

Connecting paramagnetic EDM observables to the EDMs of nucleons

Lemonia Gialidi



UNIVERSITEIT
VAN AMSTERDAM



Collaborators: Jordy de Vries,
Heleen Mulder, Wouter Dekens,
Javier Menéndez, Beatriz Romeo

Nucleon Electric Dipole Moments in Paramagnetic Molecules through Effective Field Theory

Wouter Dekens,¹ Jordy de Vries,^{2,3} Lemonia Gialidi,^{2,3} Javier Menéndez,^{4,5} Heleen Mulder,^{3,6} and Beatriz Romeo⁷

¹*Institute for Nuclear Theory, University of Washington, Seattle WA 91195-1550, USA*

²*Institute for Theoretical Physics Amsterdam and Delta Institute for Theoretical Physics, University of Amsterdam, Science Park 904, 1098 XH Amsterdam, The Netherlands*

³*Nikhef, Theory Group, Science Park 105, 1098 XG, Amsterdam, The Netherlands*

⁴*Departament de Física Quàntica i Astrofísica, Universitat de Barcelona, 08028 Barcelona, Spain*

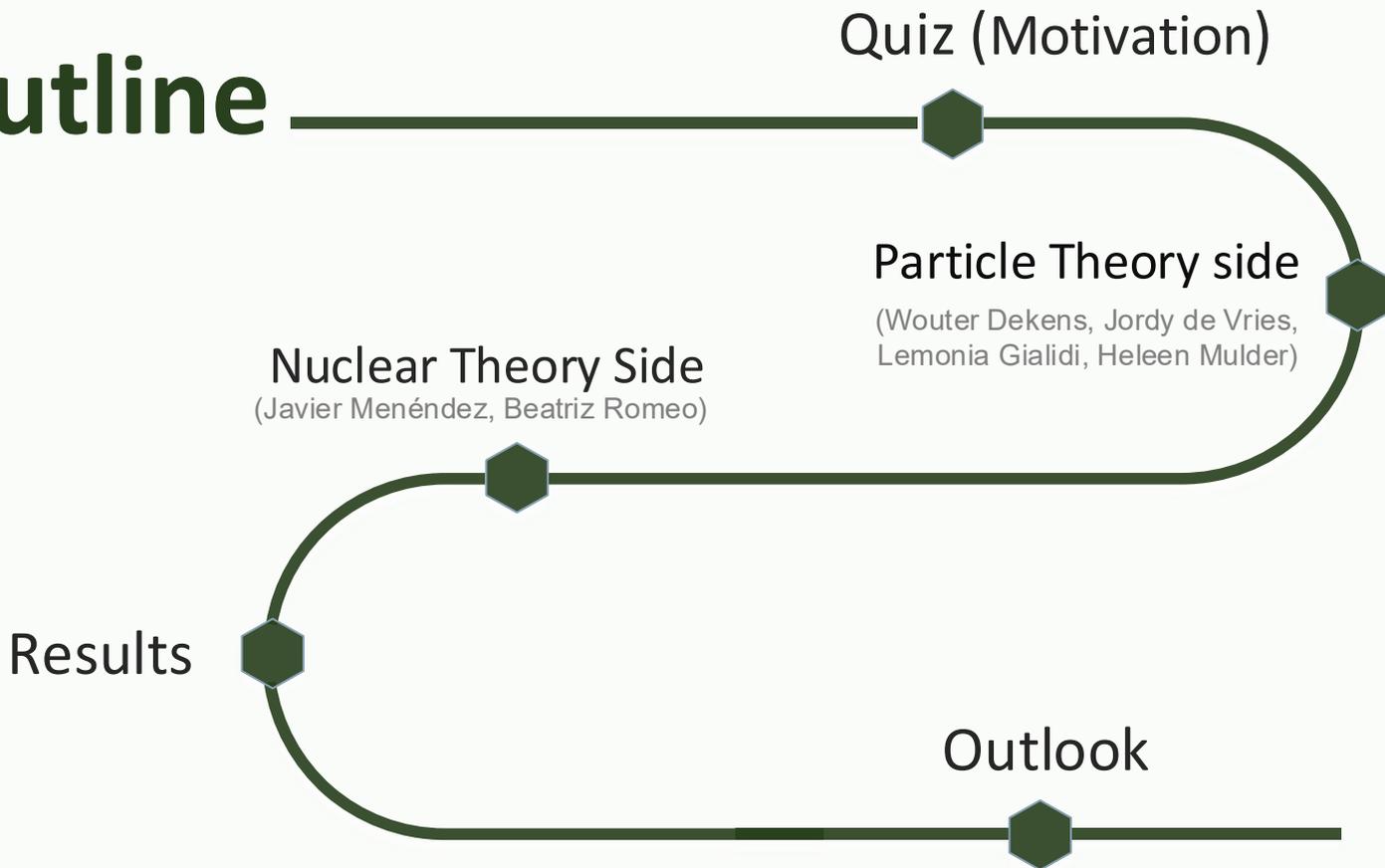
⁵*Institut de Ciències del Cosmos, Universitat de Barcelona, 08028 Barcelona, Spain*

⁶*Van Swinderen Institute for Particle Physics and Gravity,*

University of Groningen, Nijenborgh 3, 9747 AG Groningen, The Netherlands

⁷*Department of Physics and Astronomy, University of North Carolina, Chapel Hill*

Outline



Match the following:

WHAT IS THE ANSWER?

1 Paramagnetic systems

non-zero total electron spin

2 Diamagnetic systems

zero total electron spin
non-zero nucleon/nuclear spin

Electron EDM

d_e

Semi-leptonic
e-N operator

C_{SP}

Hadronic
CP Violation

d_p

$\bar{g}_{0,1}$

d_n

QCD θ

higher-
dimensional
operators

Match the following:



1 **Paramagnetic systems**
non-zero total electron spin

Electron EDM

d_e

**Semi-leptonic
e-N operator**

C_{SP}

2 **Diamagnetic systems**
zero total electron spin
non-zero nucleon/nuclear spin

**Hadronic
CP Violation**

d_p

$\bar{g}_{0,1}$

d_n

QCD θ

higher-
dimensional
operators

Match the following:

1 Paramagnetic systems

non-zero total electron spin



2 Diamagnetic systems

zero total electron spin
non-zero nuclear spin

Electron EDM

d_e

Semi-leptonic
e-N operator

C_{SP}

Hadronic
CP Violation

d_p

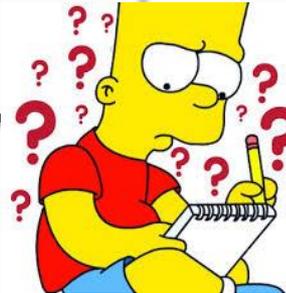
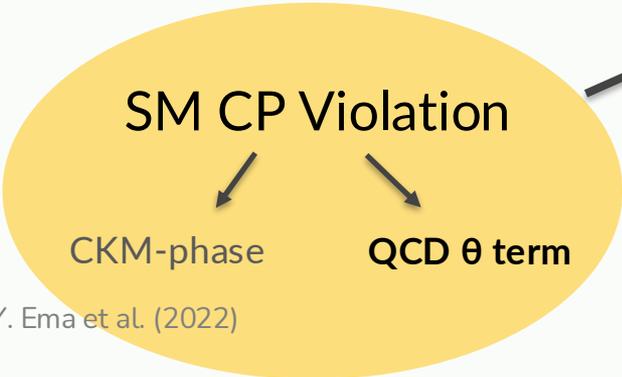
$\bar{g}_{0,1}$

d_n

QCD θ

higher-dimensional
operators

non-zero EDM measurement



BSM sources of CP Violation

Y. Ema et al. (2022)

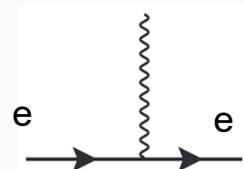
Paramagnetic systems

What do they measure?

