

Exclusion, Discovery and Identification of Dark Matter with directional detection

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Outline

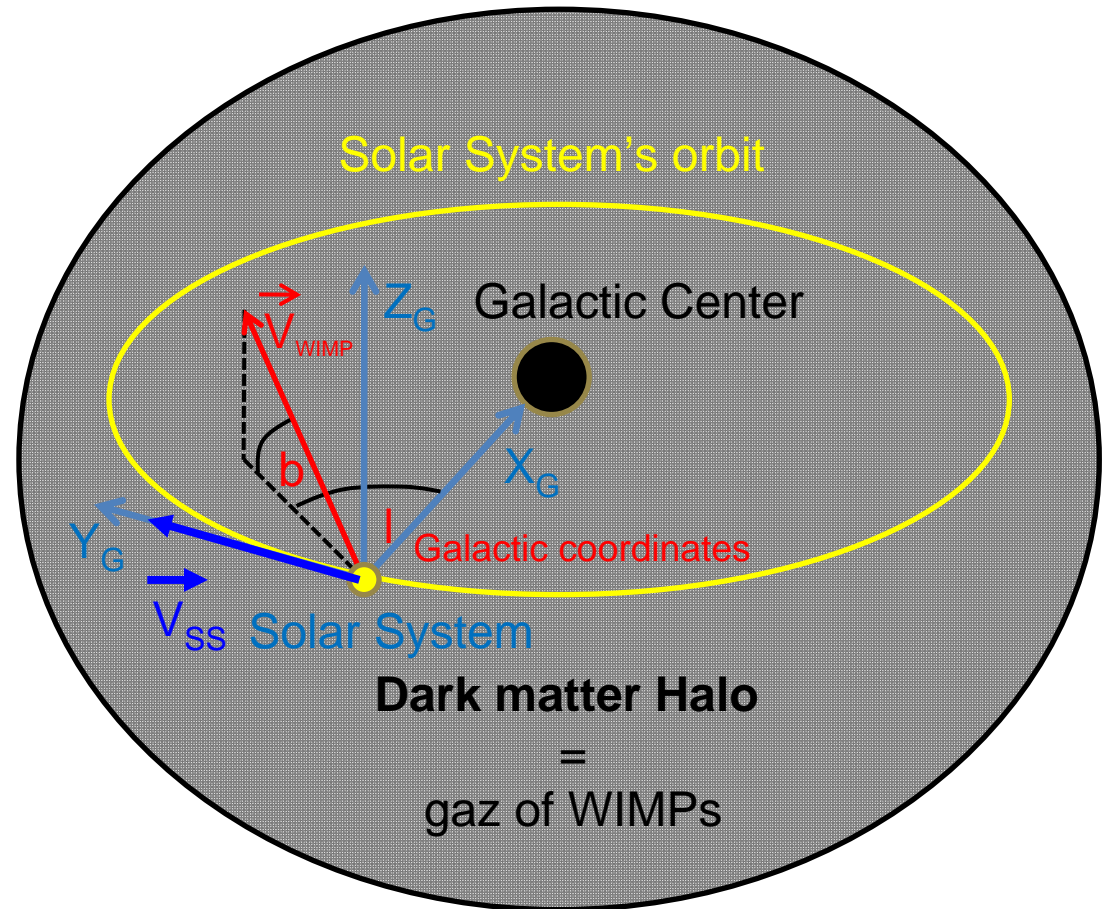
1. Characteristics of directional detection data
2. Case of a null detection: Exclusion limits
3. Case of positive detection: Claim a discovery
4. Case of a high significance detection: Constraints on WIMP properties

Conclusions & discussion

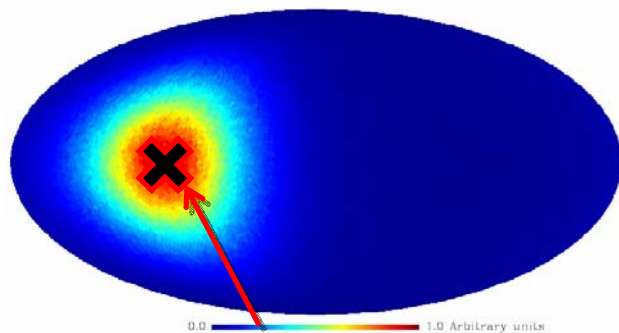
Directional detection signal

I.a WIMP signal

Considering the standard halo model,
isothermal sphere:

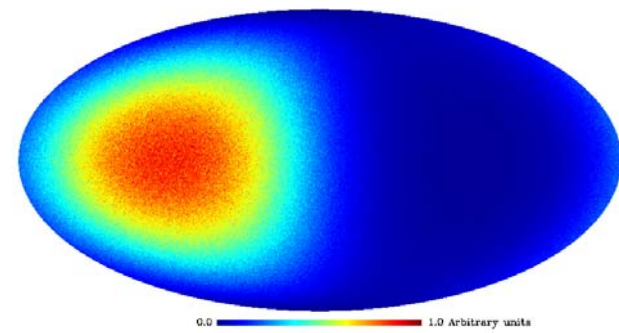


*WIMP flux entering a terrestrial detector
represented in Galactic coordinates*



Cygnus Constellation ($l = 90^\circ, b = 0^\circ$)

After scattering

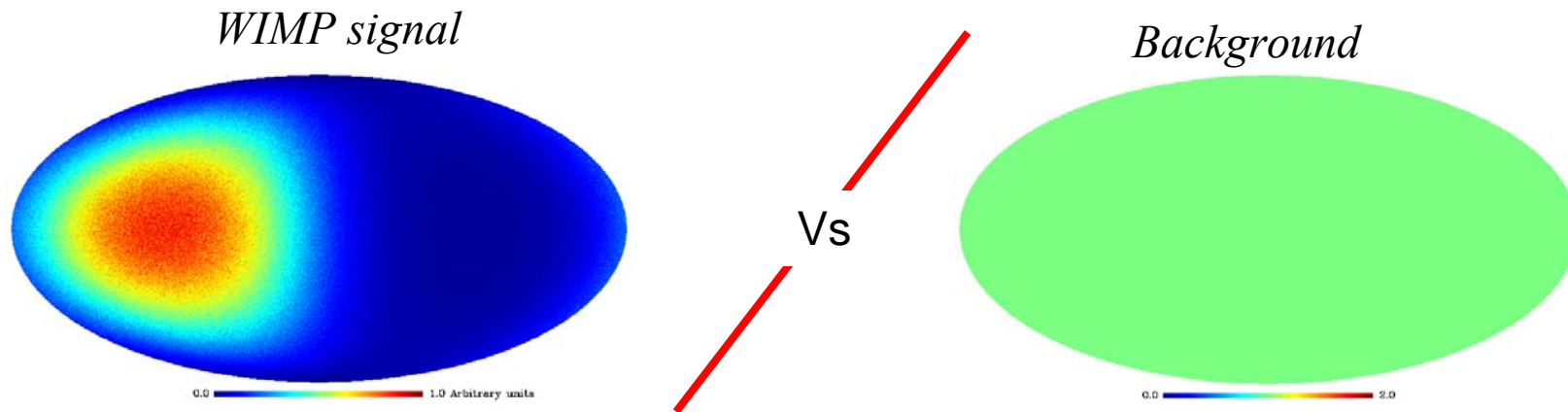


Expected WIMP signal

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I.b Interest of the directional detection

Background is supposed to be **isotropic**



Clear and unambiguous difference between WIMP signal and background

How to take the most advantage of this difference to:

- Set exclusion limits
- Claim a discovery with a sufficient significance
- Identify Dark Matter (particle and galactic physics)

**Depending on the
WIMP nucleon
cross-section**

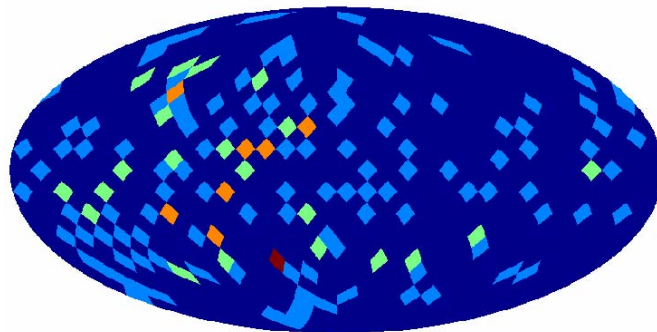
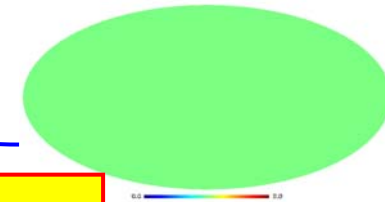
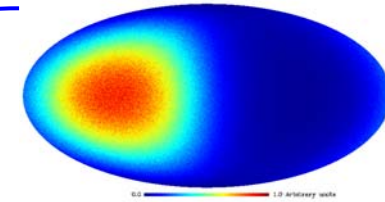
I.c Expected signal

Characteristics of directional data

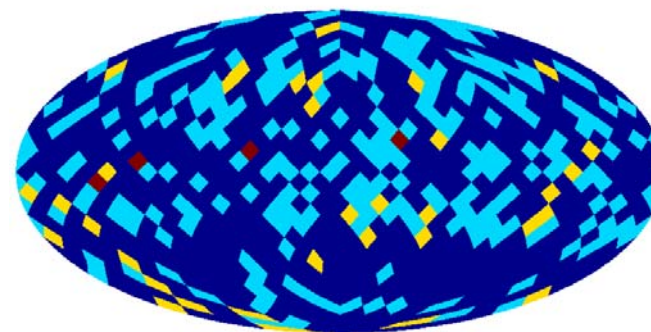
- Low number of WIMP events
- A large background fraction
- Rather low angular resolution

Pseudo data

- 10 kg CF_4
- Livetime : 3 years
- Recoil energy range : [5, 50] keV
- Background event rate $R_b = 10$ evts/kg/year



