

Anisotropy of Lepton-Jet Correlation in Inclusive and Diffractive DIS

In collaboration with [Bowen Xiao, Yuanyuan Zhang](#): PRL.130, 151902(2023)
PRD. 109, 054004 (2024)

Xuan-Bo Tong

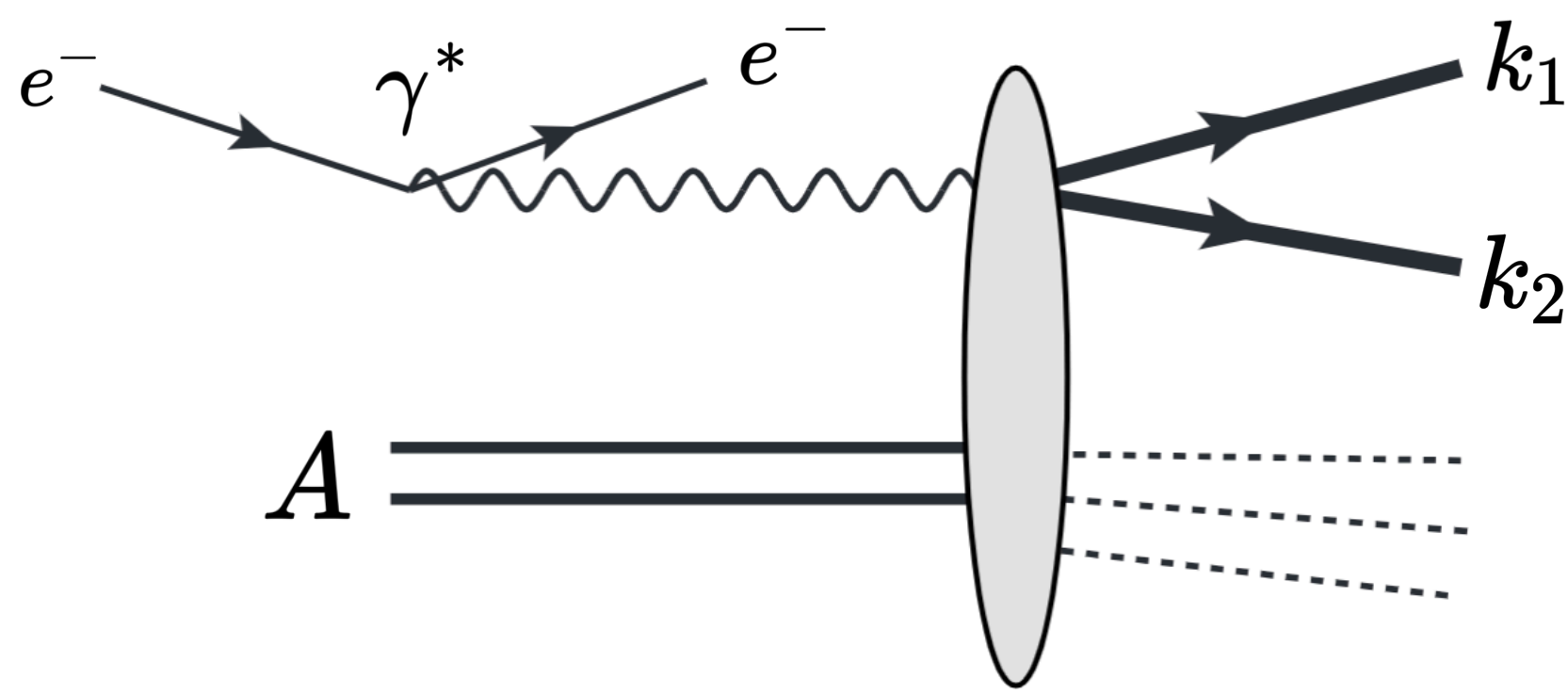
University of Jyväskylä

DIS 2024

April 10th, 2024



Two-particle correlation for saturation



•Tons of progress for the EIC !

Zheng-Aschenauer-Lee-Xiao, PRD89,074037(2014),

► Dihadron: e.g. Bergabo-Jaliilan-Marian PRD. 107, 054036 (2023)

Iancu-Mulian JHEP07(2023)121

Dominguez-Xiao-Yuan PRL106, 022301 (2011)

► Dijet: e.g. Mäntysaari-Mueller-Salazar-Schenke PRL124,112301(2020)

Caucal-Salazar-Schenke-Venugopalan JHEP11(2022)169

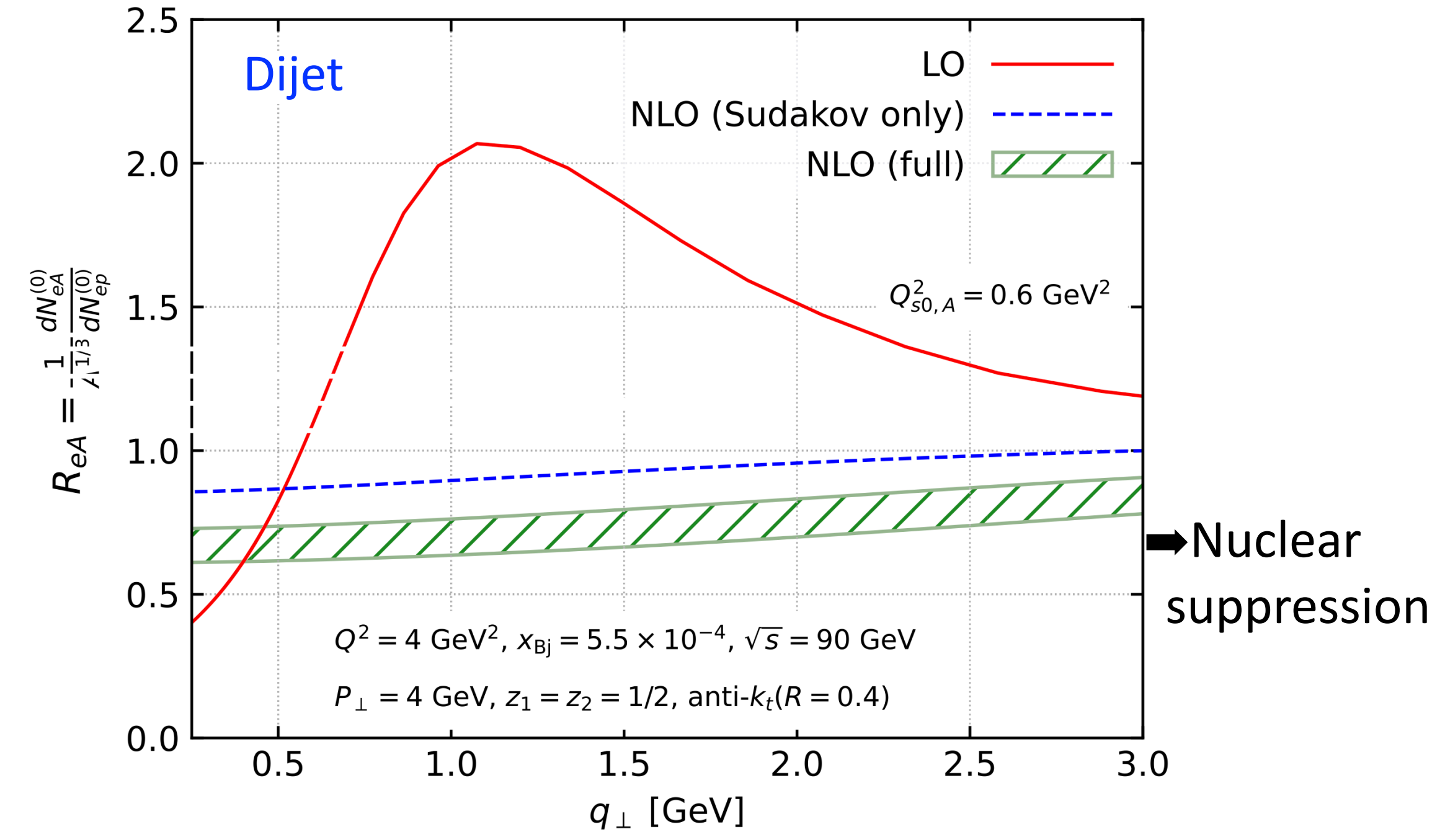
► Photon-jet: e.g. Kolbé-Roy-Salazar-Schenke-Venugopalan JHEP01(2021)052

a recent review: Morreale-Salazar, Universe 7 (2021) 8, 312

•Back-to-back configuration

► **Momentum imbalance** $\vec{q}_\perp = \vec{k}_{1\perp} + \vec{k}_{2\perp}$

► Relative momentum $\vec{P}_\perp = (\vec{k}_{1\perp} - \vec{k}_{2\perp})/2$



Caucal-Salazar-Schenke-Stebel-Venugopalan PRL 132, 081902 (2024)

•Saturation momentum Q_s

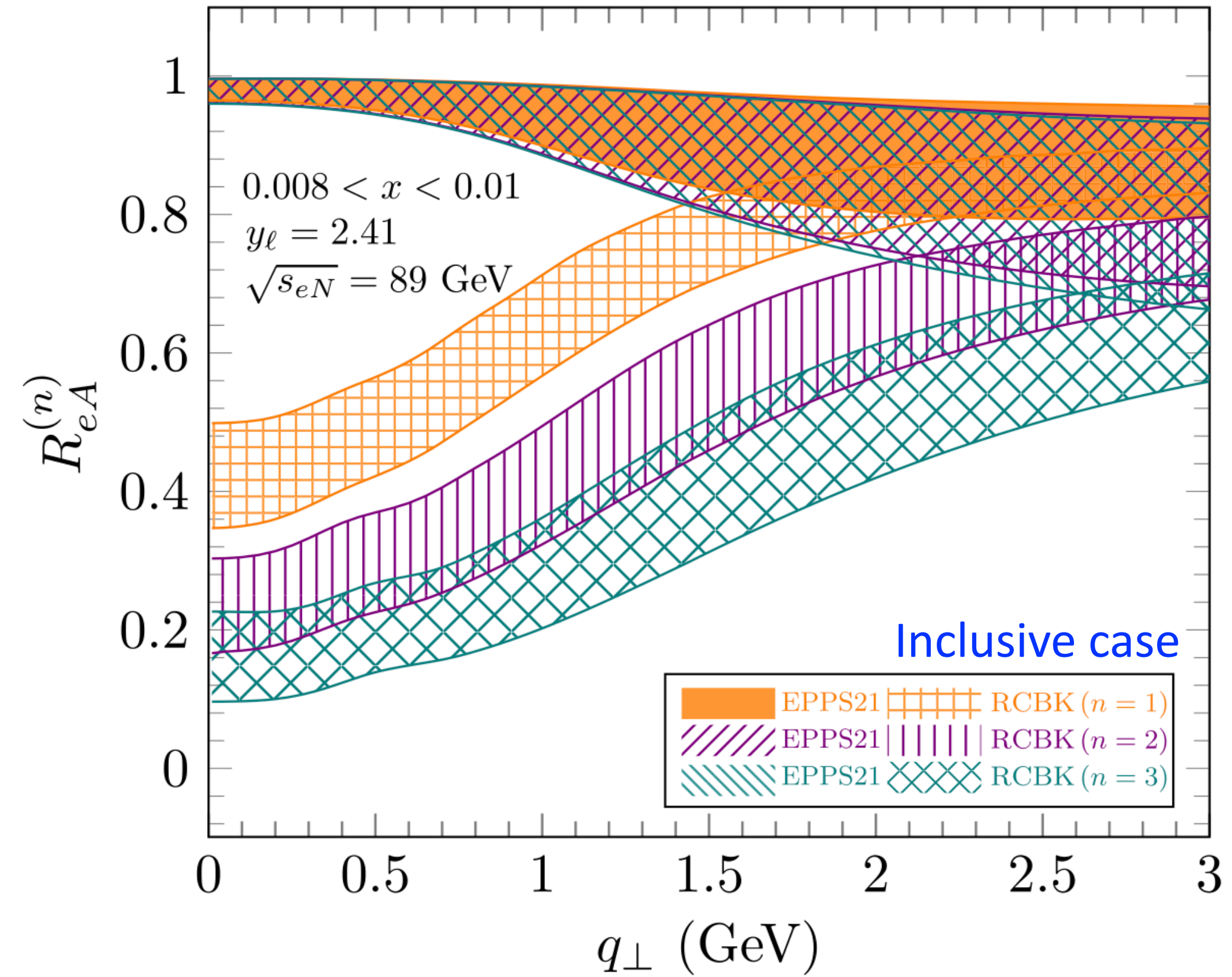
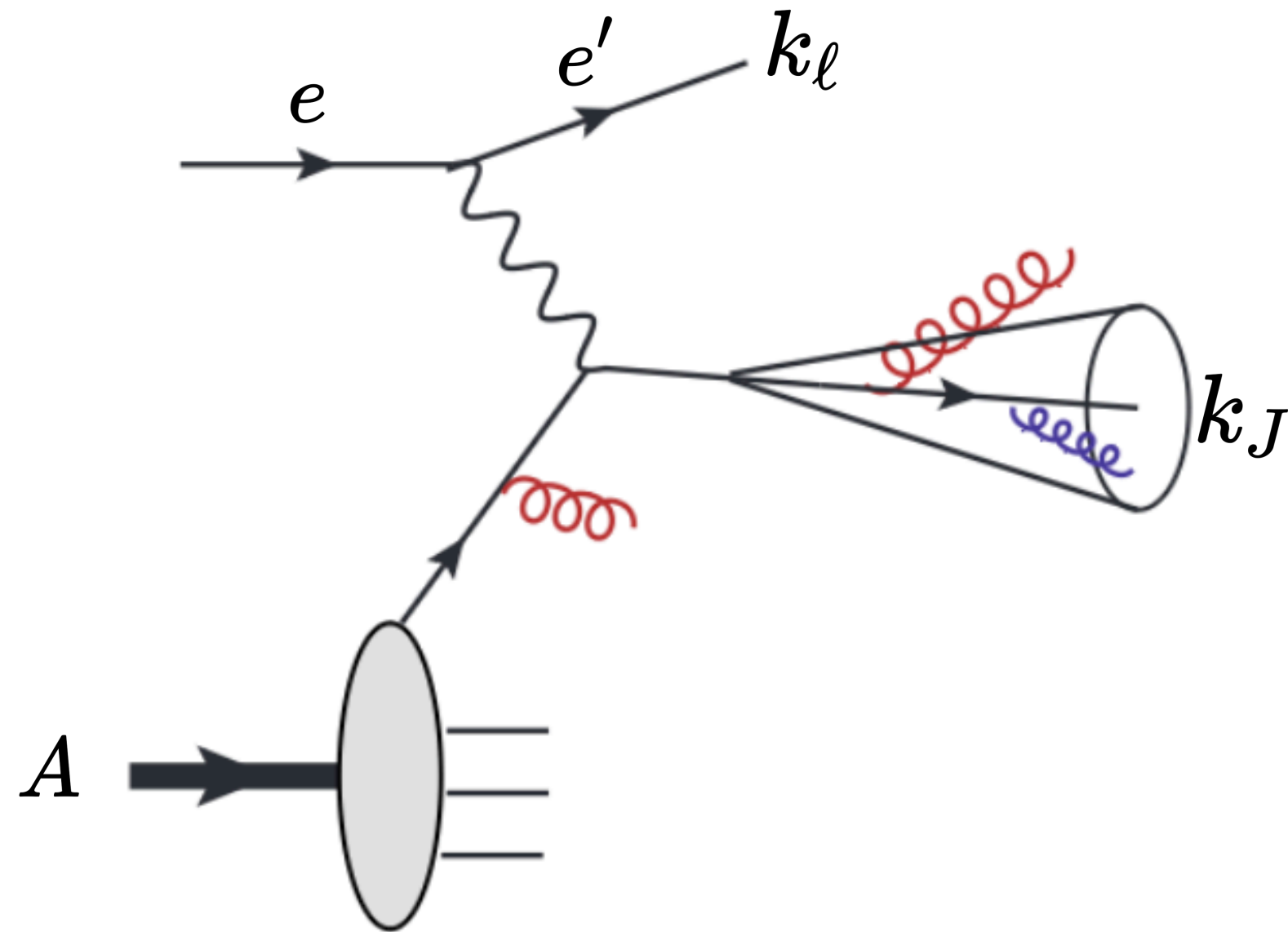
-Typical transverse momentum of small-x gluons

$$q_\perp \sim k_{g\perp} \lesssim Q_s$$

-Nuclear modification

$$Q_s^2 \propto A^{1/3} \Rightarrow R_{eA} = \frac{1}{A} \frac{d\sigma_{eA}}{d\sigma_{ep}} < 1$$

Lepton-jet correlation — a novel probe for saturation



$$R_{eA}^{(n)} = \frac{\langle \cos n\phi \rangle_{eA}}{\langle \cos n\phi \rangle_{ep}}$$

• Anisotropy $\langle \cos(n\phi) \rangle$

- Sensitive to Q_s in both inclusive and diffractive DIS
- Significant nuclear suppression.