[See Anastasia's talk]

Atomic/Molecular
structure coefficients

$$d_e \times \frac{-i}{2} \bar{\psi} \sigma_{\mu\nu} \gamma_5 F_{\mu\nu} \psi$$



Electron EDM
purely leptonic
operator

$$\text{Paramagnetic EDM} = W_{SP} \mathbf{C}_{SP} + W_d d_e$$

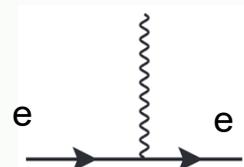
Paramagnetic systems

What do they measure?

[See Anastasia's talk]

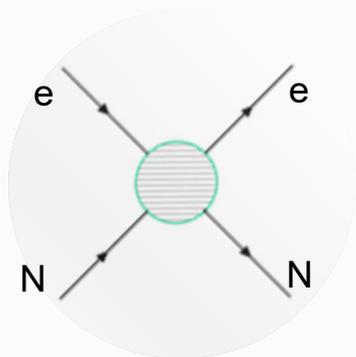
Atomic/Molecular
structure coefficients

$$d_e \times \frac{-i}{2} \bar{\psi} \sigma_{\mu\nu} \gamma_5 F_{\mu\nu} \psi$$



Electron EDM
purely leptonic
operator

$$\text{Paramagnetic EDM} = W_{SP} C_{SP} + W_d d_e$$



Semi-leptonic operator
Effective electron-Nucleon interactions

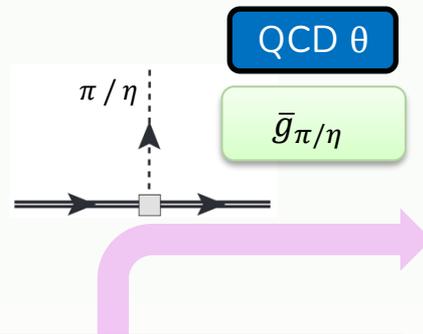
$$\mathcal{L} = \frac{G_F}{\sqrt{2}} \bar{e} i \gamma_5 e \bar{N} (C_{SP}^0 + C_{SP}^1 \tau^3) N.$$

Effective e-N interactions

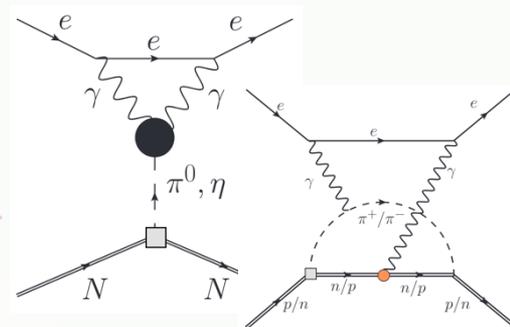
How are they induced by hadronic CPV?

[See Heleen's talk]

H. Mulder, R. Timmermans,
and J. de Vries (2025).
Flambaum, Pospelov, Ritz, Stadnik, '19



$$\mathcal{L}_\chi = \bar{g}_0 \bar{N} \tau^a N \pi^a + \bar{g}_1 \bar{N} N \pi^0 + \bar{g}_{0\eta} \bar{N} N \eta + 2\bar{N} (d_0 + d_1 \tau^3) v^\mu S^\nu N F_{\mu\nu},$$



Meson Exchange

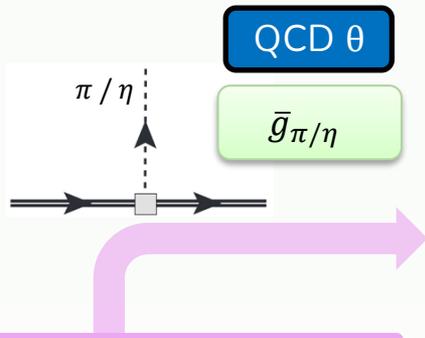
Pion Loops

Effective e-N interactions

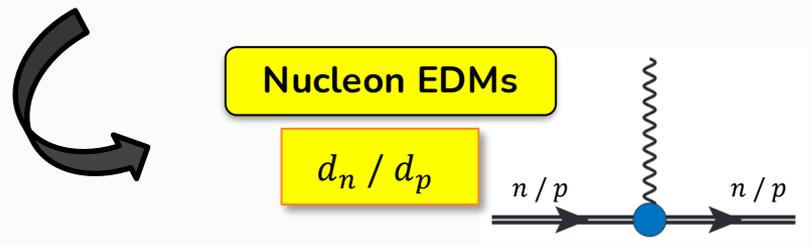
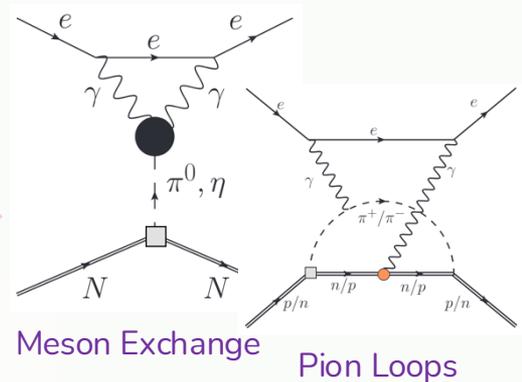
How are they induced by hadronic CPV?

H. Mulder, R. Timmermans, and J. de Vries (2025).

Flambaum, Pospelov, Ritz, Stadnik, '19



$$\mathcal{L}_\chi = \bar{g}_0 \bar{N} \tau^a N \pi^a + \bar{g}_1 \bar{N} N \pi^0 + \bar{g}_{0\eta} \bar{N} N \eta + 2\bar{N} (d_0 + d_1 \tau^3) v^\mu S^\nu N F_{\mu\nu},$$



C_{SP} induced by nucleon EDMs

We need both the **nucleon EDM** and the **nucleon MDM** here!!

Potential

Photon Momenta

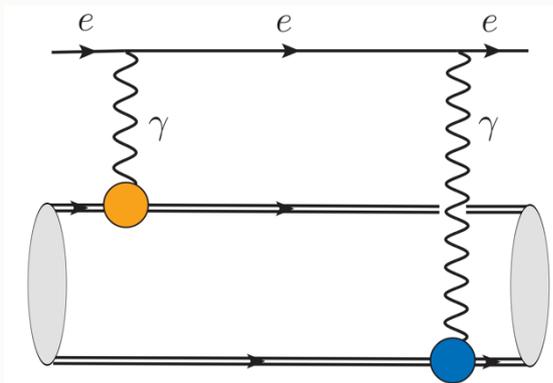
$$q_\gamma^\mu = (q_\gamma^0, \vec{q}_\gamma)$$

Ultrasoft

C_{SP} induced by nucleon EDMs

We need both the **nucleon EDM** and the **nucleon MDM** here!!

