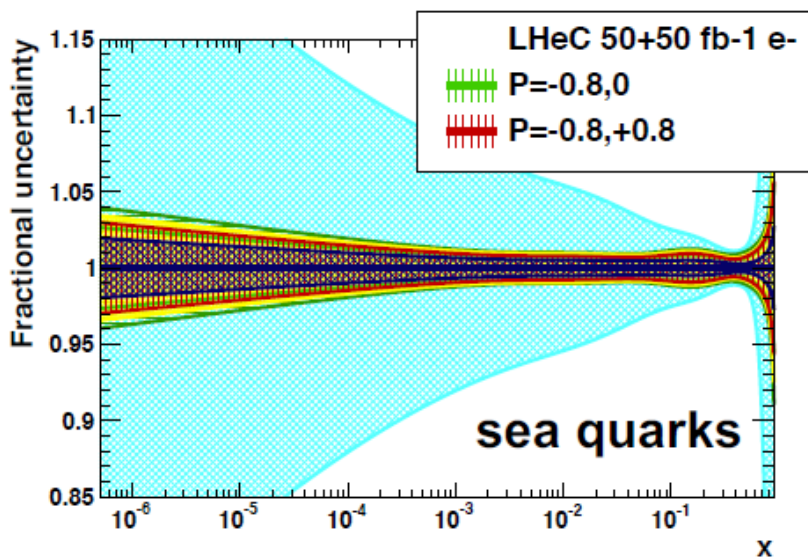
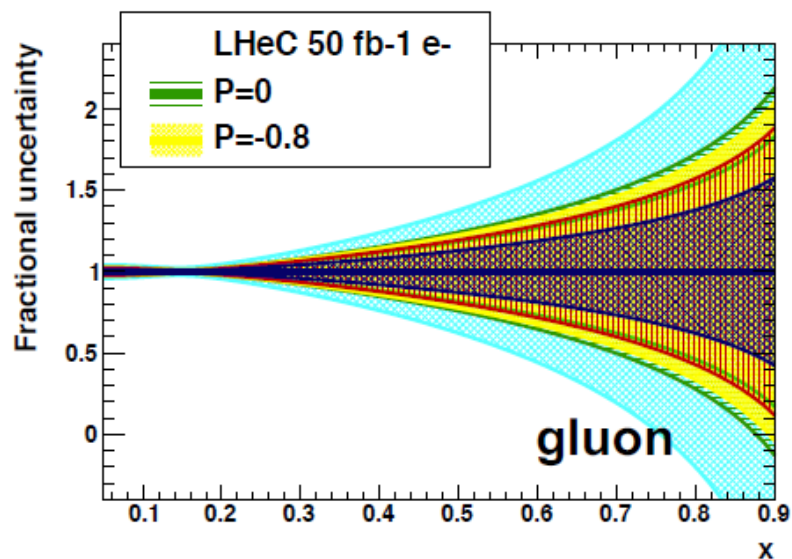
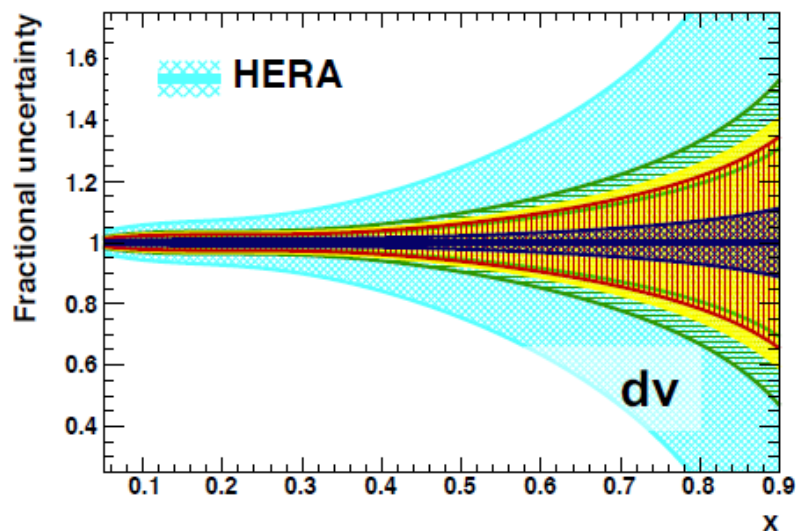
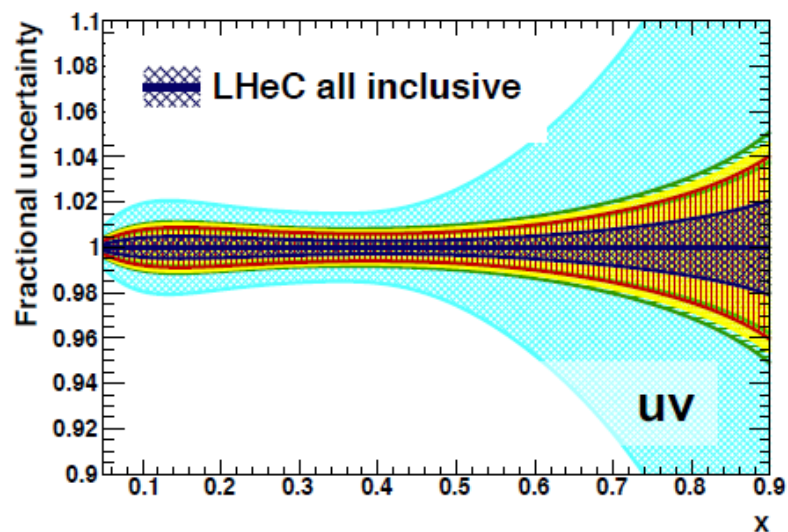