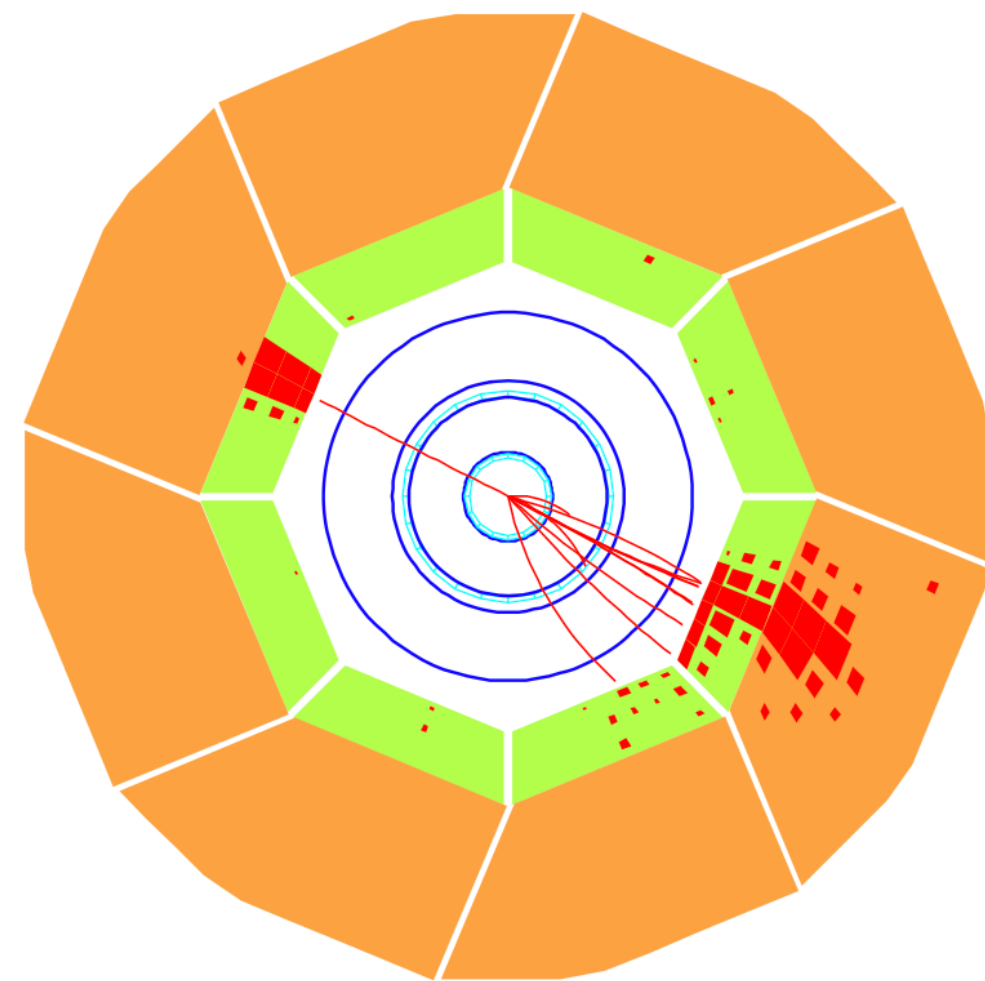
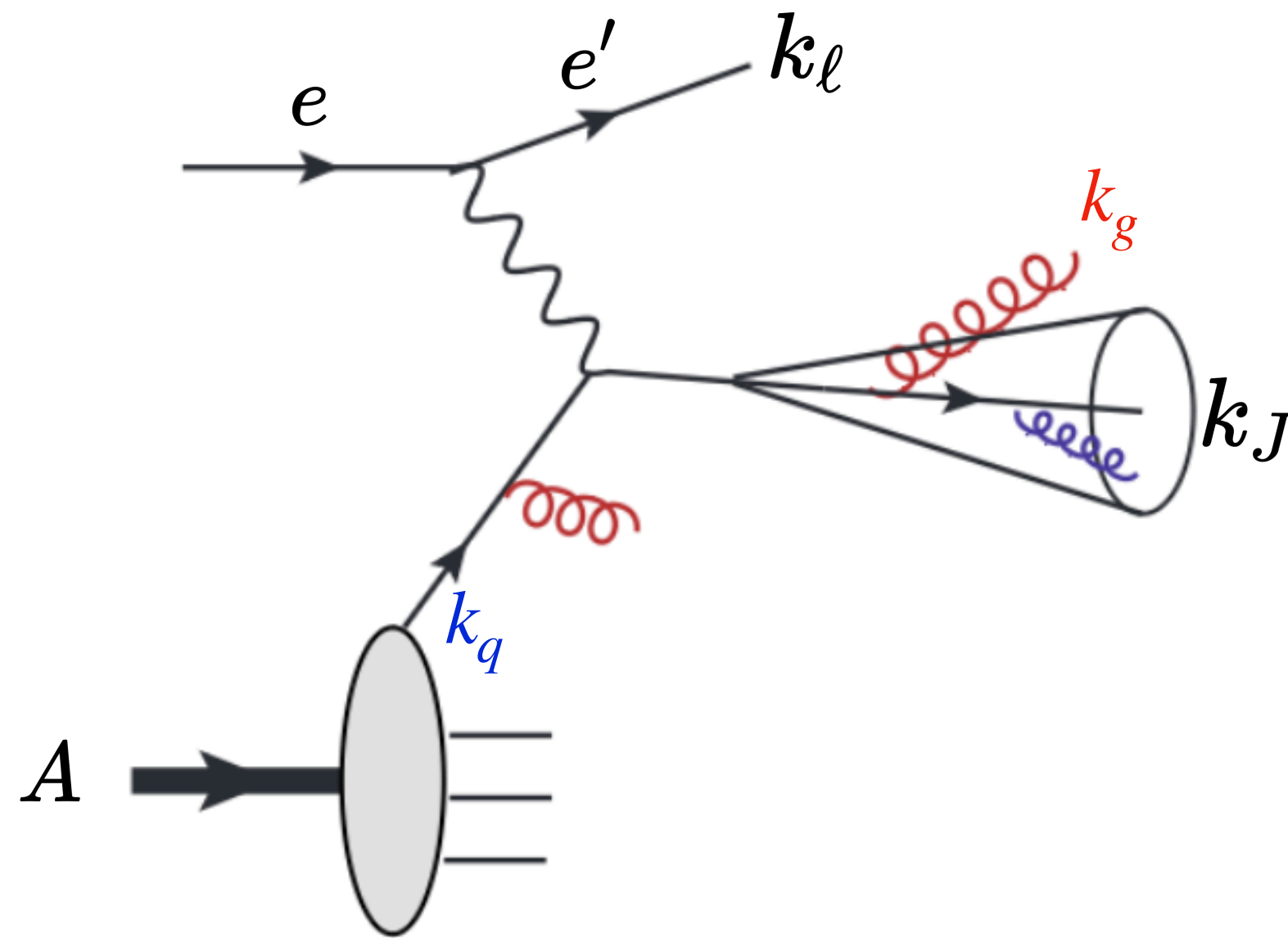
◆ Properties

⇒ ◆ Mechanism

◆ Numerics

Lepton-jet correlation

Liu-Ringer-Vogelsang-Yuan PRL22,192003 (2019); PRD102,094022 (2020)



H1 PRL 128, 132002 (2022)

•Golden channel to study quark TMDs

➡see more in WG5 talk by [Dingyu Shao](#)

$$\frac{d^5\sigma(\ell p \rightarrow \ell' J)}{dy_\ell d^2k_{\ell\perp} d^2q_\perp} = H(Q) \int d^2k_{q\perp} d^2k_{g\perp} x f_q(x, k_{q\perp}) S_J(k_{g\perp}) \times \delta^{(2)}(q_\perp - k_{q\perp} + k_{g\perp}).$$

- Clear, no fragmentation functions
- Simple kinematics, easy to measure

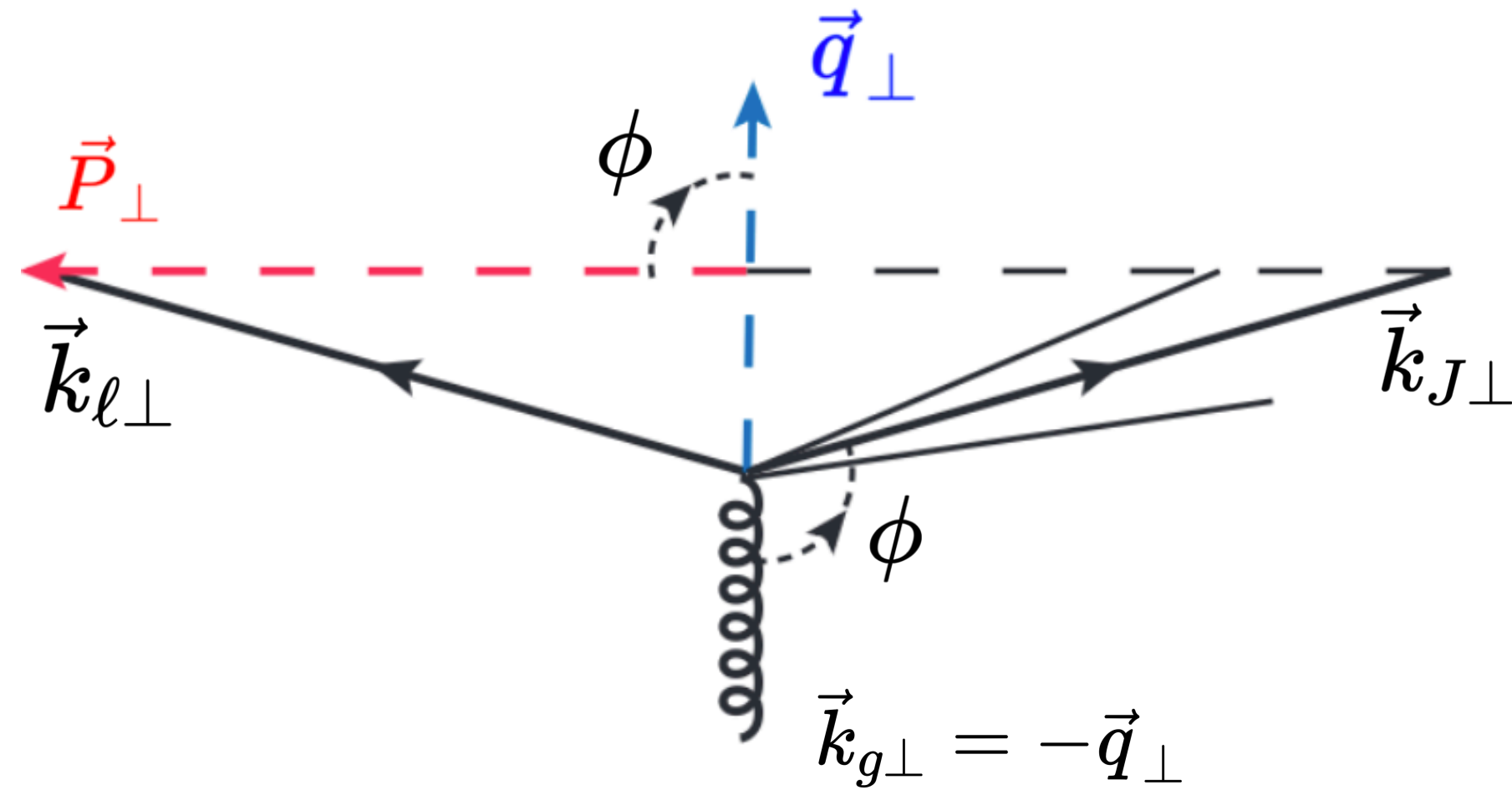
•Directly defined in the lab frame(or e-A c.m. frame)

•Final lepton and jet: back to back

- Electron as tag (precisely measured, no QCD correction)
- Jet as a hard probe ($k_{J\perp} \sim k_{\ell\perp} \gg q_\perp$)

★ $q_\perp = k_{\ell\perp} + k_{J\perp}$ comes from **Initial quark $k_{q\perp}$**

Soft gluon radiations $k_{g\perp}$



- Anisotropy:

$$\langle \cos n\phi \rangle = \frac{\sigma_n}{\sigma_0}$$

- ◆ Reveal the directional preference of \vec{q}_\perp
- ◆ Generated by **Final-state soft-gluon radiations**
 - ➔ prefer the jet-cone direction, due to collinear enhancement

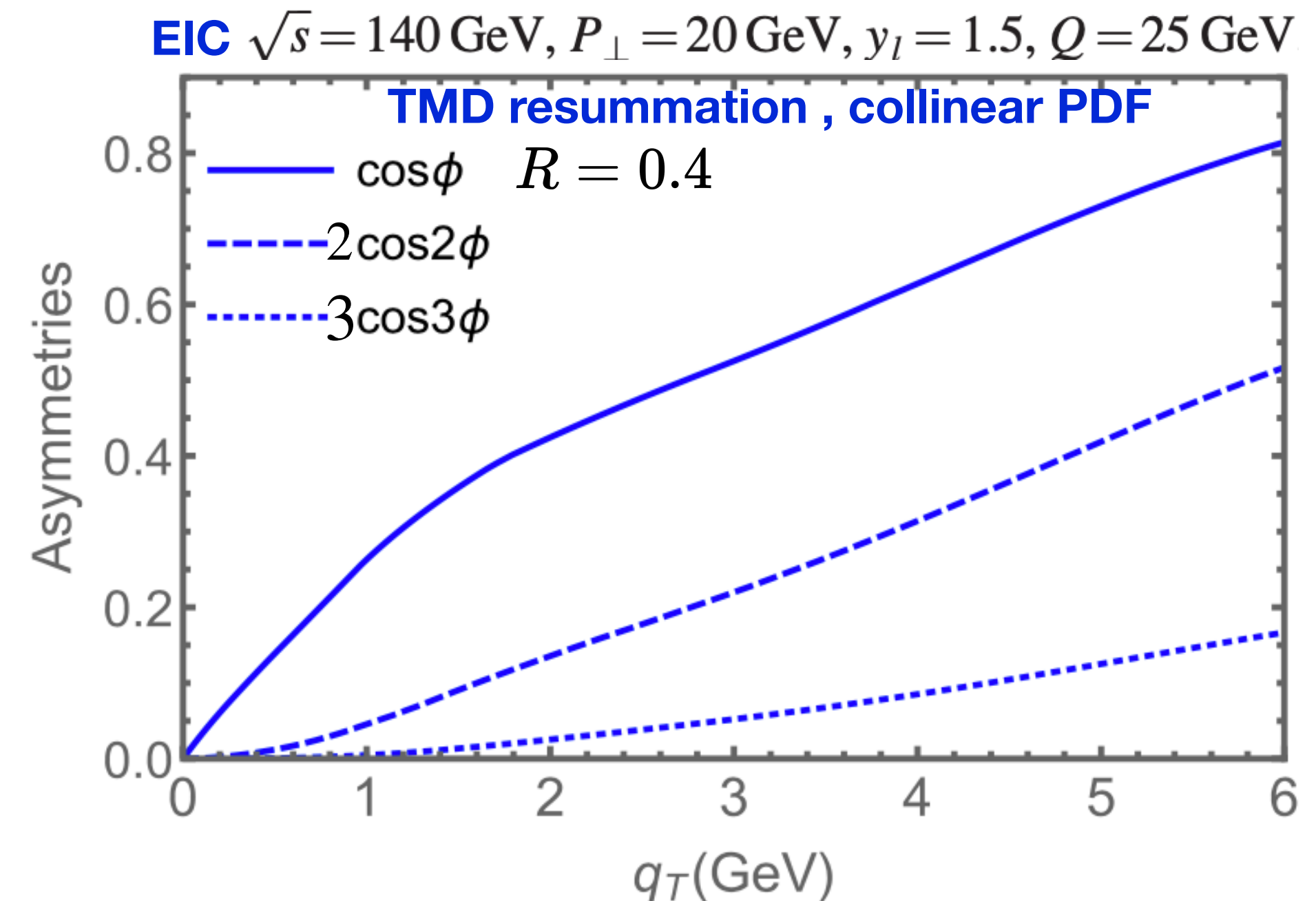
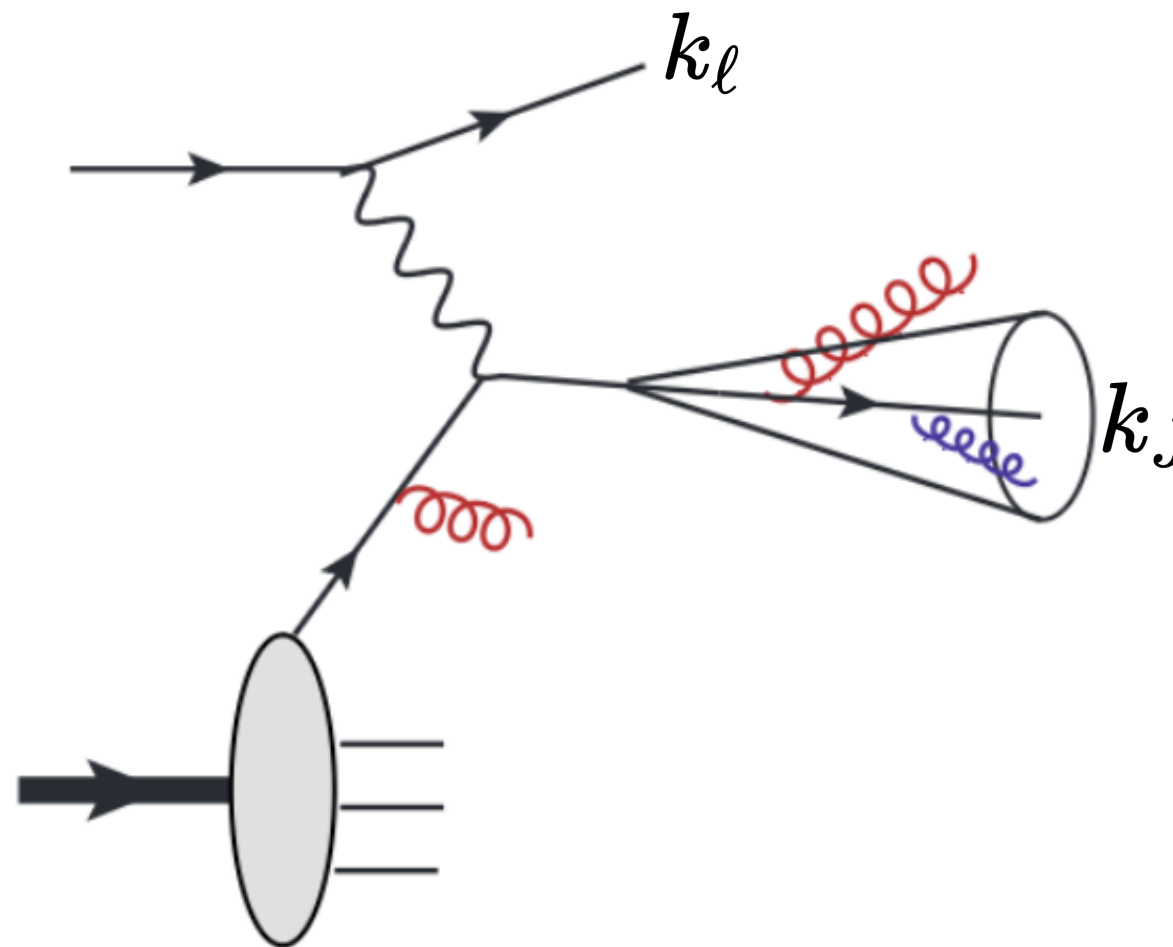
- ϕ is the azimuthal angle between:

$$\vec{q}_\perp = \vec{k}_{\ell\perp} + \vec{k}_{J\perp}$$

$$\vec{P}_\perp = (\vec{k}_{\ell\perp} - \vec{k}_{J\perp})/2$$

- Harmonic expansion:

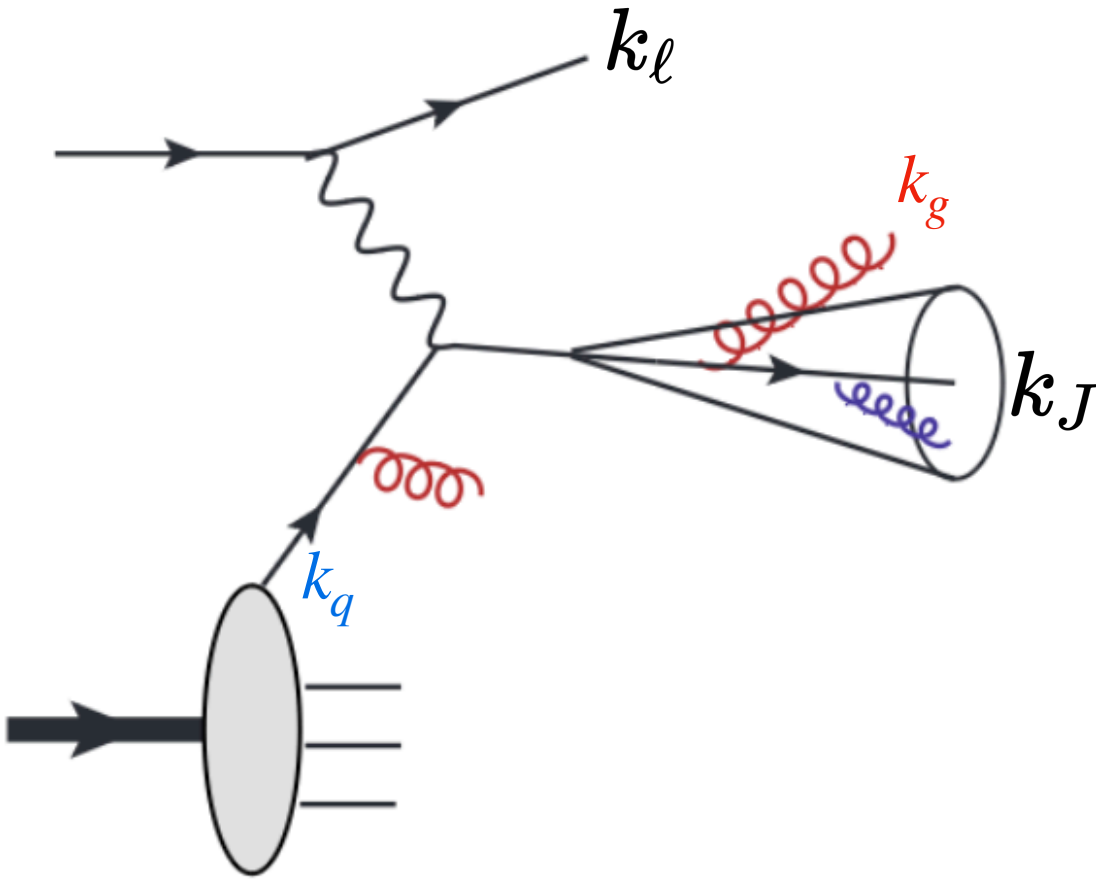
$$\frac{d\sigma}{dy_\ell d^2 P_\perp d^2 q_\perp} = \sigma_0 + 2 \sum_{n=1}^{\infty} \sigma_n \cos(n\phi)$$



Sizable! Dominated by $\cos(\phi)$ -modulation

●Azimuthal angle anisotropy

- ◆ q_{\perp} of LJC comes from (1) Initial quark $k_{q\perp}$ -> Can it produce an anisotropy?
(2) Final-state soft gluon radiations $k_{g\perp}$



<div><div>\vec{q}_{\perp}</div><div>Observables</div></div>	Dijet: $\cos 2\phi$	lepton-jet $\cos n\phi$
Intrinsic transverse momentum (Unpolarized target)	✓ linearly polarized gluon <small>e.g. Boer-Brodsky-Mulders-Pisano 2011 Metz-Zhou 2011</small>	✗ unpolarized initial quark
Radiation <small>Hatta-Xiao-Yuan-Zhou 2021</small>	✓ soft gluon	✓ soft gluon

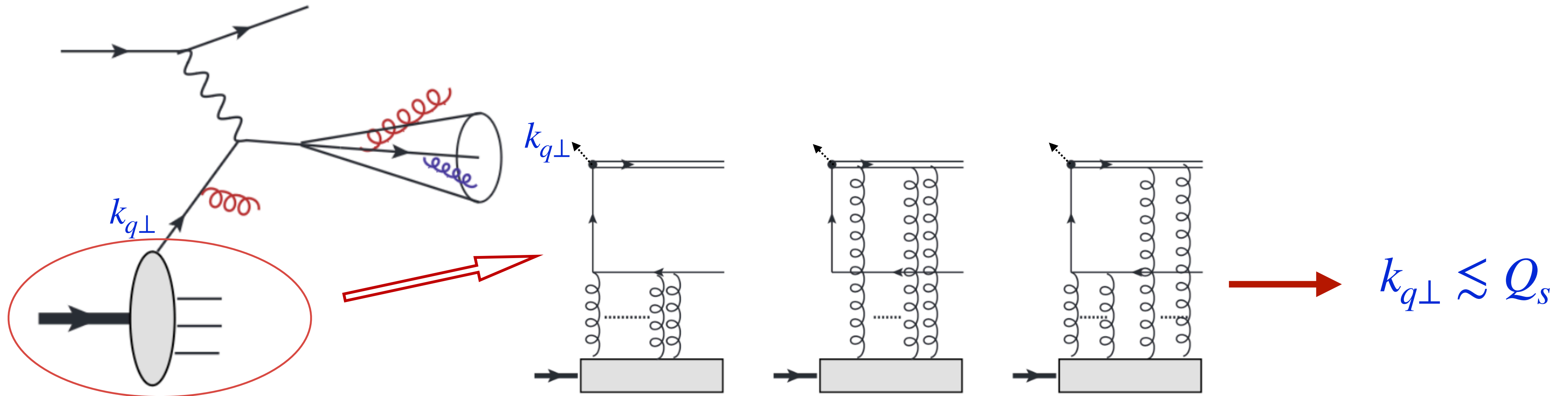
➡No angular preference!

➡Large probability in the jet direction

This unique property of the lepton-jet anisotropy -> Search for parton saturation!

● Lepton-jet anisotropy: a novel indicator of parton saturation

◆ At small x , the initial quark k_T is from multiple scatterings of small- x gluons and their radiations



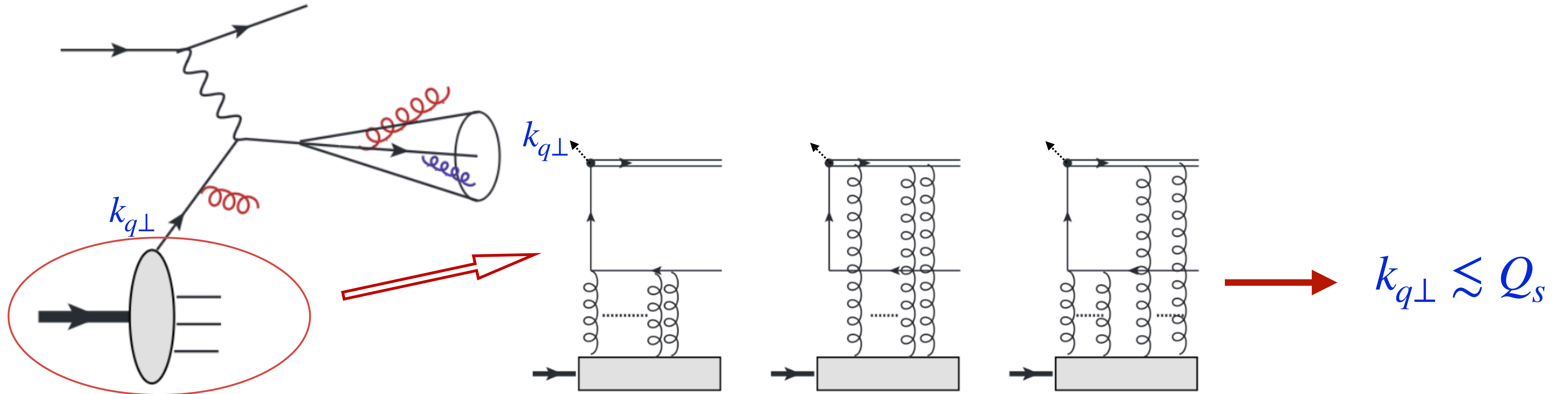
◆ For a given q_\perp , larger Q_s , “less room” left for final-state gluons to produce anisotropy

➡ Saturation effects wash out the anisotropy, especially in the region $q_\perp \lesssim Q_s$.

➡ Suppression of the anisotropy from ep to eA. $Q_s^2 \propto A^{1/3}$

● Lepton-jet anisotropy: a novel indicator of parton saturation

◆ At small x , the initial quark k_T is from multiple scatterings of small- x gluons and their radiations



➡ Small- x TMD quark distribution:

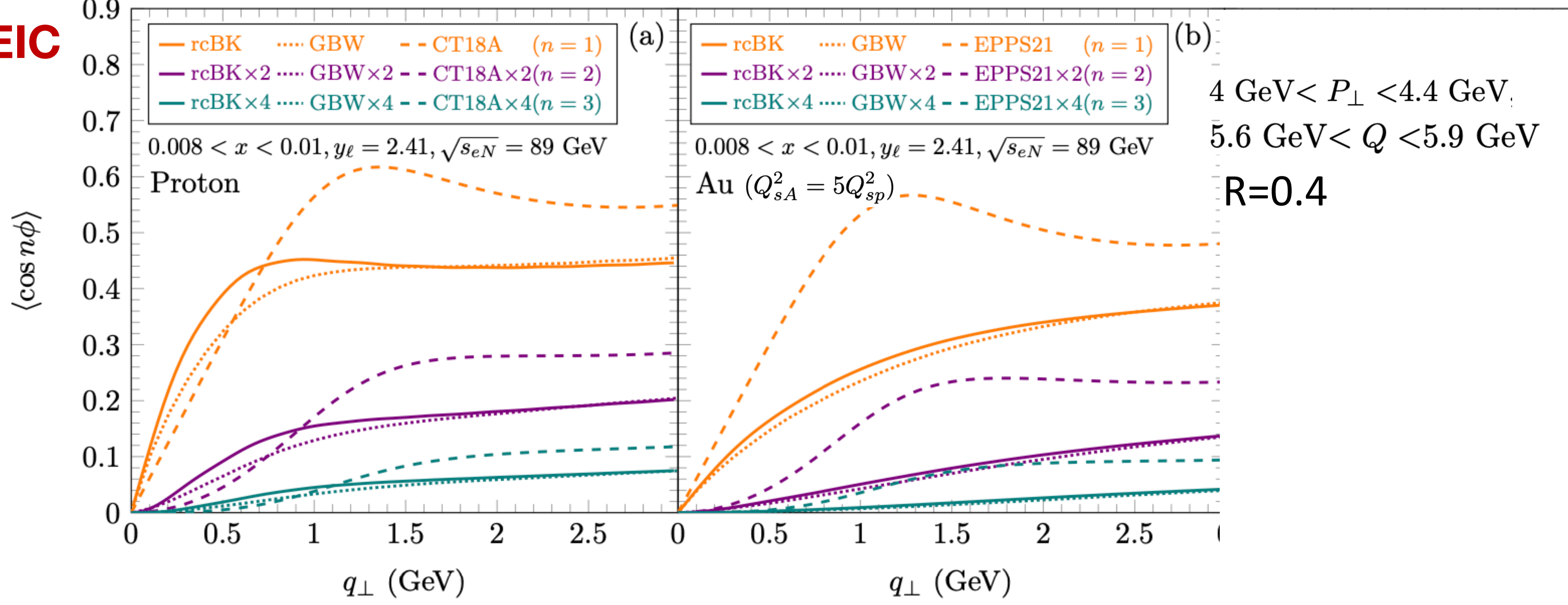
McLerran-Venugopalan, PRD 59,094002 (1999)

Mueller NPB 558, 285-303 (1999)

Xiao-Yuan-Zhou, NPB 921,104-126 (2017)

$$x f_q(x, r_\perp) = \frac{N_c S_\perp}{8\pi^4} \int d\epsilon_f^2 d^2 y_\perp \frac{(\vec{r}_\perp + \vec{y}_\perp) \cdot \vec{y}_\perp}{|\vec{r}_\perp + \vec{y}_\perp| |\vec{y}_\perp|} \\ \times \epsilon_f^2 K_1(\epsilon_f |\vec{r}_\perp + \vec{y}_\perp|) K_1(\epsilon_f |\vec{y}_\perp|) \\ \times [1 + \mathcal{S}_x(r_\perp) - \mathcal{S}_x(r_\perp + y_\perp) - \mathcal{S}_x(y_\perp)]$$

Prediction for the EIC



Resummation formula

$$\langle \cos n\phi \rangle = \frac{\sigma_{\text{LO}} \int r_\perp dr_\perp \mathbf{J}_n(q_\perp r_\perp) \frac{\alpha_s C_F c_n(R)}{n\pi} e^{-\text{Sud}(r_\perp, R)} \sum_q e_q^2 x f_q(x, r_\perp)}{\sigma_{\text{LO}} \int r_\perp dr_\perp \mathbf{J}_0(q_\perp r_\perp) e^{-\text{Sud}(r_\perp, R)} \sum_q e_q^2 x f_q(x, r_\perp)}.$$

◆ Saturation framework:

- Small- x quark TMDs with dipole amplitude

◆ Non-saturation framework: Hatta-Xiao-Yuan-Zhou, 2021

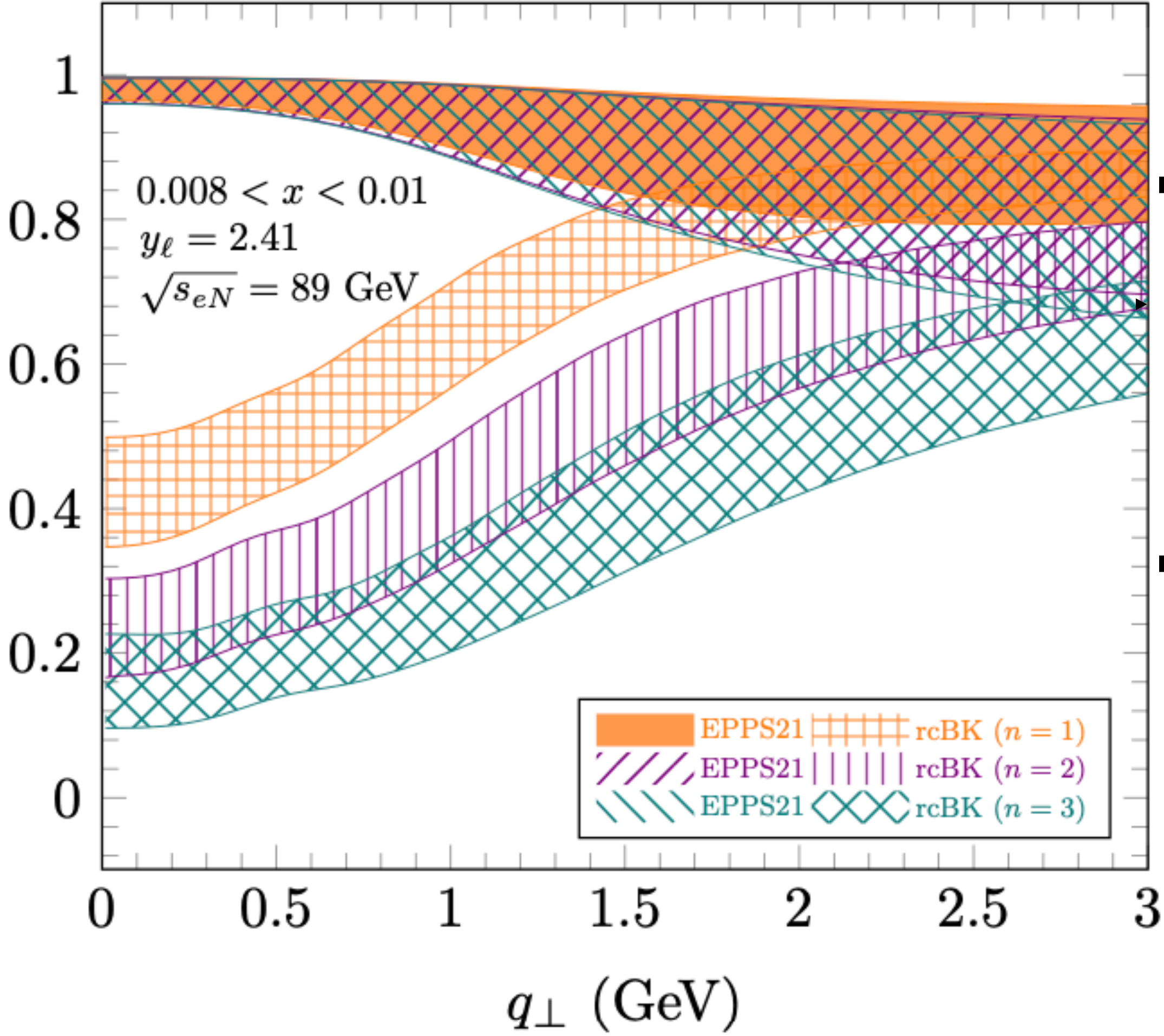
- Collinear quark PDF, proton(CT18A), Gold(EPPS21)