Potential



Photon Momenta

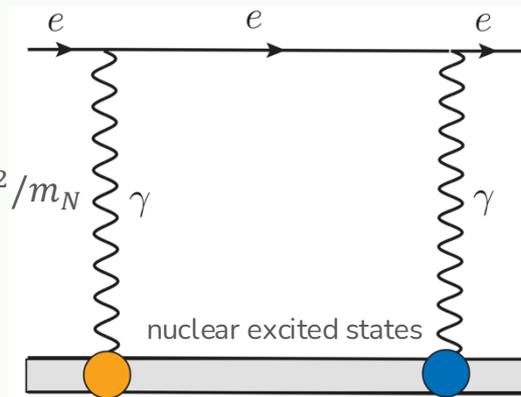
$$q_Y^\mu = (q_Y^0, \vec{q}_Y)$$

$$q_Y^0 \sim \vec{q}_Y^2 / m_N$$

$$|\vec{q}_Y| \sim m_\pi$$

$$q_Y^0 \sim |\vec{q}_Y| \sim m_\pi^2 / m_N$$

Ultrasoft



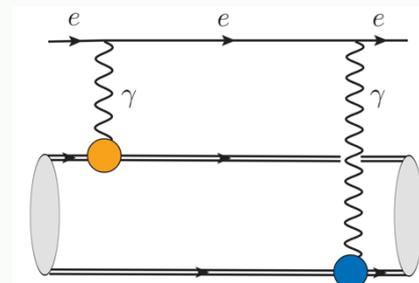
Potential Region

Sensitive to nuclear scales

expand in small scales
like $q_\gamma^0/|\vec{q}_\gamma|$



Two-nucleon effects



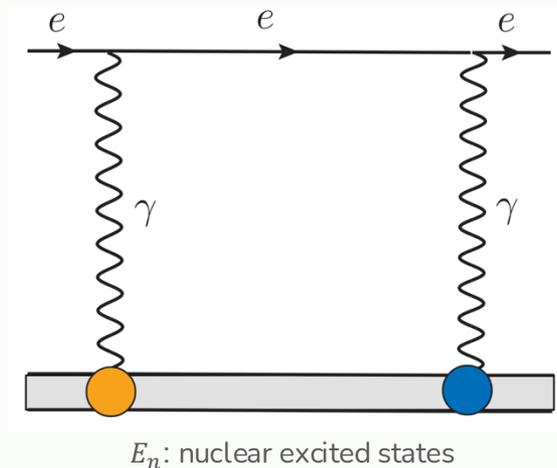
$$\mathcal{A}_{\text{pot}} = -\langle h_f | V | h_i \rangle \bar{u}(p'_e) \left(1 - \frac{v \cdot (p'_e - p_e)}{2m_e} \not{\psi} \right) i\gamma_5 u(p_e)$$

Nuclear Matrix Element (NME) of the two-body potential V

Ultrasoft

What changes here?

$$q_\gamma^0 \sim |\vec{q}_\gamma| \sim m_\pi^2/m_N$$

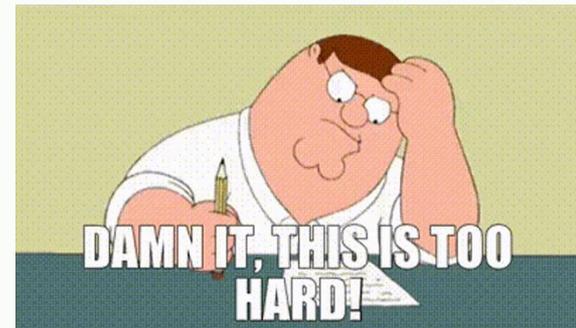


A lot of scales enter this diagram:

$$m_e, p_e, m_\gamma, E_n$$



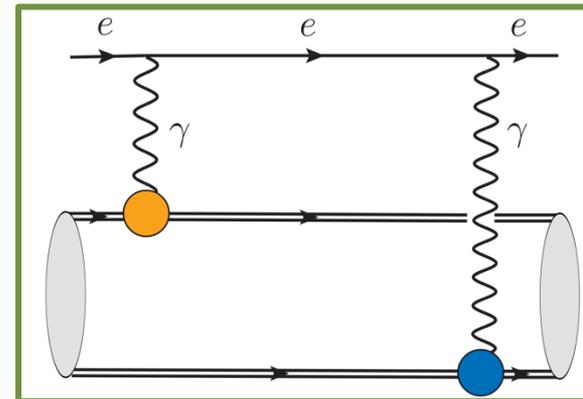
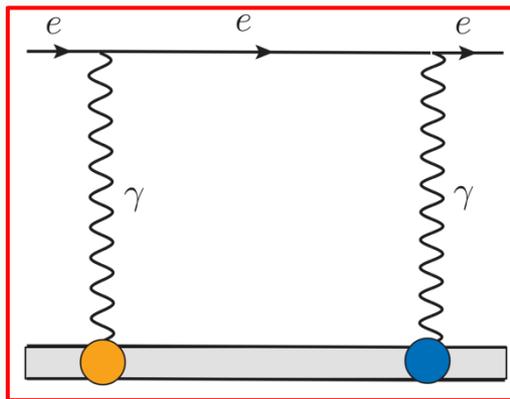
Scary Integrals



BUT!!! EFT saves us

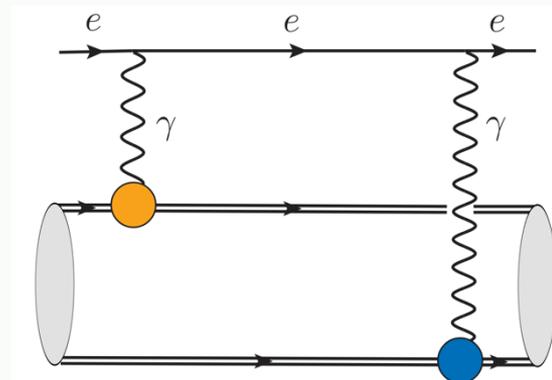
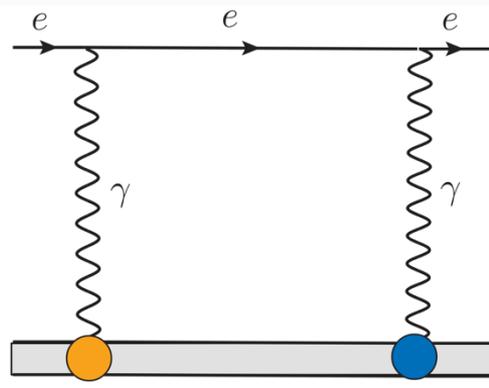
$$E_n \gg m_e$$

So far so good!



$$\bar{C}_{\text{SP}}^{\text{eff}} = -\frac{\sqrt{2}}{G_F} \left[\frac{4\alpha^2 m_e}{m_N} \sum_n \frac{A_n}{\Delta_n} \left(3 \ln \frac{m_e^2}{4\Delta_n^2} - 1 \right) + \langle h_i | V | h_i \rangle \right]$$

So far so good!