d/u essentially unknown at large x

no predictive power from current pdfs;
conflicting theory pictures;
data inconclusive, large nuclear
uncerts.

**resolve long-standing mystery
of d/u ratio at large x**

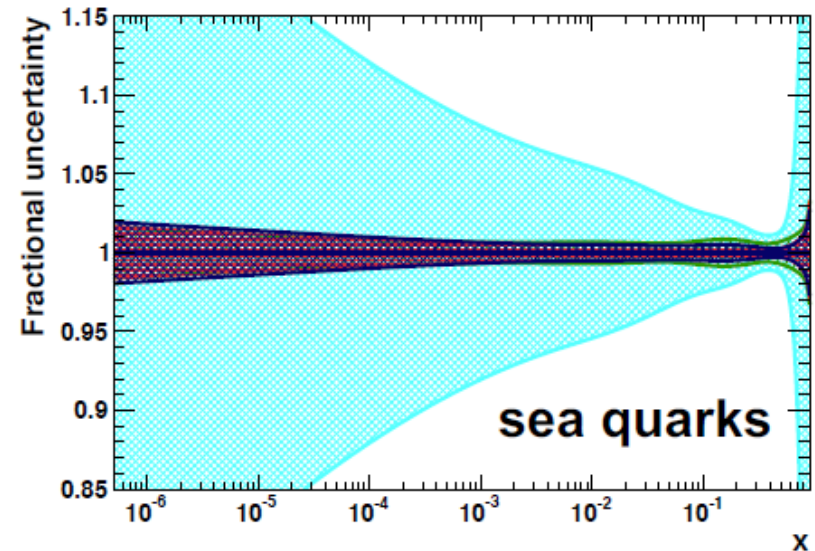