● **Prediction for the EIC**

◆ Nuclear modification factor:

$$R_{eA}^{(n)} = \frac{\langle \cos n\phi \rangle_{eA}}{\langle \cos n\phi \rangle_{ep}}$$

$R_{eA}^{(n)}$



→ Collinear framework:

▸ Uncertainty from the PDFs

→ Saturation framework

$$3Q_{sp}^2 < Q_{sA}^2 < 5Q_{sp}^2$$

◆ Saturation-framework: the anisotropies have a **sizable decrease** from ep to eA

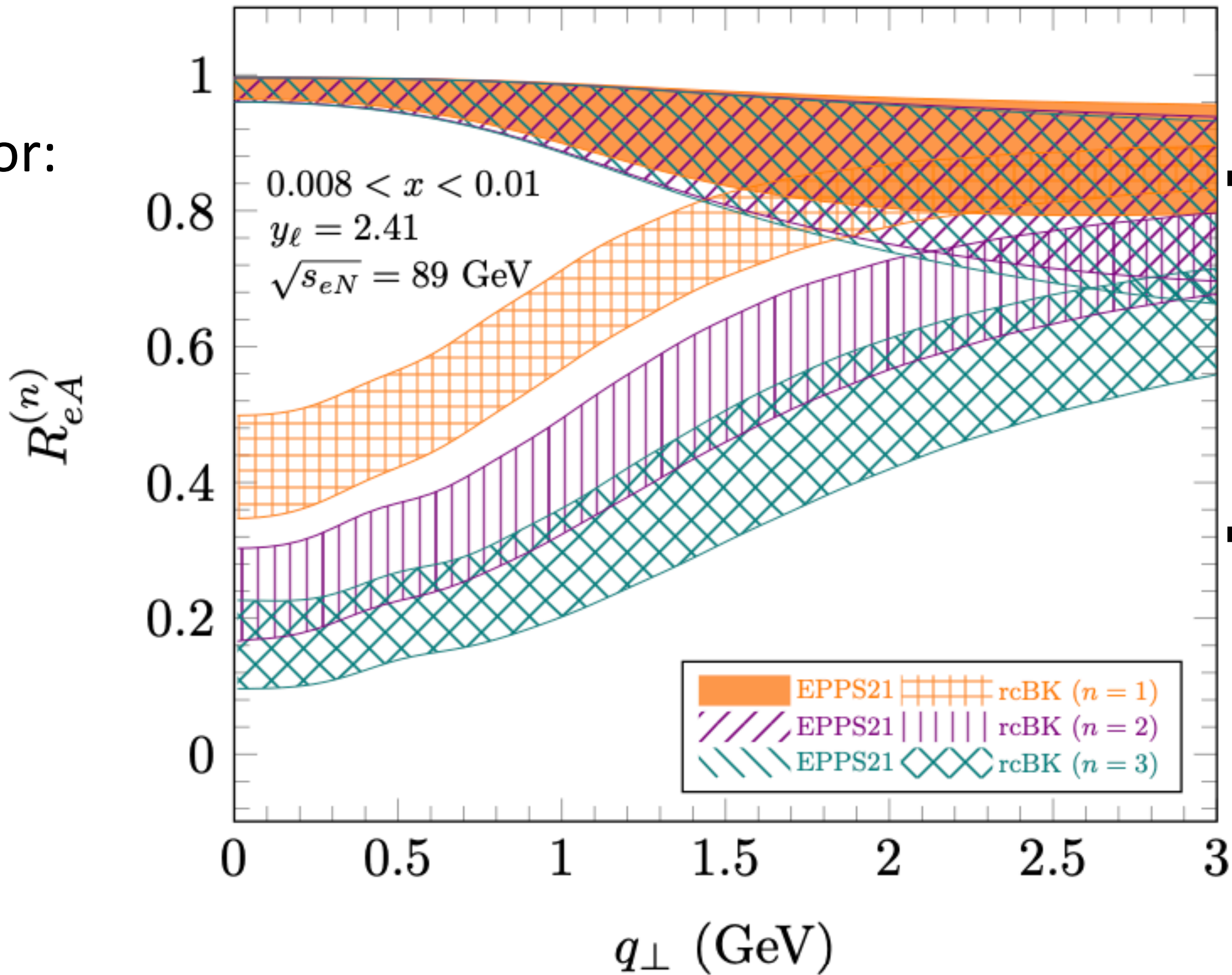
Sensitive to the saturation effects.

Significant at small q_⊥

Prediction for the EIC

◆ Nuclear modification factor:

$$R_{eA}^{(n)} = \frac{\langle \cos n\phi \rangle_{eA}}{\langle \cos n\phi \rangle_{ep}}$$



→ Collinear framework:
 ▸ Uncertainty from the PDFs

→ Saturation framework
 $3Q_{sp}^2 < Q_{sA}^2 < 5Q_{sp}^2$

◆ Collinear framework: **nearly no nuclear suppression at small- q_{\perp}**

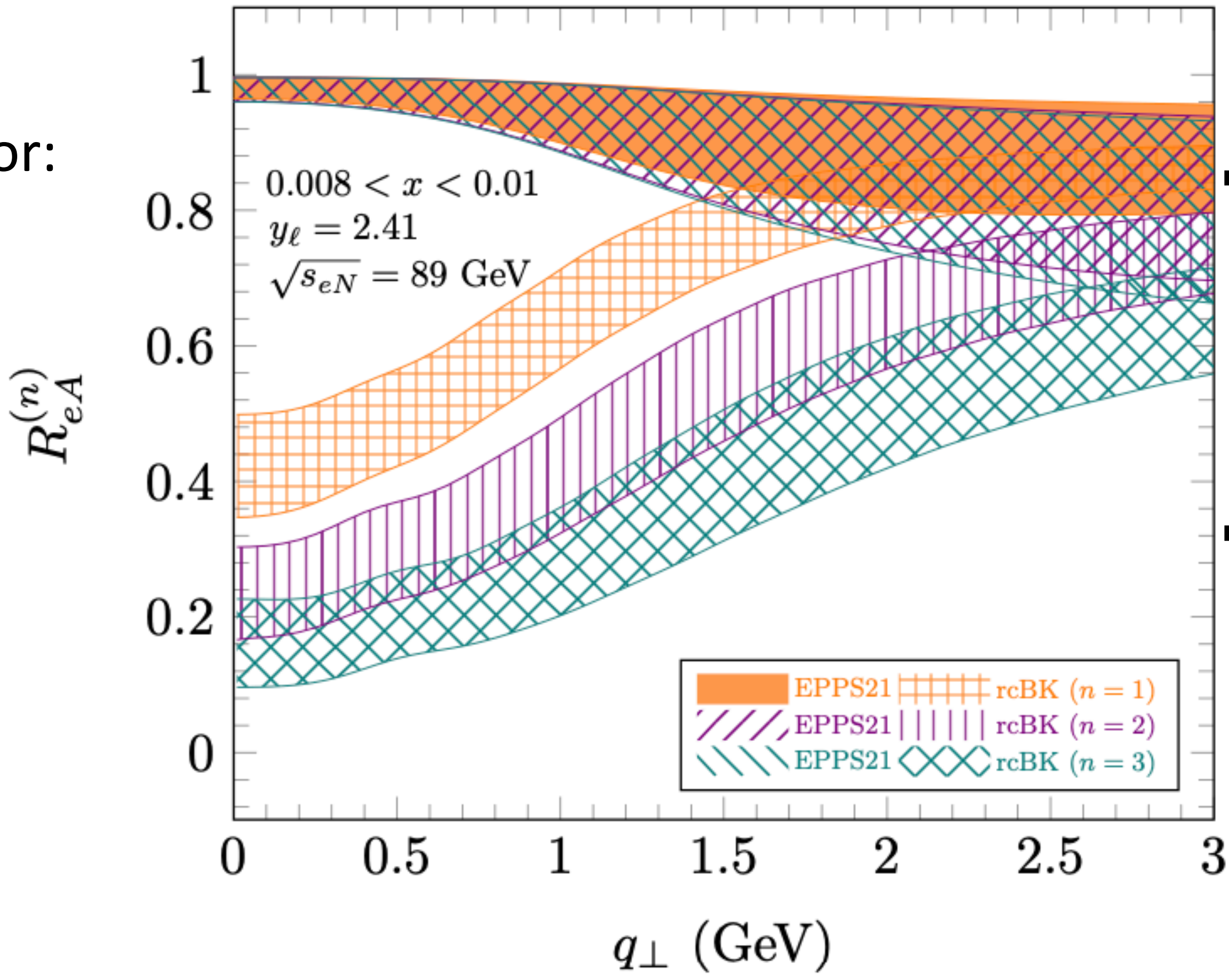
-No intrinsic kT ; Nuclear effects cancel by construction of anisotropy

$$\begin{aligned} \text{e.g., } f_q^A(x) &\approx R_q^A(x) f_q^p(x) \\ \langle \cos n\phi \rangle_A &= \frac{\sigma_{n,A}}{\sigma_{0,A}} \approx \frac{R_q^A \sigma_{n,p}}{R_q^A \sigma_{0,p}} \approx \langle \cos n\phi \rangle_p \implies R_{eA}^{(n)} \approx 1 \end{aligned}$$

Prediction for the EIC

◆ Nuclear modification factor:

$$R_{eA}^{(n)} = \frac{\langle \cos n\phi \rangle_{eA}}{\langle \cos n\phi \rangle_{ep}}$$



→ Collinear framework:

▸ Uncertainty from the PDFs

→ Saturation framework

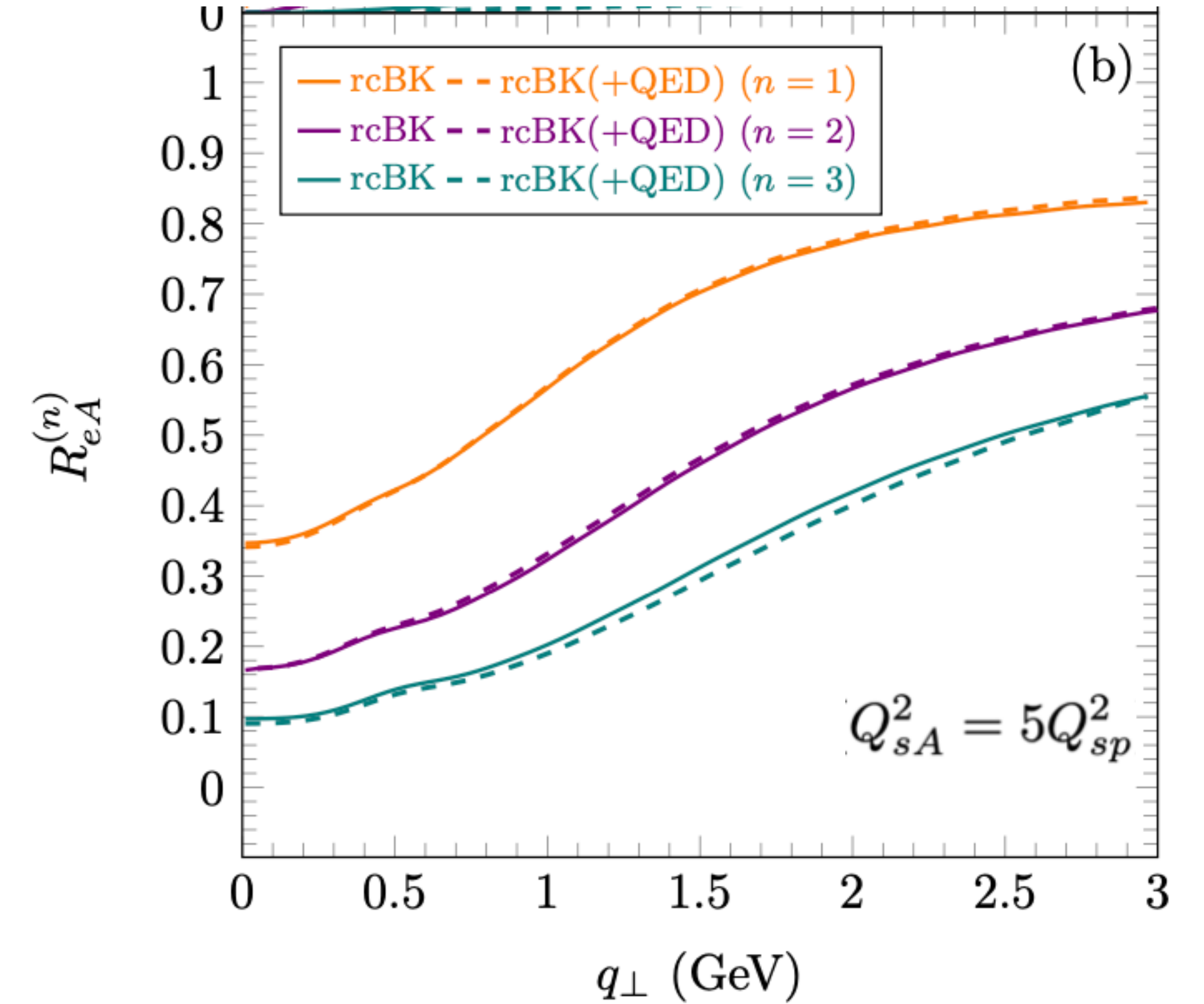
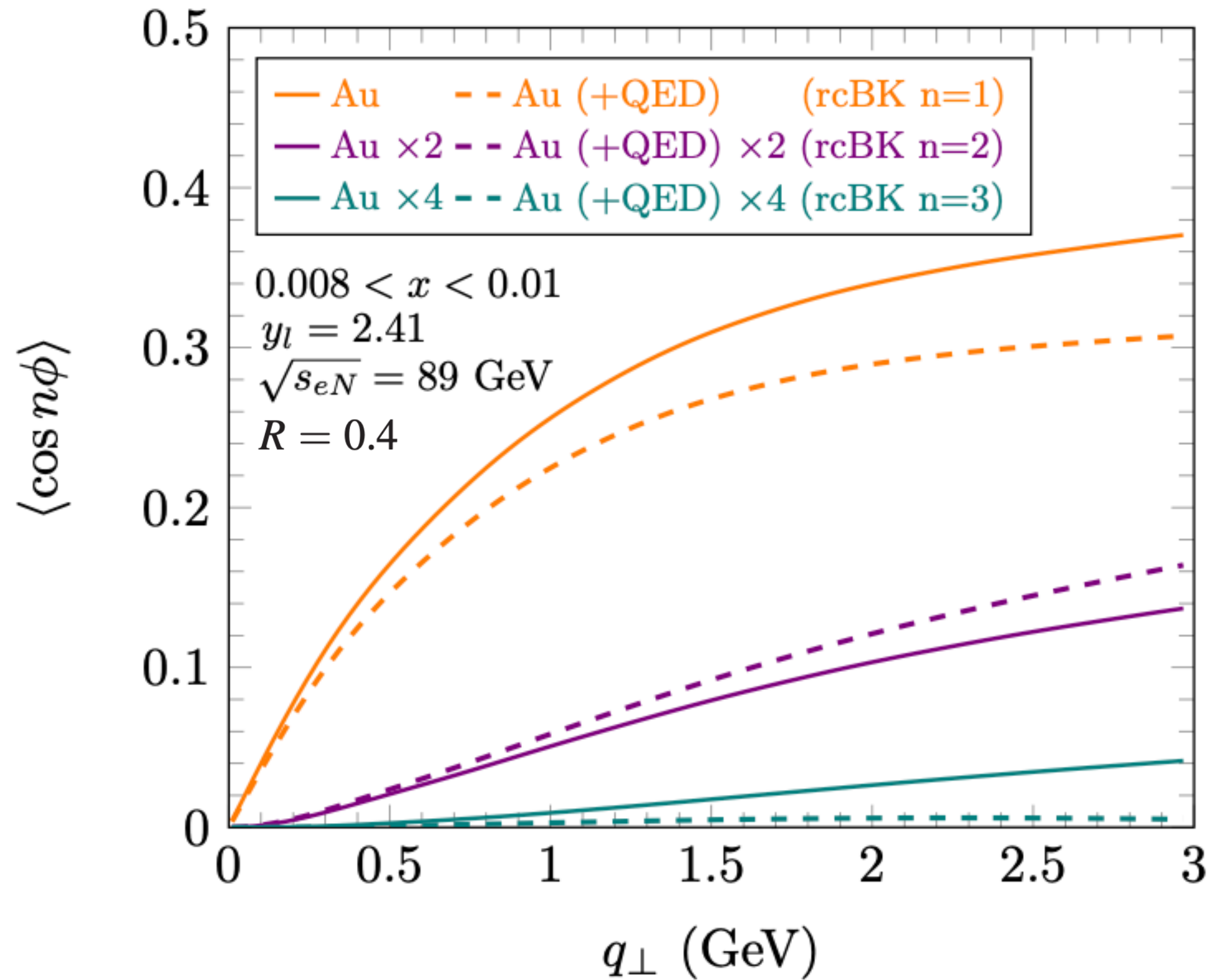
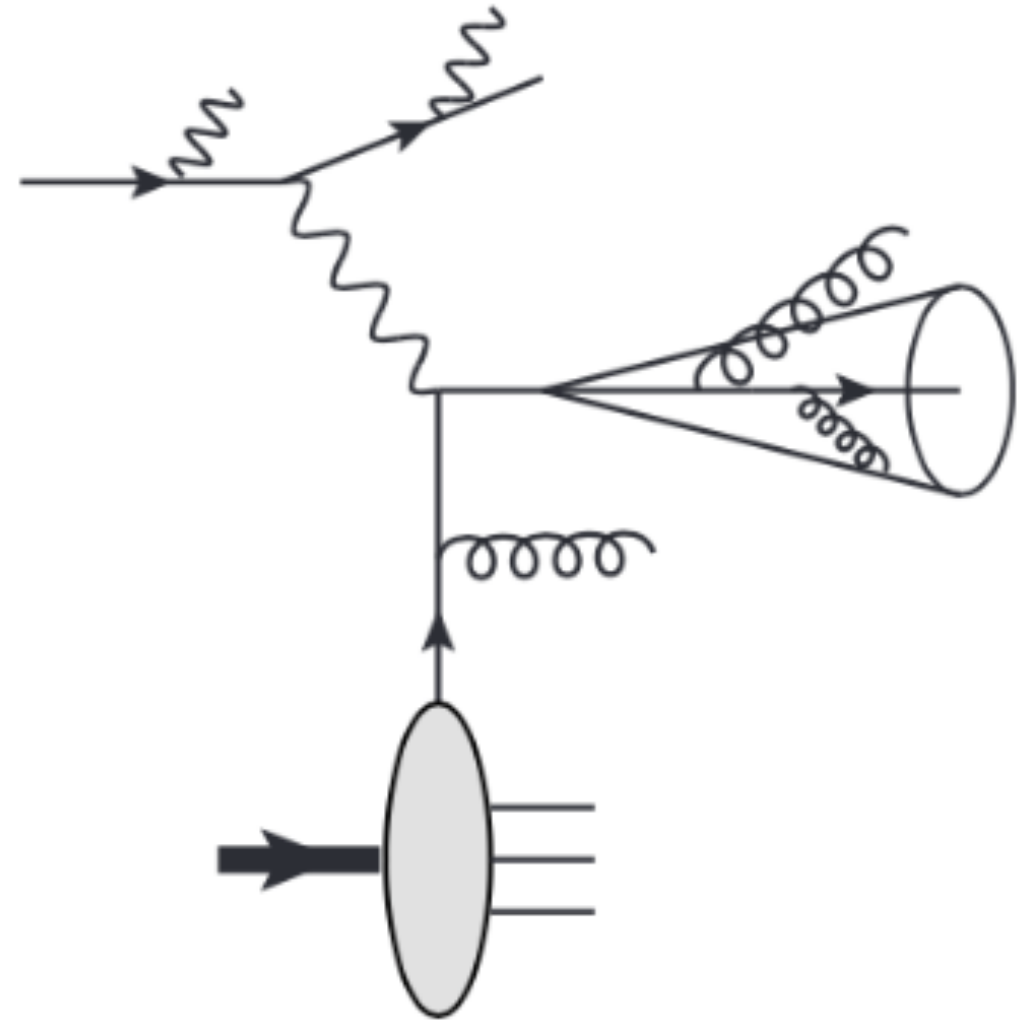
$$3Q_{sp}^2 < Q_{sA}^2 < 5Q_{sp}^2$$