$$\bar{C}_{SP}^{\text{eff}} = -\frac{\sqrt{2}}{G_F} \left[\frac{4\alpha^2 m_e}{m_N} \sum_n \frac{A_n}{\Delta_n} \left(3 \ln \frac{m_e^2}{4\Delta_n^2} - 1 \right) + \langle h_i | V | h_i \rangle \right]$$

Paramagnetic EDM measurements



Nucleon EDMs



Compute NMEs

Nuclear side

$$\bar{C}_{SP}^{\text{usoft}} = -\frac{\sqrt{2}\alpha^2 m_e}{3m_N G_F} M_{SP}^{\text{usoft}} \rightarrow \sum_n \frac{\langle h_f | D^{(i)} \vec{\sigma} | n \rangle \cdot \langle n | \mu^{(i)} \vec{\sigma} | h_i \rangle}{\Delta_n} \left(1 + 3 \ln \frac{4\Delta_n^2}{m_e^2} \right)$$

Ultrasoft

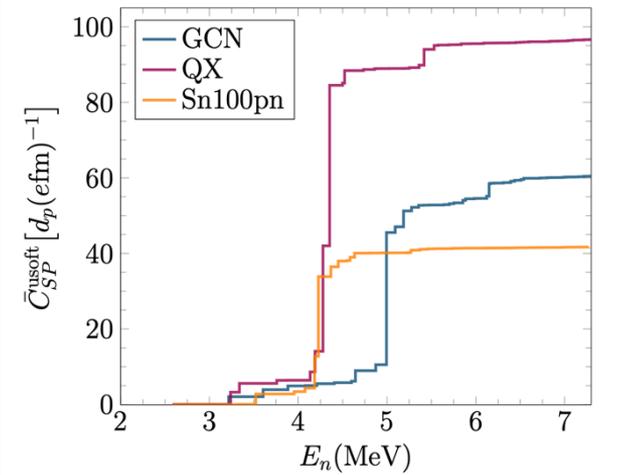
Nuclear side

$$\bar{C}_{SP}^{\text{usoft}} = -\frac{\sqrt{2}\alpha^2 m_e}{3m_N G_F} M_{SP}^{\text{usoft}} \rightarrow \sum_n \frac{\langle h_f | D^{(i)} \vec{\sigma} | n \rangle \cdot \langle n | \mu^{(i)} \vec{\sigma} | h_i \rangle}{\Delta_n} \left(1 + 3 \ln \frac{4\Delta_n^2}{m_e^2} \right)$$

Excitation energies
 $\Delta_n = E_n - E_i$
Transition elements

$E_n \gg m_e$

✓



Ultrasoft

Nuclear side

$$\bar{C}_{SP}^{\text{usoft}} = -\frac{\sqrt{2}\alpha^2 m_e}{3m_N G_F} M_{SP}^{\text{usoft}} \rightarrow \sum_n \frac{\langle h_f | D^{(i)} \vec{\sigma} | n \rangle \cdot \langle n | \mu^{(i)} \vec{\sigma} | h_i \rangle}{\Delta_n} \left(1 + 3 \ln \frac{4\Delta_n^2}{m_e^2} \right)$$

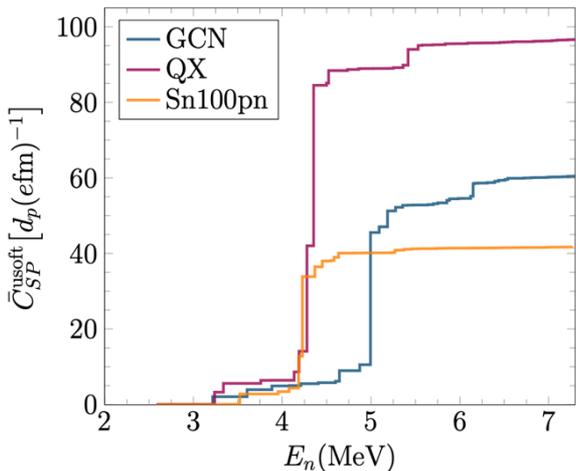
$E_n \gg m_e$

✓

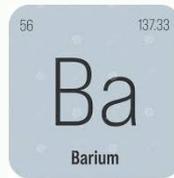
Excitation energies

$$\Delta_n = E_n - E_i$$

Transition elements



magic neutron number



$$\bar{C}_{SP}^{\text{usoft}} = (67 \pm 28) d_p (e \text{ fm})^{-1}$$

~40% nuclear uncertainty!!

↑
only d_p contributes!

Nuclear side

Coordinate space potential

$$\bar{C}_{SP}^{\text{pot}} = -\frac{\sqrt{2}}{G_F} \langle h_i | V | h_i \rangle$$

$$V(\vec{r}) = -\frac{e^4 m_e}{18\pi m_N} \sum_{i \neq j} \mu^{(i)} D^{(j)} |\vec{r}| \left[\underbrace{\sigma^{(i)} \cdot \sigma^{(j)}} + \frac{1}{16} S^{(ij)}(r) \right]$$

Nuclear side

DOMINANT CONTRIBUTION

Coordinate space potential

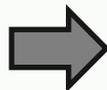
$$\bar{C}_{SP}^{\text{pot}} = -\frac{\sqrt{2}}{G_F} \langle h_i | \mathbf{V} | h_i \rangle$$

$$V(\vec{r}) = -\frac{e^4 m_e}{18\pi m_N} \sum_{i \neq j} \mu^{(i)} D^{(j)} |\vec{r}| \left[\sigma^{(i)} \cdot \sigma^{(j)} + \frac{1}{16} S^{(ij)}(r) \right]$$

56 137.33
Ba
Barium

$$\bar{C}_{SP}^{\text{pot}} = [(-433 \pm 5) d_p + (387 \pm 0.4) d_n] (e \text{ fm})^{-1}$$

- Both core and valence nucleons contribute to the potential NME
- Coherent structure



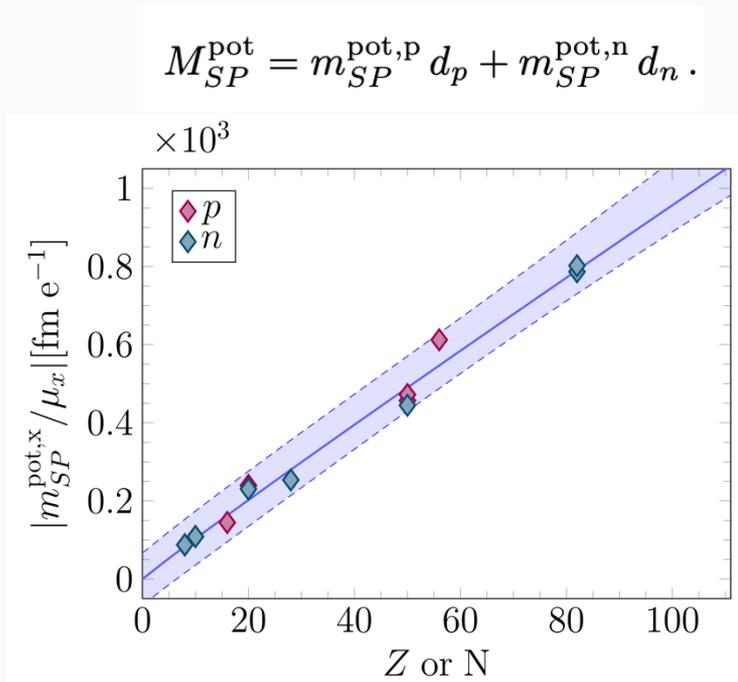
- NME scales with A
- Potential NMEs > Ultrasoft NMEs
- Smaller uncertainties

Can we go heavier?