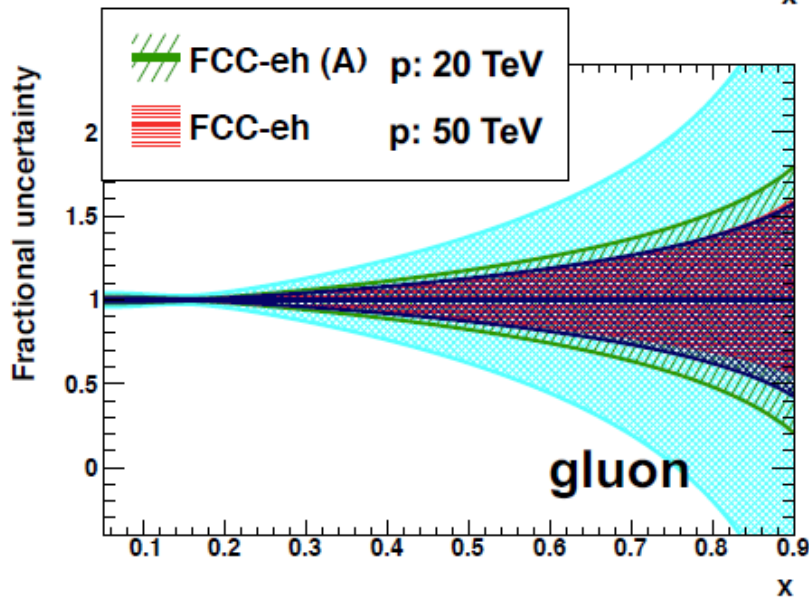
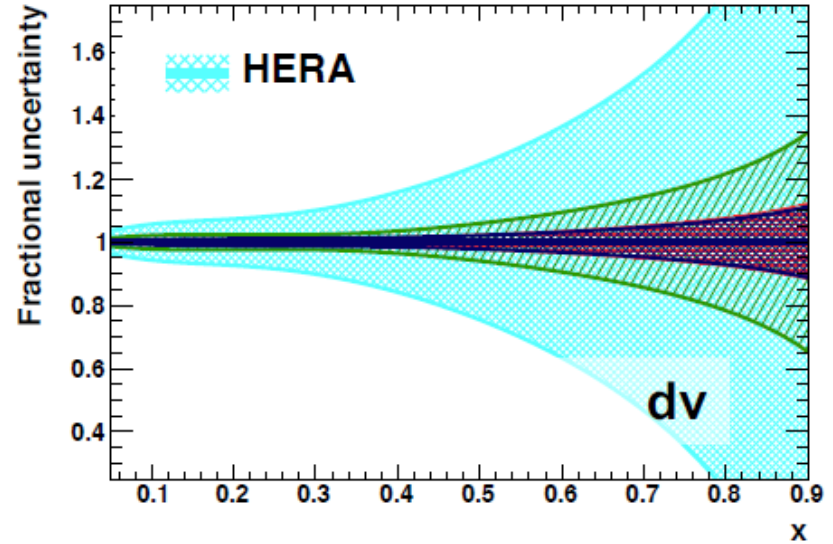
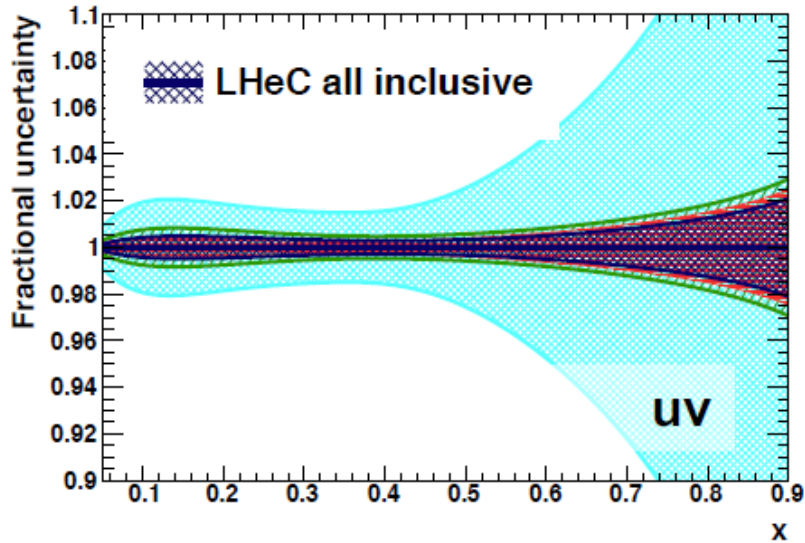
impact of polarisation on LHeC pdfs



impact of polarisation on pdfs generally small (but pol. important for ew)