◆ Striking difference between saturation framework and collinear framework at small q_{\perp}

- Power to discriminate competing mechanisms
- Can pinpoint the signature of saturation at the EIC

Prediction for the EIC

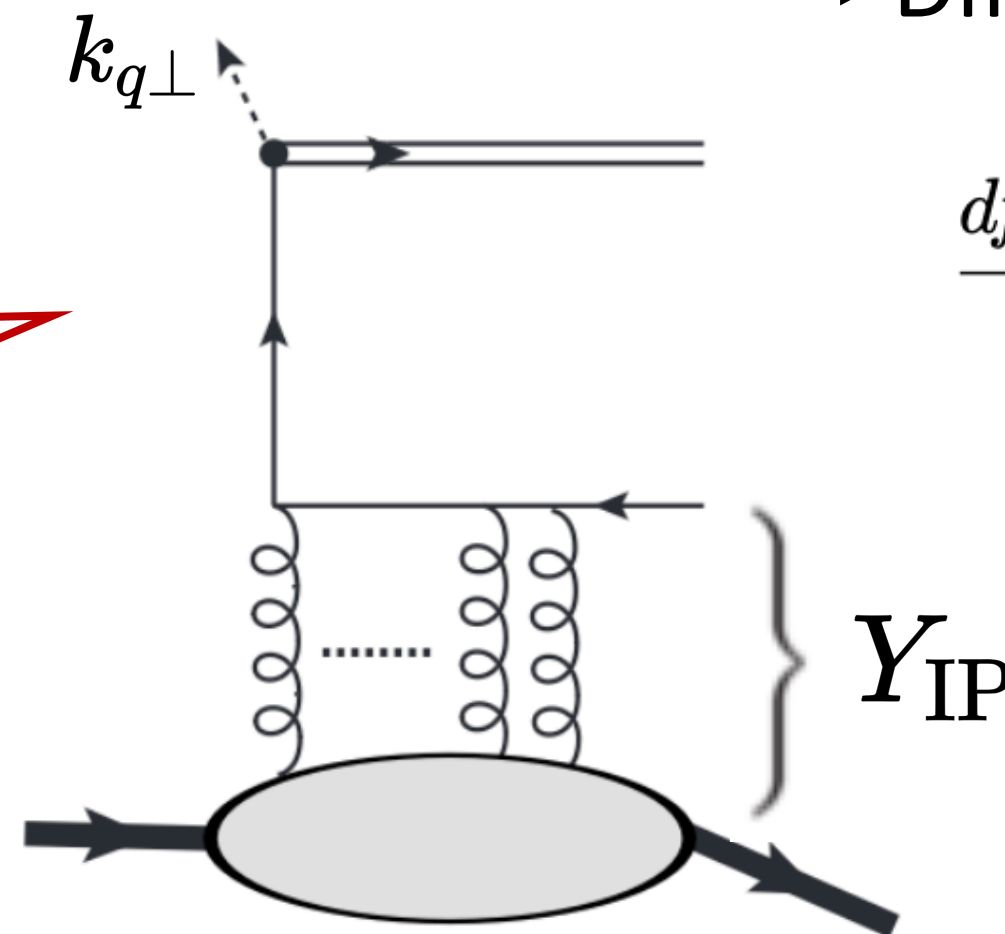
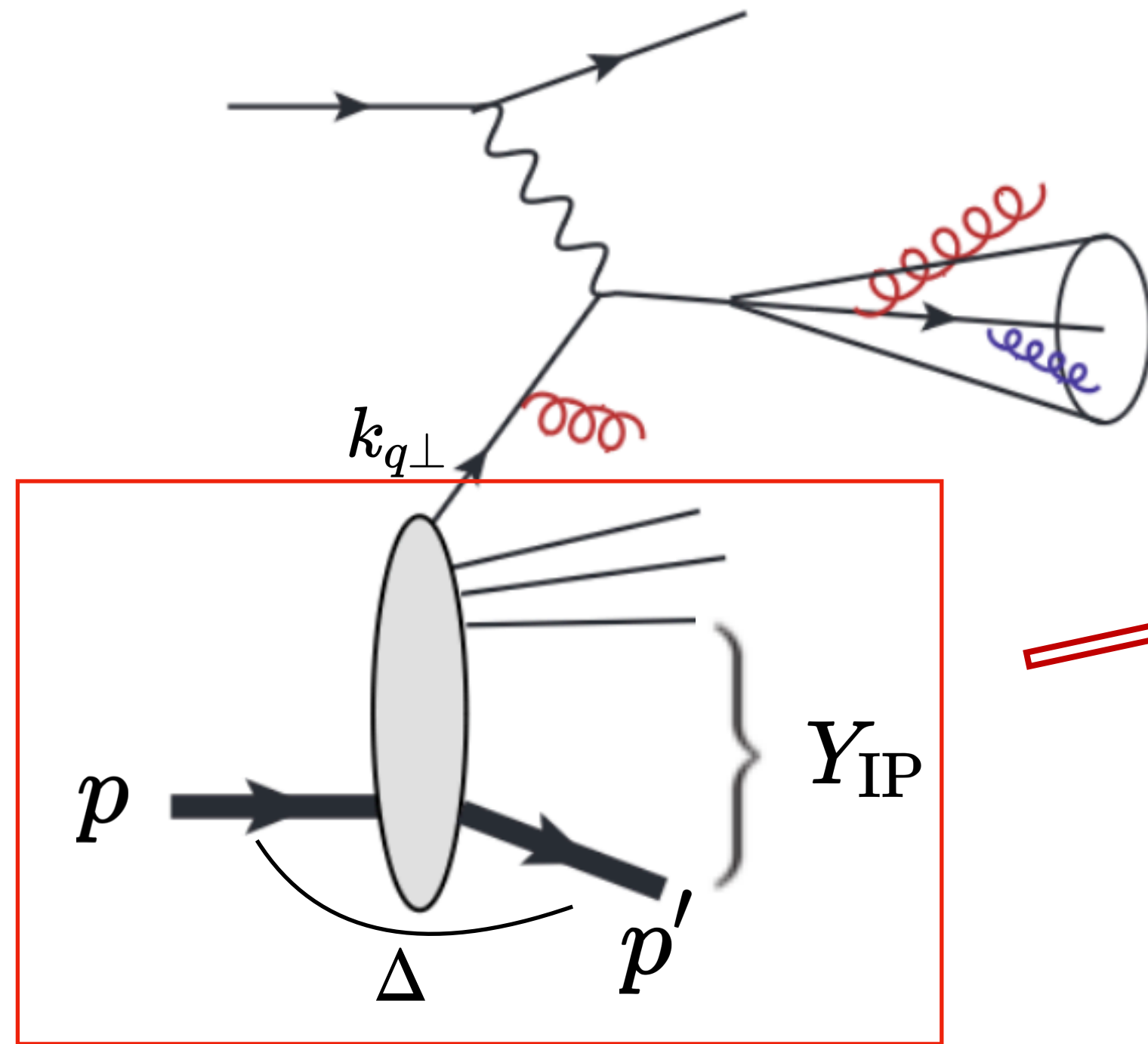
◆QED correction



➡ Corrections to $\langle \cos n\phi \rangle$ are apparent : reduce odd harmonics & increase even harmonics.

➡ Corrections to $R_{eA}^{(n)}$ are negligible, due to cancellation in the ratios .
$$R_{eA}^{(n)} = \frac{\langle \cos n\phi \rangle_{eA}}{\langle \cos n\phi \rangle_{ep}}$$

Lepton-jet correlation in Diffractive DIS



▸ Diffractive quark TMDs($\sim \text{dipole}^2$)

$$\frac{df_q^D(\beta, k_\perp, t; x_{\text{IP}})}{dY_{\text{IP}} dt} = \frac{N_c \beta}{2\pi} \int d^2 k_{1\perp} d^2 k_{2\perp} \mathcal{F}_{x_{\text{IP}}}(k_{1\perp}, \Delta_\perp) \times \mathcal{F}_{x_{\text{IP}}}(k_{2\perp}, \Delta_\perp) \mathcal{T}_q(k_\perp, k_{1\perp}, k_{2\perp})$$

Hatta et al PRD 106, 094015 (2022)

Iancu et al PRL 128, 202001 (2022)

➡ see more in the talk by [Sigtryggur Hauksson](#)

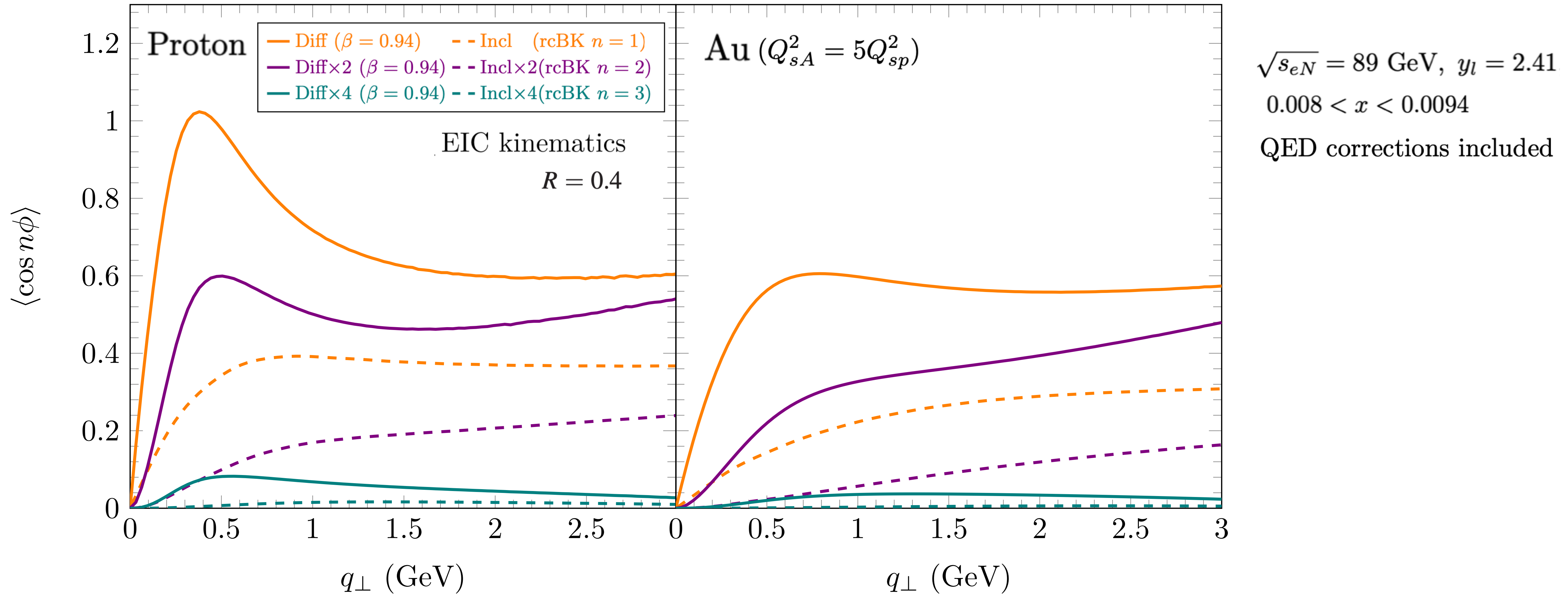
• Coherent diffraction: recoiled target & rapidity gap

▸ Final-state soft gluons & hard scatterings remain unchanged

▸ Resummation formula for $\langle \cos n\phi \rangle$: replace inclusive TMDs with diffractive TMDs