Lighter nuclei confirm linear Z/N scaling

$$m_{SP}^{\text{pot},X} = -9.74 X \mu_X (\text{fm}/e)$$

$$X = (Z, p) \text{ or } (N, n)$$



Can we go heavier?

Lighter nuclei confirm linear Z/N scaling

$$m_{SP}^{\text{pot},X} = -9.74 X \mu_X (\text{fm}/e)$$

$X = (Z, p)$ or (N, n)

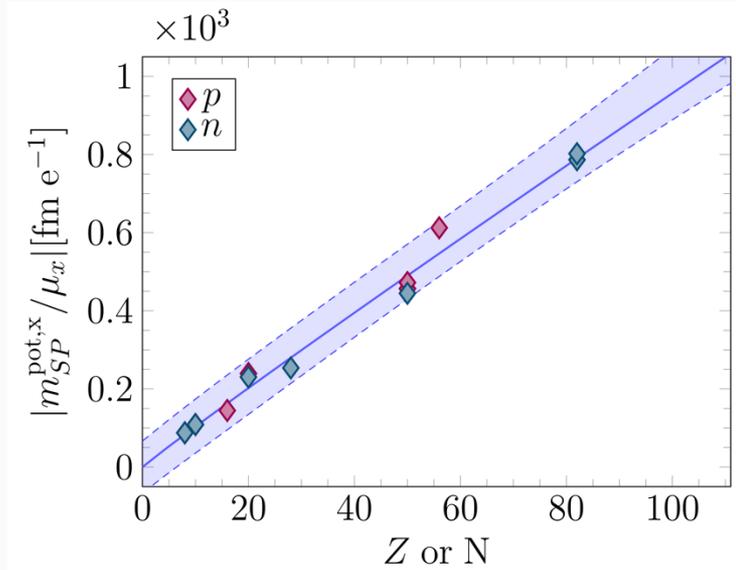


$$d_e^{\text{equiv}} \equiv r_{\text{mol}} \bar{C}_{SP} / A$$

$$d_e^{\text{equiv}} = \frac{\sqrt{2} e^4 m_e}{18 \pi G_F m_N} \frac{r_{\text{mol}}}{A} (-9.74) [Z \mu_p d_p + N \mu_n d_n] \frac{\text{fm}}{e}$$

Experimental Limit \rightarrow Limit on d_p or d_n

$$M_{SP}^{\text{pot}} = m_{SP}^{\text{pot},p} d_p + m_{SP}^{\text{pot},n} d_n .$$



Our limits

- 1 Recall the best current limit from paramagnetic molecules

Roussy et al. 2023 $|d_e|_{\text{HfF}^+} < 4.1 \cdot 10^{-30} e \text{ cm}$

- 2 Use scaling function

$$|d_p|_{\text{HfF}^+} < 1.6 \cdot 10^{-23} e \text{ cm} \quad , \quad |d_n|_{\text{HfF}^+} < 1.6 \cdot 10^{-23} e \text{ cm}$$

x100 weaker than

$$|d_p|_{\text{Hg}} < 2.0 \times 10^{-25} e$$

cm Graner et al. 2016

x1000 weaker than

$$|d_n| < 1.8 \times 10^{-26} e$$

cm PSI 2020

Our limits

1 Recall the best current limits

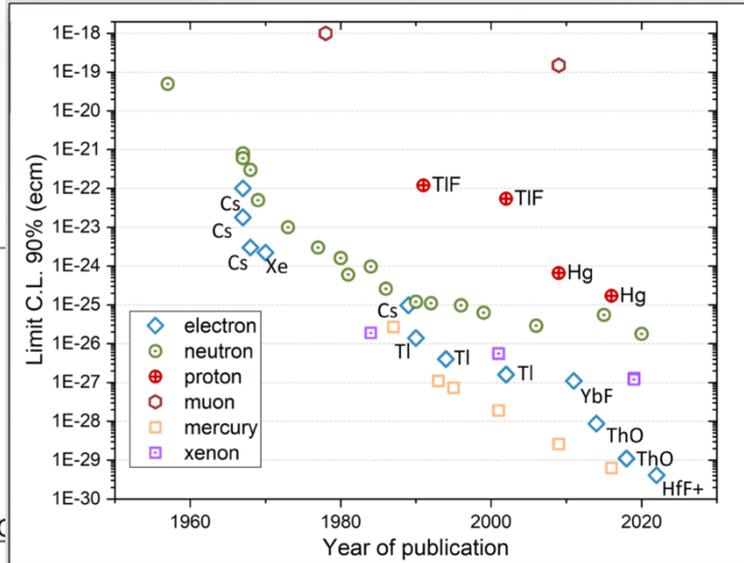
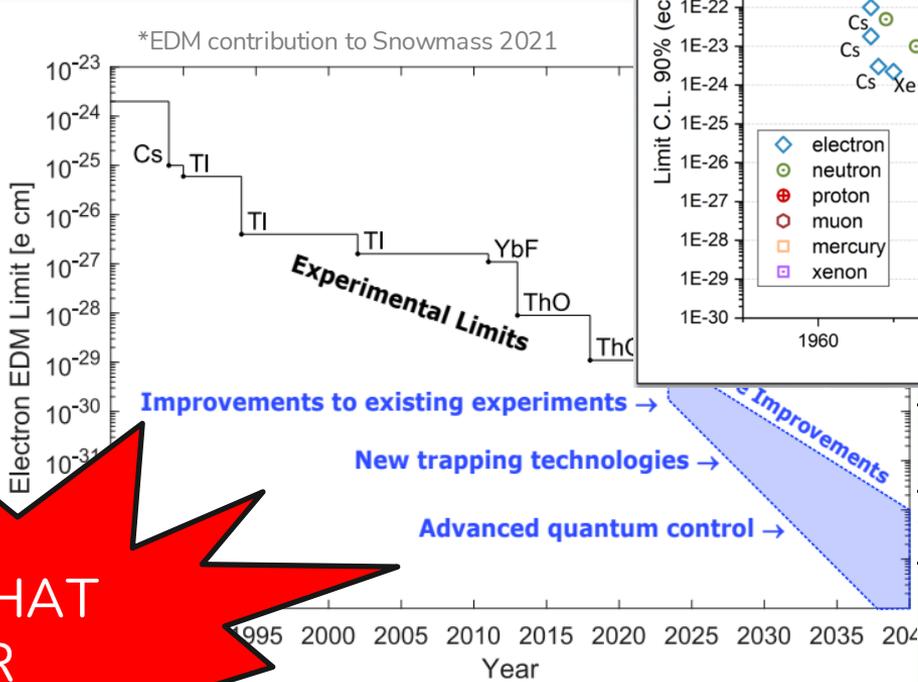
$$|d_e|_{\text{HfF}^+}$$

$$|d_p|_{\text{HfF}^+} <$$

x100

$$|d_p|_{\text{H}}$$

NOT THAT FAR AWAY!!!



than

Bennett et al. 2009

$$6 e$$



Which source did it?