(**CC**: $\sigma(e\pm)$ scales as $(1\pm P)$; **NC**: effects subtle; pol. asym. gives access to $F_2^{\nu Z}$, new quark combinations)

Collider configurations



FCC-eh (A): new preliminary simulation with 2 ab^{-1} polarised e^- (NO e^+ yet; impact especially in d at large x)

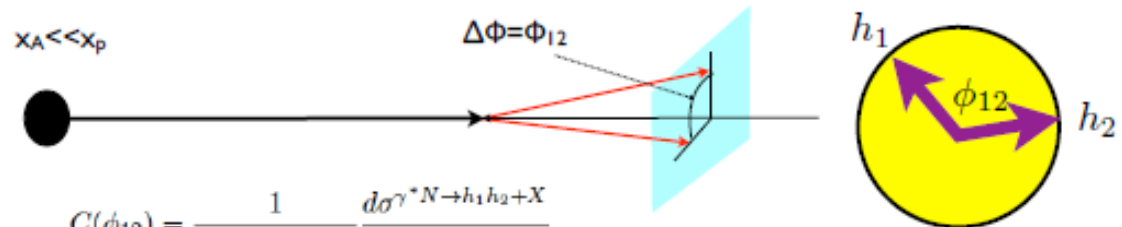
Novel small x dynamics: exclusive observables

other key probes of saturation:

- dihadron azimuthal decorrelation**

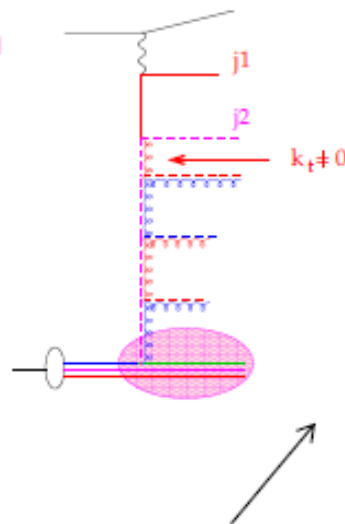
- currently discussed at RHIC as suggestive of saturation

(see also **SMALL x** plenary, A. Dumitru, MON, 11:30)

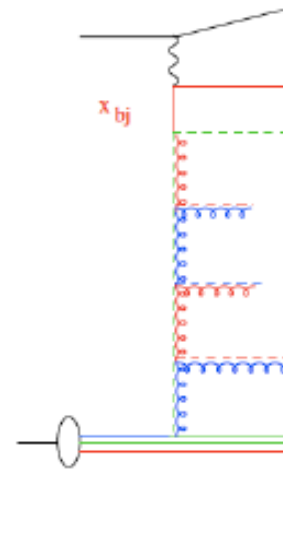
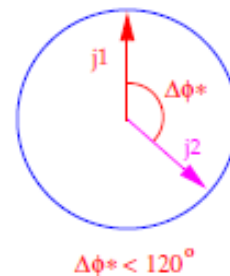


$$C(\phi_{12}) = \frac{1}{\frac{d\sigma(\gamma^* N \rightarrow h_1 X)}{dz_{h1}}} \frac{d\sigma\gamma^* N \rightarrow h_1 h_2 + X}{dz_{h1} dz_{h2} d\phi_{12}}$$

- nuclear and saturation effects** on usual BFKL signals, EG. dijet azimuthal decorrelation, Mueller-Navelet jets
- A dependence?**



if incoming gluon has sizeable k_t , jets no longer back-to-back; must balance k_t of incoming virtual gluon



measurements with large rapidity separations and different (Q, p_t) combinations to systematically test parton dynamics

DGLAP: $Q^2 \gg p_t^2$
($Q^2 = p_t^2$ suppresses DGLAP)

x_{bj} small

evolution from large to small x

'forward' jet

$$x_{jet} = \frac{E_{jet}}{E_{proton}} = \text{large}$$