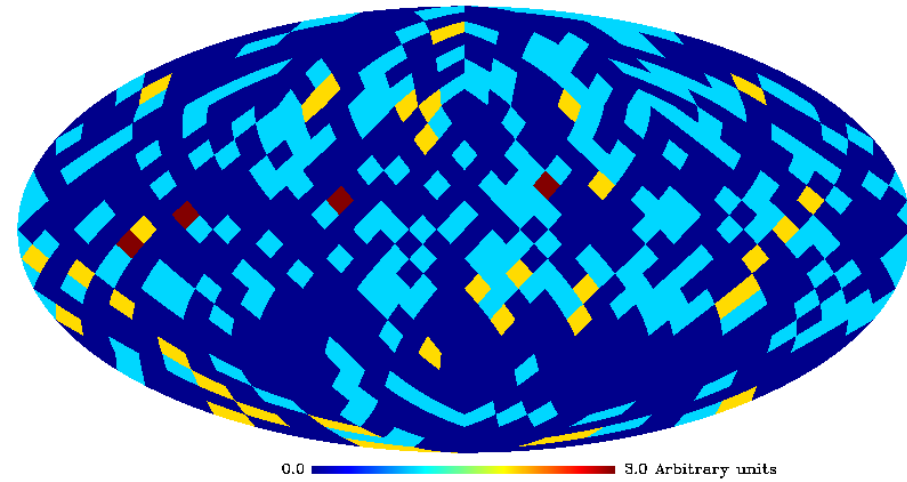
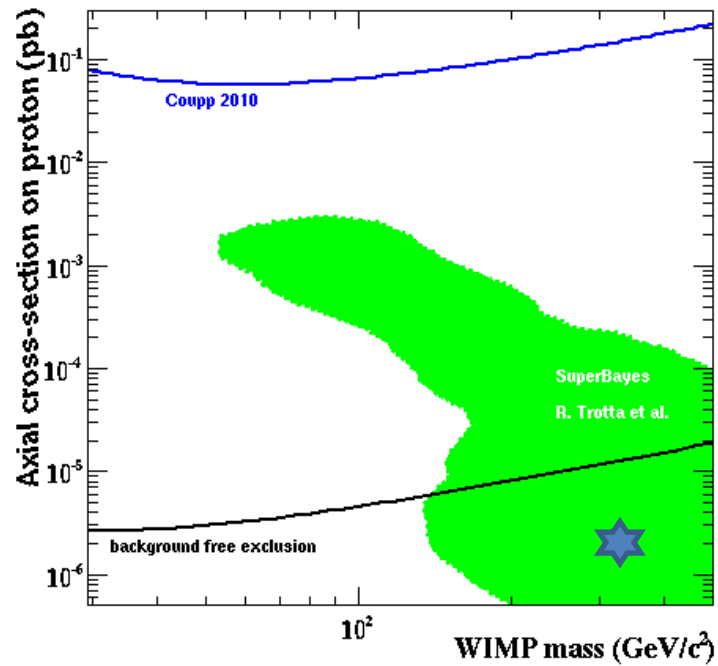
100 WIMP + 100 bck events



0 WIMP + 300 bck events

What can we conclude from such skymaps ?

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300 background events. No WIMP

Case of a null detection

Setting upper limits using directional data...

II.a Directional exclusion limit methods

Several methods can be used for directional detection:

➤ Poisson method

No assumptions on the origin of events

➤ 1D Directional Maximum Gap method (S. Yellin, Phys.Rev. D66 (2002) 032005)

Uses only the theoretical WIMP event angular distribution to set limits

➤ The Maximum Patch Method (S. Henderson et .al, Phys.Rev.D78:015020,2008)

A 2D generalization of the Maximum Gap method considering both directional and energy informations

➤ Directional Likelihood method (J. Billard et .al, Phys.Rev.D82:055011,2010)

Considers the theoretical distributions of both WIMP and background events to set the most restrictive limits

Considering only the angular part of the event distribution



*No assumptions on the energy spectrum of background: **conservative***

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II.b Directional likelihood Method

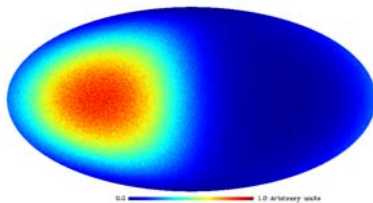
Goal = Estimate, from an observed recoil map M , the expected number of :

- WIMP events : μ_s
- Background events : μ_b

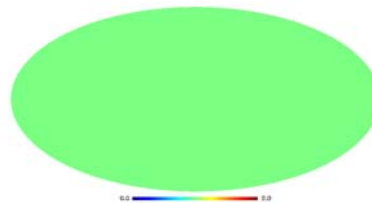
Consider flat priors and an **extended likelihood function**

$$\mathcal{L}(\mu_s, \mu_b) = \underbrace{\frac{(\mu_s + \mu_b)^N}{N!} e^{-(\mu_s + \mu_b)}}_{\text{Poisson distribution}} \times \underbrace{L(\mu_s, \mu_b)}_{\text{Likelihood}}$$

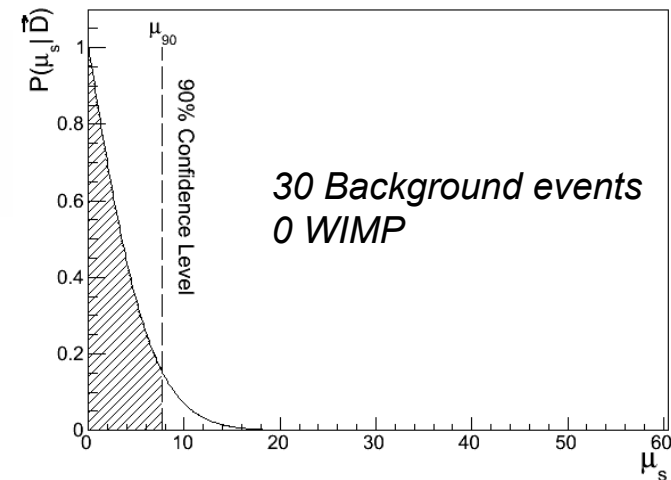
$$L(\mu_s, \mu_b) = \prod_{i=1}^{N_{\text{pixels}}} P\left(\frac{\mu_s}{\mu_s + \mu_b} \underline{S_i} + \frac{\mu_b}{\mu_s + \mu_b} \underline{B_i} \mid M_i\right)$$



S: Signal



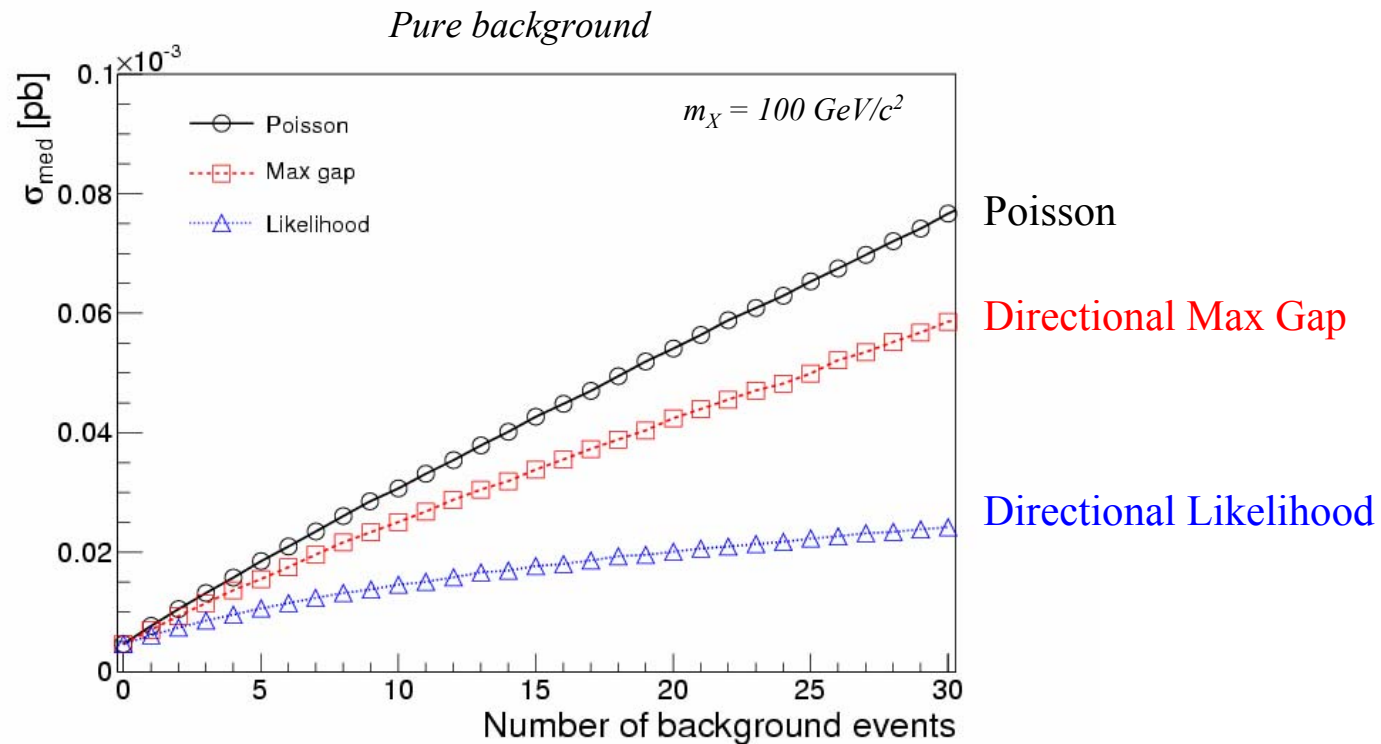
B: Background



Marginalize over μ_b to get: $P(\mu_s \mid D)$

II.c Comparison of the three methods

- For each input and each method : 10,000 toy Monte Carlo experiments.
- From each experiment, we can estimate the median value of the upper limit σ_{med} .