• Δ_\perp -dependence -> Target shape in the impact parameter b_\perp -space

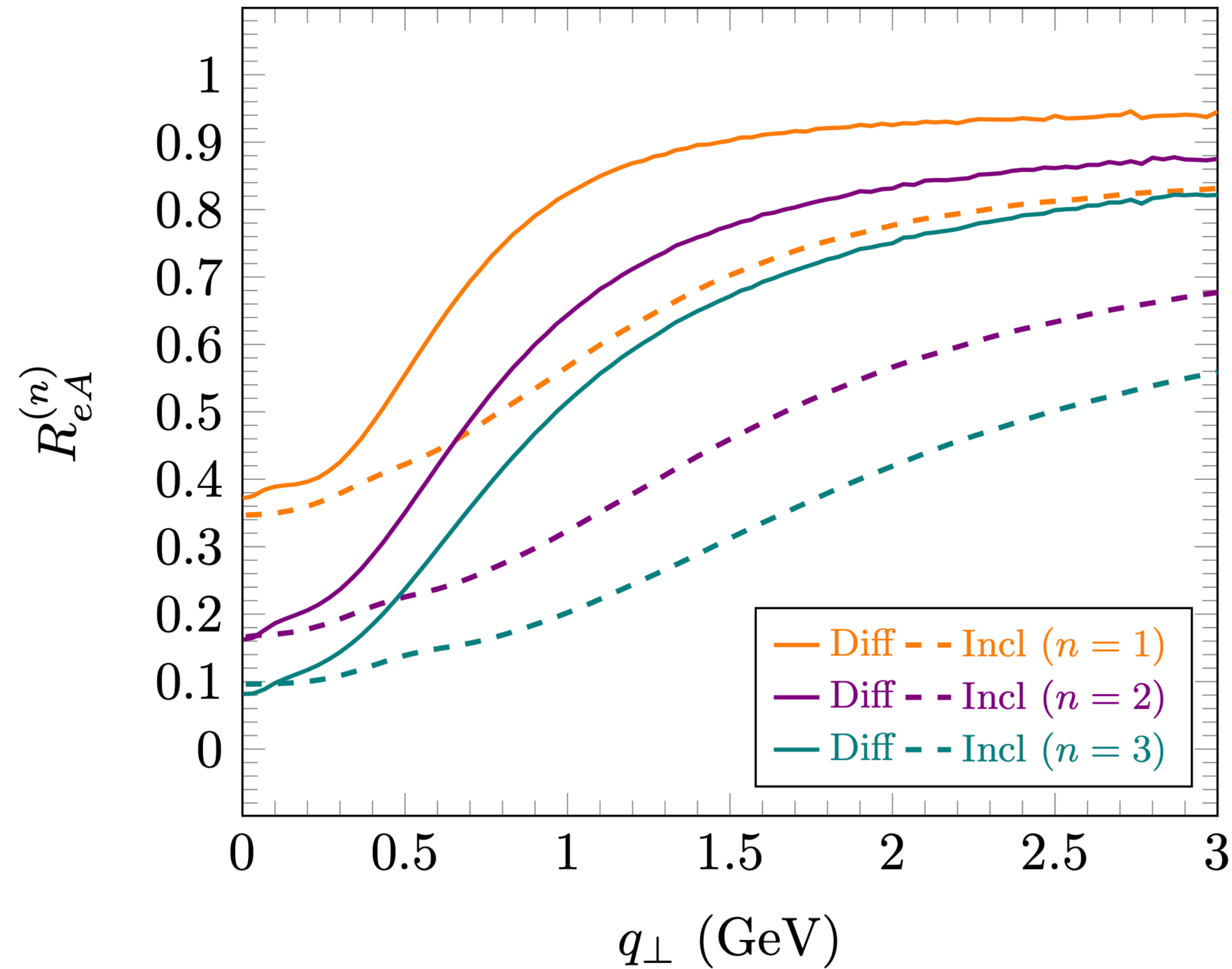
Forward limit: $\Delta_{\perp} = 0$



◆ **Diffractive anisotropies ($\Delta_{\perp} = 0, \beta = 0.94$) are much larger than inclusive ones.**

$$\text{diff: } k_{q_{\perp}} \lesssim (1 - \beta)^{1/2} Q_s \approx 0.24 Q_s$$

● Forward limit: $\Delta_{\perp} = 0$



$\sqrt{s_{eN}} = 89$ GeV, $y_l = 2.41$

$0.008 < x < 0.0094$

QED corrections included

◆ Diffractive $R_{eA}^{(n)}$ exhibit a significant nuclear suppression, similar to the inclusive case

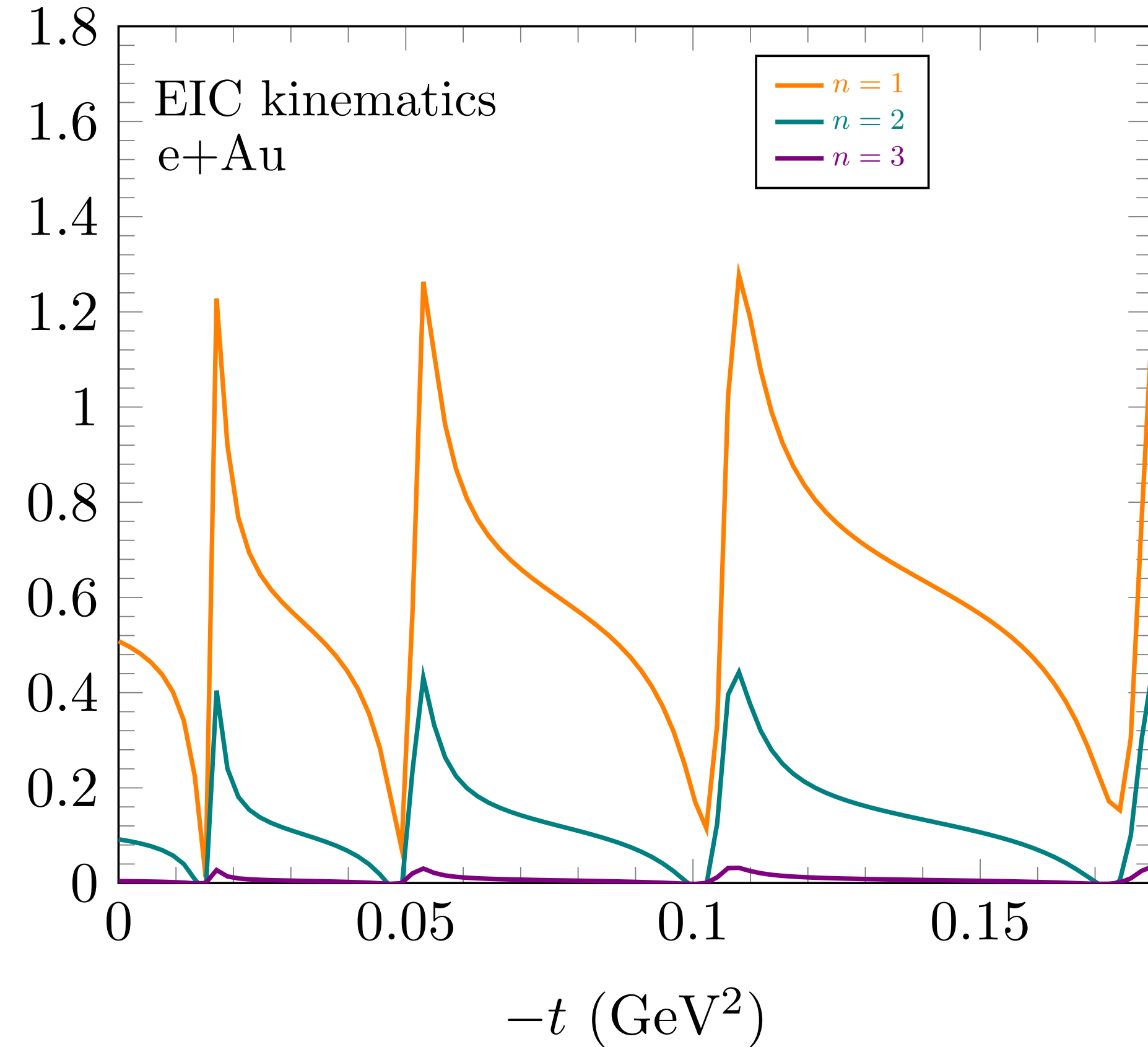
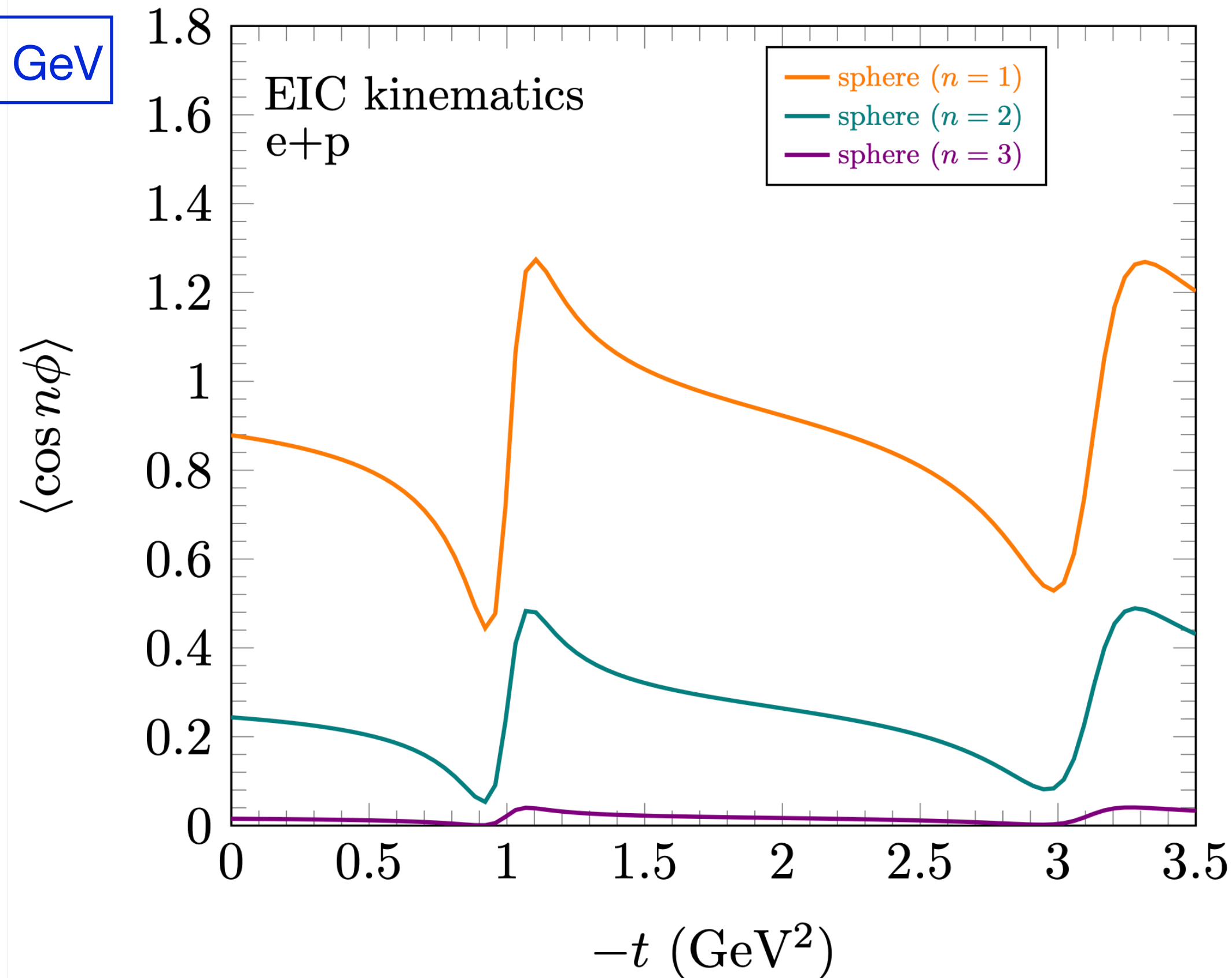
➡ Sensitive to Q_s

Δ_{\perp} -distribution

Toy model: uniform sphere

$$\mathcal{S}_x(r_{\perp}, b_{\perp}) = e^{-\frac{r_{\perp}^2 Q_{s,p}^2(x, b_{\perp})}{4}} \quad Q_{s,p}^2(x, b_{\perp}) = c_s \sqrt{1 - \frac{b_{\perp}^2}{r_p^2}} \quad \int d^2 b_{\perp} Q_{s,p}^2(x, b_{\perp}) = \pi r_p^2 Q_{s,p}^2(x)$$

$q_{\perp} = 0.5 \text{ GeV}$



★Pulse shape—diffractive pattern

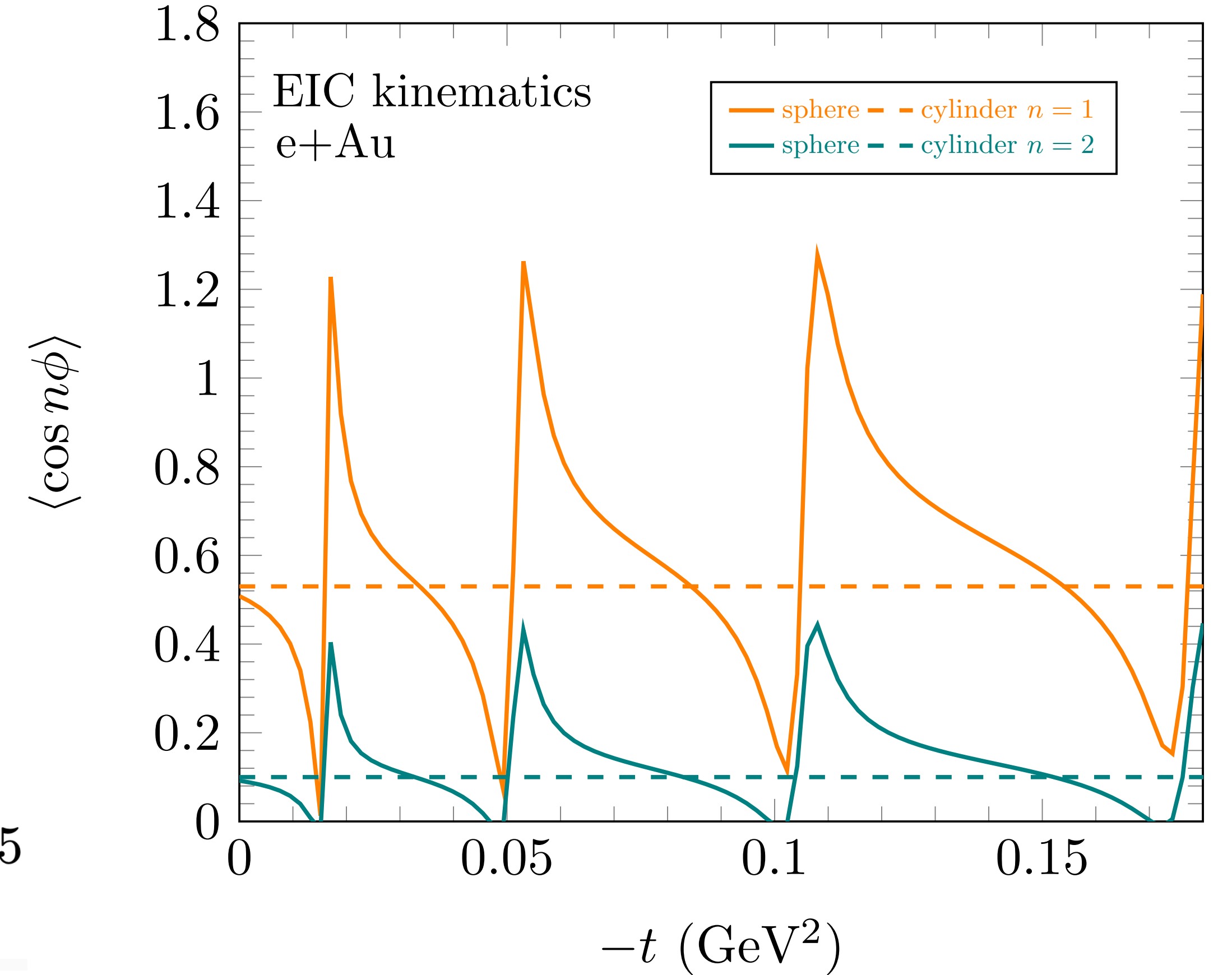
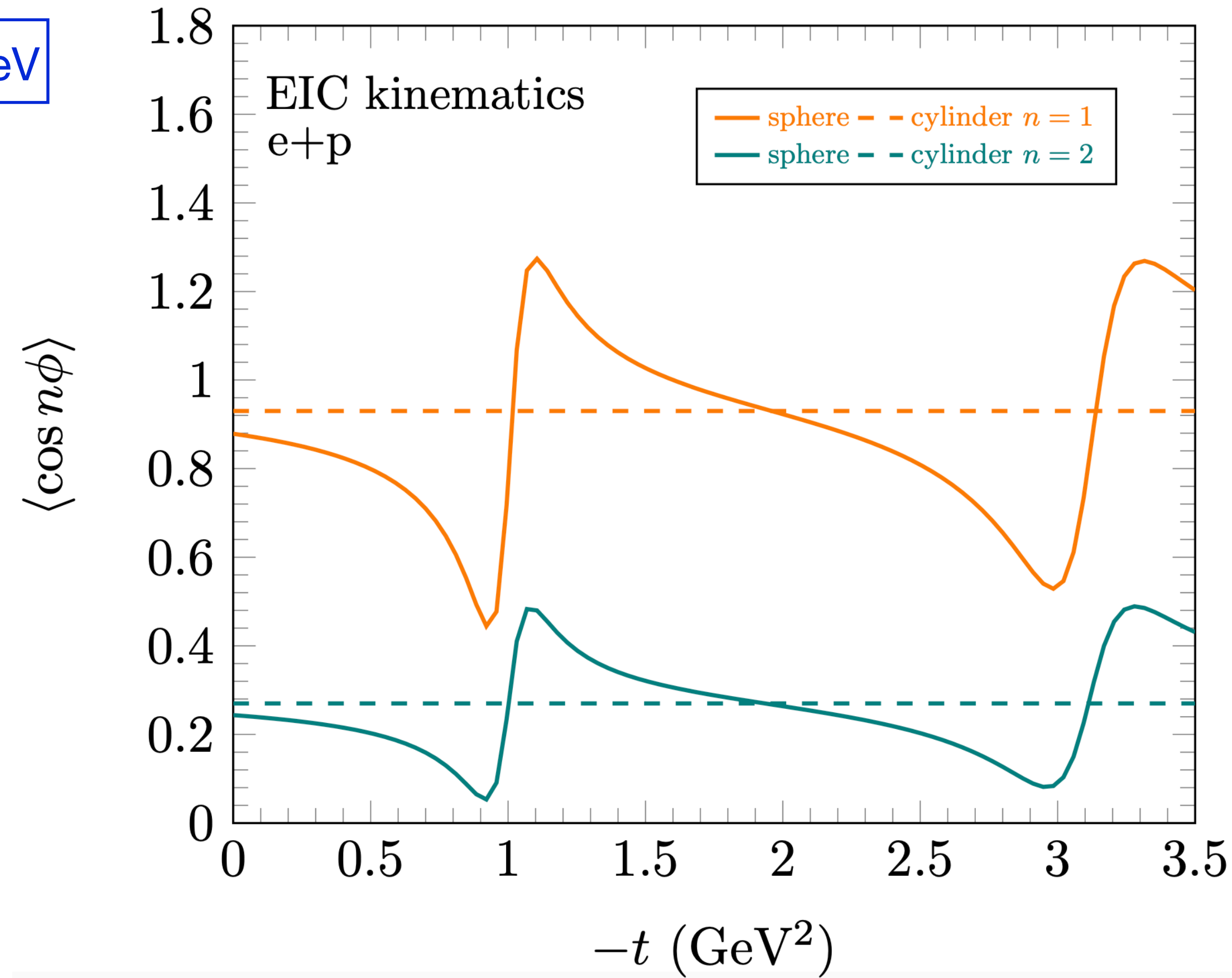
► Positions \sim zeros of $J_1(r_p \Delta_{\perp})$ —fourier transform of a circular e.g. proton $r_p \Delta_{\perp} = 3.8, 7.0, 10.2, \dots$