PART 3

Quark EDM

Quark chromo
EDM

QCD θ



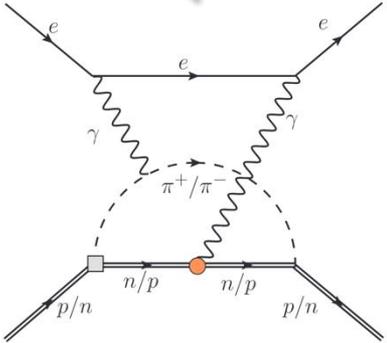
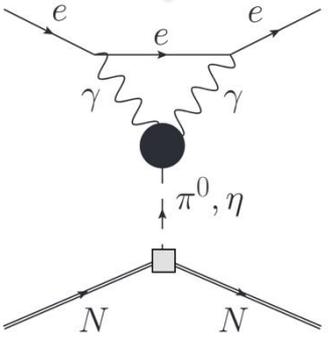
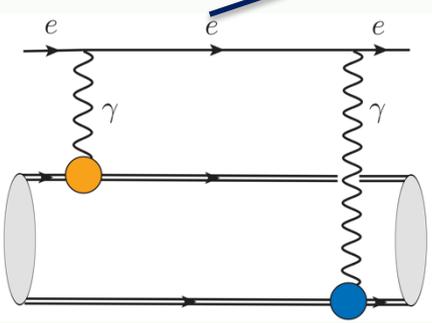
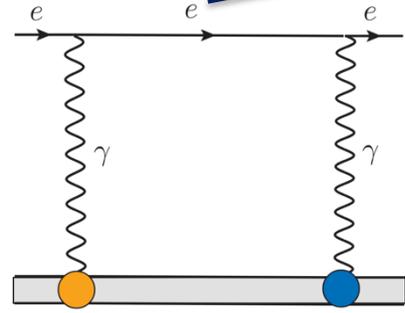
Which source did it?

PART 3

Quark EDM

Quark chromo EDM

QCD θ



Lemonia Gialdi : Connecting paramagnetic EDM observables to the ED

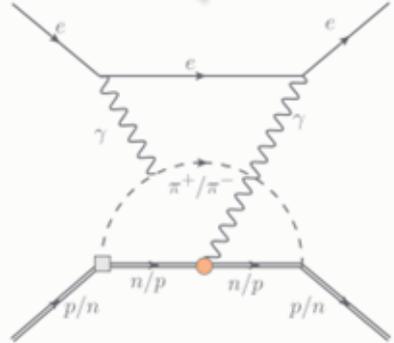
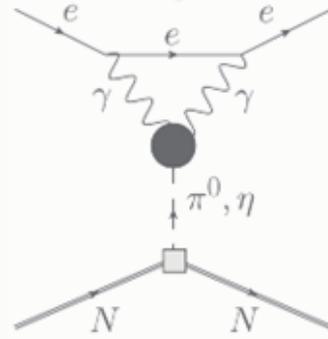
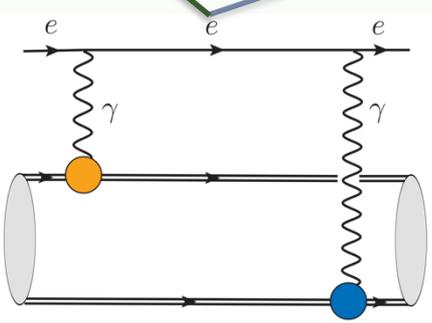
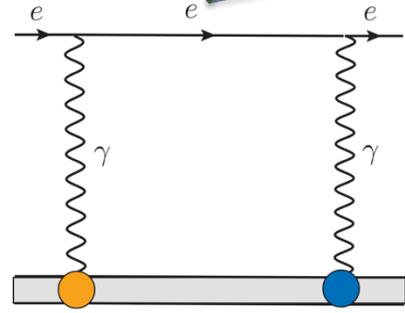


Which source did it?

Quark EDM

Quark chromo EDM

QCD θ



Lemonia Gialdi : Connecting paramagnetic EDM observables to the ED



Which source did it?

Lemonia Gialdi : Connecting paramagnetic EDM observables to the ED

Suppose QCD θ or quark (color) operators as the underlying CPV source:

$$d_n = \#_1 \bar{\theta} \text{ and } d_e^{\text{equiv}} = \#_2 \bar{\theta}$$

$$d_n = \#_3 d_q \text{ and } d_e^{\text{equiv}} = \#_4 d_q$$

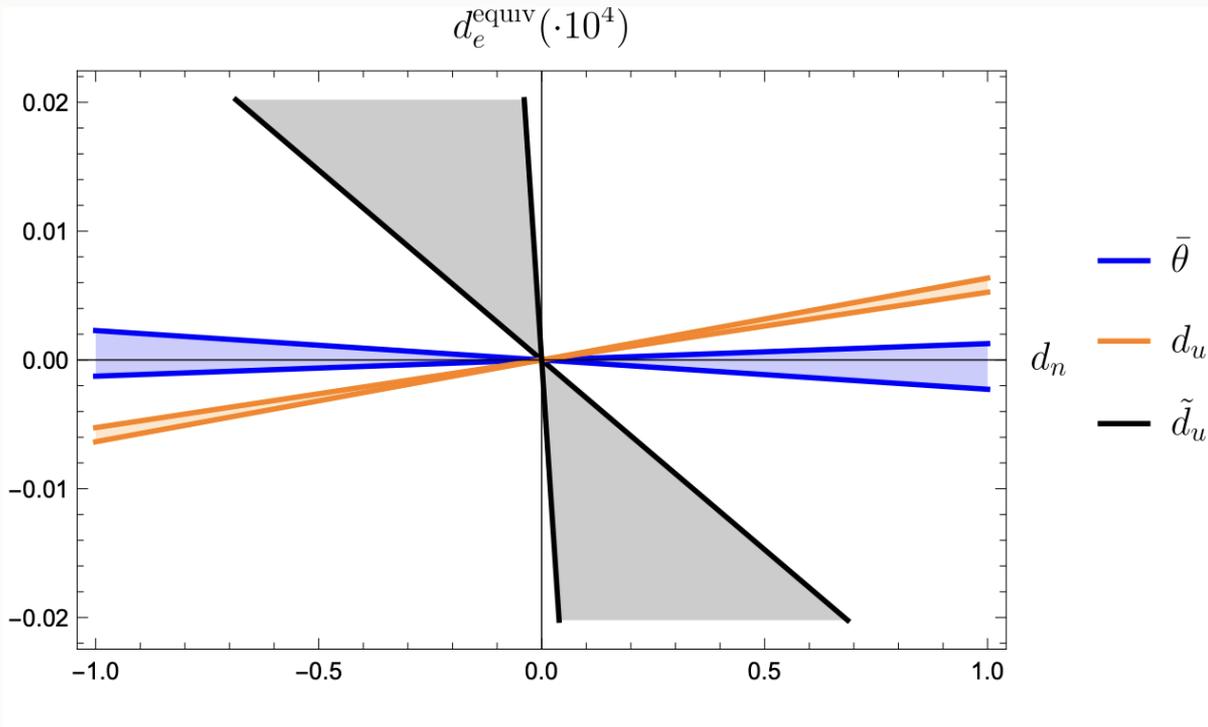


$$d_e^{\text{equiv}} / d_n$$



Ratio Plot

Helps to solve the mystery





Which source did it?