Directional Likelihood Method overcomes the others
... especially at high background contamination

II.c MIMAC expected limits

MIMAC characteristics

- 10 kg CF_4
- DAQ : 3 years
- Recoil energy [5, 50] keV
- Background rate:
10 evts/kg/year

Most restrictive limit: COUPP

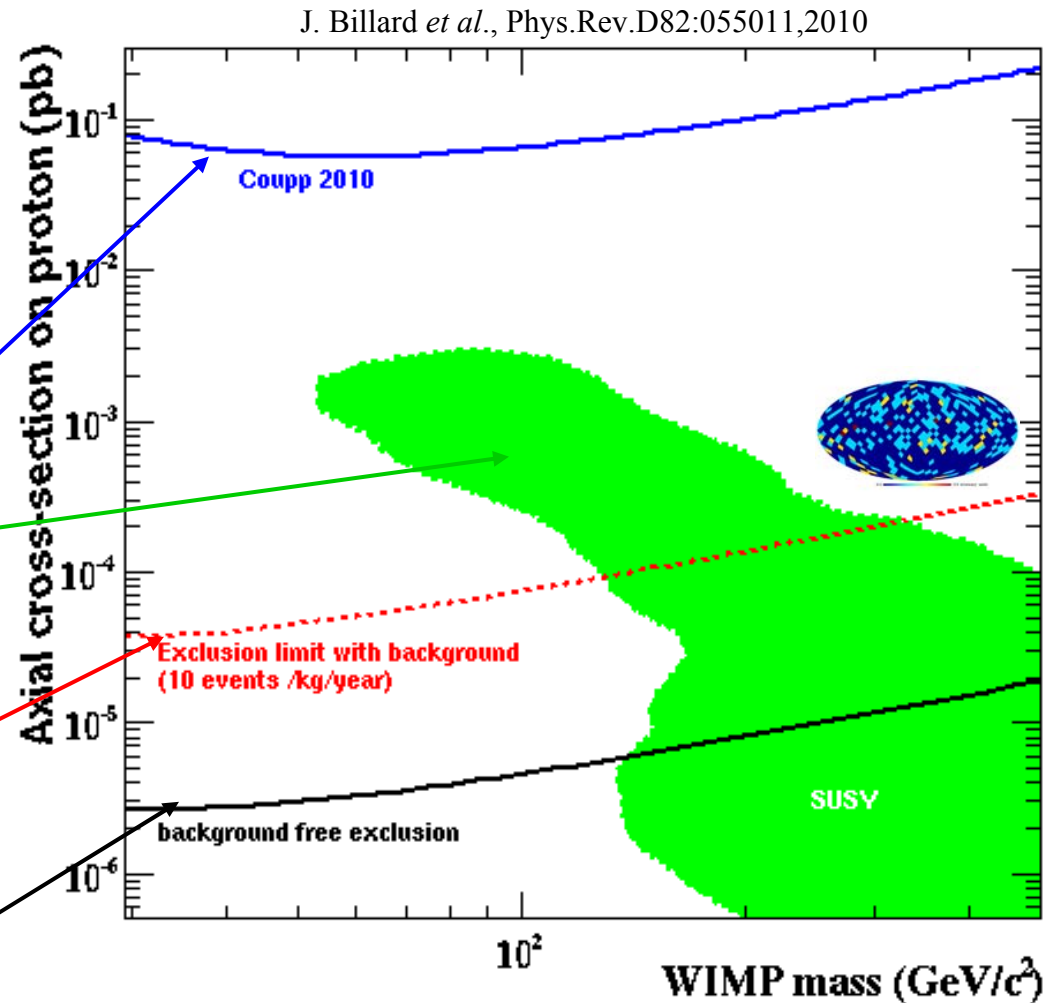
Supersymmetry: SuperBayes

Expected limit: 300 bckg events

Down to $\sim 10^{-5}$ pb

Expected sensitivity: 0 event

Down to $\sim 10^{-6}$ pb

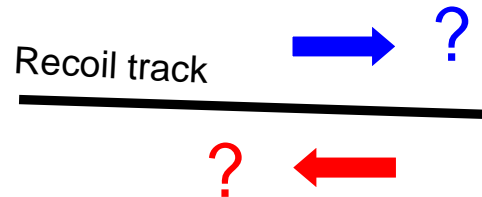


What about the effect of experimental uncertainties on these limits?

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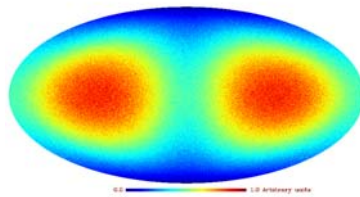
II.d Experimental effects: Sense Recognition (SR)

Sense of the recoiling nuclei?



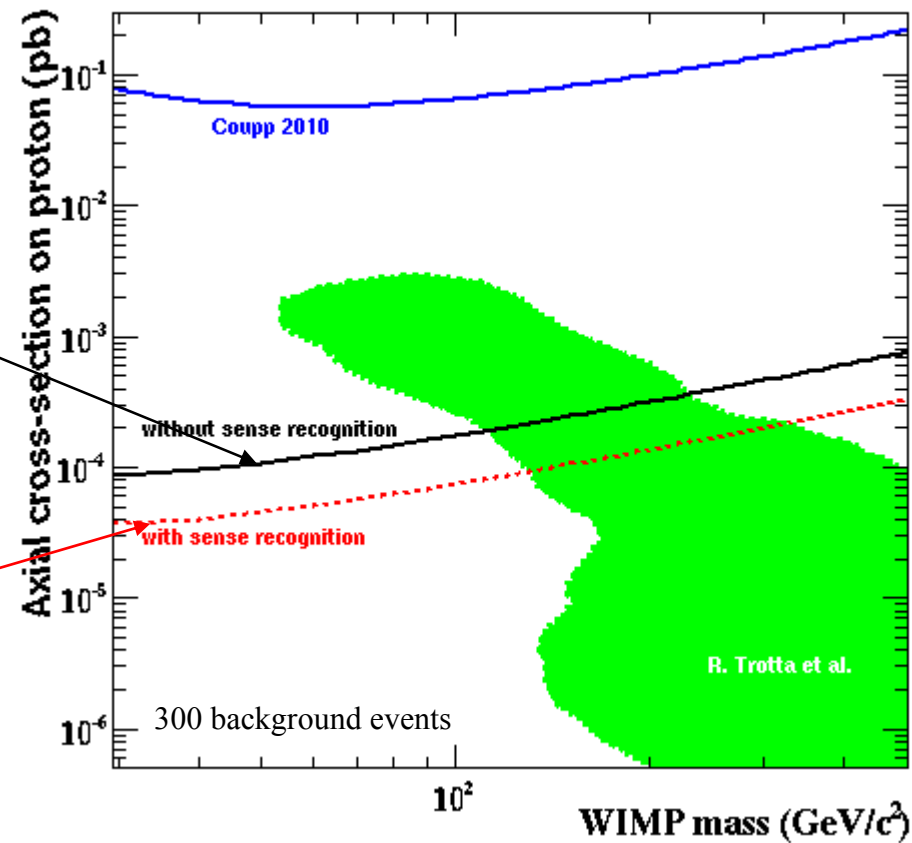
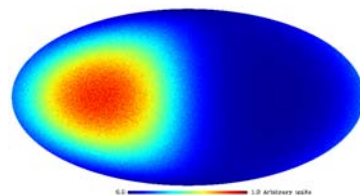
Effect on expected performance of MIMAC:

Without Sense Recognition



The WIMP distribution tends to isotropy

With Sense Recognition



Loose about a factor of 2-3



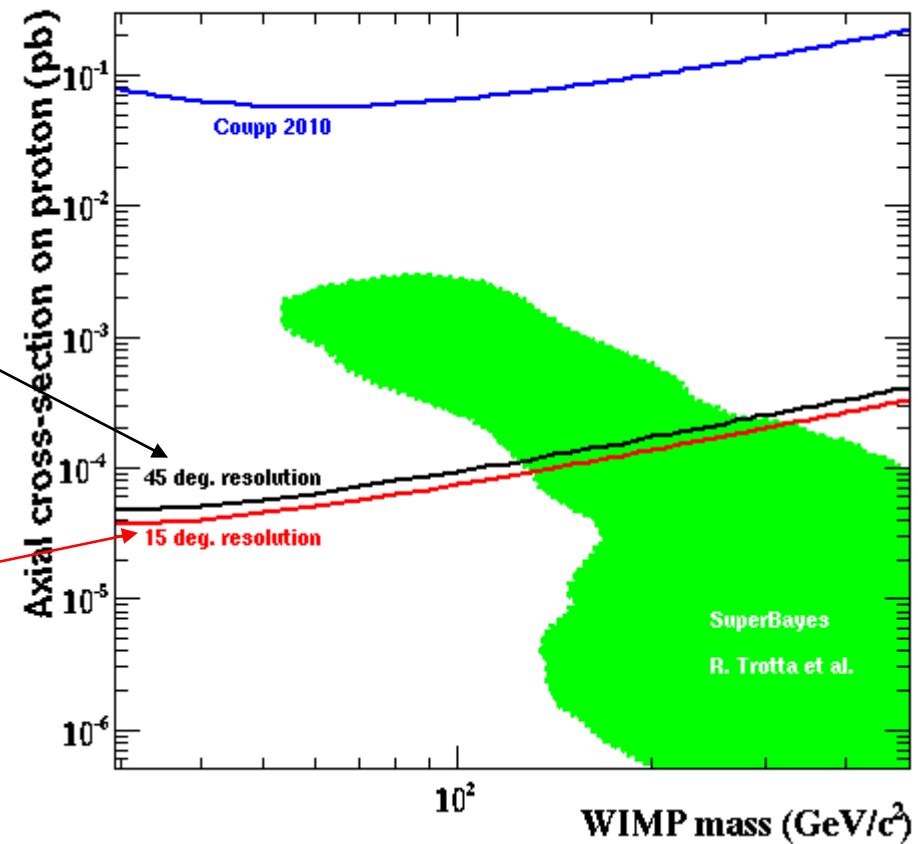
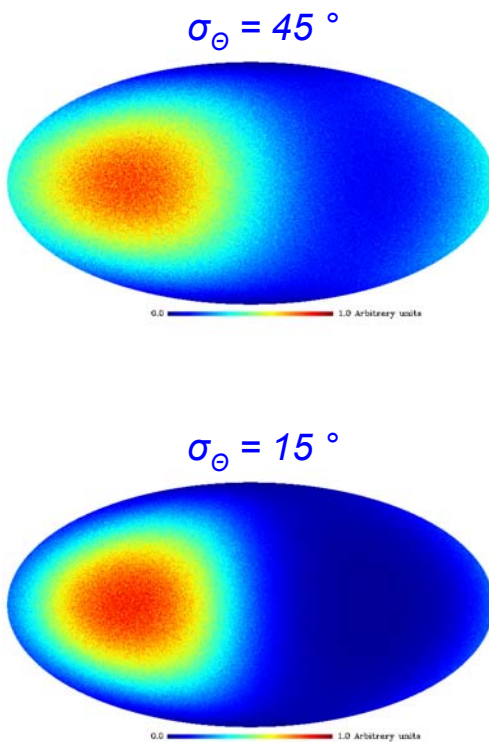
Very important experimental issue

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II.e Experimental effects: angular resolution

Key issue for directional detection

Effect on expected performance of MIMAC:



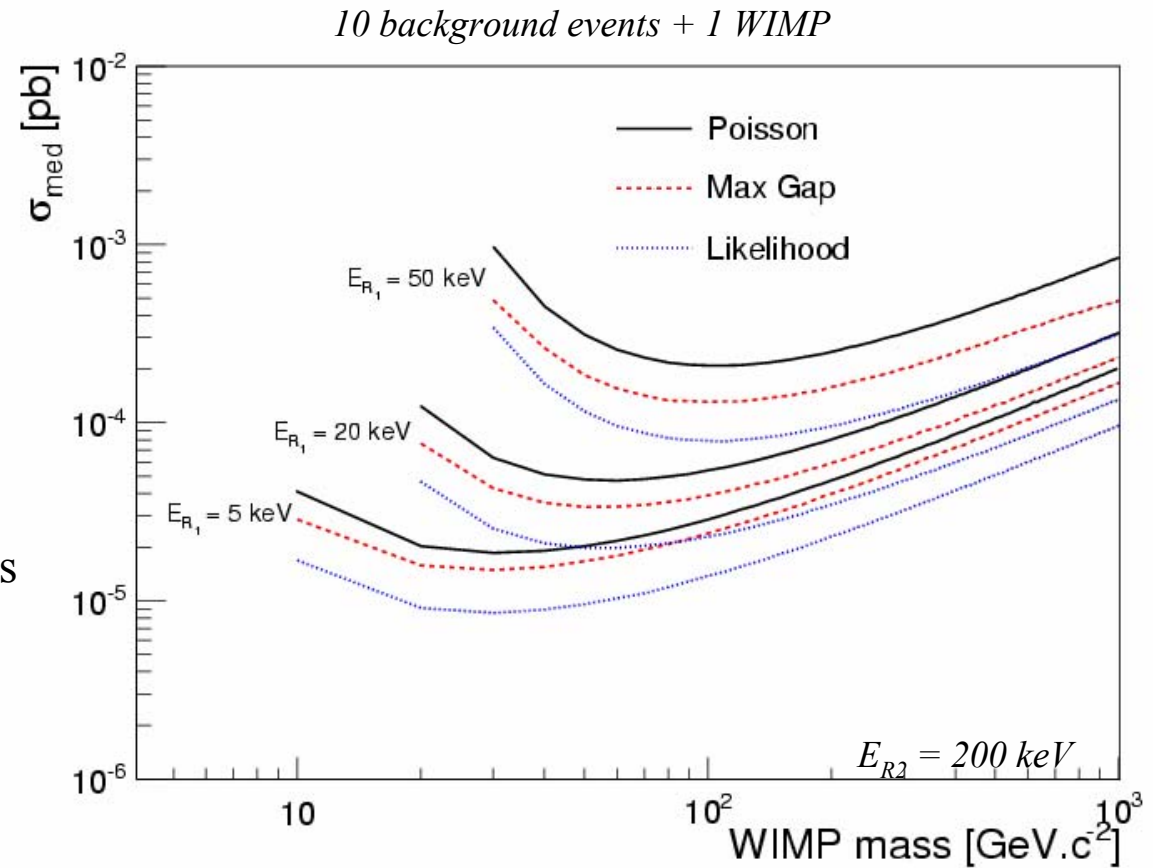
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Minor experimental issue

II.f Effect of the energy threshold E_{R1}

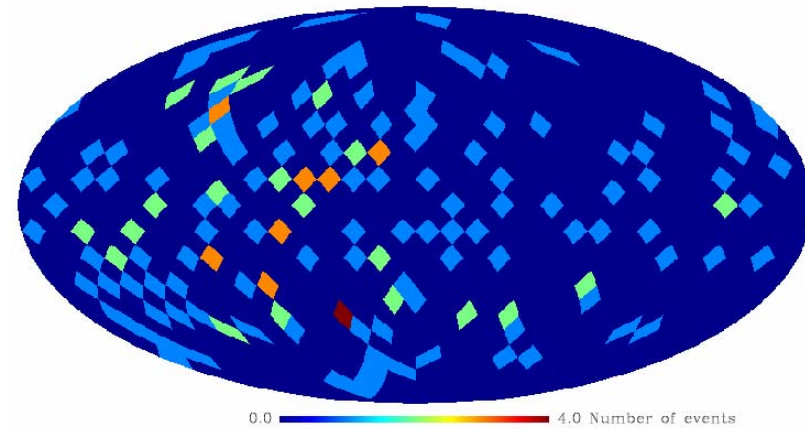
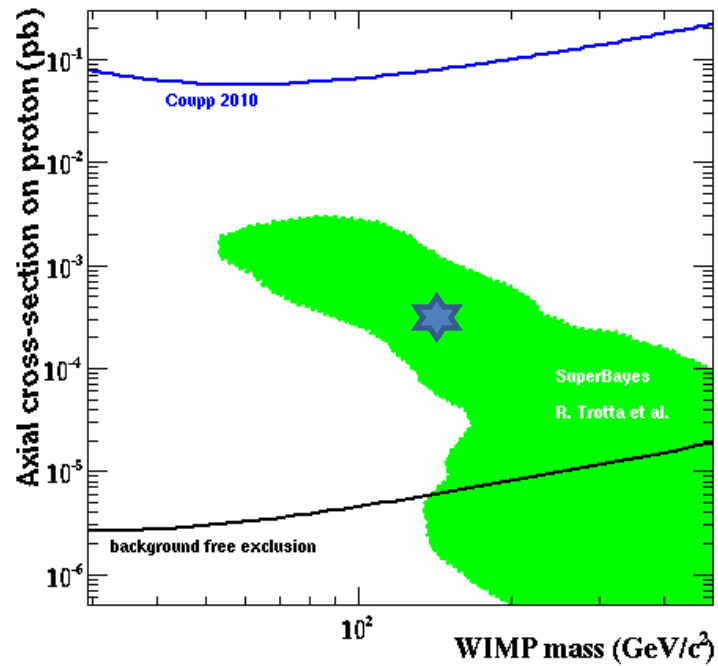
A lower energy threshold leads to:

- More restrictive limits
- A higher sensitivity to light WIMPs



One order of magnitude between 5 and 50 keV threshold

Most important experimental effect



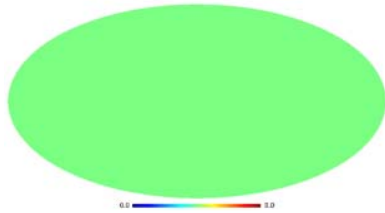
*Observed recoil map
(100 WIMPs + 100 bckg)*

Case of a positive detection

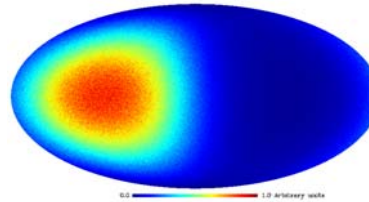
*A signal pointing
toward the
Cygnus
Constellation?*

...Is there any WIMP events in this observed recoil map?

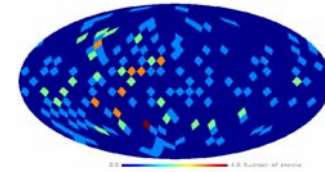
III.b Likelihood definition



B: Background



S: Theoretical WIMP signal



M: Measurement

$$\mathcal{L}(m_\chi, \lambda, \ell, b) = \prod_{i=1}^{N_{\text{bins}}} P(\underbrace{[(1 - \lambda)B_i]}_{\text{green}}, \underbrace{+ \lambda S_i(m_\chi; \ell, b)}_{\text{red}} \underbrace{)]}_{\text{blue}} | M_i)$$

A four parameter likelihood:

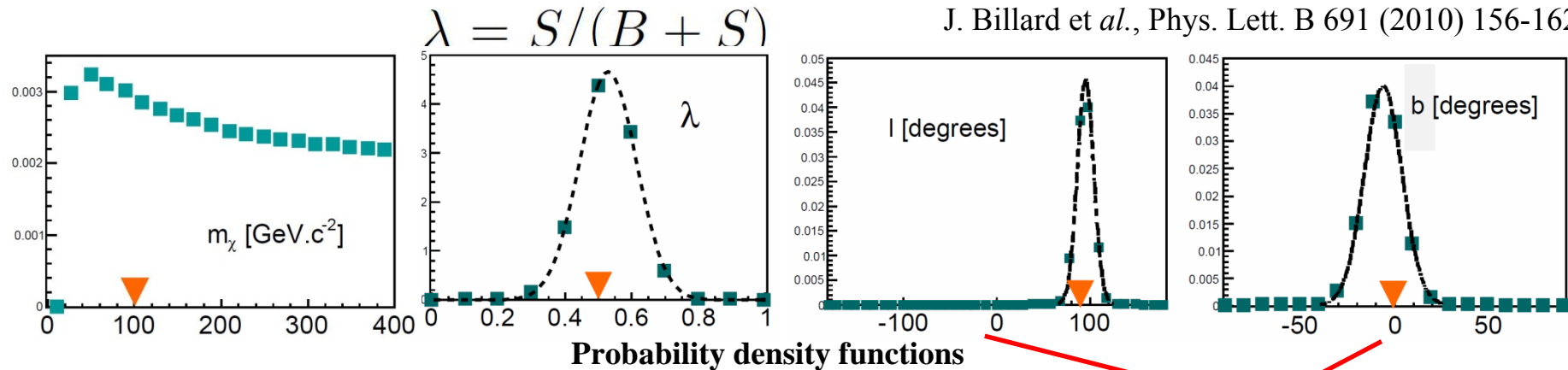
- WIMP mass m_χ
- The WIMP fraction: $\lambda = S/(B + S)$
- ℓ and b refers to the main incoming direction