Akin to Caldwell-Kowalski 2010

► Positions&shape change drastically from ep to eA-> **Sensitive to the A -dependence of geometry**

● Δ_{\perp} -distribution Toy model: sphere v.s. cylinder

$q_{\perp} = 0.5 \text{ GeV}$

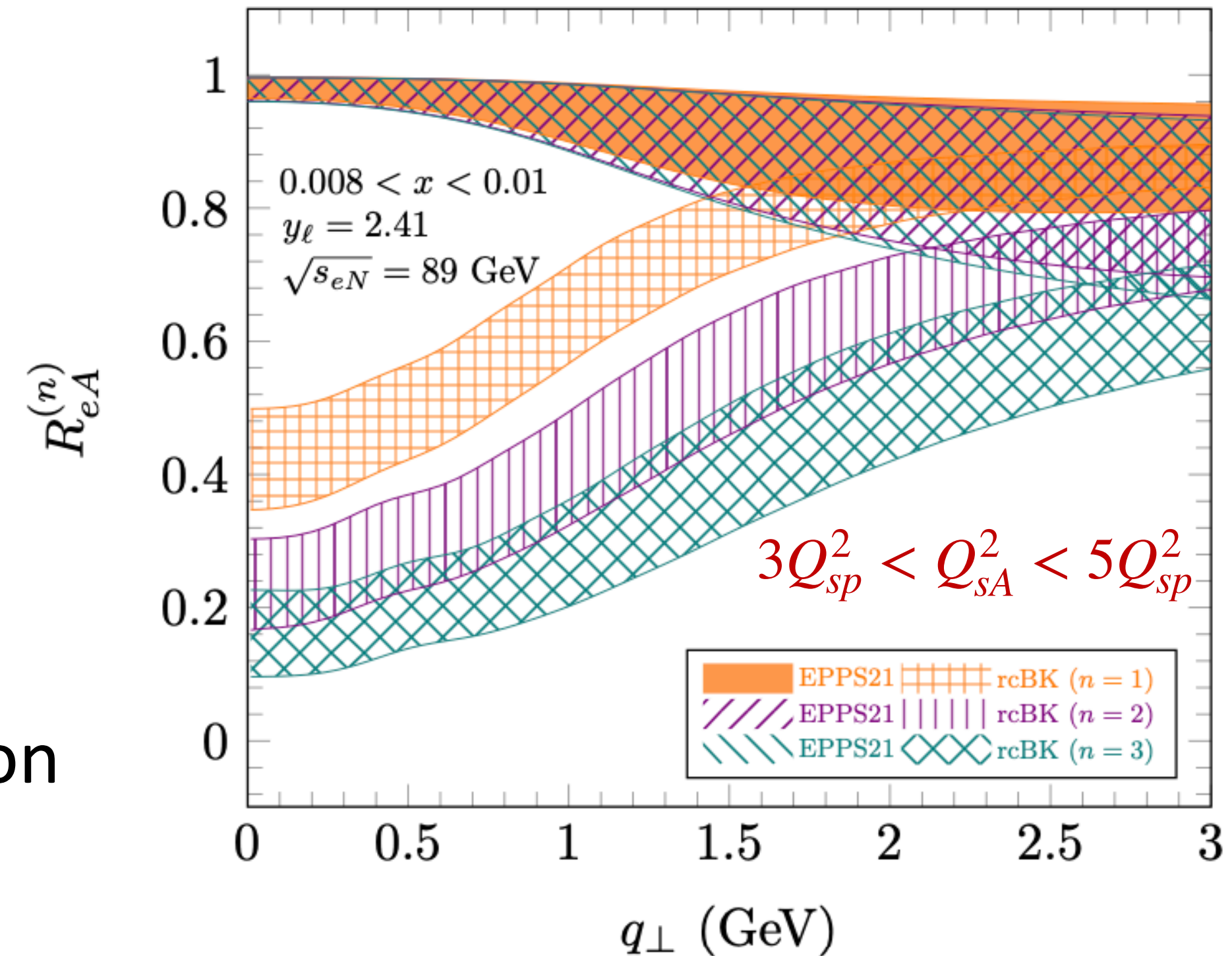


★ Potential to probe the geometry of targets

► Cylinder-like target : $d\sigma$ has t -dependence as $J_1(r_p \Delta_{\perp})/\Delta_{\perp}$, completely cancels in $\langle \cos n\phi \rangle = \frac{\sigma_n}{\sigma_0}$

Summary

- ◆ Lepton-jet correlation at small x in inclusive and diffractive DIS
 - ✓ Sensitivity of the anisotropy to the saturation effects.
 - ✓ Power to discriminate underlying mechanisms
 - ✓ t -dependent anisotropy \rightarrow proton & nuclear shape
- ◆ Great potential in searching for compelling evidences of gluon saturation at the EIC.

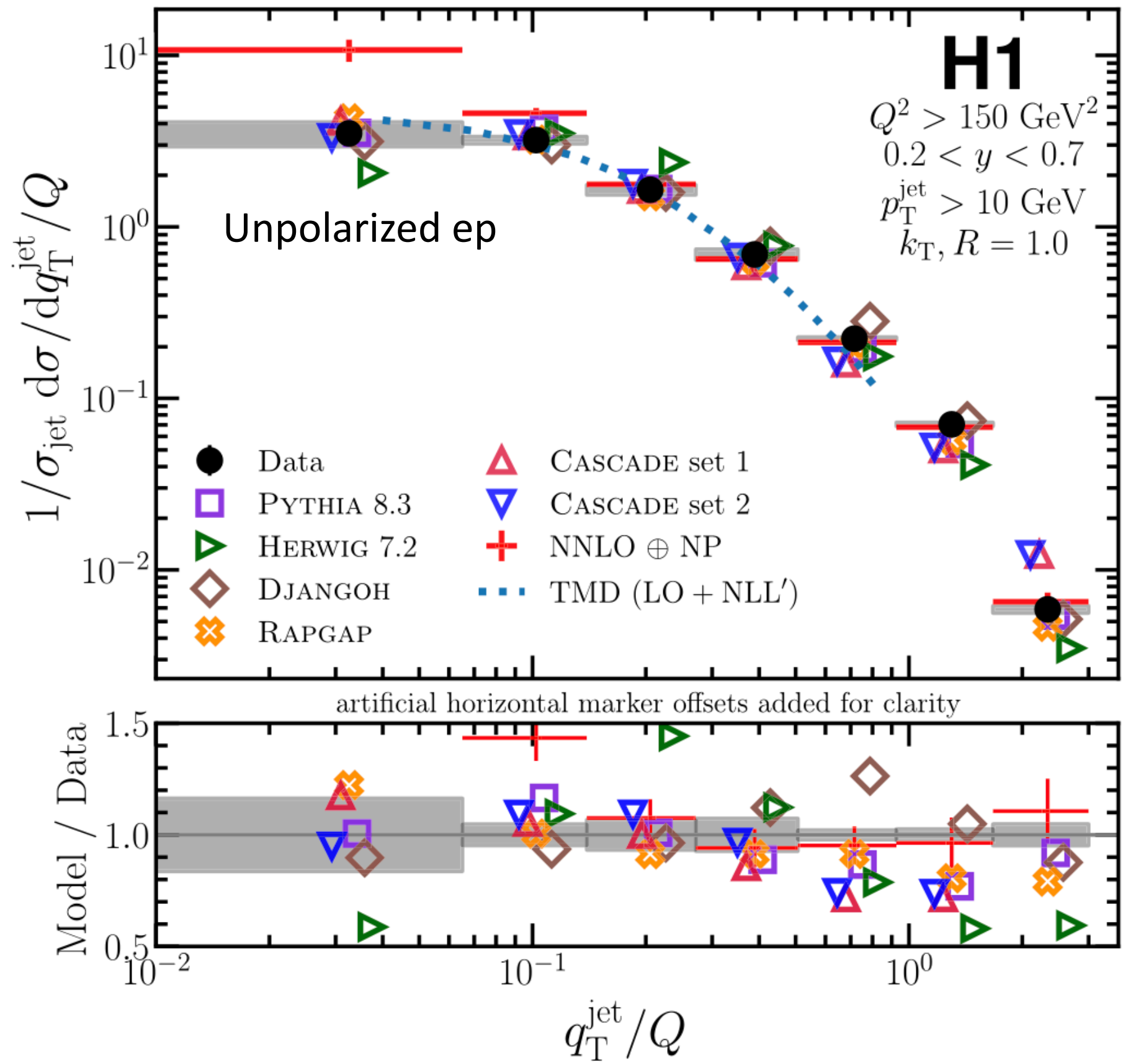


Outlook

- Improve the prediction, especially the diffractive case.
- Incoherent diffraction
- SSA of lepton-jet at small- x \Rightarrow Sivers functions & spin-dependent odderon
- H1 measurement of lepton-jet anisotropy \Rightarrow see DIS2023 talk by [Fernando Acosta](#)
- From jet to energy flow or transverse energy flow \Rightarrow see later talk by [Jani Penttala](#)

● **Measurement of LJC at HERA(H1)**

H1 PRL 128,132002(2022)

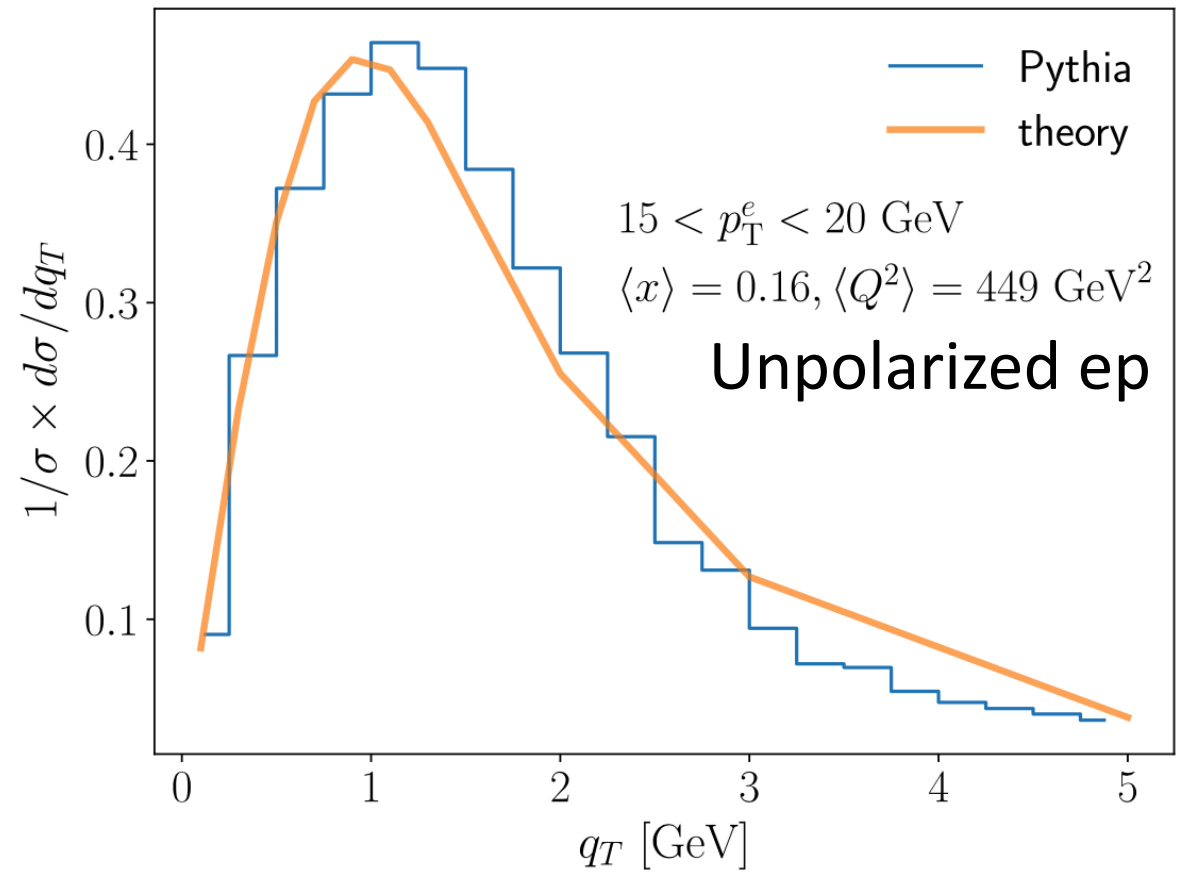


- H1 data agree with TMD calculation (with different set) in a wide kinematics.

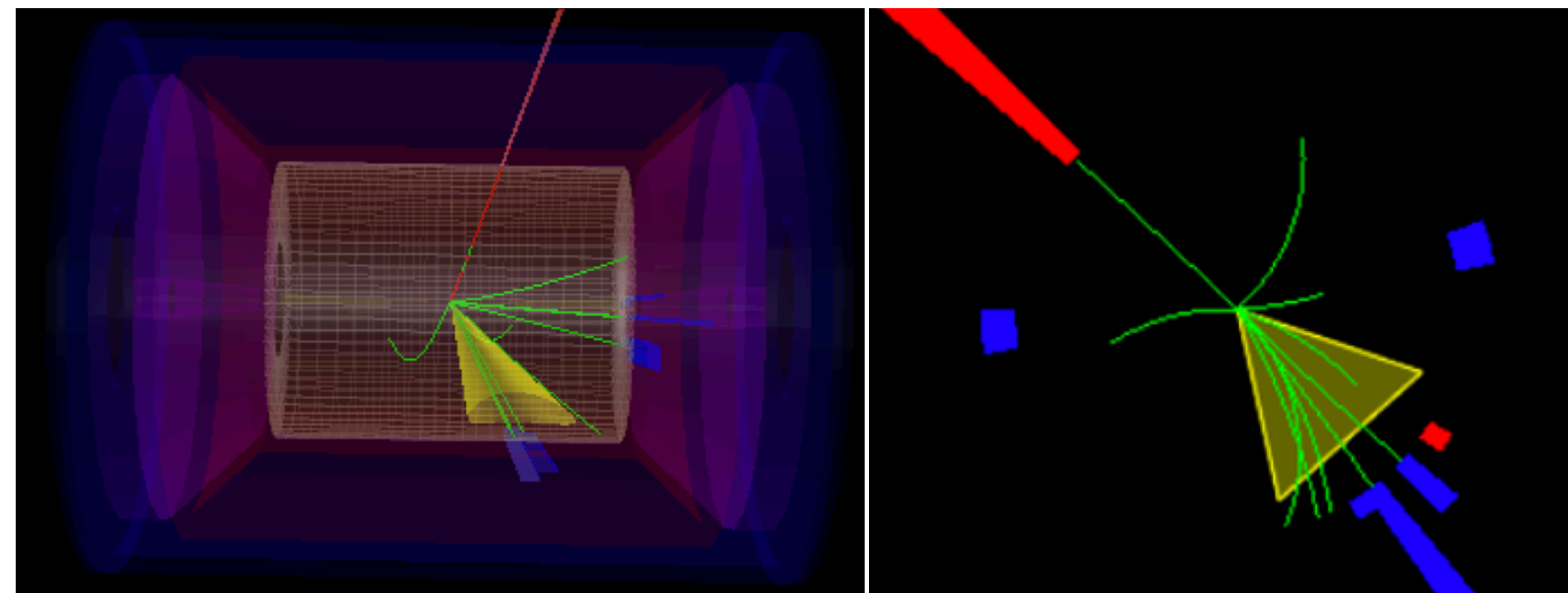
● **Simulation studies at the EIC**

Arratia-Song-Ringer-Jacak PRC101,065204(2020)

Arratia-Kang-Prokudin-Ringer PRD102,074015 (2020)



“The expected performance of a hermetic EIC detector with reasonable parameters is sufficient to perform these measurement”