Lemonia Gialdi : Connecting paramagnetic EDM observables to the ED

Example:

Say we measure

$$d_n = 10^{-27} \text{ e cm}$$

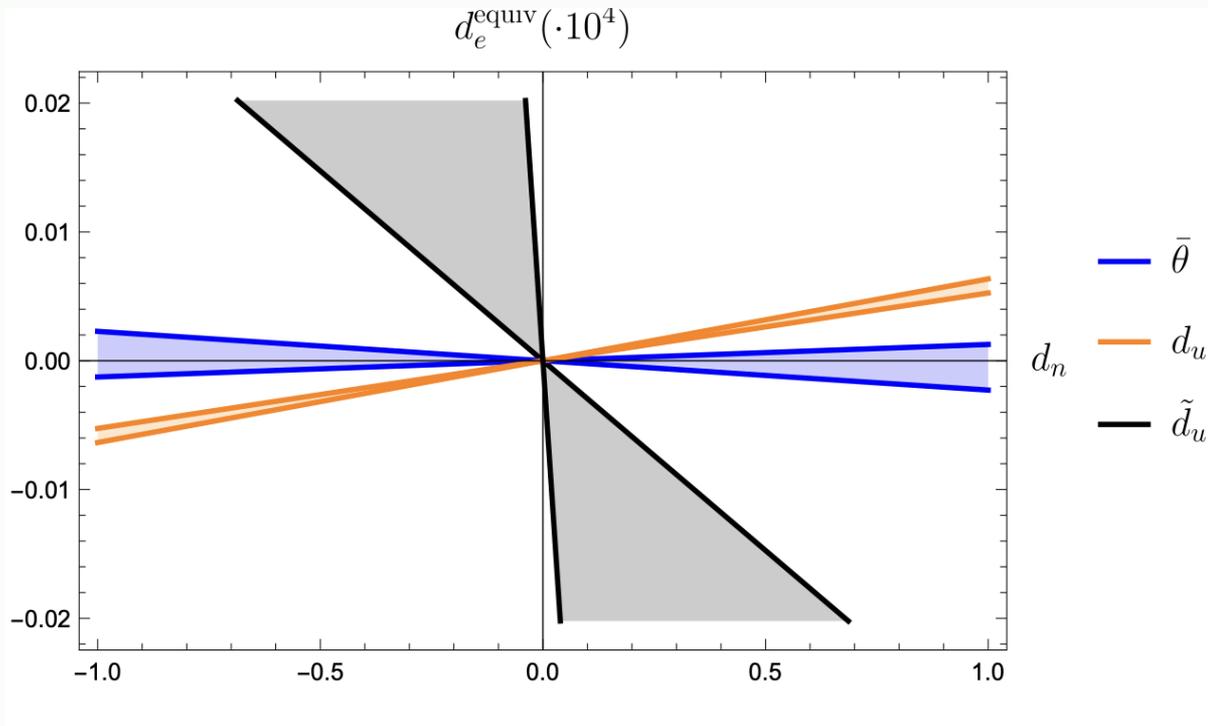
Then we expect:

for up color EDM

$$d_e^{equiv} \sim - (10^{-32} - 10^{-33}) \text{ e cm}$$

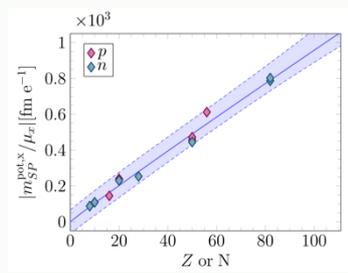
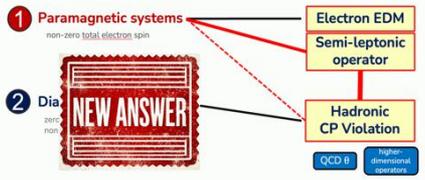
$$d_e^{equiv} \sim + 10^{-34} \text{ e cm for up EDM}$$

d_e^{equiv} even smaller for $\bar{\theta}$



Summary

Match the following:



❖ Connect paramagnetic EDM measurements to nucleon EDMs and hadronic CPV.

❖ Meson exchange and pion loop diagrams.

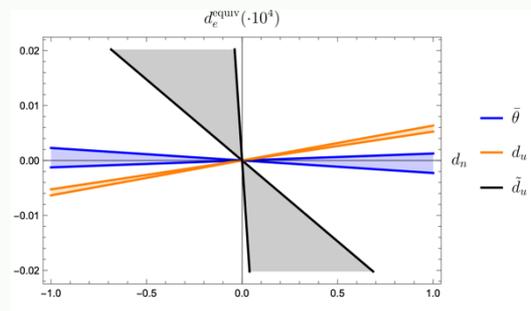
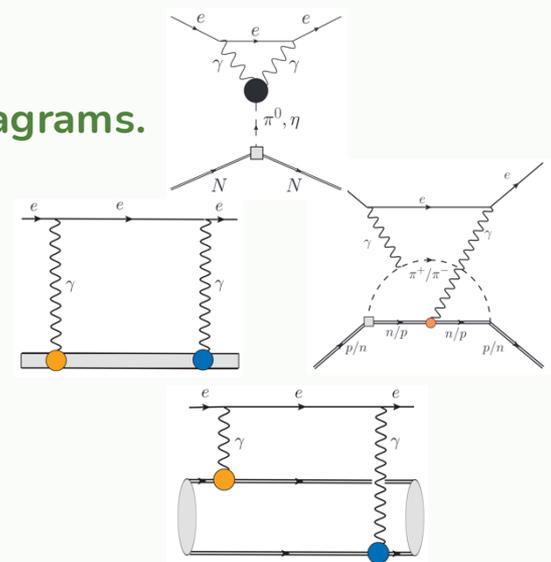
❖ Potential and ultrasoft diagrams.

❖ Nuclear model calculations and use of EFT.

❖ Potential dominates: linear scaling

❖ If there is a measurement, help to solve the CPV source mystery.