Blind analysis
Prove that the signal
comes from Cygnus

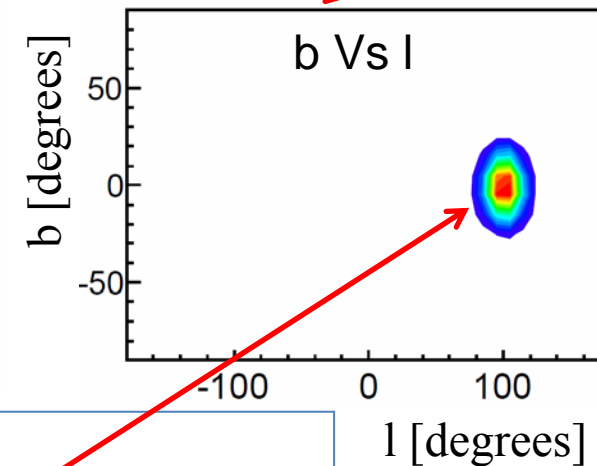
III.c A map based likelihood analysis

J. Billard et al., Phys. Lett. B 691 (2010) 156-162



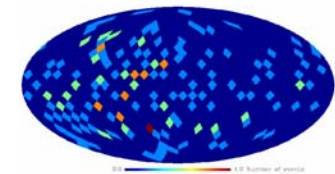
Likelihood analysis

WIMP mass: $m_\chi > 10 \text{ GeV.c}^{-2}$
 WIMP fraction: $\lambda = 0.53 \pm 0.085$ (1σ CL)
 Galactic latitude: $l = 95^\circ \pm 10^\circ$ (1σ CL)
 Galactic Longitude: $b = -6^\circ \pm 10^\circ$ (1σ CL)



Conclusions of the map analysis:

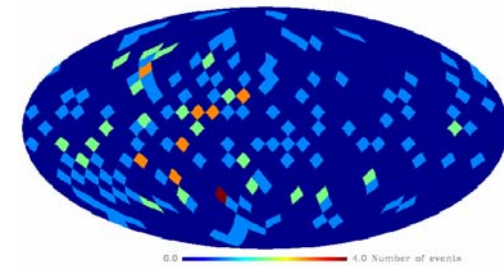
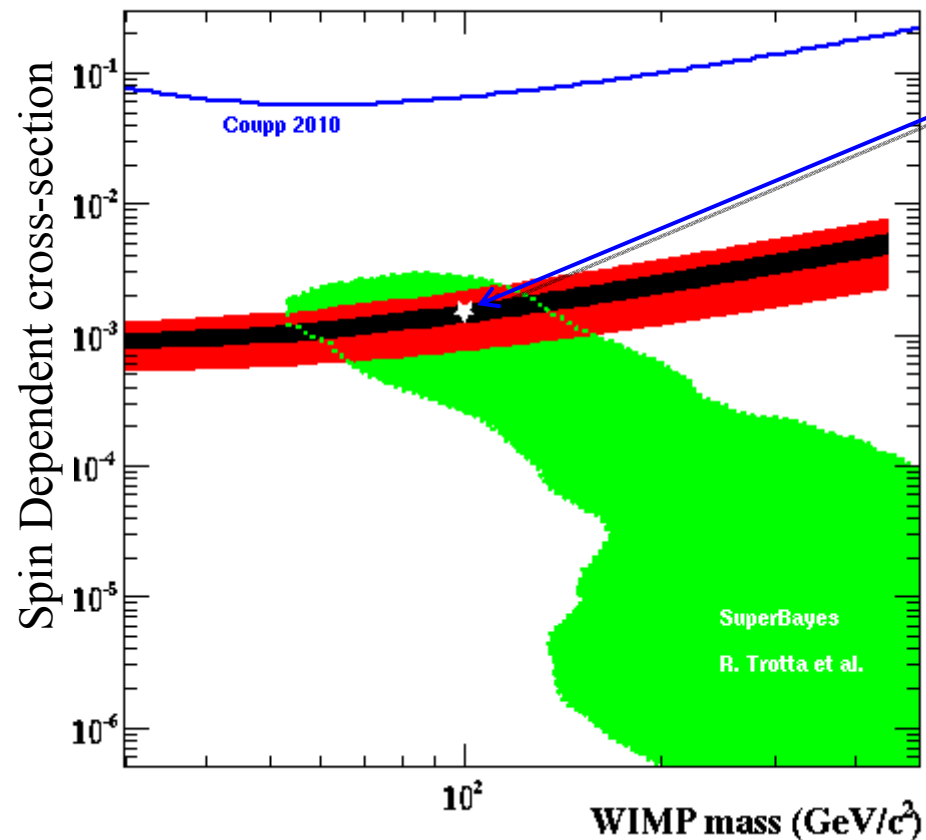
- The signal is pointing toward the Cygnus Constellation within 10° (68% CL)
- $N_{\text{WIMP}} = 106 \pm 15$ (68% CL) $\sim 7\sigma$ significance



III.d Constraining the WIMP mass and cross-section

Constraint on λ implies a constraint on the WIMP-nucleon cross-section:

Allowed regions deduced from the likelihood analysis,
NOT exclusion!



Realistic simulated data

- 10 Kg CF_4
- DAQ : 5 months
- Bckg rate = 25 evts/kg/year
- Angular resolution: 15° (FWHM)

From: Exclusion strategy



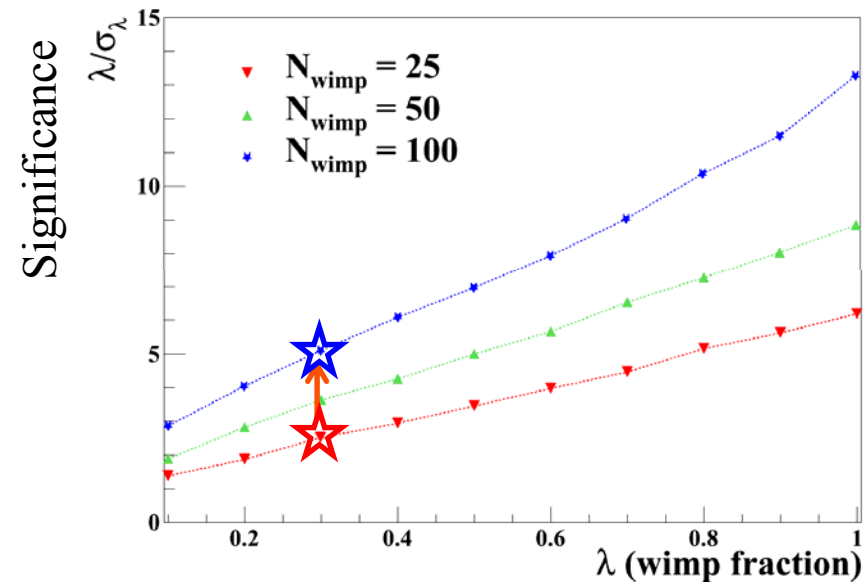
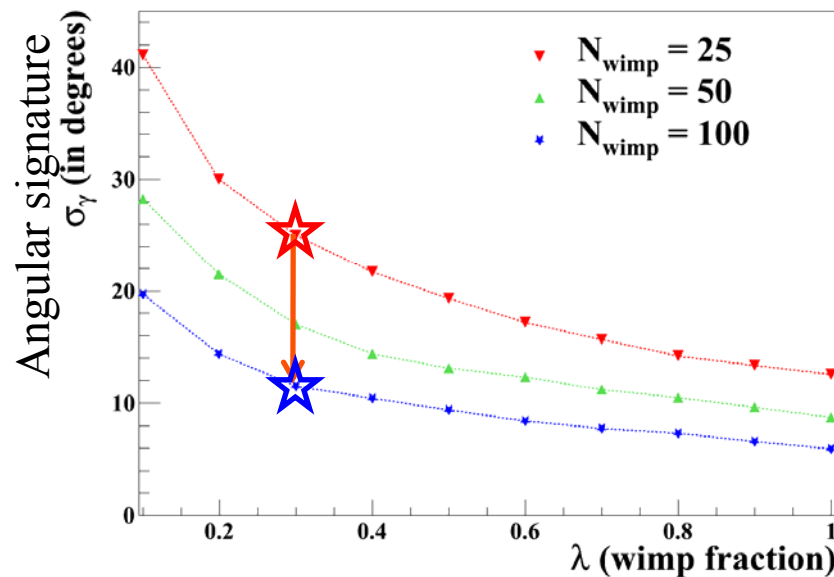
To: Discovery strategy

III.e Systematical studies

Angular signature: $\sigma_\gamma = \sqrt{\sigma_\ell \sigma_b}$

Significance: λ/σ_λ

Satisfactory results on a large range of exposure (N_{WIMP}) and background fraction (λ)



★ Low exposure results: *1.25 kg.year CF4 detector = 25 WIMPs and 50 background*
WIMP from Cygnus within 25° but... poor significance (HINT of DM detection)

★ High exposure results: *5 kg.year CF4 detector = 100 WIMPs and 200 background*
WIMP from Cygnus within 10° High significance (5σ) ! (DISCOVERY of DM)

III f: MIMAC « road map »

MIMAC characteristics

- 10 kg CF_4
- DAQ : 3 years
- Recoil energy [5, 50] keV
- Background rate:
10 evts/kg/year

Down to 10^{-4} pb:

discovery

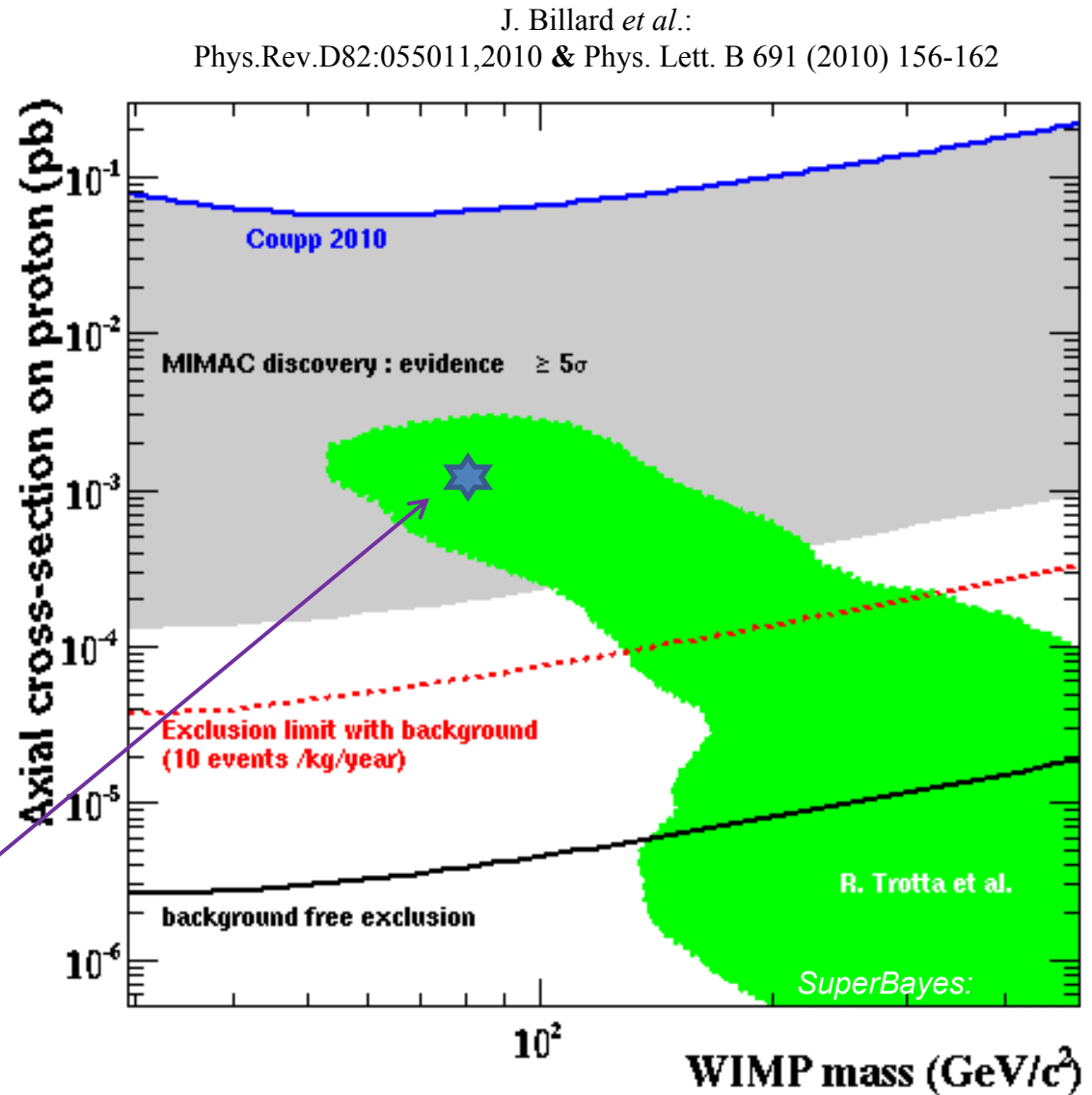
Down to 10^{-5} pb:

exclusion

Going further... = 10^{-3} pb:

Identification of DM

« Constraints on the mass, the cross-section and the halo properties »



A Markov Chain Monte Carlo analysis to identify Dark Matter

IV.a Directional event rate

$$\frac{d^2 R}{dE_R d\Omega} = \frac{\boxed{\rho_0} \boxed{\sigma_0}}{4\pi \boxed{m_\chi m_r^2}} \overset{\text{Form factor}}{\boxed{F^2(E_R) \hat{f}(v_{\min}, \hat{q})}}$$

- Astrophysics
- Particle physics
- Nuclear physics

$$F(E_R) = \frac{\sin(\sqrt{2m_N E_R} r_n)}{\sqrt{2m_N E_R} r_n}$$

In the case of an axial coupling

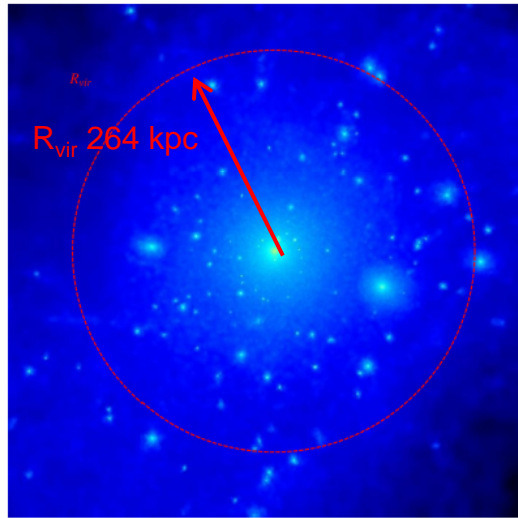
Radon transform: [P. Gondolo 2002]

$$\hat{f}(v_{\min}, \hat{q}) = \int d^3 v \overset{\text{Kinematic relationship}}{\boxed{\delta(\vec{v} \cdot \hat{q} - v_{\min})}} \boxed{f(\vec{v})} \quad ?$$

« Geometrically, the Radon transform is the integral of the velocity distribution on a plane orthogonal to the recoil direction and at a distance v_{\min} from the origin »

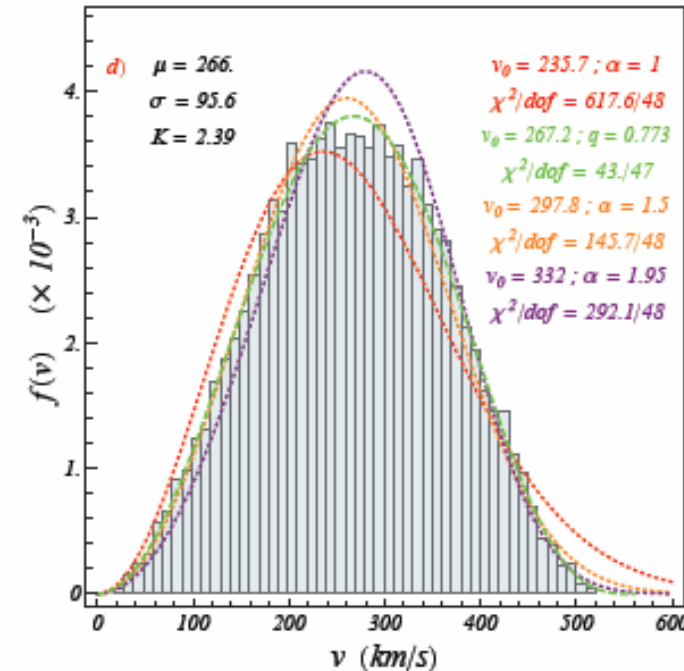
IV.b The velocity distribution

N-Body simulation with baryons (F. S. Ling et al. 2009)



Dark Matter halo from cosmological N-Body simulations (RAMSES code from R. Teyssier)

Velocity distribution of the WIMP particle within a radius of 9 kpc in the Galactic frame



- No evidence against a smooth velocity distribution
- Standard isotropic halo model disfavoured in this case: $\beta = 0.06$

Anisotropy parameter: $\beta(r) = 1 - \frac{\sigma_\theta^2 + \sigma_\phi^2}{2\sigma_r^2}$ \longrightarrow

- $\beta < 0$: Tangential anisotropy
- $\beta > 0$: Radial anisotropy
- $\beta = 0$: isotropic

Compatible with a multivariate gaussian distribution...

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IV.b The velocity distribution: Multivariate Gaussian

From the Jeans equation: the velocity tensor is symmetric

« One can find an orthogonal basis where the velocity tensor is diagonal »

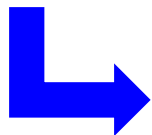


$$f(\vec{v}) = \frac{1}{(8\pi^3 \det \boldsymbol{\sigma}_v^2)^{1/2}} \exp \left[-\frac{1}{2} (\vec{v} - \vec{v}_\odot)^T \boldsymbol{\sigma}_v^{-2} (\vec{v} - \vec{v}_\odot) \right]$$

The multivariate gaussian velocity distribution function, naturally arises from the fact that:

- It is the triaxial generalization of the standard isothermal sphere [Binney and Tremaine]
- It reproduces flat rotation curves ($\rho(r) = 1/r^2$) [N. W. Evans et al. 2000]
- It is quite consistent with recent numerical N-body simulations

[M. Vogelsberger et al. 2009, M. Khullen et al. 2010, F. S. Ling et al. 2010]



The multivariate Gaussian is then used as a fitting model

IV.c Free parameters

The 8 free parameters of the fitting model are:

- The WIMP mass m_X
- The WIMP-nucleon cross- section σ_n
- The main incoming direction of the signal (l_0, b_0)
- The 3 velocity dispersions σ_x, σ_y et σ_z
- The background rate R_b

What are the posterior Probability Density Functions of each parameter according to a single experiment?

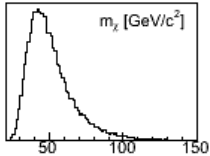


We developed a Markov Chain Monte Carlo sampling based on the Metropolis-Hastings algorithm for the following reasons:

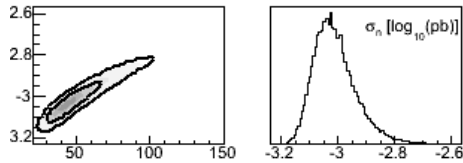
- Size of the parameter space: **8 dimensions!**
- The estimation of the PDFs are very accurate

Sub-sampling: « burn-in » and correlation lenghts => **independant samples**

Mass



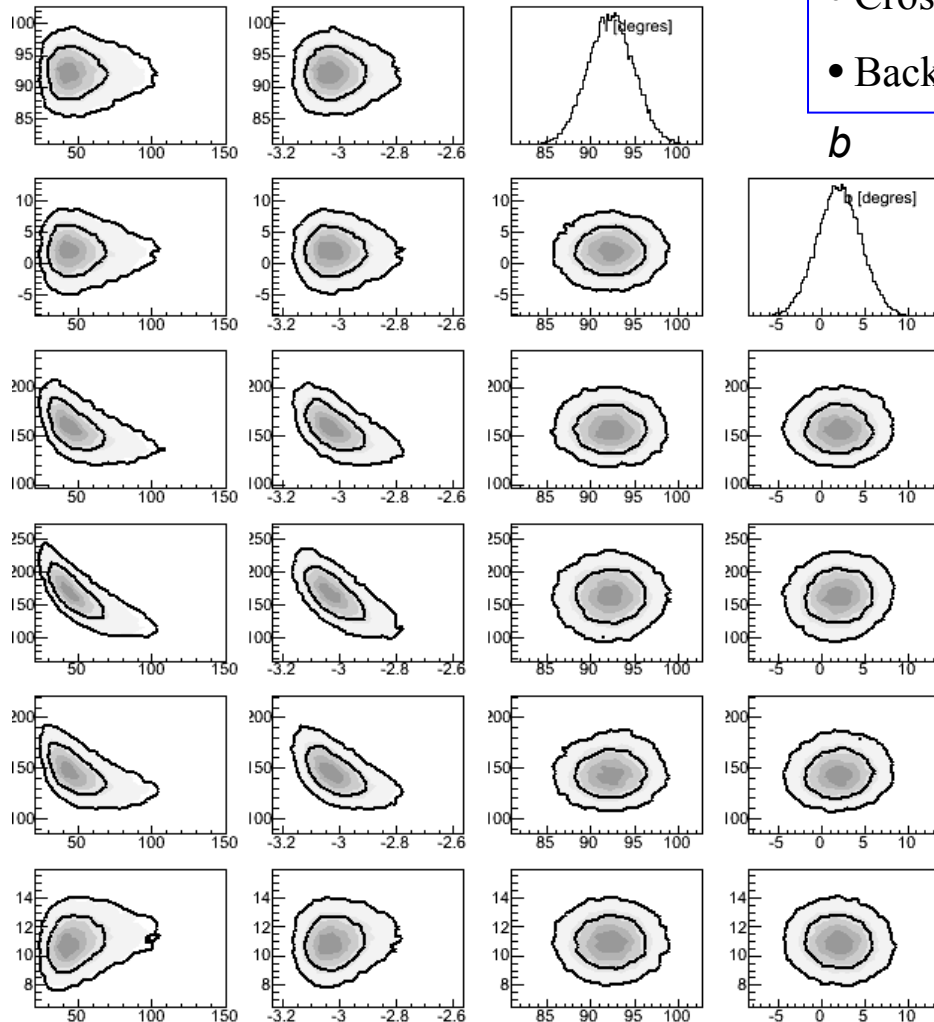
Cross-section



Full Markov Chain Monte Carlo result

Input:

- isotropic halo: $\sigma_x = \sigma_y = \sigma_z = 155 \text{ km/s}$
- WIMP mass: $50 \text{ GeV}/c^2$
- Cross-section: 10^{-3} pb
- Background rate (R_b): $10 \text{ evts/kg/year (35\%)}$

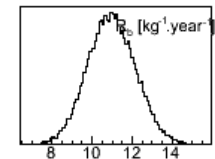


The eight fitting parameters are simultaneously constrained from a single experiment

MIMAC characteristics

- 10 kg CF_4
- DAQ : 3 years
- Recoil energy [5, 50] keV

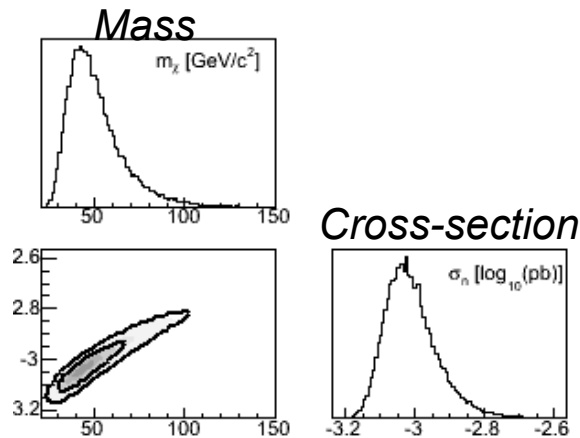
R_b



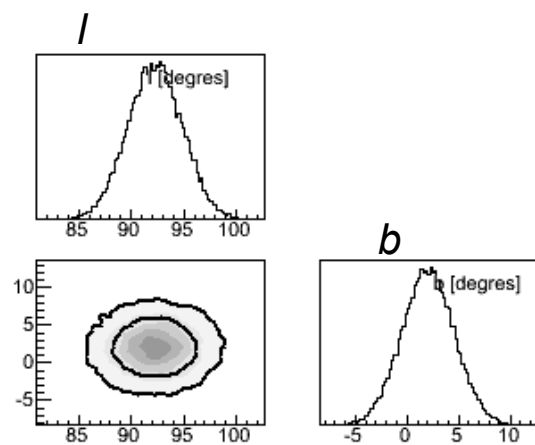
IV.d Deduced constraints

The 8 fitting parameters are strongly constrained from a single directional detection experiment:

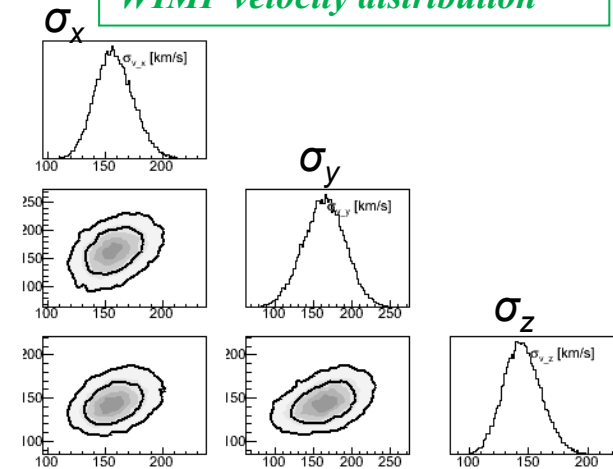
WIMP mass Vs Cross-section



Dark Matter signature



WIMP velocity distribution



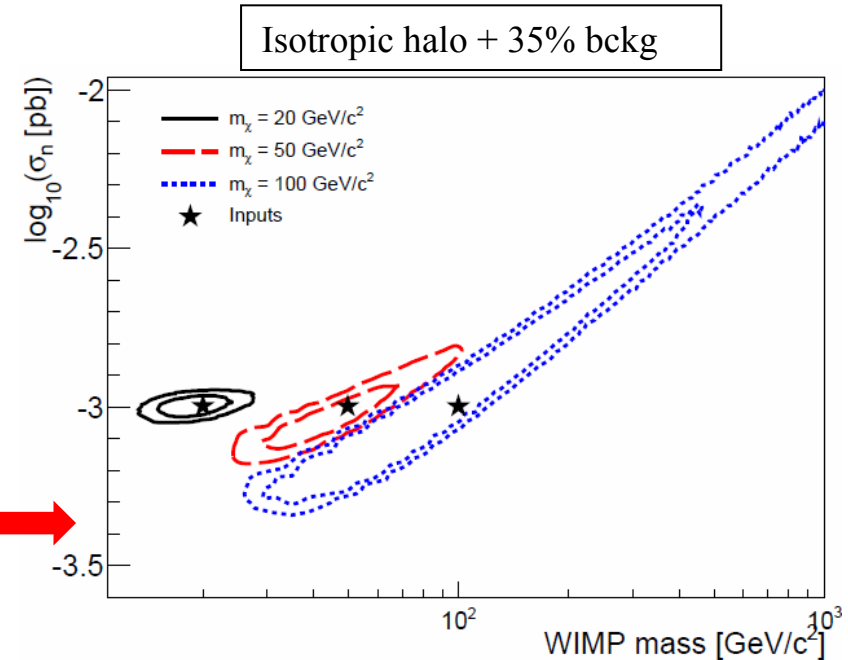
	m_χ (GeV/c ²)	$\log_{10}(\sigma_n$ (pb))	ℓ_\odot (°)	b_\odot (°)	σ_x (km.s ⁻¹)	σ_y (km.s ⁻¹)	σ_z (km.s ⁻¹)	β	R_b (kg ⁻¹ year ⁻¹)
Input	50	-3	90	0	155	155	155	0	10
Output	$51.8^{+5.6}_{-19.4}$	$-3.01^{+0.05}_{-0.08}$	$92.2^{+2.5}_{-2.5}$	$2.0^{+2.5}_{-2.5}$	158^{+15}_{-17}	164^{+27}_{-26}	145^{+14}_{-17}	$-0.073^{+0.29}_{-0.18}$	10.97 ± 1.2

IV.e Input WIMP mass

Standard halo with three different masses:

- 20 GeV
- 50 GeV
- 100 GeV

Consistent constraints on $(m_\chi, \log_{10}(\sigma_n))$



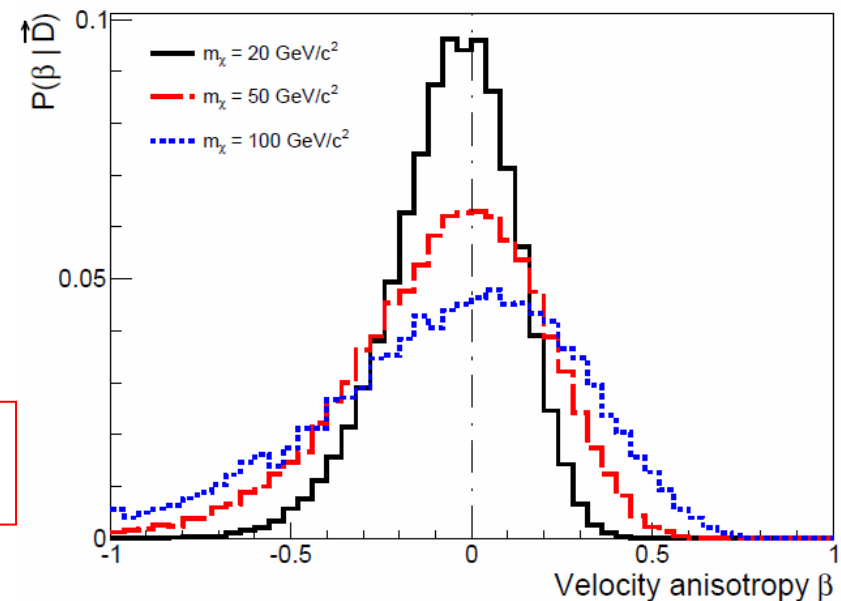
Constraints on the β parameter:

$$\beta(r) = 1 - \frac{\sigma_\theta^2 + \sigma_\phi^2}{2\sigma_r^2}$$

(Deduced from the full MCMC analysis)

Isotropic halo: $\beta = 0$

Constraints on the WIMP parameters and Dark Matter halo are consistent for all WIMP masses



35% of bckg + 50 GeV/c²

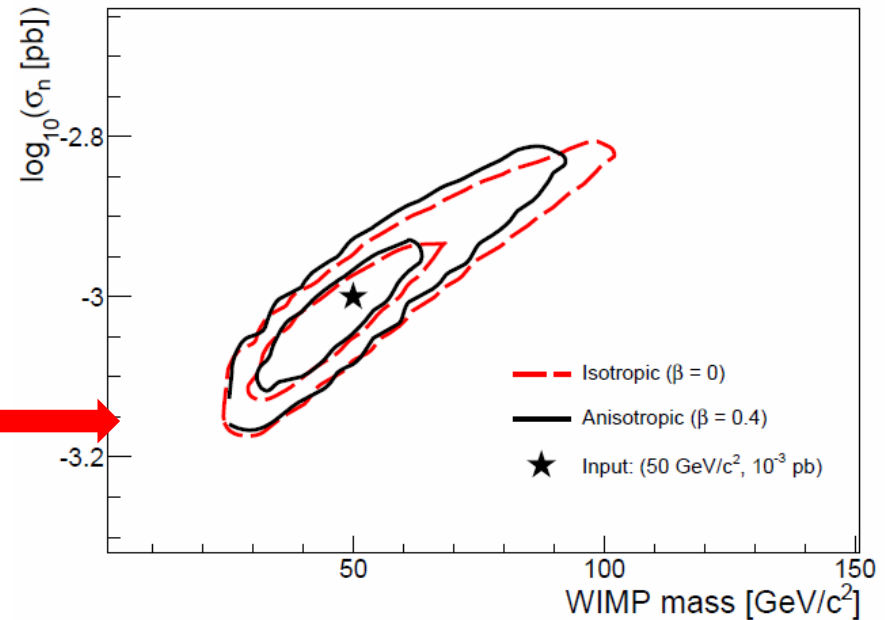
IV.f Input halo model

2 input halo models to generate pseudo-data:

Isotropic ($\beta = 0$)

Extremely Anisotropic ($\beta = 0.4$)

Similar constraints on ($m_\chi, \log_{10}(\sigma_n)$)

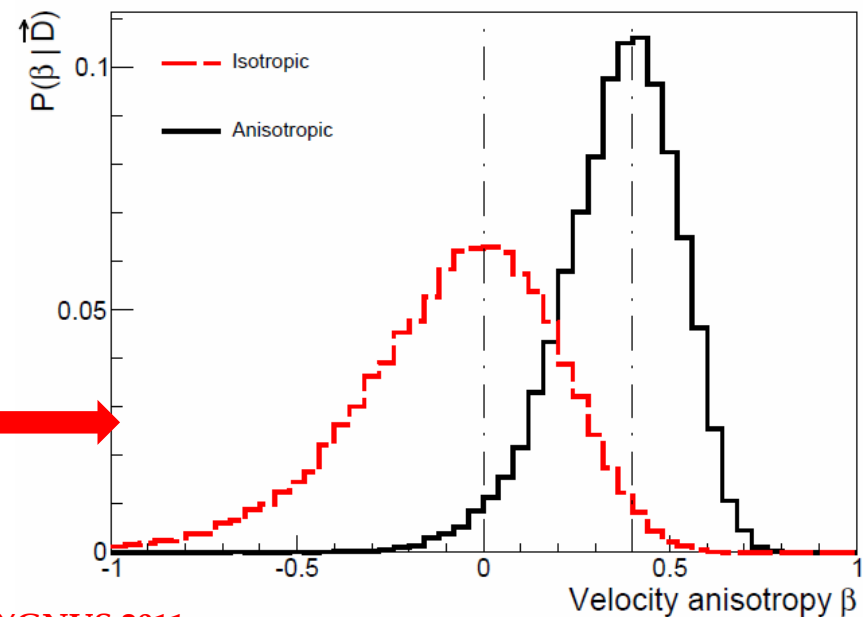


Constraints on the β parameter:

Isotropic $\longrightarrow \beta = -0.073^{+0.29}_{-0.18}$

Anisotropic $\longrightarrow \beta = 0.38^{+0.18}_{-0.10}$

Discrimination between various halo model could be achieved with directional detection

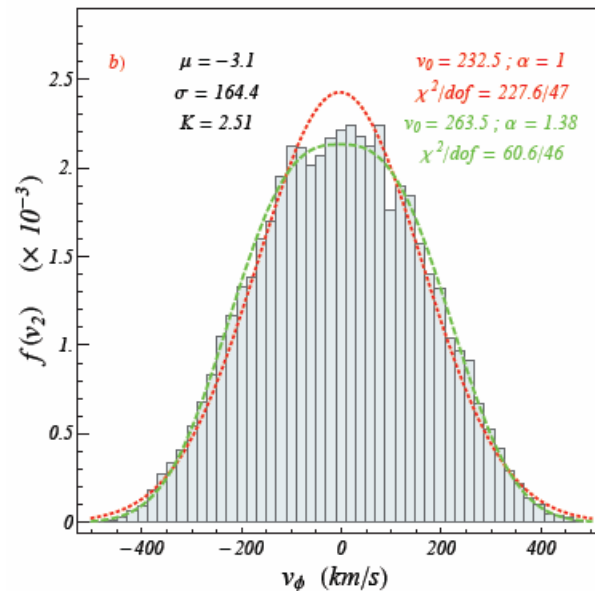


IV.h Effect of refined halo model from Nbody simulations

RAMSES [R. Teyssier et al.]: Cosmological N-Body simulations

Shell distribution:

$7 < R < 9$ kpc (16545 particles)



- Gaussian distribution disfavoured
Kurtosis = 2.51

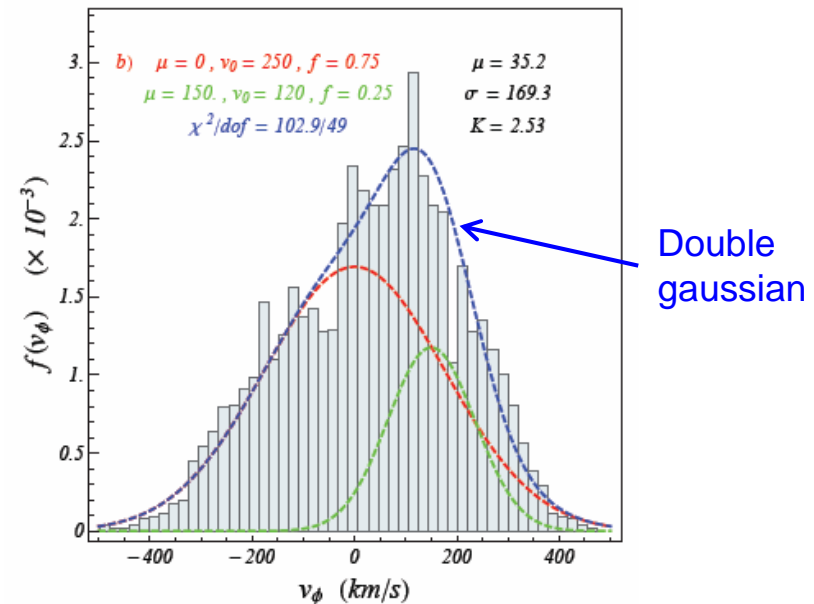
$$\beta \sim 0,06$$

Smooth, weakly anisotropic and non-gaussian

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Ring distribution:

$7 < R < 9$ kpc and $|z| < 1$ kpc (2662 particles)



- Presence of a co-rotating (**150 km/s**)
Dark Disk with a **25%** contribution to
the local WIMP velocity distribution

$$\beta \sim 0,12$$

With a corotating Dark Disk

IV.h Effect of refined halo model from Nbody simulations

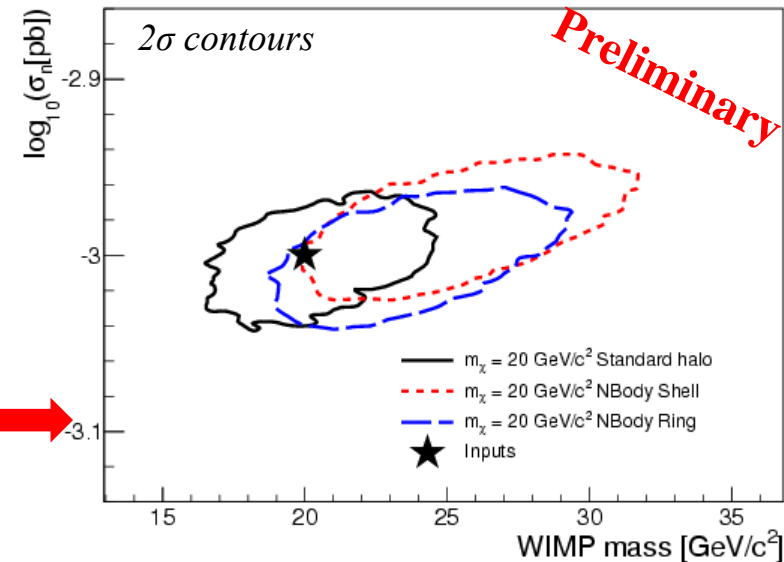
3 input halo models to generate pseudo-data:

Standard halo

Smooth

Dark Disk

Bias $\sim 2\sigma$ in the $(m_X, \log_{10}(\sigma_n))$



Constraints on the β parameter:

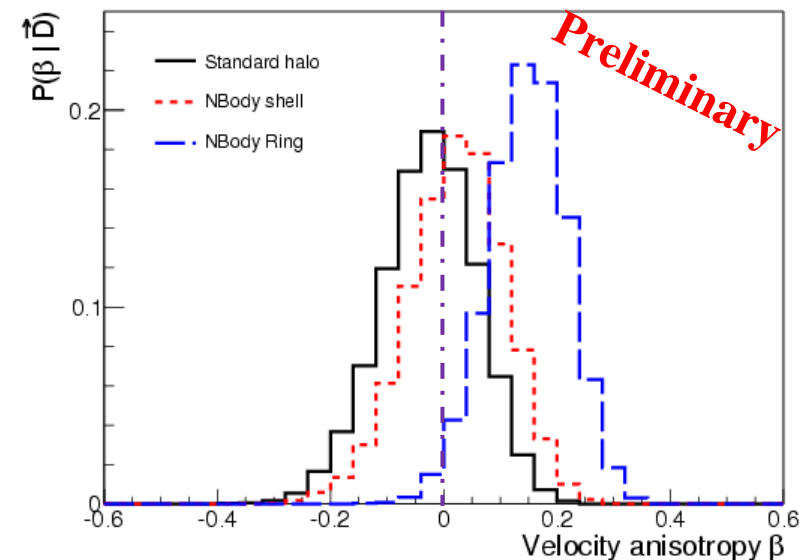
Standard halo $\longrightarrow \beta = -0.01^{+0.09}_{-0.06}$

Smooth $\longrightarrow \beta = 0.02^{+0.09}_{-0.07}$

Dark Disk $\longrightarrow \beta = 0.15^{+0.06}_{-0.06}$

Robustness of the multivariate gaussian

WIMP velocity distribution



Conclusion

Directional detection presents a lot of advantages in comparison with the classical direct detection of Dark Matter:

- **The WIMP induced signal is different from the expected background one**
- **Exclusion, discovery or identification** (Particle physics and astrophysics)

The study of the impact of Dark Matter halo from Nbody simulations on directional detection

(J. Billard et al., in preparation)

However, these results require:

- **3D Reconstruction of tracks with good resolutions**
 - **Sense recognition**
 - **An accurate measurement of the recoil energy**
- *Requires a highly performant detector with a carefull analysis...*

J. Billard - CYGNUS 2011