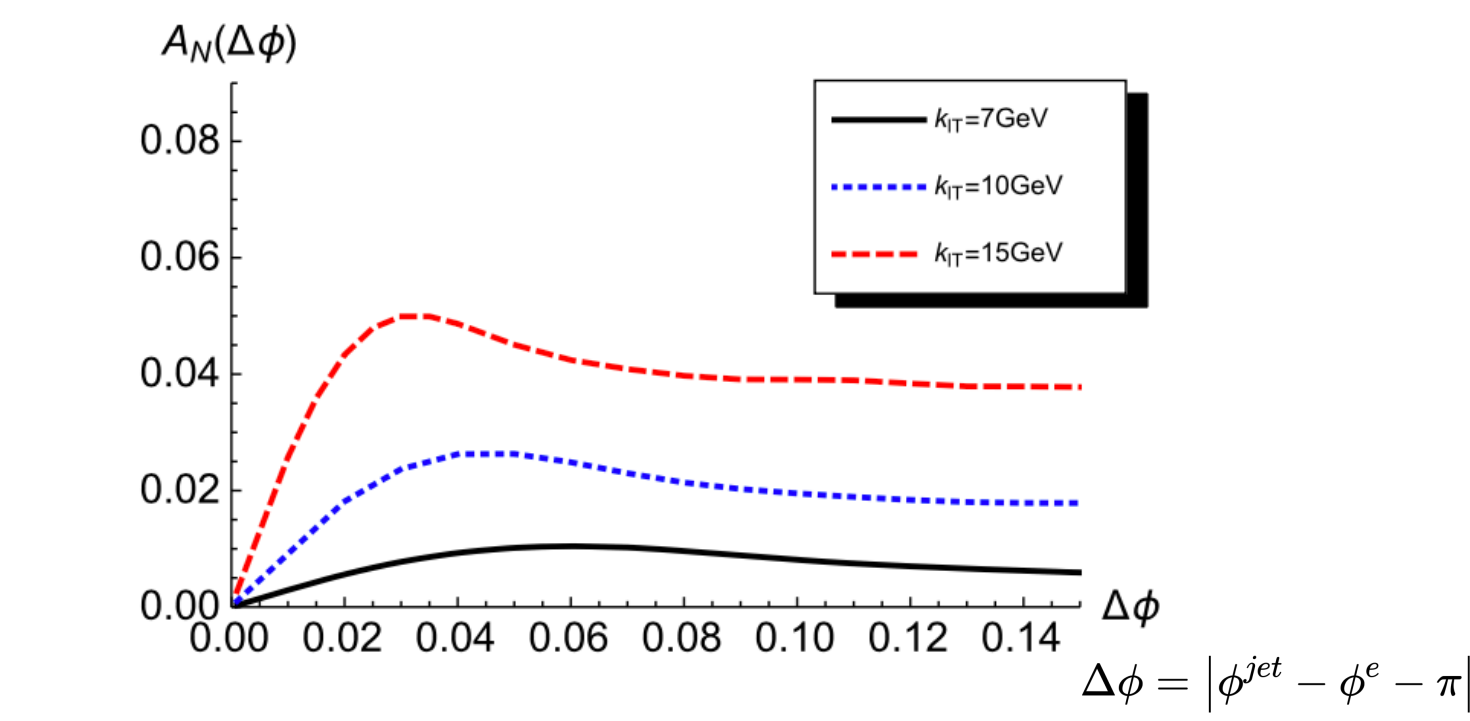


- Indicate the feasibility of LJC measurement at the EIC.

Azimuthal angle asymmetries from proton transverse spin

- Sivers asymmetry $A_{UT}^{\sin(\phi_s-\phi_q)}$ [Liu-Ringer-Vogelsan-Yuan PRL22,192003 \(2019\); PRD102,094022 \(2020\)](#)

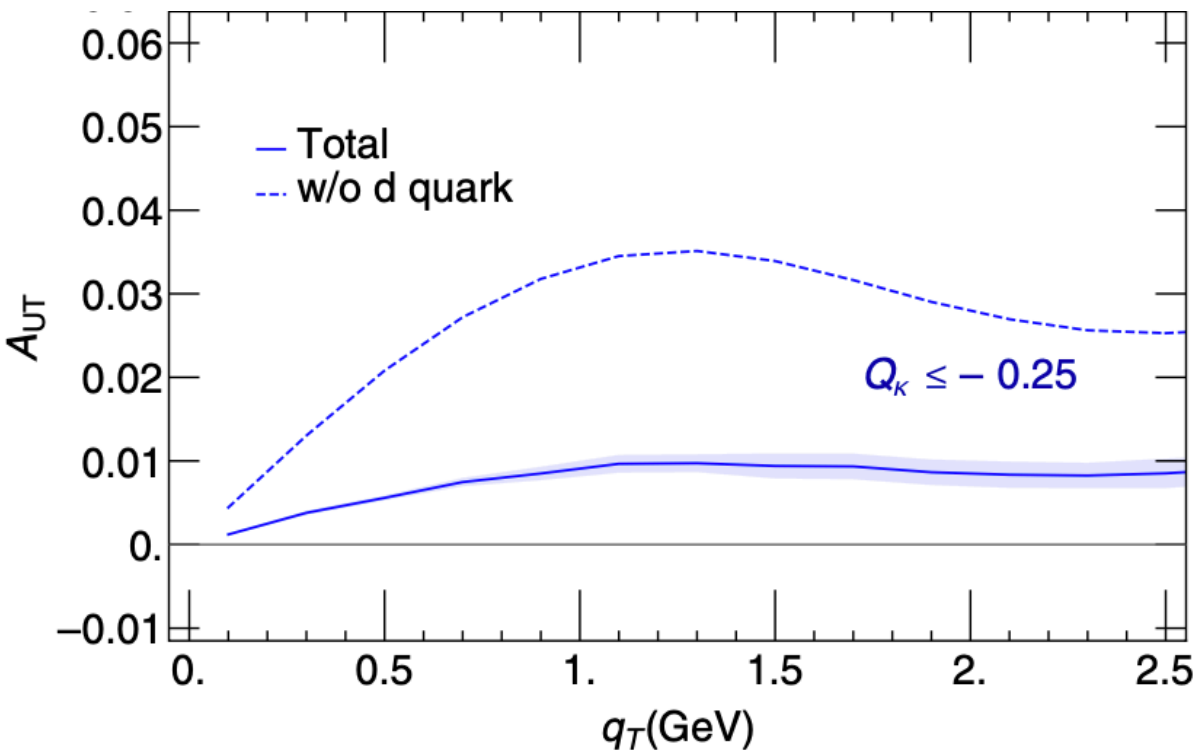
➡ Sivers function: unpolarized quark in an transversely polarized proton



▶ Jet charge: novel tool to unveil the favor structure

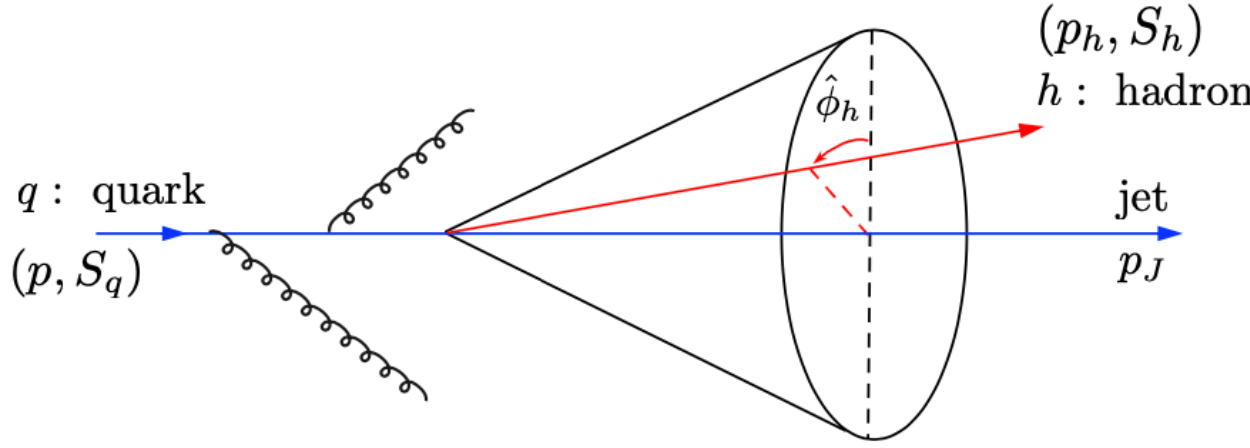
$$Q_\kappa \equiv \sum_{h \in \text{jet}} z_h^\kappa Q_h,$$

[Kang-Liu-Mantry-Shao PRL 125, 242003\(2020\)](#)



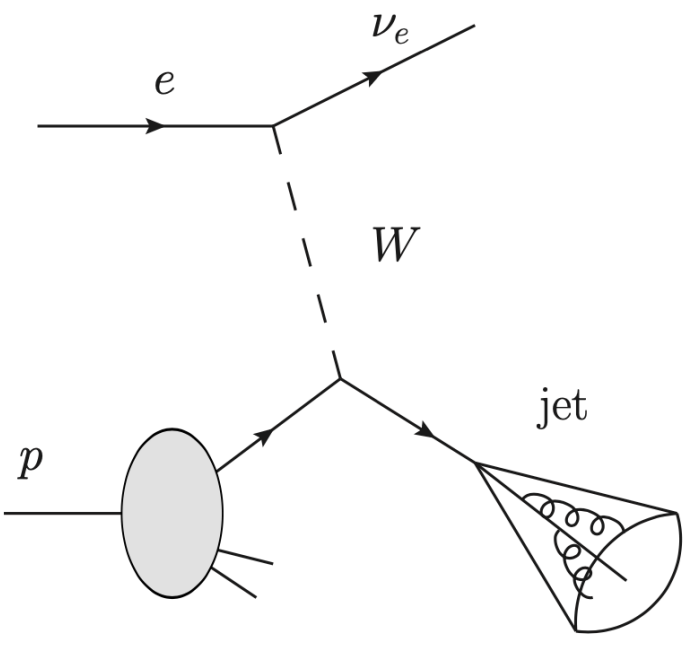
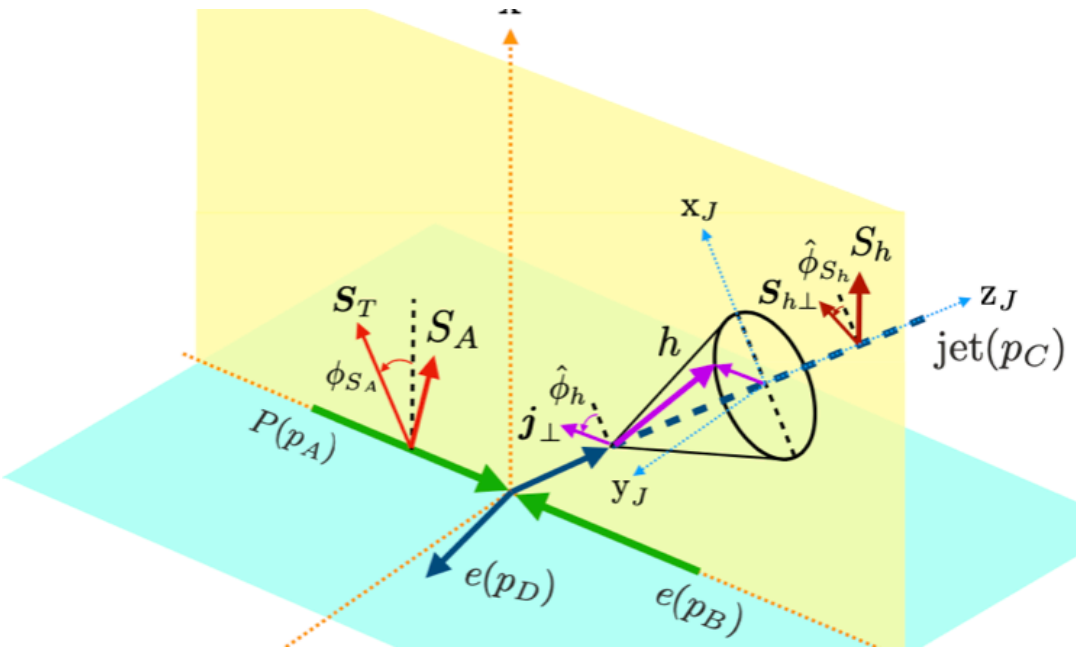
- Collins asymmetry: $A_{UT}^{\sin(\phi_s-\phi_h)}$ [Arratia-Kang-Prokudin-Ringer PRD102,074015 \(2020\)](#)
[Kang-Lee-Shao-Zhao JHEP 11 \(2021\) 005](#)

▶jet fragmentation



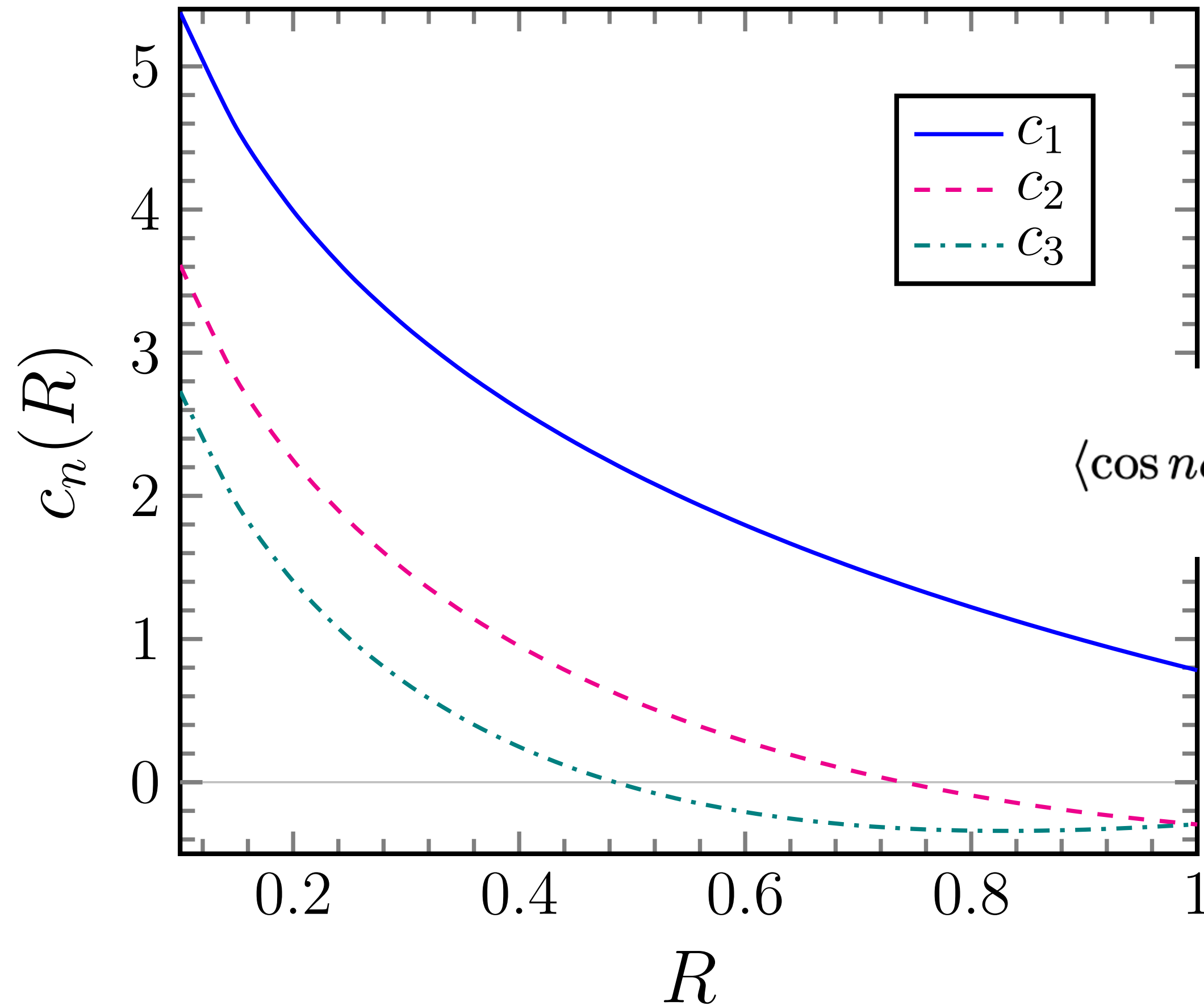
[See a review in Sec.9, TMD Handbook 2304.03302](#)

➡ Collin fragmentaion function: unpolarized hadron from transversely polarized quark



- Spin asymmetries in Neutrino-jet correlation:

[Arratia-Kang-Paul-Prokudin-Ringer-Zhao 2212.02432](#)



$$\langle \cos n\phi \rangle = \frac{\sigma_{\text{LO}} \int r_{\perp} dr_{\perp} \mathbf{J}_n(q_{\perp} r_{\perp}) \frac{\alpha_s C_F c_n(R)}{n\pi} e^{-\text{Sud}(r_{\perp}, R)} \sum_q e_q^2 x f_q(x, r_{\perp})}{\sigma_{\text{LO}} \int r_{\perp} dr_{\perp} \mathbf{J}_0(q_{\perp} r_{\perp}) e^{-\text{Sud}(r_{\perp}, R)} \sum_q e_q^2 x f_q(x, r_{\perp})}.$$

- ◆ The hierarchy of anisotropy on n is inherited from the Fourier coefficients $c_n(R)$;
- ◆ $c_n(R)$ decreases as R becomes larger; For larger jet cone, more gluons are likely included in the jet and have less probability to radiate outside the jet cone.
- ◆ R -dependence largely cancel in the $R_{eA}^{(n)}$