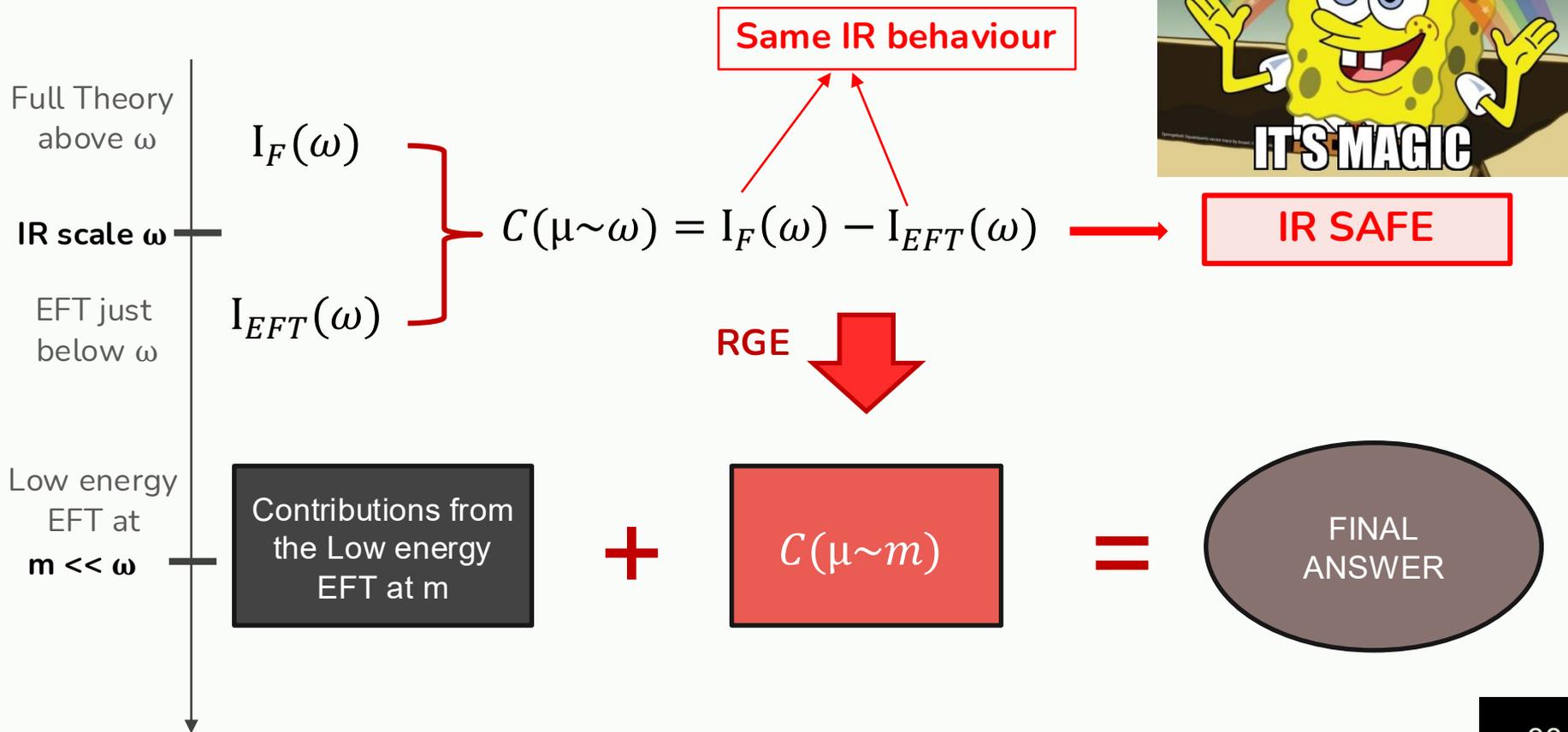
❖ What next? ...



Questions?

Thanks for listening!

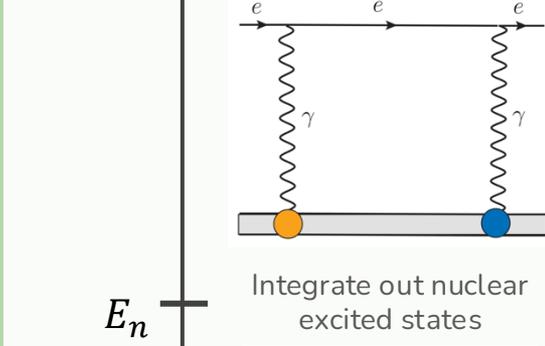
The magic of matching



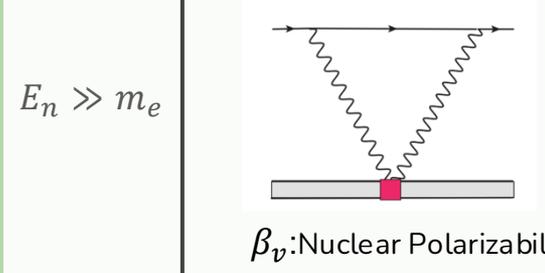
*Introduction to EFT , Manohar 2018

Energy scales

Ultrasoft Region

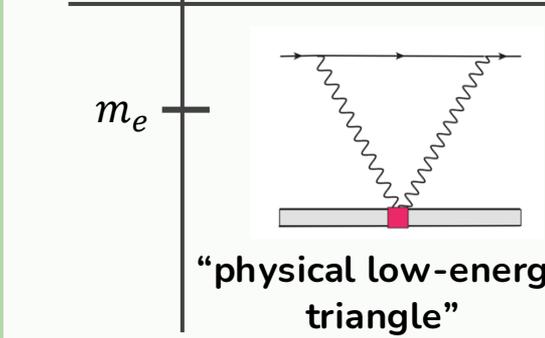


$$\bar{C}_{SP}(\mu \sim E_n) = \text{Box} - \text{Matching Triangle } \beta_\nu$$

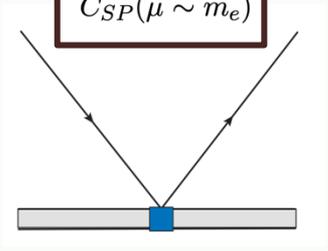


Run down to $\mu \sim m_e$

$$\bar{C}_{SP}(\mu \sim m_e)$$



+

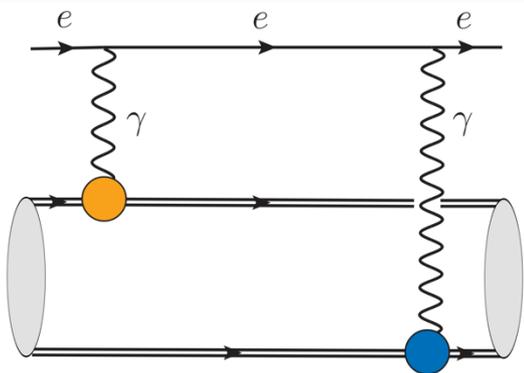


=

A_{usoft}

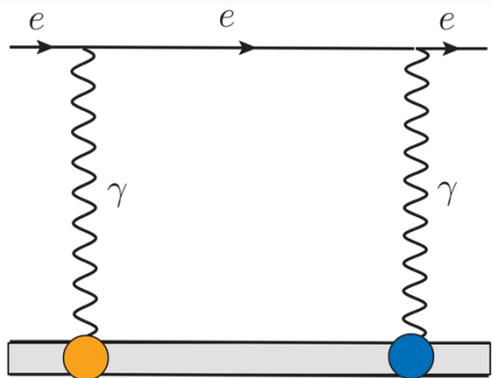
(keep low-energy scales m_e, p_e)

Power counting



$$G_F C_{SP}(\text{pot}) \sim \frac{\alpha^2 \mu_i}{m_N \mu_N} \frac{d_i}{e} \frac{m_e}{q} \frac{4\pi q}{Q}$$

$$\sim \frac{\alpha^2 \mu_i}{m_N \mu_N} \frac{d_i}{e} \frac{m_e}{q}$$



$$G_F C_{SP}(\text{usoft}) \sim \frac{\alpha^2 \mu_i}{m_N \mu_N} \frac{d_i}{e} \frac{m_e}{q}$$